This supplementary information presents:

- first, the code to generate the figures from the paper,
- second, some control experiments that were mentionned in the paper,
- finally, some perspectives for future work inspired by the algorithms presented in the paper.

# Figures for "An adaptive algorithm for unsupervised learning"

```
In [1]: %load ext autoreload
        %autoreload 2
In [2]: | import numpy as np
        np.set printoptions(precision=2, suppress=True)
        seed = 42
        np.random.seed(seed)
In [3]: | # some overhead for the formatting of figures
        import matplotlib.pyplot as plt
        fontsize = 12
        FORMATS = ['.pdf', '.eps', '.png', '.tiff']
        FORMATS = ['.pdf', '.png']
        dpi export = 600
        fig width pt = 318.670 # Get this from LaTeX using \showthe\column
        width
        fig width pt = 450  # Get this from LaTeX using \showthe\columnwidt
        #fig width pt = 1024 #221
                                       # Get this from LaTeX using \showthe\
        columnwidth / x264 asks for a multiple of 2
        ppi = 72.27 # (constant) definition of the ppi = points per inch
        inches per pt = 1.0/ppi # Convert pt to inches
        #inches per cm = 1./2.54
        fig_width = fig_width_pt*inches_per_pt # width in inches
        grid_fig_width = 2*fig_width
        phi = (np.sqrt(5) + 1.) / 2
        #legend.fontsize = 8
        #fig width = 9
        fig height = fig width/phi
        figsize = (fig width, fig height)
        def adjust spines(ax, spines):
            for loc, spine in ax.spines.items():
                if loc in spines:
                    spine.set position(('outward', 10)) # outward by 10 po
        ints
                    spine.set smart bounds(True)
                else:
```

```
# turn off ticks where there is no spine
            if 'left' in spines:
                ax.yaxis.set ticks position('left')
            else:
                # no yaxis ticks
                ax.yaxis.set_ticks([])
            if 'bottom' in spines:
                ax.xaxis.set ticks position('bottom')
            else:
                # no xaxis ticks
                ax.xaxis.set ticks([])
        import matplotlib
        pylab defaults = {
            'font.size': 10,
            'xtick.labelsize': 'medium',
             'ytick.labelsize': 'medium',
            'text.usetex': False,
             'font.family' : 'sans-serif',
             'font.sans-serif' : ['Helvetica'],
            }
        #matplotlib.rcParams.update({'font.size': 18, 'font.family': 'STIXG'
        eneral', 'mathtext.fontset': 'stix'})
        matplotlib.rcParams.update(pylab defaults)
        #matplotlib.rcParams.update({'text.usetex': True})
        import matplotlib.cm as cm
        from IPython.display import Image
        DEBUG = True
        DEBUG = False
        hl, hs = 10*'-', 10*'
In [4]: | tag = 'ICLR'
        datapath = '../../SparseHebbianLearning/database'
        # different runs
        #opts = dict(datapath=datapath, verbose=0)
        #opts = dict(cache_dir='cache_dir_cluster', datapath=datapath, verb
        ose=0)
        #opts = dict(cache dir='cache dir ICLR', datapath=datapath, verbose
        =0)
        opts = dict(cache dir='cache dir cluster25', eta=0.002, eta homeo=0
        .005, datapath=datapath, verbose=0)
In [5]: from shl scripts.shl experiments import SHL
```

shl = SHL(\*\*opts)

data = shl.get data(matname=tag)

spine.set color('none') # don't draw spine

```
In [6]: | shl?
                     SHT
        Type:
        String form: <shl scripts.shl experiments.SHL object at 0x10919412
        File:
        ~/science/SparseHebbianLearning/shl scripts/shl experiments.py
        Docstring:
        Base class to define SHL experiments:
            - initialization
            - coding and learning
            visualization
            - quantitative analysis
In [7]: print('number of patches, size of patches = ', data.shape)
        print('average of patches = ', data.mean(), ' +/- ', data.mean(axis
        =1).std())
        SE = np.sqrt(np.mean(data**2, axis=1))
        print('average energy of data = ', SE.mean(), '+/-', SE.std())
        number of patches, size of patches = (65520, 324)
        average of patches = 5.0641928164665185e-19 +/- 0.0095770518654
        37931
        average energy of data = 0.29851622590347293 +/- 0.08935954499531
        101
In [8]: #!ls -l {shl.cache dir}/{tag}*
        !ls {shl.cache dir}/{tag}*lock*
        !rm {shl.cache dir}/{tag}*lock*
        #!rm {shl.cache dir}/{tag}*
        #!ls -1 {shl.cache dir}/{tag}*
        ls: cache dir cluster25/ICLR*lock*: No such file or directory
        rm: cache dir cluster25/ICLR*lock*: No such file or directory
```

# figure 1: Role of homeostasis in learning sparse representations

TODO: cross-validate with 10 different learnings

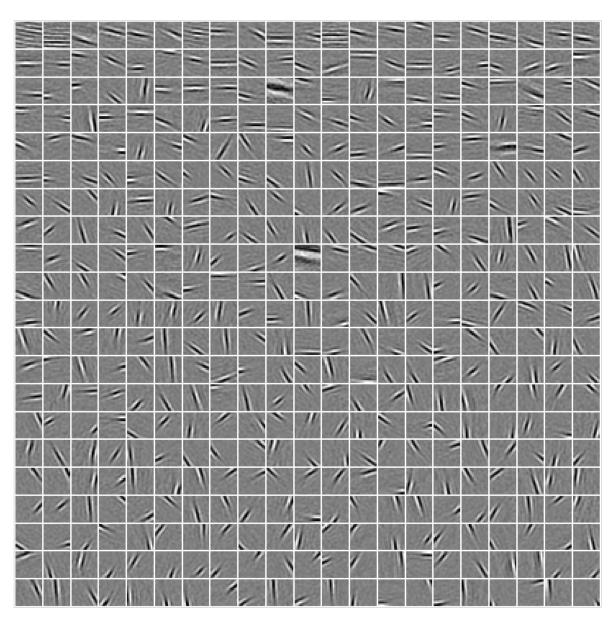
```
In [9]: fname = 'figure_map'
N_cv = 10
one_cv = 0 # picking one to display intermediate results
```

#### learning

The actual learning is done in a second object (here dico) from which we can access another set of properties and functions (see the <a href="mailto:shl\_learn.py">shl\_learn.py</a>

(https://github.com/bicv/SHL\_scripts/blob/master/shl\_scripts/shl\_learn.py) script):

```
In [10]: homeo methods = ['None', 'OLS', 'HEH']
         list figures = ['show dico', 'time plot error', 'time plot logL', '
         time_plot_MC', 'show_Pcum']
         list_figures = []
         dico = \{\}
         for i cv in range(N cv):
             dico[i cv] = \{\}
             for homeo method in homeo methods:
                 shl = SHL(homeo method=homeo method, seed=seed+i cv, **opts
                 dico[i_cv][homeo_method] = shl.learn_dico(data=data, list_f
         igures=list_figures, matname=tag + '_' + homeo_method + '_seed=' +
         str(seed+i cv))
         list figures = ['show dico']
         for i cv in [one cv]:
             for homeo_method in homeo_methods:
                 print(hl + hs + homeo method[:3] + hs + hl)
                 shl = SHL(homeo method=homeo method, seed=seed+i cv, **opts
         )
                 shl.learn dico(data=data, list figures=list figures, matnam
         e=tag + ' ' + homeo method + '_seed=' + str(seed+i_cv))
                 print('size of dictionary = (number of filters, size of ima
         gelets) = ', dico[i_cv][homeo_method].dictionary.shape)
                 print('average of filters = ', dico[i_cv][homeo_method].di
         ctionary.mean(axis=1).mean(),
                       '+/-', dico[i cv][homeo method].dictionary.mean(axis
         =1).std())
                 SE = np.sqrt(np.sum(dico[i cv][homeo method].dictionary**2,
         axis=1))
                 print('average energy of filters = ', SE.mean(), '+/-', SE.
         std())
                 plt.show()
```

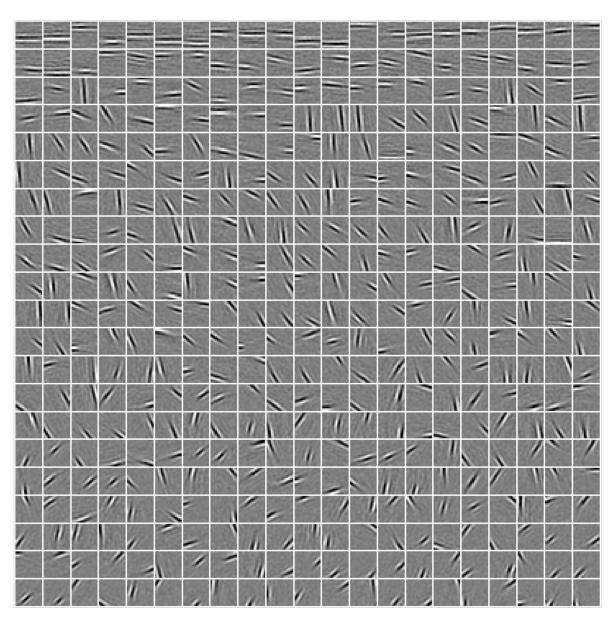


----- OLS -----

size of dictionary = (number of filters, size of imagelets) = (44
1, 324)

average of filters = -4.089243933727358e-06 +/- 0.0012410960067970878

average energy of filters = 1.0 + /- 3.9562611248144994e-17

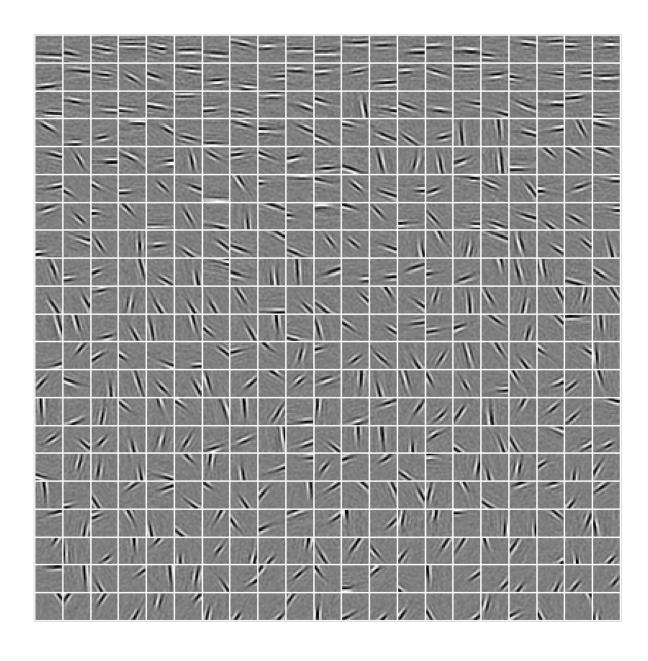


----- НЕН -----

size of dictionary = (number of filters, size of imagelets) = (44 1, 324)

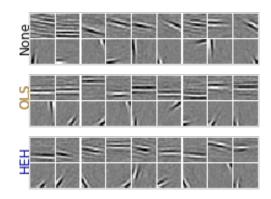
average of filters = -6.6112572753952305e-06 +/- 0.00121065448870 92556

average energy of filters = 1.0 + /- 3.700743415417188e-17



#### panel A: plotting some dictionaries

```
In [11]: pname = '/tmp/panel_A' #pname = fname + '_A'
In [12]: from shl_scripts import show_dico
    if DEBUG: show_dico(shl, dico[one_cvi_cv][homeo_method], data=data,
        dim_graph=(2,5))
In [13]: dim_graph = (2, 9)
    colors = ['black', 'orange', 'blue']
    homeo_methods
Out[13]: ['None', 'OLS', 'HEH']
```

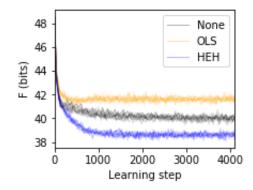


```
In [15]: ### TODO put the p_min an p_max value in the filter map
In [16]: if DEBUG: Image(pname +'.png')
In [17]: if DEBUG: help(fig.subplots_adjust)
In [18]: if DEBUG: help(plt.subplots)
In [19]: if DEBUG: help(matplotlib.gridspec.GridSpec)
```

#### panel B: quantitative comparison

```
In [20]: pname = '/tmp/panel_B' #fname + '_B'
```

```
In [21]:
        from shl_scripts import time plot
         variable = 'F'
         alpha 0, alpha = .3, .15
         subplotpars = dict(left=0.2, right=.95, bottom=0.2, top=.95)#, wspa
         ce=0.05, hspace=0.05,)
         fig, ax = plt.subplots(1, 1, figsize=(fig width/2, fig width/(1+phi
         )), gridspec kw=subplotpars)
         for i cv in range(N cv):
             for color, homeo method in zip(colors, homeo methods):
                 ax.axis(c='b', lw=2, axisbg='w')
                 ax.set facecolor('w')
                 if i cv==0:
                     fig, ax = time plot(shl, dico[i cv][homeo method], vari
         able=variable, unit='bits', color=color, label=homeo method, alpha=
         alpha 0, fig=fig, ax=ax)
                 else:
                     fig, ax = time plot(shl, dico[i cv][homeo method], vari
         able=variable, unit='bits', color=color, alpha=alpha, fig=fig, ax=a
         x)
                 # ax.set ylabel(homeo method)
                 #ax.text(-8, 7*dim graph[0], homeo method, fontsize=12, col
         or='k', rotation=90)#, backgroundcolor='white'
         ax.legend(loc='best')
         for ext in FORMATS: fig.savefig(pname + ext, dpi=dpi export)
         if DEBUG: Image(pname +'.png')
```

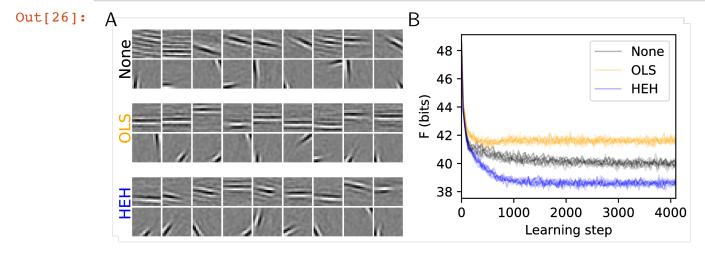


## Montage of the subplots

```
In [22]: import tikzmagic
In [23]: %load_ext tikzmagic
In [24]: #DEBUG = True
   if DEBUG: help(tikzmagic)
```

%tikz \draw (0,0) rectangle (1,1);%%tikz --save {fname}.pdf \draw[white, fill=white] (0.\linewidth,0) rectangle (1.\linewidth, .382\linewidth);

```
In [26]: !convert -density {dpi_export} {fname}.pdf {fname}.jpg
!convert -density {dpi_export} {fname}.pdf {fname}.png
#!convert -density {dpi_export} -resize 5400 -units pixelsperinch
-flatten -compress lzw -depth 8 {fname}.pdf {fname}.tiff
Image(fname +'.png')
```



!echo "width="; convert {fname}.tiff -format "%[fx:w]" info: !echo ", \nheight="; convert {fname}.tiff -format "%[fx:h]" info: !echo ", \nunit="; convert {fname}.tiff -format "%U" info:!identify {fname}.tiff

## figure 2: Histogram Equalization Homeostasis

```
In [27]: fname = 'figure_HEH'
```

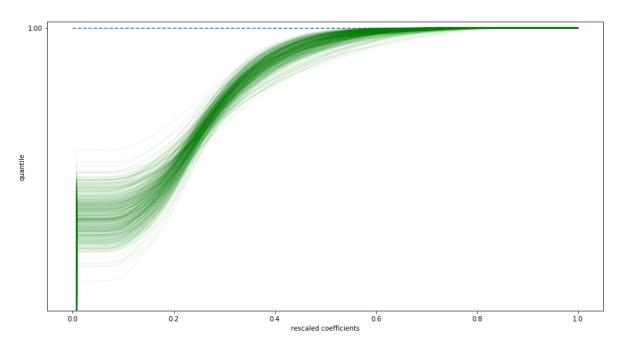
First collecting data:

```
In [28]: list_figures = ['show_Pcum']

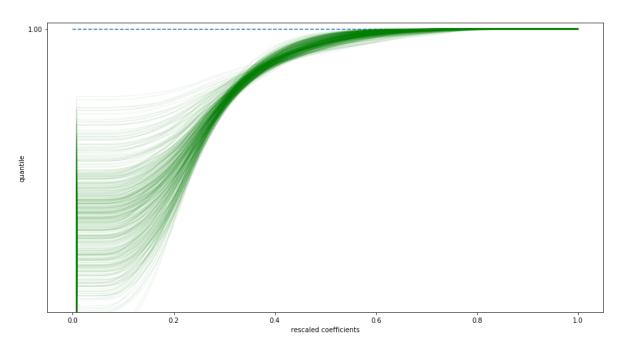
dico = {}

for homeo_method in homeo_methods:
    print(hl + hs + homeo_method + hs + hl)
    shl = SHL(homeo_method=homeo_method, **opts)
    #dico[homeo_method] = shl.learn_dico(data=data, list_figures=list_figures, matname=tag + '_' + homeo_method + '_' + str(one_cv))
    dico[homeo_method] = shl.learn_dico(data=data, list_figures=list_figures, matname=tag + '_' + homeo_method + '_seed=' + str(seed+one_cv))
    plt.show()
```

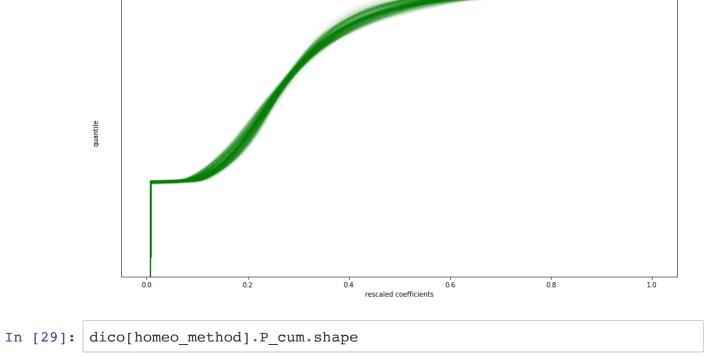
----- None -----



----- OLS -----



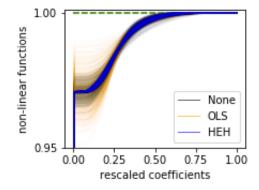
----- HEH -----



```
Out[29]: (441, 128)
```

# panel A: different P\_cum

```
In [30]: | pname = '/tmp/panel A' #pname = fname + ' A'
         from shl scripts import plot P cum
         variable = 'F'
         subplotpars = dict(left=0.2, right=.95, bottom=0.2, top=.95)#, wspa
         ce=0.05, hspace=0.05,)
         fig, ax = plt.subplots(1, 1, figsize=(fig width/2, fig width/(1+phi
         )), gridspec kw=subplotpars)
         for color, homeo method in zip(colors, homeo methods):
             ax.axis(c='b', lw=2, axisbg='w')
             ax.set facecolor('w')
             fig, ax = plot_P_cum(dico[homeo_method].P_cum, ymin=0.95, ymax=
         1.001,
                                   title=None, suptitle=None, ylabel='non-lin
         ear functions',
                                  verbose=False, n yticks=21, alpha=.02, c=c
         olor, fig=fig, ax=ax)
             ax.plot([0], [0], lw=1, color=color, label=homeo_method, alpha=
         .6)
             # ax.set ylabel(homeo method)
             #ax.text(-8, 7*dim graph[0], homeo method, fontsize=12, color='
         k', rotation=90)#, backgroundcolor='white'
         ax.legend(loc='lower right')
         for ext in FORMATS: fig.savefig(pname + ext, dpi=dpi export)
         if DEBUG: Image(pname +'.png')
```



```
In [31]: if DEBUG: help(fig.legend)
```

#### panel B: comparing the effects of parameters

```
homeo methods = ['None', 'EMP', 'HAP', 'HEH', 'OLS']
homeo methods = ['None', 'OLS', 'HEH']
variables = ['eta', 'alpha homeo', 'eta homeo', '10 sparseness', 'n
dictionary']
variables = ['eta', 'alpha homeo', 'eta homeo', '10 sparseness']
variables = ['alpha_homeo', 'eta_homeo']
variables = ['eta', 'alpha homeo', 'eta homeo']
variables = ['eta', 'eta_homeo']
list figures = []
bases = [10, 10, 2, 2]
bases = [4] * 4
for homeo_method, base in zip(homeo_methods, bases):
    opts = opts.copy()
    opts .update(homeo method=homeo method)
    experiments = SHL_set(opts_, tag=tag + '_' + homeo_method)#, ba
se=base)
    experiments.run(variables=variables, n jobs=1, verbose=0)
import matplotlib.pyplot as plt
subplotpars = dict(left=0.2, right=.95, bottom=0.2, top=.95, wspace
=0.5, hspace=0.35,)
x, y = .05, -.3
if len(variables) == 4:
    fig, axs = plt.subplots(2, 2, figsize=(fig_width/2, fig_width/(
1+phi)), gridspec kw=subplotpars, sharey=True)
    for i ax, variable in enumerate(variables):
        for color, homeo method in zip(colors, homeo methods):
            opts = opts.copy()
            opts .update(homeo method=homeo method)
            experiments = SHL set(opts , tag=tag + ' ' + homeo meth
od) #, base=base)
            ax = axs[i_ax%2][i_ax//2]
            fig, ax = experiments.scan(variable=variable, list figu
res=[], display='final', fig=fig, ax=ax, color=color, display varia
ble='F', verbose=0) #, label=homeo metho
            ax.set_xlabel('') #variable
            ax.text(x, y, variable, transform=axs[i_ax].transAxes)
            #axs[i ax].get xaxis().set major formatter(matplotlib.t
icker.ScalarFormatter())
else:
    fig, axs = plt.subplots(len(variables), 1, figsize=(fig width/2
, fig width/(1+phi)), gridspec kw=subplotpars, sharey=True)
    for i ax, variable in enumerate(variables):
        for color, homeo method in zip(colors, homeo methods):
            opts = opts.copy()
            opts .update(homeo method=homeo method)
```

```
experiments = SHL_set(opts_, tag=tag + '_' + homeo_meth
od)#, base=base)
    fig, axs[i_ax] = experiments.scan(variable=variable, li
st_figures=[], display='final', fig=fig, ax=axs[i_ax], color=color,
display_variable='F', verbose=0) #, label=homeo_metho
    axs[i_ax].set_xlabel('') #variable
    axs[i_ax].text(x, y, variable, transform=axs[i_ax].tra
nsAxes)
    #axs[i_ax].get_xaxis().set_major_formatter(matplotlib.ticker.ScalarFormatter())

#fig.legend(loc='lower right')
for ext in FORMATS: fig.savefig(pname + ext, dpi=dpi_export)
if DEBUG: Image(pname +'.png')
```

#### Montage of the subplots

```
In [ ]: !convert -density {dpi_export} {fname}.pdf {fname}.jpg
!convert -density {dpi_export} {fname}.pdf {fname}.png
#!convert -density {dpi_export} -resize 5400 -units pixelsperinch
-flatten -compress lzw -depth 8 {fname}.pdf {fname}.tiff
Image(fname +'.png')
```

!echo "width="; convert {fname}.tiff -format "%[fx:w]" info: !echo ", \nheight="; convert {fname}.tiff -format "%[fx:h]" info: !echo ", \nunit="; convert {fname}.tiff -format "%U" info:!identify {fname}.tiff

# figure 3:

#### learning

```
In [36]: fname = 'figure_HAP'
```

```
In [37]: colors = ['orange', 'red', 'green', 'blue']
         homeo methods = ['OLS', 'HEH', 'EMP', 'HAP']
         list figures = []
         dico = \{\}
         for i_cv in range(N_cv):
             dico[i cv] = \{\}
             for homeo method in homeo methods:
                 shl = SHL(homeo method=homeo method, seed=seed+i cv, **opts
                 dico[i cv][homeo method] = shl.learn dico(data=data, list f
         igures=list_figures, matname=tag + '_' + homeo_method + '_seed=' +
         str(seed+i_cv))
         list figures = ['show dico'] if DEBUG else []
         for i cv in [one cv]:
             for homeo method in homeo methods:
                 print(hl + hs + homeo method + hs + hl)
                 shl = SHL(homeo_method=homeo_method, seed=seed+i_cv, **opts
         )
                 shl.learn dico(data=data, list figures=list figures, matnam
         e=tag + '_' + homeo_method + '_seed=' + str(seed+i_cv))
                 plt.show()
                 print('size of dictionary = (number of filters, size of ima
         gelets) = ', dico[i cv][homeo method].dictionary.shape)
                 print('average of filters = ', dico[i_cv][homeo_method].di
         ctionary.mean(axis=1).mean(),
                       '+/-', dico[i_cv][homeo method].dictionary.mean(axis
         =1).std())
                 SE = np.sqrt(np.sum(dico[i cv][homeo method].dictionary**2,
         axis=1))
                 print('average energy of filters = ', SE.mean(), '+/-', SE.
         std())
```

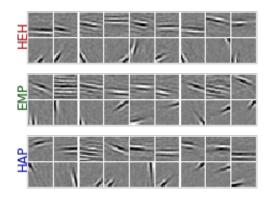
```
OLS
size of dictionary = (number of filters, size of imagelets) = (44
average of filters = -4.089243933727358e-06 +/- 0.001241096006797
0878
average energy of filters = 1.0 + /- 3.9562611248144994e-17
                   HEH
size of dictionary = (number of filters, size of imagelets) = (44
1, 324)
average of filters = -6.6112572753952305e-06 +/- 0.00121065448870
92556
average energy of filters = 1.0 + /- 3.700743415417188e-17
                   EMP
size of dictionary = (number of filters, size of imagelets) = (44
average of filters = 4.993730484951632e-05 +/- 0.0012218228270885
788
average energy of filters = 1.0 + /- 3.700743415417188e-17
                   HAP
_____
size of dictionary = (number of filters, size of imagelets) = (44
average of filters = -2.429586935952582e-05 +/- 0.001195729444507
5826
average energy of filters = 1.0 + - 3.775513461943296e - 17
```

#### panel A: plotting some dictionaries

```
In [38]: pname = '/tmp/panel_A' #pname = fname + '_A'
```

```
In [39]: subplotpars = dict( left=0.042, right=1., bottom=0., top=1., wspace
=0.05, hspace=0.05,)
fig, axs = plt.subplots(3, 1, figsize=(fig_width/2, fig_width/(1+ph
i)), gridspec_kw=subplotpars)

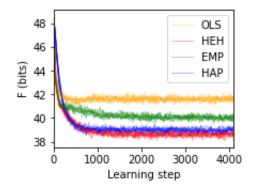
for ax, color, homeo_method in zip(axs.ravel(), colors[1:], homeo_m
ethods[1:]):
    ax.axis(c=color, lw=2, axisbg='w')
    ax.set_facecolor('w')
    from shl_scripts import show_dico
    fig, ax = show_dico(shl, dico[one_cv][homeo_method], data=data,
dim_graph=dim_graph, fig=fig, ax=ax)
    # ax.set_ylabel(homeo_method)
    ax.text(-8, 7*dim_graph[0], homeo_method, fontsize=12, color=color, rotation=90)#, backgroundcolor='white'
for ext in FORMATS: fig.savefig(pname + ext, dpi=dpi_export)
```



## panel B: quantitative comparison

```
In [40]: pname = '/tmp/panel_B' #fname + '_B'
```

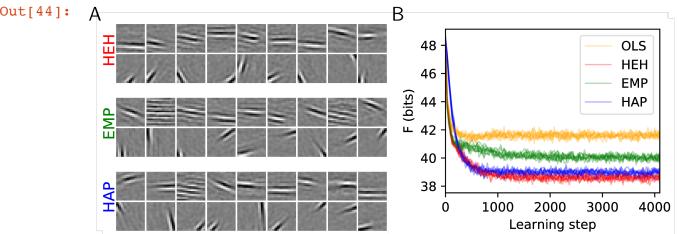
```
In [41]: | from shl_scripts import time plot
         variable = 'F'
         alpha = .3
         subplotpars = dict(left=0.2, right=.95, bottom=0.2, top=.95)#, wspa
         ce=0.05, hspace=0.05,)
         fig, ax = plt.subplots(1, 1, figsize=(fig width/2, fig width/(1+phi
         )), gridspec kw=subplotpars)
         for i cv in range(N cv):
             for color, homeo method in zip(colors, homeo methods):
                 ax.axis(c='b', lw=2, axisbg='w')
                 ax.set facecolor('w')
                 if i cv==0:
                      fig, ax = time plot(shl, dico[i cv][homeo method], vari
         able=variable, unit='bits', color=color, label=homeo method, alpha=
         alpha 0, fig=fig, ax=ax)
                 else:
                      fig, ax = time plot(shl, dico[i cv][homeo method], vari
         able=variable, unit='bits', color=color, alpha=alpha, fig=fig, ax=a
         x)
         ax.legend(loc='best')
         for ext in FORMATS: fig.savefig(pname + ext, dpi=dpi_export)
         if DEBUG: Image(pname +'.png')
```



```
In [42]: if DEBUG: Image(pname +'.png')
```

#### Montage of the subplots

```
In [44]: !convert -density {dpi_export} {fname}.pdf {fname}.jpg
!convert -density {dpi_export} {fname}.pdf {fname}.png
#!convert -density {dpi_export} -resize 5400 -units pixelsperinch
-flatten -compress lzw -depth 8 {fname}.pdf {fname}.tiff
Image(fname +'.png')
Out[44]: A
```



!echo "width="; convert {fname}.tiff -format "%[fx:w]" info: !echo ", \nheight="; convert {fname}.tiff -format "%[fx:h]" info: !echo ", \nunit="; convert {fname}.tiff -format "%U" info:!identify {fname}.tiff

# figure 4: Convolutional Neural Network

```
In [45]: fname = 'figure_CNN'
```

```
In [46]: from CHAMP.DataLoader import LoadData
         from CHAMP. DataTools import LocalContrastNormalization, FilterInput
         Data, GenerateMask
         from CHAMP.Monitor import DisplayDico, DisplayConvergenceCHAMP, Dis
         playWhere
         import os
         datapath = os.path.join("/tmp", "database")
         path = os.path.join(datapath, "Raw_DataBase")
         TrSet, TeSet = LoadData('Face', path, decorrelate=False, resize=(65
         , 65))
         # MP Parameters
         nb dico = 20
         width = 9
         dico size = (width, width)
         10 = 20
         seed = 42
         # Learning Parameters
         eta = .05
         nb epoch = 500
         TrSet, TeSet = LoadData('Face', path, decorrelate=False, resize=(65
         , 65))
         N_TrSet, _, _, _ = LocalContrastNormalization(TrSet)
         Filtered L TrSet = FilterInputData(
             N_TrSet, sigma=0.25, style='Custom', start R=15)
         mask = GenerateMask(full size=(nb dico, 1, width, width), sigma=0.8
         , style='Gaussian')
         from CHAMP.CHAMP Layer import CHAMP Layer
         from CHAMP. DataTools import SaveNetwork, LoadNetwork
         homeo methods = ['None', 'HAP']
         for homeo method, eta homeo in zip(homeo methods, [0., 0.0025]):
             ffname = 'cache_dir_CNN/CHAMP_low_' + homeo_method + '.pkl'
             try:
                 L1 mask = LoadNetwork(loading path=ffname)
             except:
                 L1 mask = CHAMP Layer(10 sparseness=10, nb dico=nb dico,
                                    dico size=dico size, mask=mask, verbose=1
         )
                 dico mask = L1 mask.TrainLayer(
                     Filtered_L_TrSet, eta=eta, eta_homeo=eta_homeo, nb_epoc
         h=nb epoch, seed=seed)
                 SaveNetwork(Network=L1 mask, saving path=ffname)
```

#### panel A: plotting some dictionaries

```
In [47]: pname = '/tmp/panel_A' #pname = fname + '_A'
```

plt.subplots(2, 1, figsize=(fig\_width/2, fig\_width/(1+phi)), gridspec\_kw=subplotpars) for ax, color, homeo\_method in zip(axs.ravel(), ['black', 'green'], homeo\_methods): ax.axis(c=color, lw=2, axisbg='w') ax.set\_facecolor('w') ffname = 'cache\_dir/CHAMP\_low\_' + homeo\_method + '.pkl' L1\_mask = LoadNetwork(loading\_path=ffname) fig, ax = DisplayDico(L1\_mask.dictionary, fig=fig, ax=ax) # ax.set\_ylabel(homeo\_method) ax.text(-8, 7\*dim\_graph[0], homeo\_method, fontsize=12, color=color, rotation=90)#, backgroundcolor='white' for ext in FORMATS: fig.savefig(pname + ext, dpi=dpi\_export)

```
subplotpars = dict(left=0.042, right=1., bottom=0., top=1., wspace=
In [48]:
         0.05, hspace=0.05,)
         for color, homeo method in zip(['black', 'green'], homeo methods):
             #fig, axs = plt.subplots(1, 1, figsize=(fig_width/2, fig_width/
         (1+phi)), gridspec_kw=subplotpars)
             ffname = 'cache dir CNN/CHAMP low ' + homeo method + '.pkl'
             L1 mask = LoadNetwork(loading path=ffname)
             fig, ax = DisplayDico(L1 mask.dictionary)
             # ax.set ylabel(homeo method)
             #for ax in list(axs):
                  ax.axis(c=color, lw=2, axisbg='w')
                  ax.set facecolor('w')
             ax[0].text(-4, 3, homeo method, fontsize=8, color=color, rotati
         on=90)#, backgroundcolor='white'
             plt.tight layout( pad=0., w pad=0., h pad=.0)
             for ext in FORMATS: fig.savefig(pname + '_' + homeo_method + ex
         t, dpi=dpi export)
```

<Figure size 576x28.8 with 0 Axes>



<Figure size 576x28.8 with 0 Axes>

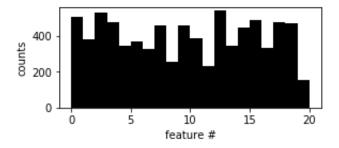


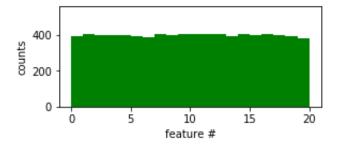
#### panel B: quantitative comparison

```
In [49]: pname = '/tmp/panel_B' #fname + '_B'
```

from shl\_scripts import time\_plot variable = 'F' alpha = .3 subplotpars = dict(left=0.2, right=.95, bottom=0.2, top=.95)#, wspace=0.05, hspace=0.05,) fig, axs = plt.subplots(2, 1, figsize=(fig\_width/2, fig\_width/(1+phi)), gridspec\_kw=subplotpars) for ax, color, homeo\_method in zip(axs, ['black', 'green'], homeo\_methods): print(ax, axs) ffname = 'cache\_dir\_CNN/CHAMP\_low\_' + homeo\_method + '.pkl' L1\_mask = LoadNetwork(loading\_path=ffname) fig, ax = DisplayConvergenceCHAMP(L1\_mask, to\_display=['histo'], fig=fig, ax=ax) ax.axis(c=color, lw=2, axisbg='w') ax.set\_facecolor('w') # ax.set\_ylabel(homeo\_method) #ax.text(-8, 7\*dim\_graph[0], homeo\_method, fontsize=12, color=color, rotation=90)#, backgroundcolor='white' for ext in FORMATS: fig.savefig(pname + ext, dpi=dpi\_export) if DEBUG: Image(pname +'.png')

```
In [50]:
         from shl_scripts import time plot
         variable = 'F'
         alpha = .3
         subplotpars = dict(left=0.2, right=.95, bottom=0.2, top=.95)#, wspa
         ce=0.05, hspace=0.05,)
         for color, homeo_method in zip(['black', 'green'], homeo methods):
             #fig, axs = plt.subplots(1, 1, figsize=(fig width/2, fig width/
         (1+phi)), gridspec kw=subplotpars)
             ffname = 'cache dir CNN/CHAMP low ' + homeo method + '.pkl'
             L1 mask = LoadNetwork(loading path=ffname)
             fig, ax = DisplayConvergenceCHAMP(L1_mask, to_display=['histo']
         , color=color)
             ax.axis(c=color, lw=2, axisbg='w')
             ax.set facecolor('w')
             ax.set ylabel('counts')
             ax.set_xlabel('feature #')
             ax.set_ylim(0, 560)
             #ax.text(-8, 7*dim_graph[0], homeo_method, fontsize=12, color=c
         olor, rotation=90)#, backgroundcolor='white'
             #ax[0].text(-8, 3, homeo_method, fontsize=12, color=color, rota
         tion=90)#, backgroundcolor='white'
             for ext in FORMATS: fig.savefig(pname + '_' + homeo_method + ex
         t, dpi=dpi_export)
             if DEBUG: Image(pname +'.png')
```





#### Montage of the subplots

```
%ls -ltr /tmp/panel *
In [51]:
                     1 501
                            wheel
                                    67281 Nov 27 00:04 /tmp/panel_A.pdf
         -rw-r--r--
                     1 501
                            wheel
                                    79492 Nov 27 00:04 /tmp/panel A.png
         -rw-r--r--
                     1 501
                                    49220 Nov 27 00:04 /tmp/panel B.pdf
         -rw-r--r--
                            wheel
         -rw-r--r-- 1 501
                                   555716 Nov 27 00:04 /tmp/panel B.png
                            wheel
         -rw-r--r 1 501
                            wheel
                                    27370 Nov 27 00:05 /tmp/panel A None.pd
         f
         -rw-r--r-- 1 501
                            wheel
                                    18909 Nov 27 00:05 /tmp/panel A None.pn
                     1 501
                            wheel
                                    26909 Nov 27 00:05 /tmp/panel_A_HAP.pdf
         -rw-r--r--
         -rw-r--r-- 1 501
                                    16431 Nov 27 00:05 /tmp/panel_A_HAP.png
                            wheel
                     1 501
                            wheel
                                     8816 Nov 27 00:05 /tmp/panel B None.pd
         -rw-r--r--
         f
                                    39035 Nov 27 00:05 /tmp/panel B None.pn
         -rw-r--r--
                    1 501
                            wheel
                     1 501
                            wheel
                                     8813 Nov 27 00:05 /tmp/panel B HAP.pdf
         -rw-r--r--
         -rw-r--r--
                     1 501
                            wheel
                                    38743 Nov 27 00:05 /tmp/panel_B_HAP.png
In [52]:
         fname
Out[52]: 'figure_CNN'
In [53]:
         382+191
Out[53]: 573
         %%tikz -f pdf --save {fname}.pdf
In [54]:
         \draw[white, fill=white] (0.\linewidth,0) rectangle (1.\linewidth,
         .382\linewidth);
         \draw [anchor=north west] (.0\linewidth, .375\linewidth) node {\inc
         ludegraphics[width=.95\linewidth]{/tmp/panel A None}};
         \draw [anchor=north west] (.0\linewidth, .300\linewidth) node {\inc
         ludegraphics[width=.95\linewidth]{/tmp/panel_A_HAP}};
         \draw [anchor=north west] (.0\linewidth, .191\linewidth) node {\inc
         ludegraphics[width=.45\linewidth]{/tmp/panel_B_None}};
         \draw [anchor=north west] (.5\linewidth, .191\linewidth) node {\inc
         ludegraphics[width=.45\linewidth]{/tmp/panel B HAP}};
         \begin{scope}[font=\bf\sffamily\large]
         %\draw [anchor=west,fill=white] (.0\linewidth, .382\linewidth) node
         [above right=-3mm] {$\mathsf{A}\$};
         \draw [anchor=west,fill=white] (.0\linewidth, .191\linewidth) node
         [above right=-3mm] {$\mathsf{A}}$;
         \draw [anchor=west, fill=white] (.53\linewidth, .191\linewidth) node
         [above right=-3mm] {$\mathsf{B}$};
         \end{scope}
```

!echo "width="; convert {fname}.tiff -format "%[fx:w]" info: !echo ", \nheight="; convert {fname}.tiff -format "%[fx:h]" info: !echo ", \nunit="; convert {fname}.tiff -format "%U" info:!identify {fname}.tiff

## coding

The learning itself is done via a gradient descent but is highly dependent on the coding / decoding algorithm. This belongs to a another function (in the <a href="mailto:shl\_encode.py">shl\_encode.py</a>

(https://github.com/bicv/SHL\_scripts/blob/master/shl\_scripts/shl\_encode.py) script)

# **Supplementary controls**

## starting a learning

print('average energy of filters = ', SE.mean(), '+/-', SE.std())

## getting help

```
In [ ]: help(shl)
In [ ]: help(dico)
```

## loading a database

Loading patches, with or without mask:

## **Testing different algorithms**

## Testing two different dictionary initalization strategies

White Noise Initialization + Learning

```
In [ ]: shl = SHL(one_over_F=False, **opts)
    dico_w = shl.learn_dico(data=data, matname=tag + '_WHITE', list_fig
        ures=[])
    shl = SHL(one_over_F=True, **opts)
    dico_loF = shl.learn_dico(data=data, matname=tag + '_OVF', list_fig
        ures=[])
    fig_error, ax_error = None, None
    fig_error, ax_error = shl.time_plot(dico_w, variable='F', fig=fig_e
        rror, ax=ax_error, color='blue', label='white noise')
    fig_error, ax_error = shl.time_plot(dico_loF, variable='F', fig=fig
        _error, ax=ax_error, color='red', label='one over f')
    #ax_error.set_ylim((0, .65))
    ax_error.legend(loc='best')
```

## **Testing two different learning rates strategies**

We use by defaut the strategy of ADAM, see <a href="https://arxiv.org/pdf/1412.6980.pdf">https://arxiv.org/pdf/1412.6980.pdf</a> <a href="https://arxiv.org/pdf/1412.6980.pdf">https://arxiv.org/pdf/1412.6980.pdf</a>

## Testing different number of neurons and sparsity

As suggested by AnonReviewer3, we have tested how the convergence was modified by changing the number of neurons. By comparing different numbers of neurons we could re-draw the same figures for the convergence of the algorithm as in our original figures. In addition, we have also checked that this result will hold on a range of sparsity levels. In particular, we found that in general, increasing the <code>lo\_sparseness</code> parameter, the convergence took progressively longer. Importantly, we could see that in both cases, this did not depend on the kind of homeostasis heuristic chosen, proving the generality of our results.

This is shown in the supplementary material that we have added to our revision ("Testing different number of neurons and sparsity"). This useful extension proves the originality of our work as highlighted in point 4, and the generality of these results compared to the parameters of the network.

```
In [ ]: from shl_scripts.shl_experiments import SHL set
        homeo_methods = ['None', 'OLS', 'HEH']
        homeo_methods = ['None', 'EMP', 'HAP', 'HEH', 'OLS']
        variables = ['10_sparseness', 'n_dictionary']
        list figures = []
        #n dictionary=21**2
        for homeo method in homeo methods:
            opts = opts.copy()
            opts .update(homeo_method=homeo_method, datapath=datapath)
            experiments = SHL_set(opts_, tag=tag + '_' + homeo_method)
            experiments.run(variables=variables, n jobs=1, verbose=0)
        fig, axs = plt.subplots(len(variables), 1, figsize=(fig width/2, fi
        g width/(1+phi)), gridspec kw=subplotpars, sharey=True)
        for i ax, variable in enumerate(variables):
            for color, homeo method in zip(colors, homeo methods):
                opts = opts.copy()
                opts .update(homeo method=homeo method, datapath=datapath)
                experiments = SHL set(opts , tag=tag + ' ' + homeo method)
                fig, axs[i ax] = experiments.scan(variable=variable, list f
        igures=[], display='final', fig=fig, ax=axs[i_ax], color=color, dis
        play_variable='F', verbose=0) #, label=homeo_metho
                axs[i_ax].set_xlabel('') #variable
                axs[i_ax].text(.1, .8, variable, transform=axs[i ax].trans
        Axes)
                #axs[i ax].get xaxis().set major formatter(matplotlib.ticke
        r.ScalarFormatter())
```

# **Perspectives**

#### Convolutional neural networks

#### Training on a face database

```
In [ ]: # MP Parameters
        nb dico = 20
        width = 9
        dico size = (width, width)
        10 = 20
        seed = 42
        # Learning Parameters
        eta = .05
        nb epoch = 500
        TrSet, TeSet = LoadData('Face', path, decorrelate=False, resize=(65)
        , 65))
        N_TrSet, _, _, _ = LocalContrastNormalization(TrSet)
        Filtered L TrSet = FilterInputData(
            N TrSet, sigma=0.25, style='Custom', start R=15)
        to display = Filtered L TrSet[0][0, 0:10, :, :, :]
        DisplayDico(to display)
        mask = GenerateMask(full size=(nb dico, 1, width, width), sigma=0.8
        , style='Gaussian')
        DisplayDico(mask)
```

#### Training the ConvMP Layer with homeostasis

#### Training the ConvMP Layer with homeostasis

```
In [ ]: fname = 'cache dir CNN/CHAMP low HAP.pkl'
        try:
            L1 mask = LoadNetwork(loading path=fname)
        except:
            # Learning Parameters
            eta homeo = 0.0025
            L1 mask = CHAMP Layer(10 sparseness=10, nb dico=nb dico,
                                   dico size=dico size, mask=mask, verbose=1
        )
            dico mask = L1 mask.TrainLayer(
                Filtered L TrSet, eta=eta, eta homeo=eta homeo, nb epoch=nb
        _epoch, seed=seed)
            SaveNetwork(Network=L1 mask, saving path=fname)
        DisplayDico(L1 mask.dictionary)
        DisplayConvergenceCHAMP(L1_mask, to_display=['error', 'histo'])
        DisplayWhere(L1 mask.where)
```

#### Reconstructing the input image

```
In [ ]: from CHAMP.DataTools import Rebuilt
    import torch
    rebuilt_image = Rebuilt(torch.FloatTensor(L1_mask.code), L1_mask.di
    ctionary)
    DisplayDico(rebuilt_image[0:10, :, :, :])
```

#### Training the ConvMP Layer with higher-level filters

We train higher-level feature vectors by forcing the network to:

- learn bigger filters,
- represent the information using a bigger dictionary (higher sparseness)
- represent the information with less features (higher sparseness)

```
In [ ]: fname = 'cache dir CNN/CHAMP high None.pkl'
            L1 mask = LoadNetwork(loading path=fname)
        except:
            nb dico = 60
            width = 19
            dico size = (width, width)
            10 = 5
            mask = GenerateMask(full size=(nb dico, 1, width, width), sigma
        =0.8, style='Gaussian')
            # Learning Parameters
            eta homeo = 0.0
            eta = .05
            nb epoch = 500
            # learn
            L1_mask = CHAMP_Layer(10_sparseness=10, nb_dico=nb dico,
                                   dico size=dico size, mask=mask, verbose=0
        )
            dico mask = L1 mask.TrainLayer(
                Filtered L TrSet, eta=eta, eta homeo=eta homeo, nb epoch=nb
        _epoch, seed=seed)
            SaveNetwork(Network=L1 mask, saving path=fname)
        DisplayDico(L1_mask.dictionary)
        DisplayConvergenceCHAMP(L1 mask, to display=['error'])#, 'histo'])
        DisplayWhere(L1 mask.where)
```

```
In [ ]: | fname = 'cache_dir_CNN/CHAMP high HAP.pkl'
            L1 mask = LoadNetwork(loading path=fname)
        except:
            nb dico = 60
            width = 19
            dico size = (width, width)
            10 = 5
            mask = GenerateMask(full size=(nb dico, 1, width, width), sigma
        =0.8, style='Gaussian')
            # Learning Parameters
            eta homeo = 0.0025
            eta = .05
            nb epoch = 500
            # learn
            L1 mask = CHAMP Layer(10 sparseness=10, nb dico=nb dico,
                                   dico_size=dico_size, mask=mask, verbose=0
        )
            dico mask = L1 mask.TrainLayer(
                Filtered L TrSet, eta=eta, eta homeo=eta homeo, nb epoch=nb
        epoch, seed=seed)
            SaveNetwork(Network=L1 mask, saving path=fname)
        DisplayDico(L1 mask.dictionary)
        DisplayConvergenceCHAMP(L1_mask, to_display=['error'])#, 'histo'])
        DisplayWhere(L1 mask.where)
```

#### Training on MNIST database

fname = 'cache\_dir\_CNN/CHAMP\_MNIST\_HAP.pkl' try: L1\_mask = LoadNetwork(loading\_path=fname) except: path = os.path.join(datapath, "MNISTtorch") TrSet, TeSet = LoadData('MNIST', data\_path=path) N\_TrSet, \_, \_, \_ = LocalContrastNormalization(TrSet) Filtered\_L\_TrSet = FilterInputData( N\_TrSet, sigma=0.25, style='Custom', start\_R=15) nb\_dico = 60 width = 7 dico\_size = (width, width) I0 = 15 # Learning Parameters eta\_homeo = 0.0025 eta = .05 nb\_epoch = 500 # learn L1\_mask = CHAMP\_Layer(I0\_sparseness=I0, nb\_dico=nb\_dico, dico\_size=dico\_size, mask=mask, verbose=2) dico\_mask = L1\_mask.TrainLayer( Filtered\_L\_TrSet, eta=eta, eta\_homeo=eta\_homeo, nb\_epoch=nb\_epoch, seed=seed) SaveNetwork(Network=L1\_mask, saving\_path=fname) DisplayDico(L1\_mask.dictionary) DisplayConvergenceCHAMP(L1\_mask, to\_display=['error', 'histo']) DisplayWhere(L1\_mask.where)

# **Computational details**

## caching simulation data

A convenience script to run and cache most learning items in this notebooks:

```
In [ ]: |!ls -l {shl.cache dir}/{tag}*
        #!rm {shl.cache dir}/{tag}*lock*
        #!rm {shl.cache dir}/{tag}*
        #!ls -l {shl.cache dir}/{tag}*
In [ ]: | %%writefile model.py
        #!/usr/bin/env python3
        # -*- coding: utf-8 -*
        tag = 'ICLR'
        from shl scripts.shl experiments import SHL, prun
        # pre-loading data
        datapath = '../../SparseHebbianLearning/database'
        # different runs
        #opts = dict(cache dir='cache dir ICLR', datapath=datapath, verbose
        #opts = dict(cache dir='cache dir cluster', datapath=datapath, verb
        opts = dict(datapath=datapath, verbose=0)
        shl = SHL(**opts)
        data = shl.get data(matname=tag)
        # running main simulations
        # Figure 1 & 3
        N cv = 10
        homeo methods = ['None', 'OLS', 'HEH', 'HAP', 'EMP']
        seed = 42
        # running in parallel on a multi-core machine
        import sys
        try:
            n_jobs = int(sys.argv[1])
            print('n_jobs=', n_jobs)
        except:
            n jobs = 4
            n jobs = 9
            n jobs = 10
            n jobs = 1
            n jobs = 35
        if n jobs>0:
            list figures = []
            from shl scripts.shl experiments import SHL set
            for homeo_method in homeo_methods:
                opts_ = opts.copy()
                 opts .update(homeo method=homeo method)
                 experiments = SHL set(opts , tag=tag + ' ' + homeo method,
        N scan=N cv)
                experiments.run(variables=['seed'], n_jobs=n_jobs, verbose=
        0)
            # Figure 2-B
            variables = ['eta', 'alpha_homeo', 'eta_homeo']
```

```
variables = ['eta', 'eta_homeo', '10_sparseness', 'n_dictionary
' 1
   bases = [10, 10, 2, 2]
    for homeo method, base in zip(homeo methods, bases):
        opts = opts.copy()
        opts .update(homeo method=homeo method)
        experiments = SHL_set(opts_, tag=tag + '_' + homeo_method,
base=base)
        experiments.run(variables=variables, n jobs=n jobs, verbose
=0)
   # Annex X.X
    shl = SHL(**opts)
    dico = shl.learn dico(data=data, list figures=list figures, mat
name=tag + ' vanilla')
    for algorithm in ['lasso lars', 'lasso cd', 'lars', 'elastic',
'omp', 'mp']: # 'threshold',
        opts_ = opts.copy()
        opts .update(homeo method='None', learning algorithm=algori
thm, verbose=0)
        shl = SHL(**opts)
        dico= shl.learn dico(data=data, list figures=[],
                       matname=tag + ' - algorithm={}'.format(algor
ithm))
    for homeo_method in ['None', 'HAP']:
        for algorithm in ['lasso_lars', 'lars', 'elastic', 'omp', '
mp']: # 'threshold', 'lasso cd',
            opts = opts.copy()
            opts .update(homeo method=homeo method, learning algori
thm=algorithm, verbose=0)
            shl = SHL(**opts )
            dico= shl.learn dico(data=data, list figures=[],
                           matname=tag + ' - algorithm={}'.format(a
lgorithm) + ' - homeo method={}'.format(homeo method))
    shl = SHL(one over F=False, **opts)
    dico w = shl.learn dico(data=data, matname=tag + ' WHITE', list
figures=[])
    shl = SHL(one over F=True, **opts)
    dico 1oF = shl.learn dico(data=data, matname=tag + ' OVF', list
figures=[])
    shl = SHL(beta1=0., **opts)
    dico fixed = shl.learn dico(data=data, matname=tag + ' fixed',
list figures=[])
    shl = SHL(**opts)
    dico default = shl.learn dico(data=data, matname=tag + ' defaul
t', list figures=[])
```

## **Version used**

```
In [ ]: %load_ext version_information
%version_information numpy, shl_scripts
```

## version control

```
In [ ]: !git status
In [ ]: !git pull
In [ ]: !git commit -am' {tag} : re-running notebooks'
In [ ]: !git push
```

# exporting the notebook

```
In [ ]: !jupyter nbconvert Annex.ipynb
In [ ]: #!jupyter-nbconvert --template report --to pdf Annex.ipynb
In [ ]: !pandoc Annex.html -o Annex.pdf
In [ ]: !zip Annex.zip Annex.html
```

Done. Thanks for your attention!