This supplementary information presents:

- first, the code to generate the figures from the paper,
- second, some control experiments that were mentionned in the paper,
- finally, some perspectives for future work inspired by the algorithms presented in the paper.

Figures for "An adaptive algorithm for unsupervised learning"

```
In [1]: %load ext autoreload
        %autoreload 2
In [2]: | import numpy as np
        np.set printoptions(precision=2, suppress=True)
        seed = 42
        np.random.seed(seed)
In [3]: | # some overhead for the formatting of figures
        import matplotlib.pyplot as plt
        fontsize = 12
        FORMATS = ['.pdf', '.eps', '.png', '.tiff']
        FORMATS = ['.pdf', '.png']
        dpi export = 600
        fig width pt = 318.670 # Get this from LaTeX using \showthe\column
        width
        fig width pt = 450  # Get this from LaTeX using \showthe\columnwidt
        #fig width pt = 1024 #221
                                       # Get this from LaTeX using \showthe\
        columnwidth / x264 asks for a multiple of 2
        ppi = 72.27 # (constant) definition of the ppi = points per inch
        inches per pt = 1.0/ppi # Convert pt to inches
        #inches per cm = 1./2.54
        fig_width = fig_width_pt*inches_per_pt # width in inches
        grid_fig_width = 2*fig_width
        phi = (np.sqrt(5) + 1.) / 2
        #legend.fontsize = 8
        #fig width = 9
        fig height = fig width/phi
        figsize = (fig width, fig height)
        def adjust spines(ax, spines):
            for loc, spine in ax.spines.items():
                if loc in spines:
                    spine.set position(('outward', 10)) # outward by 10 po
        ints
                    spine.set smart bounds(True)
                else:
```

```
# turn off ticks where there is no spine
            if 'left' in spines:
                ax.yaxis.set ticks position('left')
            else:
                # no yaxis ticks
                ax.yaxis.set_ticks([])
            if 'bottom' in spines:
                ax.xaxis.set ticks position('bottom')
            else:
                # no xaxis ticks
                ax.xaxis.set ticks([])
        import matplotlib
        pylab defaults = {
            'font.size': 10,
            'xtick.labelsize': 'medium',
             'ytick.labelsize': 'medium',
            'text.usetex': False,
             'font.family' : 'sans-serif',
             'font.sans-serif' : ['Helvetica'],
            }
        #matplotlib.rcParams.update({'font.size': 18, 'font.family': 'STIXG'
        eneral', 'mathtext.fontset': 'stix'})
        matplotlib.rcParams.update(pylab defaults)
        #matplotlib.rcParams.update({'text.usetex': True})
        import matplotlib.cm as cm
        from IPython.display import Image
        DEBUG = True
        DEBUG = False
        hl, hs = 10*'-', 10*'
In [4]: | tag = 'ICLR'
        datapath = '../../SparseHebbianLearning/database'
        # different runs
        opts = dict(datapath=datapath, verbose=0)
        #opts = dict(cache_dir='cache_dir_cluster', datapath=datapath, verb
        ose=0)
        #opts = dict(cache dir='cache dir ICLR', datapath=datapath, verbose
        =0)
In [5]: from shl_scripts.shl_experiments import SHL
```

shl = SHL(**opts)

data = shl.get data(matname=tag)

spine.set color('none') # don't draw spine

```
In [6]: | shl?
                     SHL
        Type:
        String form: <shl scripts.shl experiments.SHL object at 0x10bb0640
        File:
        ~/science/SparseHebbianLearning/shl scripts/shl experiments.py
        Docstring:
        Base class to define SHL experiments:
            - initialization
            - coding and learning
            visualization
            - quantitative analysis
In [7]: print('number of patches, size of patches = ', data.shape)
        print('average of patches = ', data.mean(), ' +/- ', data.mean(axis
        =1).std())
        SE = np.sqrt(np.mean(data**2, axis=1))
        print('average energy of data = ', SE.mean(), '+/-', SE.std())
        number of patches, size of patches = (65520, 324)
        average of patches = -3.981519488962365e-05 +/- 0.0073902087809
        88323
        average energy of data = 0.2483654920811686 +/- 0.076717536535440
        79
In [8]: #!ls -l {shl.cache dir}/{tag}*
        !ls {shl.cache dir}/{tag}*lock*
        !rm {shl.cache dir}/{tag}*lock*
        #!rm {shl.cache dir}/{tag}*
        #!ls -l {shl.cache dir}/{tag}*
        cache dir/ICLR None eta=0.00030 dico.pkl lock
        cache dir/ICLR None eta=0.00030 dico.pkl lock pid-56154 host-ekla
```

figure 1: Role of homeostasis in learning sparse representations

TODO: cross-validate with 10 different learnings

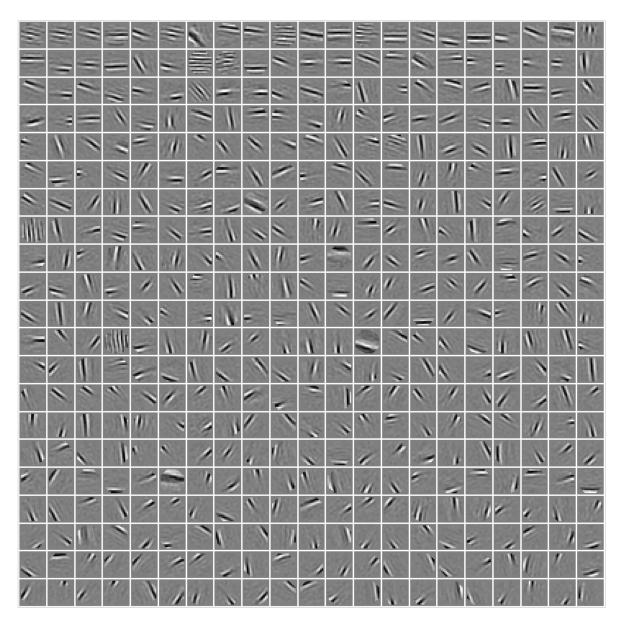
```
In [9]: fname = 'figure_map'
N_cv = 10
one_cv = 0 # picking one to display intermediate results
```

learning

The actual learning is done in a second object (here dico) from which we can access another set of properties and functions (see the shl_learn.py

(https://github.com/bicv/SHL_scripts/blob/master/shl_scripts/shl_learn.py) script):

```
In [10]: homeo methods = ['None', 'OLS', 'HEH']
         list figures = ['show dico', 'time plot error', 'time plot logL', '
         time_plot_MC', 'show_Pcum']
         list_figures = []
         dico = \{\}
         for i cv in range(N cv):
             dico[i cv] = \{\}
             for homeo method in homeo methods:
                 shl = SHL(homeo method=homeo method, seed=seed+i cv, **opts
                 dico[i_cv][homeo_method] = shl.learn_dico(data=data, list_f
         igures=list_figures, matname=tag + '_' + homeo_method + '_seed=' +
         str(seed+i cv))
         list figures = ['show dico']
         for i cv in [one cv]:
             for homeo_method in homeo_methods:
                 print(hl + hs + homeo method[:3] + hs + hl)
                 shl = SHL(homeo method=homeo method, seed=seed+i cv, **opts
                 shl.learn dico(data=data, list figures=list figures, matnam
         e=tag + ' ' + homeo method + '_seed=' + str(seed+i_cv))
                 print('size of dictionary = (number of filters, size of ima
         gelets) = ', dico[i_cv][homeo_method].dictionary.shape)
                 print('average of filters = ', dico[i_cv][homeo_method].di
         ctionary.mean(axis=1).mean(),
                       '+/-', dico[i cv][homeo method].dictionary.mean(axis
         =1).std())
                 SE = np.sqrt(np.sum(dico[i cv][homeo method].dictionary**2,
         axis=1))
                 print('average energy of filters = ', SE.mean(), '+/-', SE.
         std())
                 plt.show()
```

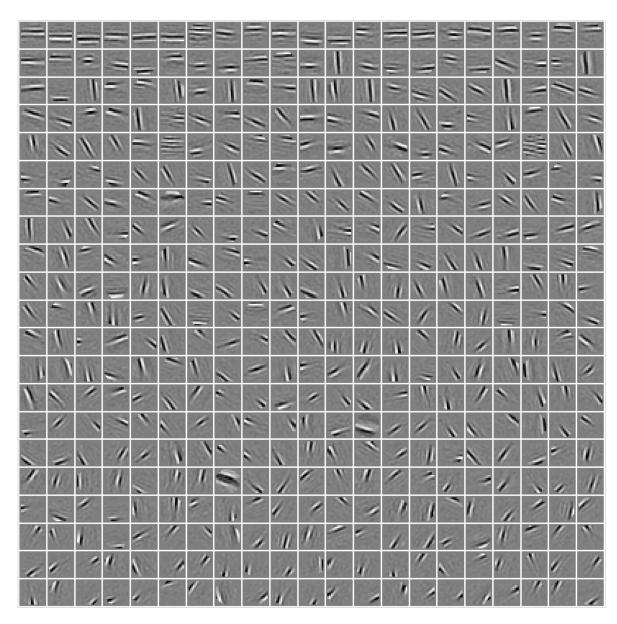


----- OLS -----

size of dictionary = (number of filters, size of imagelets) = (44
1, 324)

average of filters = -3.1258426798939783e-07 +/- 0.0011127198695686763

average energy of filters = 1.0 + /- 3.8488312480383476e-17

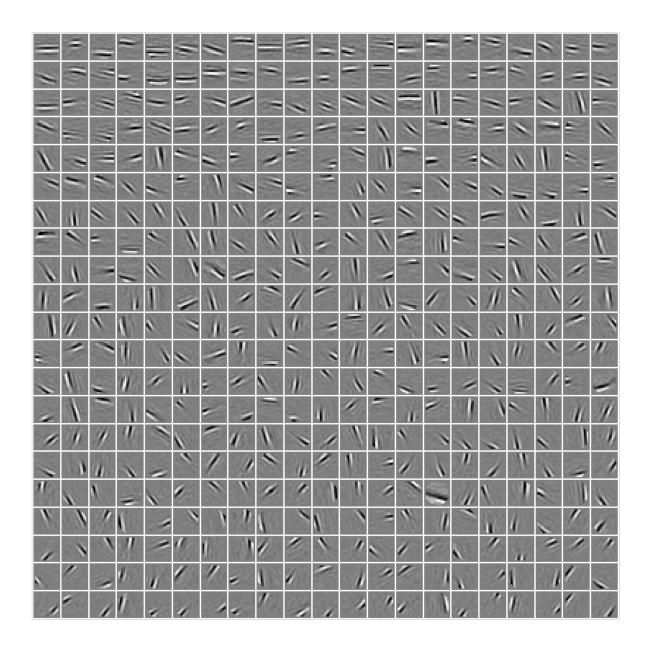


----- НЕН -----

size of dictionary = (number of filters, size of imagelets) = (44
1, 324)

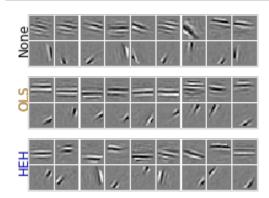
average of filters = 2.9233139706507077e-06 +/- 0.0011063921818456044

average energy of filters = 1.0 + - 4.06084993561207e-17



panel A: plotting some dictionaries

```
In [11]: pname = '/tmp/panel_A' #pname = fname + '_A'
In [12]: from shl_scripts import show_dico
    if DEBUG: show_dico(shl, dico[one_cvi_cv][homeo_method], data=data,
        dim_graph=(2,5))
In [13]: dim_graph = (2, 9)
    colors = ['black', 'orange', 'blue']
    homeo_methods
Out[13]: ['None', 'OLS', 'HEH']
```

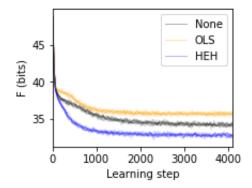


```
In [15]: ### TODO put the p_min an p_max value in the filter map
In [16]: if DEBUG: Image(pname +'.png')
In [17]: if DEBUG: help(fig.subplots_adjust)
In [18]: if DEBUG: help(plt.subplots)
In [19]: if DEBUG: help(matplotlib.gridspec.GridSpec)
```

panel B: quantitative comparison

```
In [20]: pname = '/tmp/panel_B' #fname + '_B'
```

```
In [21]:
        from shl_scripts import time plot
         variable = 'F'
         alpha 0, alpha = .3, .15
         subplotpars = dict(left=0.2, right=.95, bottom=0.2, top=.95)#, wspa
         ce=0.05, hspace=0.05,)
         fig, ax = plt.subplots(1, 1, figsize=(fig width/2, fig width/(1+phi
         )), gridspec kw=subplotpars)
         for i cv in range(N cv):
             for color, homeo method in zip(colors, homeo methods):
                 ax.axis(c='b', lw=2, axisbg='w')
                 ax.set facecolor('w')
                 if i cv==0:
                     fig, ax = time plot(shl, dico[i cv][homeo method], vari
         able=variable, unit='bits', color=color, label=homeo method, alpha=
         alpha_0, fig=fig, ax=ax)
                 else:
                     fig, ax = time plot(shl, dico[i cv][homeo method], vari
         able=variable, unit='bits', color=color, alpha=alpha, fig=fig, ax=a
         x)
                 # ax.set ylabel(homeo method)
                 #ax.text(-8, 7*dim graph[0], homeo method, fontsize=12, col
         or='k', rotation=90)#, backgroundcolor='white'
         ax.legend(loc='best')
         for ext in FORMATS: fig.savefig(pname + ext, dpi=dpi export)
         if DEBUG: Image(pname +'.png')
```

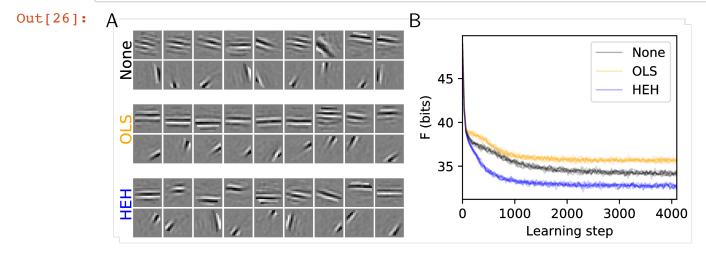


Montage of the subplots

```
In [22]: import tikzmagic
In [23]: %load_ext tikzmagic
In [24]: #DEBUG = True
   if DEBUG: help(tikzmagic)
```

%tikz \draw (0,0) rectangle (1,1);%%tikz --save {fname}.pdf \draw[white, fill=white] (0.\linewidth,0) rectangle (1.\linewidth, .382\linewidth);

```
In [26]: !convert -density {dpi_export} {fname}.pdf {fname}.jpg
!convert -density {dpi_export} {fname}.pdf {fname}.png
#!convert -density {dpi_export} -resize 5400 -units pixelsperinch
-flatten -compress lzw -depth 8 {fname}.pdf {fname}.tiff
Image(fname +'.png')
```



!echo "width="; convert {fname}.tiff -format "%[fx:w]" info: !echo ", \nheight="; convert {fname}.tiff -format "%[fx:h]" info: !echo ", \nunit="; convert {fname}.tiff -format "%U" info:!identify {fname}.tiff

figure 2: Histogram Equalization Homeostasis

```
In [27]: fname = 'figure_HEH'
```

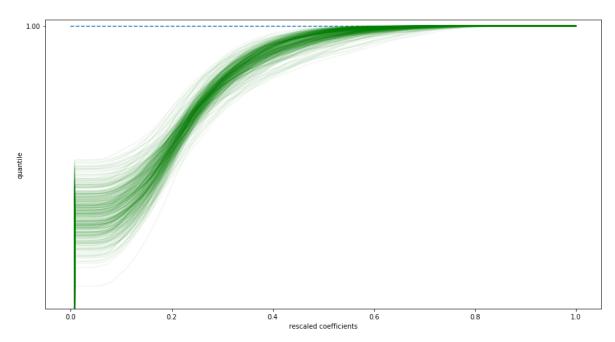
First collecting data:

```
In [28]: list_figures = ['show_Pcum']

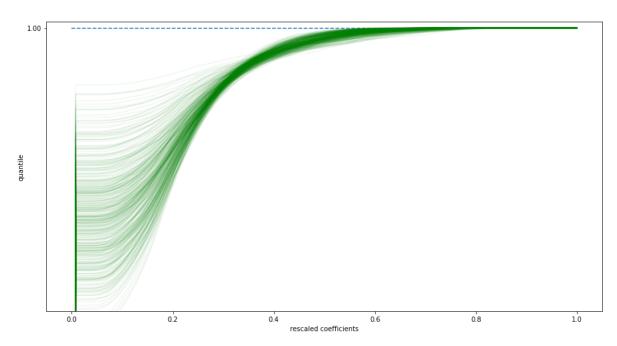
dico = {}

for homeo_method in homeo_methods:
    print(hl + hs + homeo_method + hs + hl)
    shl = SHL(homeo_method=homeo_method, **opts)
    #dico[homeo_method] = shl.learn_dico(data=data, list_figures=list_figures, matname=tag + '_' + homeo_method + '_' + str(one_cv))
    dico[homeo_method] = shl.learn_dico(data=data, list_figures=list_figures, matname=tag + '_' + homeo_method + '_seed=' + str(seed+one_cv))
    plt.show()
```

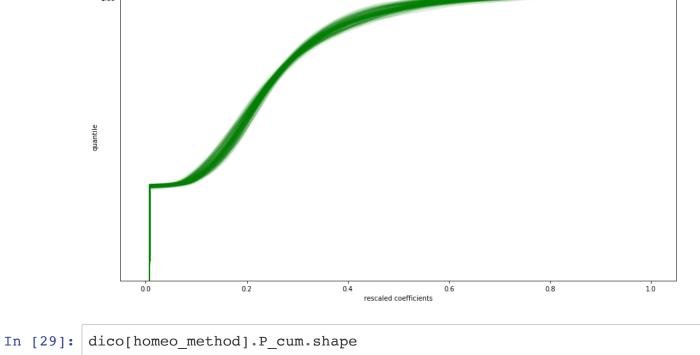
----- None -----



----- OLS ------



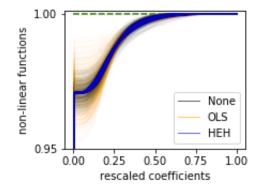
----- HEH -----



```
In [29]: dico[homeo_method].P_cum.shape
Out[29]: (441, 128)
```

panel A: different P_cum

```
In [30]: | pname = '/tmp/panel A' #pname = fname + ' A'
         from shl scripts import plot P cum
         variable = 'F'
         subplotpars = dict(left=0.2, right=.95, bottom=0.2, top=.95)#, wspa
         ce=0.05, hspace=0.05,)
         fig, ax = plt.subplots(1, 1, figsize=(fig width/2, fig width/(1+phi
         )), gridspec kw=subplotpars)
         for color, homeo method in zip(colors, homeo methods):
             ax.axis(c='b', lw=2, axisbg='w')
             ax.set facecolor('w')
             fig, ax = plot_P_cum(dico[homeo_method].P_cum, ymin=0.95, ymax=
         1.001,
                                   title=None, suptitle=None, ylabel='non-lin
         ear functions',
                                  verbose=False, n yticks=21, alpha=.02, c=c
         olor, fig=fig, ax=ax)
             ax.plot([0], [0], lw=1, color=color, label=homeo_method, alpha=
         .6)
             # ax.set ylabel(homeo method)
             #ax.text(-8, 7*dim_graph[0], homeo_method, fontsize=12, color='
         k', rotation=90)#, backgroundcolor='white'
         ax.legend(loc='lower right')
         for ext in FORMATS: fig.savefig(pname + ext, dpi=dpi export)
         if DEBUG: Image(pname +'.png')
```



```
In [31]: if DEBUG: help(fig.legend)
```

panel B: comparing the effects of parameters

```
In [ ]: pname = '/tmp/panel_B' #fname + '_B'

from shl_scripts.shl_experiments import SHL_set

homeo_methods = ['None', 'EMP', 'HAP', 'HEH', 'OLS']

homeo_methods = ['None', 'OLS', 'HEH']

variables = ['eta', 'alpha_homeo', 'eta_homeo', '10_sparseness', 'n_dictionary']
 variables = ['eta', 'alpha_homeo', 'eta_homeo', '10_sparseness']
```

```
variables = ['alpha_homeo', 'eta_homeo']
variables = ['eta', 'alpha_homeo', 'eta_homeo']
variables = ['eta', 'eta_homeo']
list figures = []
bases = [10, 10, 2, 2]
bases = [4, 4, 4, 4]
for homeo method, base in zip(homeo methods, bases):
    opts_ = opts.copy()
    opts .update(homeo method=homeo method)
    experiments = SHL set(opts_, tag=tag + '_' + homeo_method, base
=base)
    experiments.run(variables=variables, n_jobs=1, verbose=0)
import matplotlib.pyplot as plt
subplotpars = dict(left=0.2, right=.95, bottom=0.2, top=.95, wspace
=0.5, hspace=0.35,)
x, y = .05, -.3
if len(variables) == 4:
    fig, axs = plt.subplots(2, 2, figsize=(fig_width/2, fig_width/(
1+phi)), gridspec kw=subplotpars, sharey=True)
    for i ax, variable in enumerate(variables):
        for color, homeo method in zip(colors, homeo methods):
            opts = opts.copy()
            opts .update(homeo method=homeo method)
            experiments = SHL set(opts , tag=tag + ' ' + homeo meth
od)
            ax = axs[i ax%2][i ax//2]
            fig, ax = experiments.scan(variable=variable, list figu
res=[], display='final', fig=fig, ax=ax, color=color, display varia
ble='F', verbose=0) #, label=homeo metho
            ax.set_xlabel('') #variable
            ax.text(x, y, variable, transform=axs[i ax].transAxes)
            #axs[i ax].get xaxis().set major formatter(matplotlib.t
icker.ScalarFormatter())
else:
    fig, axs = plt.subplots(len(variables), 1, figsize=(fig width/2
, fig width/(1+phi)), gridspec kw=subplotpars, sharey=True)
    for i ax, variable in enumerate(variables):
        for color, homeo method in zip(colors, homeo methods):
            opts = opts.copy()
            opts .update(homeo method=homeo method)
            experiments = SHL_set(opts_, tag=tag + '_' + homeo meth
od)
            fig, axs[i ax] = experiments.scan(variable=variable, li
st_figures=[], display='final', fig=fig, ax=axs[i_ax], color=color,
display_variable='F', verbose=0) #, label=homeo_metho
            axs[i ax].set xlabel('') #variable
            axs[i ax].text(x, y, variable, transform=axs[i ax].tra
nsAxes)
```

```
#axs[i_ax].get_xaxis().set_major_formatter(matplotlib.t
icker.ScalarFormatter())

#fig.legend(loc='lower right')
for ext in FORMATS: fig.savefig(pname + ext, dpi=dpi_export)
if DEBUG: Image(pname +'.png')
```

Montage of the subplots

```
In [ ]: !convert -density {dpi_export} {fname}.pdf {fname}.jpg
!convert -density {dpi_export} {fname}.pdf {fname}.png
#!convert -density {dpi_export} -resize 5400 -units pixelsperinch
-flatten -compress lzw -depth 8 {fname}.pdf {fname}.tiff
Image(fname +'.png')
```

!echo "width="; convert {fname}.tiff -format "%[fx:w]" info: !echo ", \nheight="; convert {fname}.tiff -format "%[fx:h]" info: !echo ", \nunit="; convert {fname}.tiff -format "%U" info:!identify {fname}.tiff

figure 3:

learning

```
In [ ]: fname = 'figure_HAP'
```

```
In [ ]: colors = ['orange', 'red', 'green', 'blue']
        homeo methods = ['OLS', 'HEH', 'EMP', 'HAP']
        list figures = []
        dico = \{\}
        for i_cv in range(N_cv):
            dico[i\_cv] = \{\}
            for homeo method in homeo methods:
                shl = SHL(homeo method=homeo method, seed=seed+i cv, **opts
                dico[i cv][homeo method] = shl.learn dico(data=data, list f
        igures=list_figures, matname=tag + '_' + homeo_method + '_seed=' +
        str(seed+i_cv))
        list figures = ['show dico'] if DEBUG else []
        for i cv in [one cv]:
            for homeo method in homeo methods:
                print(hl + hs + homeo method + hs + hl)
                shl = SHL(homeo_method=homeo_method, seed=seed+i_cv, **opts
                shl.learn dico(data=data, list figures=list figures, matnam
        e=tag + '_' + homeo_method + '_seed=' + str(seed+i_cv))
                plt.show()
                print('size of dictionary = (number of filters, size of ima
        gelets) = ', dico[i cv][homeo method].dictionary.shape)
                print('average of filters = ', dico[i_cv][homeo_method].di
        ctionary.mean(axis=1).mean(),
                      '+/-', dico[i_cv][homeo method].dictionary.mean(axis
        =1).std())
                SE = np.sqrt(np.sum(dico[i cv][homeo method].dictionary**2,
        axis=1))
                print('average energy of filters = ', SE.mean(), '+/-', SE.
        std())
```

panel A: plotting some dictionaries

```
In [ ]: pname = '/tmp/panel_A' #pname = fname + '_A'
```

panel B: quantitative comparison

```
In [ ]: | pname = '/tmp/panel_B' #fname + '_B'
In [ ]: from shl_scripts import time plot
        variable = 'F'
        alpha = .3
        subplotpars = dict(left=0.2, right=.95, bottom=0.2, top=.95)#, wspa
        ce=0.05, hspace=0.05,)
        fig, ax = plt.subplots(1, 1, figsize=(fig width/2, fig width/(1+phi
        )), gridspec_kw=subplotpars)
        for i cv in range(N cv):
            for color, homeo_method in zip(colors, homeo_methods):
                ax.axis(c='b', lw=2, axisbg='w')
                ax.set facecolor('w')
                if i cv==0:
                    fig, ax = time plot(shl, dico[i cv][homeo method], vari
        able=variable, unit='bits', color=color, label=homeo method, alpha=
        alpha 0, fig=fig, ax=ax)
                else:
                    fig, ax = time_plot(shl, dico[i_cv][homeo_method], vari
        able=variable, unit='bits', color=color, alpha=alpha, fig=fig, ax=a
        x)
        ax.legend(loc='best')
        for ext in FORMATS: fig.savefig(pname + ext, dpi=dpi export)
        if DEBUG: Image(pname +'.png')
```

Montage of the subplots

In []: if DEBUG: Image(pname +'.png')

```
In [ ]: !convert -density {dpi_export} {fname}.pdf {fname}.jpg
!convert -density {dpi_export} {fname}.pdf {fname}.png
#!convert -density {dpi_export} -resize 5400 -units pixelsperinch
-flatten -compress lzw -depth 8 {fname}.pdf {fname}.tiff
Image(fname +'.png')
```

!echo "width="; convert {fname}.tiff -format "%[fx:w]" info: !echo ", \nheight="; convert {fname}.tiff -format "%[fx:h]" info: !echo ", \nunit="; convert {fname}.tiff -format "%U" info:!identify {fname}.tiff

figure 4: Convolutional Neural Network

```
In [ ]: fname = 'figure_CNN'
```

```
In [ ]: from CHAMP.DataLoader import LoadData
        from CHAMP. DataTools import LocalContrastNormalization, FilterInput
        Data, GenerateMask
        from CHAMP.Monitor import DisplayDico, DisplayConvergenceCHAMP, Dis
        playWhere
        import os
        datapath = os.path.join("/tmp", "database")
        path = os.path.join(datapath, "Raw_DataBase")
        TrSet, TeSet = LoadData('Face', path, decorrelate=False, resize=(65
        , 65))
        # MP Parameters
        nb dico = 20
        width = 9
        dico size = (width, width)
        10 = 20
        seed = 42
        # Learning Parameters
        eta = .05
        nb epoch = 500
        TrSet, TeSet = LoadData('Face', path, decorrelate=False, resize=(65
        , 65))
        N_TrSet, _, _, _ = LocalContrastNormalization(TrSet)
        Filtered L TrSet = FilterInputData(
            N_TrSet, sigma=0.25, style='Custom', start R=15)
        mask = GenerateMask(full size=(nb dico, 1, width, width), sigma=0.8
        , style='Gaussian')
        from CHAMP.CHAMP Layer import CHAMP Layer
        from CHAMP. DataTools import SaveNetwork, LoadNetwork
        homeo methods = ['None', 'HAP']
        for homeo method, eta homeo in zip(homeo methods, [0., 0.0025]):
            ffname = 'cache_dir_CNN/CHAMP_low_' + homeo_method + '.pkl'
            try:
                L1 mask = LoadNetwork(loading path=ffname)
            except:
                L1 mask = CHAMP Layer(10 sparseness=10, nb dico=nb dico,
                                   dico size=dico size, mask=mask, verbose=1
        )
                dico mask = L1 mask.TrainLayer(
                    Filtered_L_TrSet, eta=eta, eta_homeo=eta_homeo, nb_epoc
        h=nb epoch, seed=seed)
                SaveNetwork(Network=L1 mask, saving path=ffname)
```

panel A: plotting some dictionaries

```
In [ ]: pname = '/tmp/panel_A' #pname = fname + '_A'
```

plt.subplots(2, 1, figsize=(fig_width/2, fig_width/(1+phi)), gridspec_kw=subplotpars) for ax, color, homeo_method in zip(axs.ravel(), ['black', 'green'], homeo_methods): ax.axis(c=color, lw=2, axisbg='w') ax.set_facecolor('w') ffname = 'cache_dir/CHAMP_low_' + homeo_method + '.pkl' L1_mask = LoadNetwork(loading_path=ffname) fig, ax = DisplayDico(L1_mask.dictionary, fig=fig, ax=ax) # ax.set_ylabel(homeo_method) ax.text(-8, 7*dim_graph[0], homeo_method, fontsize=12, color=color, rotation=90)#, backgroundcolor='white' for ext in FORMATS: fig.savefig(pname + ext, dpi=dpi_export)

```
subplotpars = dict(left=0.042, right=1., bottom=0., top=1., wspace=
In [ ]:
        0.05, hspace=0.05,)
        for color, homeo method in zip(['black', 'green'], homeo methods):
            #fig, axs = plt.subplots(1, 1, figsize=(fig_width/2, fig_width/
        (1+phi)), gridspec_kw=subplotpars)
            ffname = 'cache dir CNN/CHAMP low ' + homeo method + '.pkl'
            L1 mask = LoadNetwork(loading path=ffname)
            fig, ax = DisplayDico(L1 mask.dictionary)
            # ax.set ylabel(homeo method)
            #for ax in list(axs):
                 ax.axis(c=color, lw=2, axisbg='w')
                 ax.set_facecolor('w')
            ax[0].text(-4, 3, homeo method, fontsize=8, color=color, rotati
        on=90)#, backgroundcolor='white'
            plt.tight layout( pad=0., w pad=0., h pad=.0)
            for ext in FORMATS: fig.savefig(pname + '_' + homeo_method + ex
        t, dpi=dpi export)
```

panel B: quantitative comparison

```
In [ ]: pname = '/tmp/panel_B' #fname + '_B'
```

from shl_scripts import time_plot variable = 'F' alpha = .3 subplotpars = dict(left=0.2, right=.95, bottom=0.2, top=.95)#, wspace=0.05, hspace=0.05,) fig, axs = plt.subplots(2, 1, figsize=(fig_width/2, fig_width/(1+phi)), gridspec_kw=subplotpars) for ax, color, homeo_method in zip(axs, ['black', 'green'], homeo_methods): print(ax, axs) ffname = 'cache_dir_CNN/CHAMP_low_' + homeo_method + '.pkl' L1_mask = LoadNetwork(loading_path=ffname) fig, ax = DisplayConvergenceCHAMP(L1_mask, to_display=['histo'], fig=fig, ax=ax) ax.axis(c=color, lw=2, axisbg='w') ax.set_facecolor('w') # ax.set_ylabel(homeo_method) #ax.text(-8, 7*dim_graph[0], homeo_method, fontsize=12, color=color, rotation=90)#, backgroundcolor='white' for ext in FORMATS: fig.savefig(pname + ext, dpi=dpi_export) if DEBUG: Image(pname +'.png')

```
In [ ]: | from shl_scripts import time plot
        variable = 'F'
        alpha = .3
        subplotpars = dict(left=0.2, right=.95, bottom=0.2, top=.95)#, wspa
        ce=0.05, hspace=0.05,)
        for color, homeo_method in zip(['black', 'green'], homeo methods):
            #fig, axs = plt.subplots(1, 1, figsize=(fig width/2, fig width/
        (1+phi)), gridspec kw=subplotpars)
            ffname = 'cache dir CNN/CHAMP low ' + homeo method + '.pkl'
            L1 mask = LoadNetwork(loading path=ffname)
            fig, ax = DisplayConvergenceCHAMP(L1_mask, to_display=['histo']
        , color=color)
            ax.axis(c=color, lw=2, axisbg='w')
            ax.set facecolor('w')
            ax.set ylabel('counts')
            ax.set_xlabel('feature #')
            ax.set_ylim(0, 560)
            #ax.text(-8, 7*dim_graph[0], homeo_method, fontsize=12, color=c
        olor, rotation=90)#, backgroundcolor='white'
            #ax[0].text(-8, 3, homeo_method, fontsize=12, color=color, rota
        tion=90)#, backgroundcolor='white'
            for ext in FORMATS: fig.savefig(pname + '_' + homeo_method + ex
        t, dpi=dpi_export)
            if DEBUG: Image(pname +'.png')
```

Montage of the subplots

```
In [ ]: %ls -ltr /tmp/panel_*
In [ ]: fname
In [ ]: 382+191
```

```
In []: |% tikz -f pdf --save {fname}.pdf
        \draw[white, fill=white] (0.\linewidth,0) rectangle (1.\linewidth,
        .382\linewidth);
        \draw [anchor=north west] (.0\linewidth, .375\linewidth) node {\inc
        ludegraphics[width=.95\linewidth]{/tmp/panel_A_None}};
        \draw [anchor=north west] (.0\linewidth, .300\linewidth) node {\inc
        ludegraphics[width=.95\linewidth]{/tmp/panel A HAP}};
        \draw [anchor=north west] (.0\linewidth, .191\linewidth) node {\inc
        ludegraphics[width=.45\linewidth]{/tmp/panel B None}};
        \draw [anchor=north west] (.5\linewidth, .191\linewidth) node {\inc
        ludegraphics[width=.45\linewidth]{/tmp/panel B HAP}};
        \begin{scope}[font=\bf\sffamily\large]
        %\draw [anchor=west,fill=white] (.0\linewidth, .382\linewidth) node
        [above right=-3mm] {$\mathsf{A}}$;
        \draw [anchor=west, fill=white] (.0\linewidth, .191\linewidth) node
        [above right=-3mm] {$\mathsf{A}}$;
        \draw [anchor=west, fill=white] (.53\linewidth, .191\linewidth) node
        [above right=-3mm] {$\mathsf{B}$};
        \end{scope}
```

```
In [ ]: !convert -density {dpi_export} {fname}.pdf {fname}.jpg
!convert -density {dpi_export} {fname}.pdf {fname}.png
#!convert -density {dpi_export} -resize 5400 -units pixelsperinch
-flatten -compress lzw -depth 8 {fname}.pdf {fname}.tiff
Image(fname +'.png')
```

!echo "width="; convert {fname}.tiff -format "%[fx:w]" info: !echo ", \nheight="; convert {fname}.tiff -format "%[fx:h]" info: !echo ", \nunit="; convert {fname}.tiff -format "%U" info:!identify {fname}.tiff

coding

The learning itself is done via a gradient descent but is highly dependent on the coding / decoding algorithm. This belongs to a another function (in the shl encode.py

(https://github.com/bicv/SHL_scripts/blob/master/shl_scripts/shl_encode.py) script)

Supplementary controls

starting a learning

getting help

```
In [ ]: help(shl)
In [ ]: help(dico)
```

loading a database

Loading patches, with or without mask:

```
In [ ]: N_patches = 12
    from shl_scripts.shl_tools import show_data
        opts_ = opts.copy()
        opts_.update(verbose=0)
        for i, (do_mask, label) in enumerate(zip([False, True], ['Without m ask', 'With mask'])):
            data_ = SHL(DEBUG_DOWNSCALE=1, N_patches=N_patches, n_image=1,
            do_mask=do_mask, seed=seed, **opts_).get_data()
            fig, axs = show_data(data_)
            axs[0].set_ylabel(label);
            plt.show()
```

Testing different algorithms

Testing two different dictionary initalization strategies

White Noise Initialization + Learning

```
In [ ]: shl = SHL(one_over_F=False, **opts)
    dico_w = shl.learn_dico(data=data, matname=tag + '_WHITE', list_fig
    ures=[])
    shl = SHL(one_over_F=True, **opts)
    dico_loF = shl.learn_dico(data=data, matname=tag + '_OVF', list_fig
    ures=[])
    fig_error, ax_error = None, None
    fig_error, ax_error = shl.time_plot(dico_w, variable='F', fig=fig_e
    rror, ax=ax_error, color='blue', label='white noise')
    fig_error, ax_error = shl.time_plot(dico_loF, variable='F', fig=fig
    _error, ax=ax_error, color='red', label='one over f')
    #ax_error.set_ylim((0, .65))
    ax_error.legend(loc='best')
```

Testing two different learning rates strategies

We use by defaut the strategy of ADAM, see https://arxiv.org/pdf/1412.6980.pdf (https://arxiv.org/pdf/1412.6980.pdf

Testing different number of neurons and sparsity

As suggested by AnonReviewer3, we have tested how the convergence was modified by changing the number of neurons. By comparing different numbers of neurons we could re-draw the same figures for the convergence of the algorithm as in our original figures. In addition, we have also checked that this result will hold on a range of sparsity levels. In particular, we found that in general, increasing the 10_sparseness parameter, the convergence took progressively longer. Importantly, we could see that in both cases, this did not depend on the kind of homeostasis heuristic chosen, proving the generality of our results.

This is shown in the supplementary material that we have added to our revision ("Testing different number of neurons and sparsity"). This useful extension proves the originality of our work as highlighted in point 4, and the generality of these results compared to the parameters of the network.

```
In [ ]: from shl_scripts.shl_experiments import SHL set
        homeo_methods = ['None', 'OLS', 'HEH']
        homeo_methods = ['None', 'EMP', 'HAP', 'HEH', 'OLS']
        variables = ['10_sparseness', 'n_dictionary']
        list figures = []
        #n dictionary=21**2
        for homeo method in homeo methods:
            opts = opts.copy()
            opts .update(homeo_method=homeo_method, datapath=datapath)
            experiments = SHL_set(opts_, tag=tag + '_' + homeo_method)
            experiments.run(variables=variables, n jobs=1, verbose=0)
        fig, axs = plt.subplots(len(variables), 1, figsize=(fig width/2, fi
        g width/(1+phi)), gridspec kw=subplotpars, sharey=True)
        for i ax, variable in enumerate(variables):
            for color, homeo method in zip(colors, homeo methods):
                opts = opts.copy()
                opts .update(homeo method=homeo method, datapath=datapath)
                experiments = SHL set(opts , tag=tag + ' ' + homeo method)
                fig, axs[i ax] = experiments.scan(variable=variable, list f
        igures=[], display='final', fig=fig, ax=axs[i_ax], color=color, dis
        play_variable='F', verbose=0) #, label=homeo_metho
                axs[i_ax].set_xlabel('') #variable
                axs[i_ax].text(.1, .8, variable, transform=axs[i ax].trans
        Axes)
                #axs[i ax].get xaxis().set major formatter(matplotlib.ticke
        r.ScalarFormatter())
```

Perspectives

Convolutional neural networks

Training on a face database

```
In [ ]: # MP Parameters
        nb dico = 20
        width = 9
        dico size = (width, width)
        10 = 20
        seed = 42
        # Learning Parameters
        eta = .05
        nb epoch = 500
        TrSet, TeSet = LoadData('Face', path, decorrelate=False, resize=(65)
        , 65))
        N_TrSet, _, _, _ = LocalContrastNormalization(TrSet)
        Filtered L TrSet = FilterInputData(
            N TrSet, sigma=0.25, style='Custom', start R=15)
        to display = Filtered L TrSet[0][0, 0:10, :, :, :]
        DisplayDico(to display)
        mask = GenerateMask(full size=(nb dico, 1, width, width), sigma=0.8
        , style='Gaussian')
        DisplayDico(mask)
```

Training the ConvMP Layer with homeostasis

Training the ConvMP Layer with homeostasis

```
In [ ]: fname = 'cache dir CNN/CHAMP low HAP.pkl'
        try:
            L1 mask = LoadNetwork(loading path=fname)
        except:
            # Learning Parameters
            eta homeo = 0.0025
            L1 mask = CHAMP Layer(10 sparseness=10, nb dico=nb dico,
                                   dico size=dico size, mask=mask, verbose=1
        )
            dico mask = L1 mask.TrainLayer(
                Filtered L TrSet, eta=eta, eta homeo=eta homeo, nb epoch=nb
        _epoch, seed=seed)
            SaveNetwork(Network=L1 mask, saving path=fname)
        DisplayDico(L1 mask.dictionary)
        DisplayConvergenceCHAMP(L1_mask, to_display=['error', 'histo'])
        DisplayWhere(L1 mask.where)
```

Reconstructing the input image

```
In [ ]: from CHAMP.DataTools import Rebuilt
    import torch
    rebuilt_image = Rebuilt(torch.FloatTensor(L1_mask.code), L1_mask.di
    ctionary)
    DisplayDico(rebuilt_image[0:10, :, :, :])
```

Training the ConvMP Layer with higher-level filters

We train higher-level feature vectors by forcing the network to:

- learn bigger filters,
- represent the information using a bigger dictionary (higher sparseness)
- represent the information with less features (higher sparseness)

```
In [ ]: fname = 'cache dir CNN/CHAMP high None.pkl'
            L1 mask = LoadNetwork(loading path=fname)
        except:
            nb dico = 60
            width = 19
            dico size = (width, width)
            10 = 5
            mask = GenerateMask(full size=(nb dico, 1, width, width), sigma
        =0.8, style='Gaussian')
            # Learning Parameters
            eta homeo = 0.0
            eta = .05
            nb epoch = 500
            # learn
            L1_mask = CHAMP_Layer(10_sparseness=10, nb_dico=nb dico,
                                   dico size=dico size, mask=mask, verbose=0
        )
            dico mask = L1 mask.TrainLayer(
                Filtered L TrSet, eta=eta, eta homeo=eta homeo, nb epoch=nb
        _epoch, seed=seed)
            SaveNetwork(Network=L1 mask, saving path=fname)
        DisplayDico(L1_mask.dictionary)
        DisplayConvergenceCHAMP(L1 mask, to display=['error'])#, 'histo'])
        DisplayWhere(L1 mask.where)
```

```
In [ ]: | fname = 'cache_dir_CNN/CHAMP high HAP.pkl'
            L1 mask = LoadNetwork(loading path=fname)
        except:
            nb dico = 60
            width = 19
            dico size = (width, width)
            10 = 5
            mask = GenerateMask(full size=(nb dico, 1, width, width), sigma
        =0.8, style='Gaussian')
            # Learning Parameters
            eta homeo = 0.0025
            eta = .05
            nb epoch = 500
            # learn
            L1 mask = CHAMP Layer(10 sparseness=10, nb dico=nb dico,
                                   dico_size=dico_size, mask=mask, verbose=0
        )
            dico mask = L1 mask.TrainLayer(
                Filtered L TrSet, eta=eta, eta homeo=eta homeo, nb epoch=nb
        epoch, seed=seed)
            SaveNetwork(Network=L1 mask, saving path=fname)
        DisplayDico(L1 mask.dictionary)
        DisplayConvergenceCHAMP(L1_mask, to_display=['error'])#, 'histo'])
        DisplayWhere(L1 mask.where)
```

Training on MNIST database

fname = 'cache_dir_CNN/CHAMP_MNIST_HAP.pkl' try: L1_mask = LoadNetwork(loading_path=fname) except: path = os.path.join(datapath, "MNISTtorch") TrSet, TeSet = LoadData('MNIST', data_path=path) N_TrSet, _, _, _ = LocalContrastNormalization(TrSet) Filtered_L_TrSet = FilterInputData(N_TrSet, sigma=0.25, style='Custom', start_R=15) nb_dico = 60 width = 7 dico_size = (width, width) I0 = 15 # Learning Parameters eta_homeo = 0.0025 eta = .05 nb_epoch = 500 # learn L1_mask = CHAMP_Layer(I0_sparseness=I0, nb_dico=nb_dico, dico_size=dico_size, mask=mask, verbose=2) dico_mask = L1_mask.TrainLayer(Filtered_L_TrSet, eta=eta, eta_homeo=eta_homeo, nb_epoch=nb_epoch, seed=seed) SaveNetwork(Network=L1_mask, saving_path=fname) DisplayDico(L1_mask.dictionary) DisplayConvergenceCHAMP(L1_mask, to_display=['error', 'histo']) DisplayWhere(L1_mask.where)

Computational details

caching simulation data

A convenience script to run and cache most learning items in this notebooks:

```
In [ ]: |!ls -l {shl.cache dir}/{tag}*
        #!rm {shl.cache dir}/{tag}*lock*
        #!rm {shl.cache dir}/{tag}*
        #!ls -l {shl.cache dir}/{tag}*
In [ ]: | %%writefile model.py
        #!/usr/bin/env python3
        # -*- coding: utf-8 -*
        tag = 'ICLR'
        from shl scripts.shl experiments import SHL, prun
        # pre-loading data
        datapath = '../../SparseHebbianLearning/database'
        # different runs
        #opts = dict(cache dir='cache dir ICLR', datapath=datapath, verbose
        #opts = dict(cache dir='cache dir cluster', datapath=datapath, verb
        opts = dict(datapath=datapath, verbose=0)
        shl = SHL(**opts)
        data = shl.get data(matname=tag)
        # running main simulations
        # Figure 1 & 3
        N cv = 10
        homeo methods = ['None', 'OLS', 'HEH', 'HAP', 'EMP']
        seed = 42
        # running in parallel on a multi-core machine
        import sys
        try:
            n_jobs = int(sys.argv[1])
            print('n_jobs=', n_jobs)
        except:
            n jobs = 4
            n jobs = 9
            n jobs = 10
            n jobs = 1
            n jobs = 35
        if n jobs>0:
            list figures = []
            from shl scripts.shl experiments import SHL set
            for homeo_method in homeo_methods:
                opts_ = opts.copy()
                 opts .update(homeo method=homeo method)
                 experiments = SHL set(opts , tag=tag + ' ' + homeo method,
        N scan=N cv)
                experiments.run(variables=['seed'], n_jobs=n_jobs, verbose=
        0)
            # Figure 2-B
            variables = ['eta', 'alpha_homeo', 'eta_homeo']
```

```
variables = ['eta', 'eta_homeo', '10_sparseness', 'n_dictionary
' 1
   bases = [10, 10, 2, 2]
    for homeo method, base in zip(homeo methods, bases):
        opts = opts.copy()
        opts .update(homeo method=homeo method)
        experiments = SHL_set(opts_, tag=tag + '_' + homeo_method,
base=base)
        experiments.run(variables=variables, n jobs=n jobs, verbose
=0)
   # Annex X.X
    shl = SHL(**opts)
    dico = shl.learn dico(data=data, list figures=list figures, mat
name=tag + ' vanilla')
    for algorithm in ['lasso lars', 'lasso cd', 'lars', 'elastic',
'omp', 'mp']: # 'threshold',
        opts_ = opts.copy()
        opts .update(homeo method='None', learning algorithm=algori
thm, verbose=0)
        shl = SHL(**opts)
        dico= shl.learn dico(data=data, list figures=[],
                       matname=tag + ' - algorithm={}'.format(algor
ithm))
    for homeo_method in ['None', 'HAP']:
        for algorithm in ['lasso_lars', 'lars', 'elastic', 'omp', '
mp']: # 'threshold', 'lasso cd',
            opts = opts.copy()
            opts .update(homeo method=homeo method, learning algori
thm=algorithm, verbose=0)
            shl = SHL(**opts )
            dico= shl.learn dico(data=data, list figures=[],
                           matname=tag + ' - algorithm={}'.format(a
lgorithm) + ' - homeo method={}'.format(homeo method))
    shl = SHL(one over F=False, **opts)
    dico w = shl.learn dico(data=data, matname=tag + ' WHITE', list
figures=[])
    shl = SHL(one over F=True, **opts)
    dico 1oF = shl.learn dico(data=data, matname=tag + ' OVF', list
figures=[])
    shl = SHL(beta1=0., **opts)
    dico fixed = shl.learn dico(data=data, matname=tag + ' fixed',
list figures=[])
    shl = SHL(**opts)
    dico default = shl.learn dico(data=data, matname=tag + ' defaul
t', list figures=[])
```

Version used

```
In [ ]: %load_ext version_information
%version_information numpy, shl_scripts
```

version control

```
In [ ]: !git status
In [ ]: !git pull
In [ ]: !git commit -am' {tag} : re-running notebooks'
In [ ]: !git push
```

exporting the notebook

```
In [ ]: !jupyter nbconvert Annex.ipynb
In [ ]: #!jupyter-nbconvert --template report --to pdf Annex.ipynb
In [ ]: !pandoc Annex.html -o Annex.pdf
In [ ]: !zip Annex.zip Annex.html
```

Done. Thanks for your attention!