

Annex

This supplementary information presents :

- first, the code to generate the figures from the paper,
- second, some control experiments that were mentionned in the paper,
- finally, some perspectives for future work inspired by the algorithms presented in the paper.

Figures for "An adaptive algorithm for unsupervised learning"¶

In [1]:

```
%load_ext autoreload
%autoreload 2
```

In [2]:

```
import numpy as np
np.set_printoptions(precision=2, suppress=True)
seed = 42
np.random.seed(seed)
```

In [3]:

```
# some overhead for the formatting of figures
import matplotlib.pyplot as plt
```

```
fontsize = 12
FORMATS = ['.pdf', '.eps', '.png', '.tiff']
FORMATS = ['.pdf', '.png']
dpi_export = 600
```

```
fig_width_pt = 318.670 # Get this from LaTeX using \showthe\columnwidth
fig_width_pt = 450 # Get this from LaTeX using \showthe\columnwidth
#fig_width_pt = 1024 #221 # Get this from LaTeX using \showthe\columnwidth / x264 asks 1
ppi = 72.27 # (constant) definition of the ppi = points per inch
inches_per_pt = 1.0/ppi # Convert pt to inches
```

```

#inches_per_cm = 1./2.54
fig_width = fig_width_pt*inches_per_pt # width in inches
grid_fig_width = 2*fig_width
phi = (np.sqrt(5) + 1. ) /2
#legend.fontsize = 8
#fig_width = 9
fig_height = fig_width/phi
figsize = (fig_width, fig_height)

def adjust_spines(ax, spines):
    for loc, spine in ax.spines.items():
        if loc in spines:
            spine.set_position(('outward', 10)) # outward by 10 points
            spine.set_smart_bounds(True)
        else:
            spine.set_color('none') # don't draw spine

    # turn off ticks where there is no spine
    if 'left' in spines:
        ax.yaxis.set_ticks_position('left')
    else:
        # no yaxis ticks
        ax.yaxis.set_ticks([])

    if 'bottom' in spines:
        ax.xaxis.set_ticks_position('bottom')
    else:
        # no xaxis ticks
        ax.xaxis.set_ticks([])

import matplotlib
pylab_defaults = {
    'font.size': 10,
    'xtick.labelsize': 'medium',
    'ytick.labelsize': 'medium',
    'text.usetex': False,
    # 'font.family' : 'sans-serif',
    # 'font.sans-serif' : ['Helvetica'],
}

#matplotlib.rcParams.update({'font.size': 18, 'font.family': 'STIXGeneral', 'mathtext.fonts
matplotlib.rcParams.update(pylab_defaults)
#matplotlib.rcParams.update({'text.usetex': True})

import matplotlib.cm as cm

```

```

from IPython.display import Image

DEBUG = True
DEBUG = False
hl, hs = 10*'-', 10*' '

In [4]:
tag = 'ICLR'
datapath = '../..SparseHebbianLearning/database'

# different runs
#opts = dict(eta=0.007, eta_homeo=0.02, alpha_homeo=.5, cache_dir='cache_dir_1100', datapath=datapath)
#opts = dict(eta=0.007, eta_homeo=0.02, alpha_homeo=.08, cache_dir='cache_dir_1900', datapath=datapath)
#opts = dict(eta=0.007, eta_homeo=0.005, alpha_homeo=5., cache_dir='cache_dir_1700', datapath=datapath)
#opts = dict(eta=0.0033, eta_homeo=0.05, alpha_homeo=.5, cache_dir='cache_dir_frioul', datapath=datapath)
#opts = dict(eta=0.007, eta_homeo=0.005, alpha_homeo=5., cache_dir='cache_dir', datapath=datapath)
opts = dict(eta=0.0033, eta_homeo=0.05, alpha_homeo=2.5, cache_dir='cache_dir_42', datapath=datapath)

In [5]:
from shl_scripts.shl_experiments import SHL
shl = SHL(**opts)
data = shl.get_data(matname=tag)

In [6]:
print('number of patches, size of patches = ', data.shape)
print('average of patches = ', data.mean(), ' +/- ', data.mean(axis=1).std())
SE = np.sqrt(np.mean(data**2, axis=1))
print('average energy of data = ', SE.mean(), '+/-', SE.std())

number of patches, size of patches = (65520, 324)
average of patches = 1.6601716040762679e-19 +/- 0.009395020606115053
average energy of data = 0.30840286225885366 +/- 0.08622704306730453

!ls -l {shl.cache_dir}/{tag}* #!rm {shl.cache_dir}/{tag}*lock* #!rm
{shl.cache_dir}/{tag}* #!ls -l {shl.cache_dir}/{tag}*

```

figure 1: Role of homeostasis in learning sparse representations¶

TODO : cross-validate with 10 different learnings¶

```

In [7]:
fname = 'figure_map'
N_cv = 10
one_cv = 0 # picking one to display intermediate results

```

learning¶

The actual learning is done in a second object (here `dico`) from which we can access another set of properties and functions (see the `shl_learn.py` script):

In [8]:

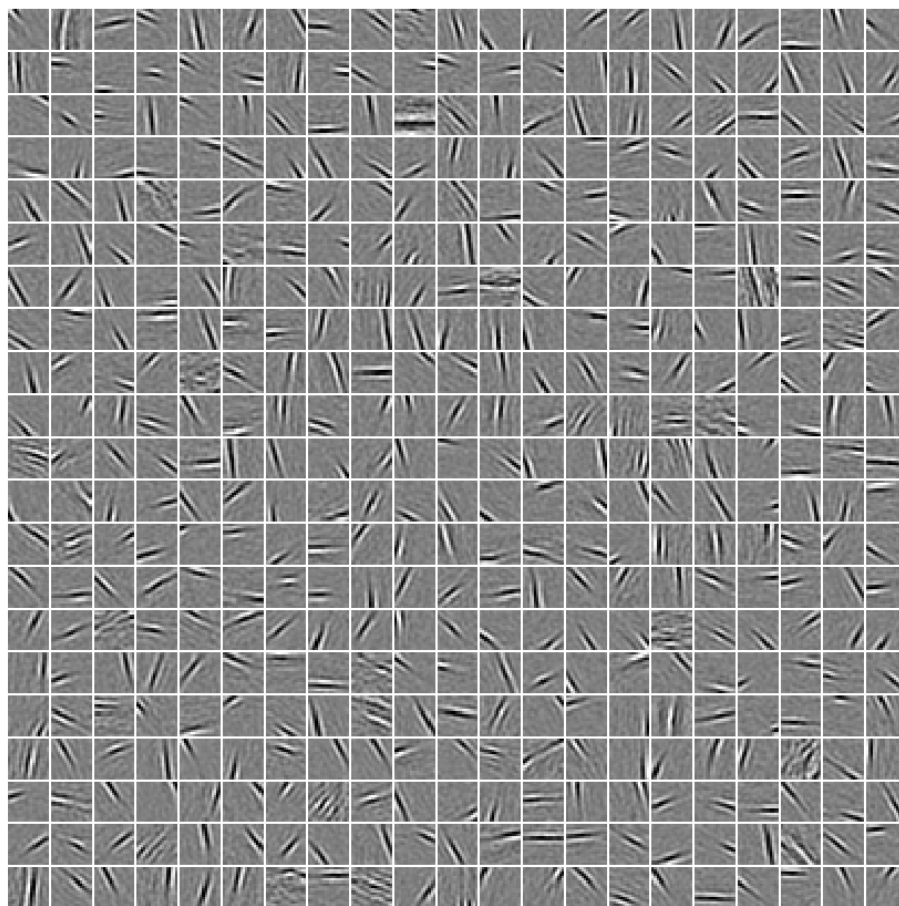
```
homeo_methods = ['None', 'OLS', 'HEH']

list_figures = ['show_dico', 'time_plot_error', 'time_plot_logL', 'time_plot_MC', 'show_Pcur']
list_figures = []
dico = {}
for i_cv in range(N_cv):
    dico[i_cv] = {}
    for homeo_method in homeo_methods:
        shl = SHL(homeo_method=homeo_method, seed=seed+i_cv, **opts)
        dico[i_cv][homeo_method] = shl.learn_dico(data=data, list_figures=list_figures, matname=tag + '_' + homeo_method)

list_figures = ['show_dico']
for i_cv in [one_cv]:
    for homeo_method in homeo_methods:
        print(hl + hs + homeo_method[:3] + hs + hl)
        shl = SHL(homeo_method=homeo_method, seed=seed+i_cv, **opts)
        shl.learn_dico(data=data, list_figures=list_figures, matname=tag + '_' + homeo_method)

        print('size of dictionary = (number of filters, size of imagelets) = ', dico[i_cv][homeo_method].dictionary.shape)
        print('average of filters = ', dico[i_cv][homeo_method].dictionary.mean(axis=1).mean())
        print(' +/- ', dico[i_cv][homeo_method].dictionary.mean(axis=1).std())
        SE = np.sqrt(np.sum(dico[i_cv][homeo_method].dictionary**2, axis=1))
        print('average energy of filters = ', SE.mean(), ' +/- ', SE.std())
        plt.show()

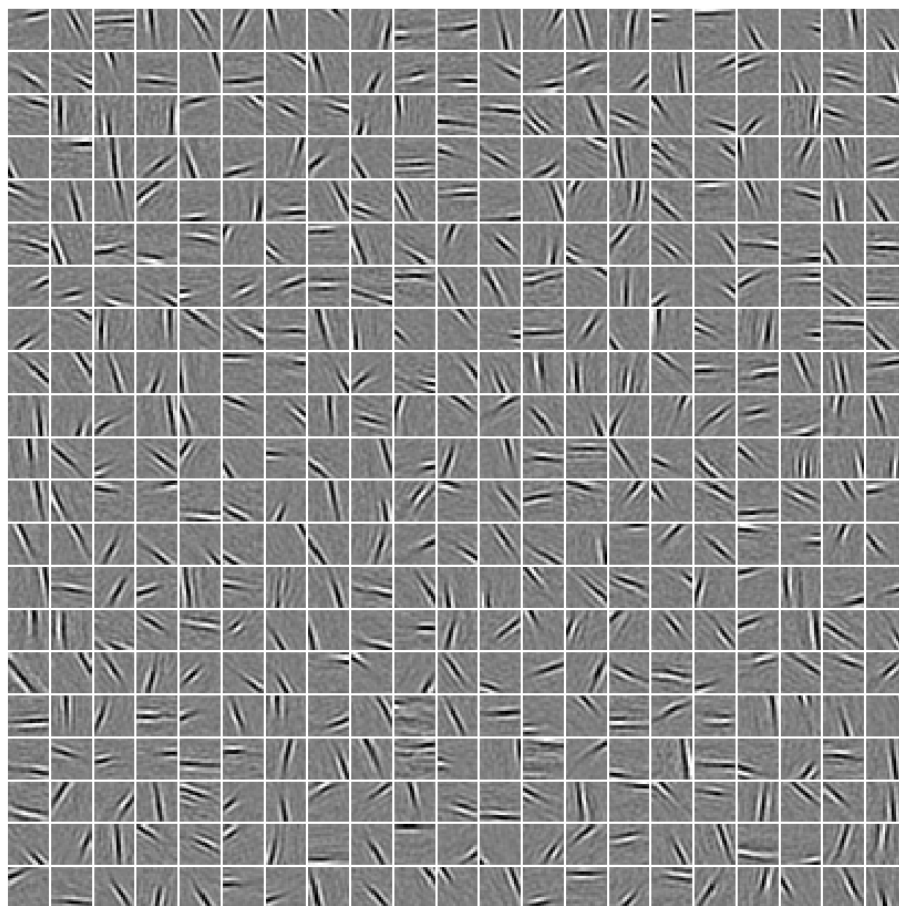
----- Non -----
size of dictionary = (number of filters, size of imagelets) = (441, 324)
average of filters = -8.681523664810371e-06 +/- 0.0010856202387987371
average energy of filters = 1.0 +/- 4.698989566404069e-17
```



```

-----      OLS      -----
size of dictionary = (number of filters, size of imagelets) = (441, 324)
average of filters = 1.4204508020925339e-05 +/- 0.0011077610780090214
average energy of filters = 1.0 +/- 3.991428581974025e-17

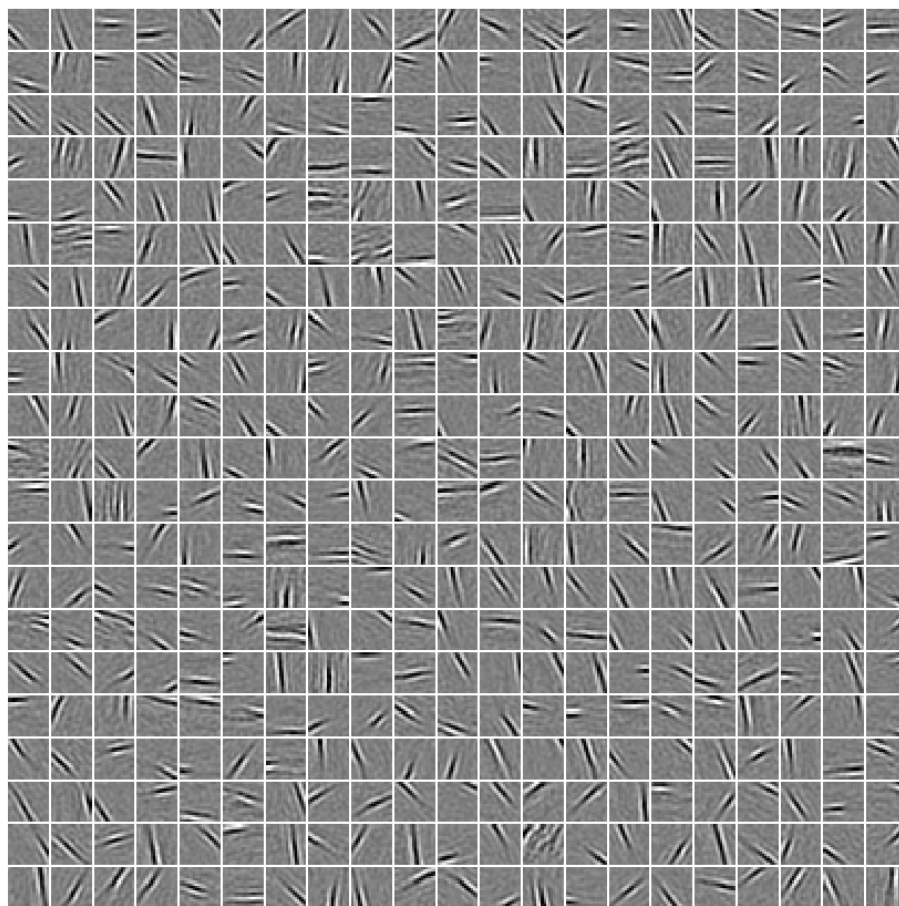
```



```

-----      HEH      -----
size of dictionary = (number of filters, size of imagelets) = (441, 324)
average of filters = -7.478164618956859e-06 +/- 0.0010812190907883345
average energy of filters = 1.0 +/- 3.738315377818512e-17

```



panel A: plotting some dictionaries¶

In [9]:

```
pname = '/tmp/panel_A' #pname = fname + '_A'
```

In [10]:

```
from shl_scripts import show_dico
if DEBUG: show_dico(shl, dico[one_cvi_cv][homeo_method], dim_graph=(2,5))
```

In [11]:

```
dim_graph = (2, 9)
colors = ['black', 'orange', 'blue']
homeo_methods
```

Out[11]:

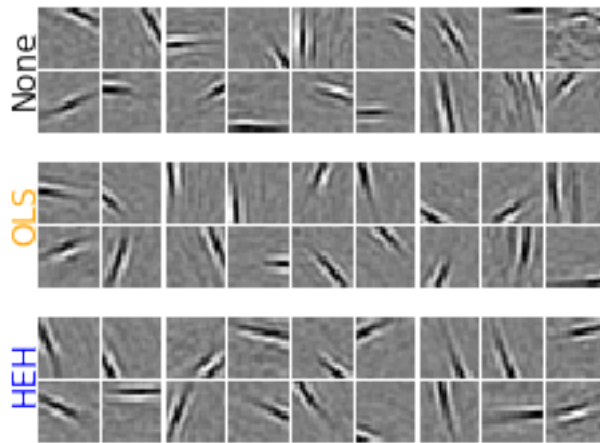
```
['None', 'OLS', 'HEH']
```

```
In [12]:
```

```
subplotpars = dict( left=0.042, right=1., bottom=0., top=1., wspace=0.05, hspace=0.05,)
fig, axs = plt.subplots(3, 1, figsize=(fig_width/2, fig_width/(1+phi)), gridspec_kw=subplotpars)

for ax, color, homeo_method in zip(axs.ravel(), colors, homeo_methods):
    ax.axis(c=color, lw=2, axisbg='w')
    ax.set_facecolor('w')
    fig, ax = show_dico(shl, dico[one_cv][homeo_method], dim_graph=dim_graph, seed=194, fig=fig)
    # ax.set_ylabel(homeo_method)
    ax.text(-8, 7*dim_graph[0], homeo_method, fontsize=12, color=color, rotation=90)#, backgroundcolor='w')

for ext in FORMATS: fig.savefig(pname + ext, dpi=dpi_export)
```



```
In [13]:
```

```
if DEBUG: Image(pname + '.png')
```

```
In [14]:
```

```
if DEBUG: help(fig.subplots_adjust)
```

```
In [15]:
```

```
if DEBUG: help(plt.subplots)
```

```
In [16]:
```

```
if DEBUG: help(matplotlib.gridspec.GridSpec)
```

panel B: quantitative comparison¶

```
In [17]:
```



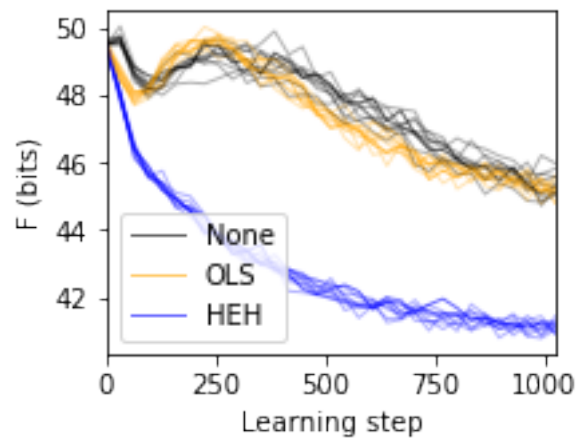
```

pname = '/tmp/panel_B' #fname + '_B'

In [18]:

from shl_scripts import time_plot
variable = 'F'
alpha = .3
subplotspars = dict(left=0.2, right=.95, bottom=0.2, top=.95)#, wspace=0.05, hspace=0.05,)
fig, ax = plt.subplots(1, 1, figsize=(fig_width/2, fig_width/(1+phi)), gridspec_kw=subplotspars)
for i_cv in range(N_cv):
    for color, homeo_method in zip(colors, homeo_methods):
        ax.axis(c='b', lw=2, axisbg='w')
        ax.set_facecolor('w')
        if i_cv==0:
            fig, ax = time_plot(shl, dico[i_cv][homeo_method], variable=variable, unit='bits')
        else:
            fig, ax = time_plot(shl, dico[i_cv][homeo_method], variable=variable, unit='bits')
        # ax.set_ylabel(homeo_method)
        #ax.text(-8, 7*dim_graph[0], homeo_method, fontsize=12, color='k', rotation=90)#, ba
ax.legend(loc='best')
for ext in FORMATS: fig.savefig(pname + ext, dpi=dpi_export)
if DEBUG: Image(pname + '.png')

```



Montage of the subplots¶

```

In [19]:

import tikzmagic

In [20]:

%load_ext tikzmagic

```

In [21]:

```
#DEBUG = True
if DEBUG: help(tikzmagic)

%tikz \draw (0,0) rectangle (1,1);%%tikz --save {fname}.pdf \draw[white,
fill=white] (0.\linewidth,0) rectangle (1.\linewidth, .382\linewidth) ;
```

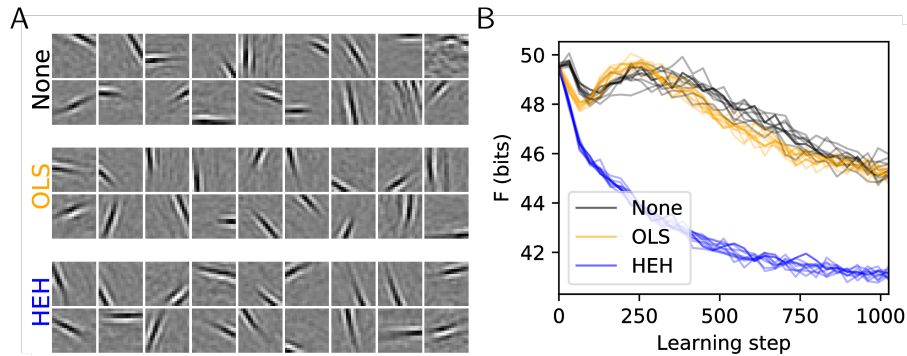
In [22]:

```
%tikz -f pdf --save {fname}.pdf
\draw[white, fill=white] (0.\linewidth,0) rectangle (1.\linewidth, .382\linewidth) ;
\draw [anchor=north west] (.0\linewidth, .382\linewidth) node {\includegraphics[width=.5\linewidth]{None}};
\draw [anchor=north west] (.5\linewidth, .382\linewidth) node {\includegraphics[width=.5\linewidth]{OLS}};
\begin{scope}[font=\bf\sffamily\large]
\draw [anchor=west,fill=white] (.0\linewidth, .382\linewidth) node [above right=-3mm] {\$matr};
\draw [anchor=west,fill=white] (.53\linewidth, .382\linewidth) node [above right=-3mm] {\$matr};
\end{scope}
```

In [23]:

```
!convert -density {dpi_export} {fname}.pdf {fname}.jpg
!convert -density {dpi_export} {fname}.pdf {fname}.png
#!convert -density {dpi_export} -resize 5400 -units pixelsperinch -flatten -compress lzw
Image(fname + '.png')
```

Out[23]:



```
!echo "width=" ; convert {fname}.tiff -format "%[fx:w]" info: !echo ", \nheight="
; convert {fname}.tiff -format "%[fx:h]" info: !echo ", \nunit=" ; convert
{fname}.tiff -format "%U" info:!identify {fname}.tiff
```

figure 2: Histogram Equalization Homeostasis

In [24]:

```
fname = 'figure_HEH'
```

First collecting data:

In [25]:

```
list_figures = ['show_Pcum']
```

```
dico = {}
```

```
for homeo_method in homeo_methods:
```

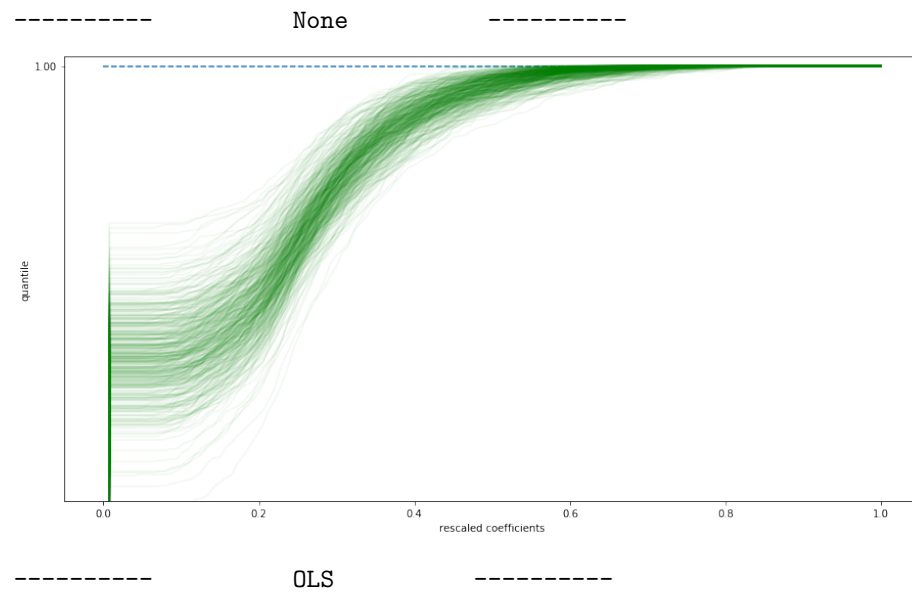
```
    print(hl + hs + homeo_method + hs + hl)
```

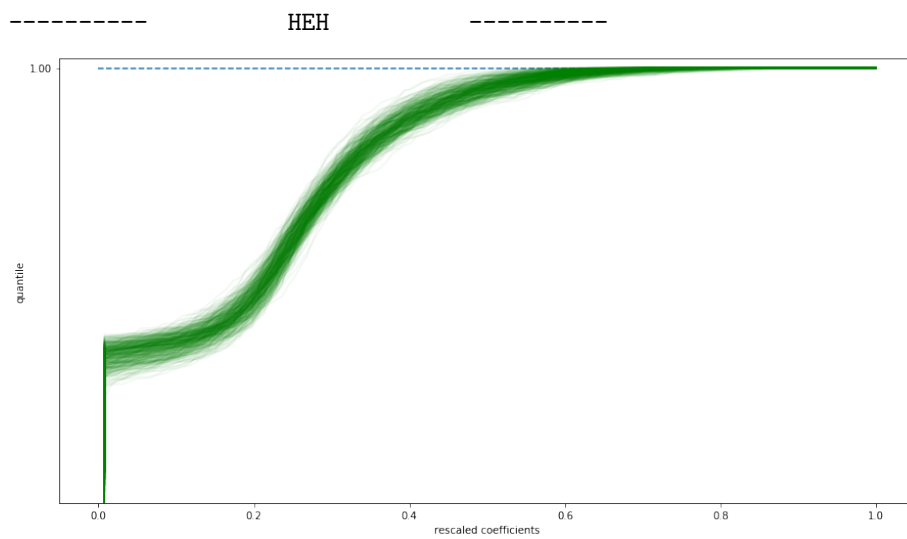
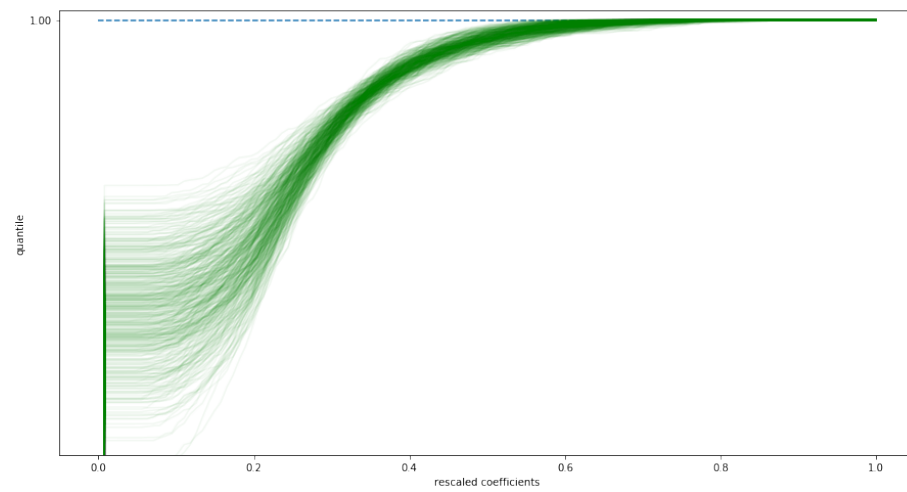
```
    shl = SHL(homeo_method=homeo_method, **opts)
```

```
    #dico[homeo_method] = shl.learn_dico(data=data, list_figures=list_figures, matname=tag +
```

```
    dico[homeo_method] = shl.learn_dico(data=data, list_figures=list_figures, matname=tag +
```

```
    plt.show()
```





In [26]:

```
dico[homeo_method].P_cum.shape
```

Out[26]:

```
(441, 128)
```

panel A: different P_cum¶

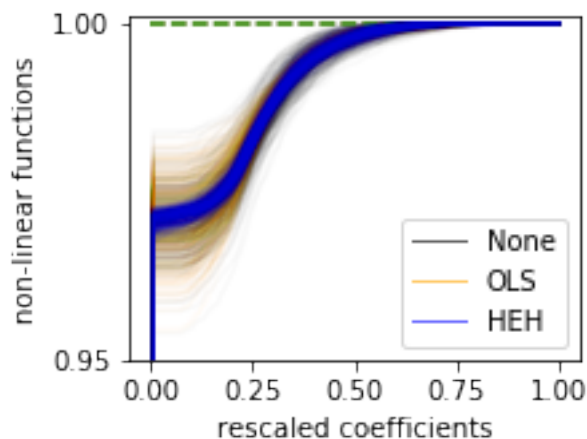
In [27]:

```
pname = '/tmp/panel_A' #pname = fname + '_A'
```

```

from shl_scripts import plot_P_cum
variable = 'F'
subplotpars = dict(left=0.2, right=.95, bottom=0.2, top=.95)#, wspace=0.05, hspace=0.05,)
fig, ax = plt.subplots(1, 1, figsize=(fig_width/2, fig_width/(1+phi)), gridspec_kw=subplotpars)
for color, homeo_method in zip(colors, homeo_methods):
    ax.axis(c='b', lw=2, axisbg='w')
    ax.set_facecolor('w')
    fig, ax = plot_P_cum(dico[homeo_method].P_cum, ymin=0.95, ymax=1.001,
                        title=None, subtitle=None, ylabel='non-linear functions',
                        verbose=False, n_yticks=21, alpha=.02, c=color, fig=fig, ax=ax)
    ax.plot([0], [0], lw=1, color=color, label=homeo_method, alpha=.6)
    # ax.set_ylabel(homeo_method)
    #ax.text(-8, 7*dim_graph[0], homeo_method, fontsize=12, color='k', rotation=90)#, backgroundcolor='w')
ax.legend(loc='lower right')
for ext in FORMATS: fig.savefig(pname + ext, dpi=dpi_export)
if DEBUG: Image(pname + '.png')

```



In [28]:

```
if DEBUG: help(fig.legend)
```

panel B: comparing the effects of parameters¶

In [29]:

```
pname = '/tmp/panel_B' #fname + '_B'
```

```
from shl_scripts.shl_experiments import SHL_set
```

```
homeo_methods = ['None', 'EMP', 'HAP', 'HEH', 'OLS']
```

```

homeo_methods = ['None', 'OLS', 'HEH']

variables = ['eta', 'alpha_homeo', 'eta_homeo', 'l0_sparseness', 'n_dictionary']
variables = ['eta', 'alpha_homeo', 'eta_homeo', 'l0_sparseness']
variables = ['alpha_homeo', 'eta_homeo']
variables = ['eta', 'alpha_homeo', 'eta_homeo']
variables = ['eta', 'eta_homeo']

list_figures = []

for homeo_method in homeo_methods:
    opts_ = opts.copy()
    opts_.update(homeo_method=homeo_method, datapath=datapath)
    experiments = SHL_set(opts_, tag=tag + '_' + homeo_method)
    experiments.run(variables=variables, n_jobs=1, verbose=0)

import matplotlib.pyplot as plt
subplotpars = dict(left=0.2, right=.95, bottom=0.2, top=.95, wspace=0.5, hspace=0.35,)

if len(variables)==4:
    fig, axs = plt.subplots(2, 2, figsize=(fig_width/2, fig_width/(1+phi)), gridspec_kw=subp
    for i_ax, variable in enumerate(variables):
        for color, homeo_method in zip(colors, homeo_methods):
            opts_ = opts.copy()
            opts_.update(homeo_method=homeo_method, datapath=datapath)
            experiments = SHL_set(opts_, tag=tag + '_' + homeo_method)
            ax = axs[i_ax%2][i_ax//2]
            fig, ax = experiments.scan(variable=variable, list_figures=[], display='final',
            ax.set_xlabel('') #variable
            ax.text(.1, .8, variable, transform=axs[i_ax].transAxes)
            #axs[i_ax].get_xaxis().set_major_formatter(matplotlib.ticker.ScalarFormatter())
        else:
            fig, axs = plt.subplots(len(variables), 1, figsize=(fig_width/2, fig_width/(1+phi)), gri

    for i_ax, variable in enumerate(variables):
        for color, homeo_method in zip(colors, homeo_methods):
            opts_ = opts.copy()
            opts_.update(homeo_method=homeo_method, datapath=datapath)
            experiments = SHL_set(opts_, tag=tag + '_' + homeo_method)
            fig, axs[i_ax] = experiments.scan(variable=variable, list_figures=[], display='f
            axs[i_ax].set_xlabel('') #variable

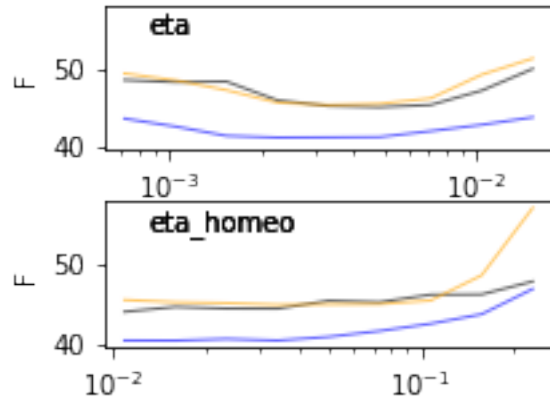
```

```

        axs[i_ax].text(.1, .8, variable, transform=axs[i_ax].transAxes)
        #axs[i_ax].get_xaxis().set_major_formatter(matplotlib.ticker.ScalarFormatter())

fig.legend(loc='lower right')
for ext in FORMATS: fig.savefig(pname + ext, dpi=dpi_export)
if DEBUG: Image(pname + '.png')

```



Montage of the subplots¶

In [30]:

```

%%tikz -f pdf --save {fname}.pdf
\draw[white, fill=white] (0.\linewidth,0) rectangle (1.\linewidth, .382\linewidth) ;
\draw [anchor=north west] (.0\linewidth, .382\linewidth) node {\includegraphics[width=.5\linewidth]{eta.png}}
\draw [anchor=north west] (.5\linewidth, .382\linewidth) node {\includegraphics[width=.5\linewidth]{eta_homeo.png}}
\begin{scope}[font=\bf\sffamily\large]
\draw [anchor=west,fill=white] (.0\linewidth, .382\linewidth) node [above right=-3mm] {\$ \eta}
\draw [anchor=west,fill=white] (.53\linewidth, .382\linewidth) node [above right=-3mm] {\$ \eta_{homeo}}
\end{scope}
\end{tikzpicture}

```

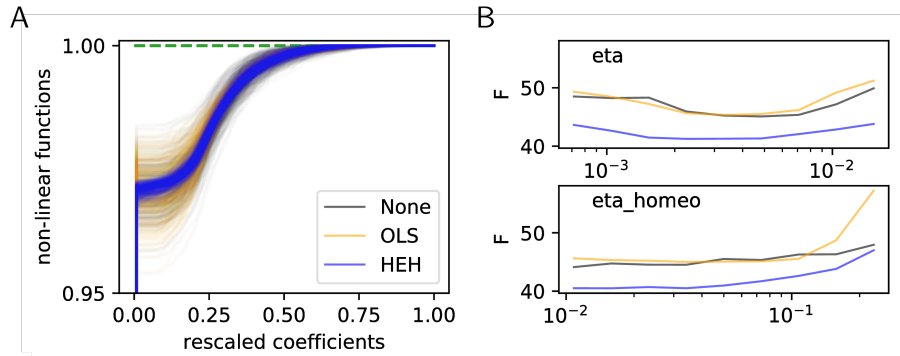
In [31]:

```

!convert -density {dpi_export} {fname}.pdf {fname}.jpg
!convert -density {dpi_export} {fname}.pdf {fname}.png
#!convert -density {dpi_export} -resize 5400 -units pixelsperinch -flatten -compress lzw
Image(fname + '.png')

```

Out[31]:



```
!echo "width=" ; convert {fname}.tiff -format "%[fx:w]" info: !echo ", \nheight="
; convert {fname}.tiff -format "%[fx:h]" info: !echo ", \nunit=" ; convert
{fname}.tiff -format "%U" info: !identify {fname}.tiff
```

figure 3:¶

learning¶

In [32]:

```
fname = 'figure_HAP'
```

In [33]:

```
colors = ['orange', 'red', 'green', 'blue']
homeo_methods = ['OLS', 'EMP', 'HAP', 'HEH']
list_figures = []
dico = {}
for i_cv in range(N_cv):
    dico[i_cv] = {}
    for homeo_method in homeo_methods:
        shl = SHL(homeo_method=homeo_method, seed=seed+i_cv, **opts)
        dico[i_cv][homeo_method] = shl.learn_dico(data=data, list_figures=list_figures, matr

list_figures = ['show_dico'] if DEBUG else []
for i_cv in [one_cv]:
    for homeo_method in homeo_methods:
        print(hl + hs + homeo_method + hs + hl)
        shl = SHL(homeo_method=homeo_method, seed=seed+i_cv, **opts)
        shl.learn_dico(data=data, list_figures=list_figures, matname=tag + '_' + homeo_metho
        plt.show()
        print('size of dictionary = (number of filters, size of imagelets) = ', dico[i_cv][h
        print('average of filters = ', dico[i_cv][homeo_method].dictionary.mean(axis=1).mea
            '+/-', dico[i_cv][homeo_method].dictionary.mean(axis=1).std())
        SE = np.sqrt(np.sum(dico[i_cv][homeo_method].dictionary**2, axis=1))
```



```

        print('average energy of filters = ', SE.mean(), '+/-', SE.std())

-----
                OLS
size of dictionary = (number of filters, size of imagelets) = (441, 324)
average of filters = 1.4204508020925339e-05 +/- 0.0011077610780090214
average energy of filters = 1.0 +/- 3.991428581974025e-17
-----
                EMP
size of dictionary = (number of filters, size of imagelets) = (441, 324)
average of filters = -3.523143673793376e-05 +/- 0.0011205197173717286
average energy of filters = 1.0 +/- 4.1962486042515756e-17
-----
                HAP
size of dictionary = (number of filters, size of imagelets) = (441, 324)
average of filters = 1.4205846034666029e-05 +/- 0.0010952255730414218
average energy of filters = 1.0 +/- 3.215820483078219e-17
-----
                HEH
size of dictionary = (number of filters, size of imagelets) = (441, 324)
average of filters = -7.478164618956859e-06 +/- 0.0010812190907883345
average energy of filters = 1.0 +/- 3.738315377818512e-17

```

panel A: plotting some dictionaries¶

In [34]:

```
pname = '/tmp/panel_A' #pname = fname + '_A'
```

In [35]:

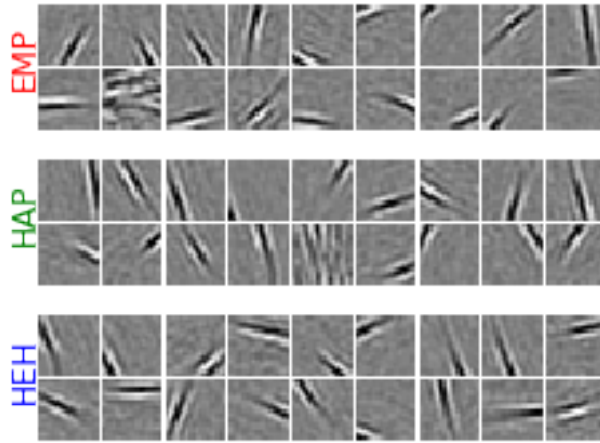
```

subplotpars = dict( left=0.042, right=1., bottom=0., top=1., wspace=0.05, hspace=0.05,)
fig, axs = plt.subplots(3, 1, figsize=(fig_width/2, fig_width/(1+phi)), gridspec_kw=subplotpars)

for ax, color, homeo_method in zip(axs.ravel(), colors[1:], homeo_methods[1:]):
    ax.axis(c=color, lw=2, axisbg='w')
    ax.set_facecolor('w')
    from shl_scripts import show_dico
    fig, ax = show_dico(shl, dico[one_cv][homeo_method], dim_graph=dim_graph, seed=194, figsize=fig_size)
    # ax.set_ylabel(homeo_method)
    ax.text(-8, 7*dim_graph[0], homeo_method, fontsize=12, color=color, rotation=90)#, backgroundcolor='w')

for ext in FORMATS: fig.savefig(pname + ext, dpi=dpi_export)

```



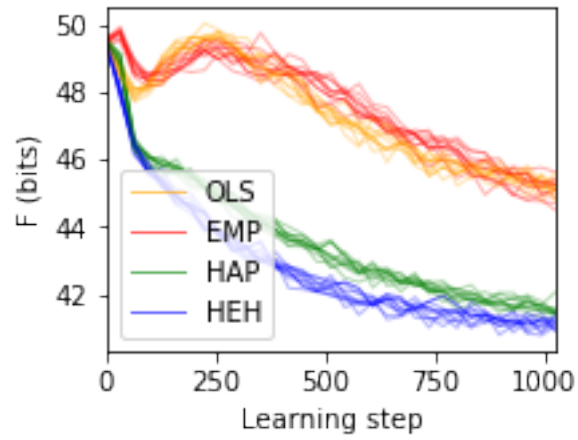
panel B: quantitative comparison¶

In [36]:

```
pname = '/tmp/panel_B' #fname + '_B'
```

In [37]:

```
from shl_scripts import time_plot
variable = 'F'
alpha = .3
subplotpars = dict(left=0.2, right=.95, bottom=0.2, top=.95)#, wspace=0.05, hspace=0.05,)
fig, ax = plt.subplots(1, 1, figsize=(fig_width/2, fig_width/(1+phi)), gridspec_kw=subplotpars)
for i_cv in range(N_cv):
    for color, homeo_method in zip(colors, homeo_methods):
        ax.axis(c='b', lw=2, axisbg='w')
        ax.set_facecolor('w')
        if i_cv==0:
            fig, ax = time_plot(shl, dico[i_cv][homeo_method], variable=variable, unit='bits')
        else:
            fig, ax = time_plot(shl, dico[i_cv][homeo_method], variable=variable, unit='bits')
ax.legend(loc='best')
for ext in FORMATS: fig.savefig(pname + ext, dpi=dpi_export)
if DEBUG: Image(pname + '.png')
```



In [38]:

```
if DEBUG: Image(pname + '.png')
```

Montage of the subplots¶

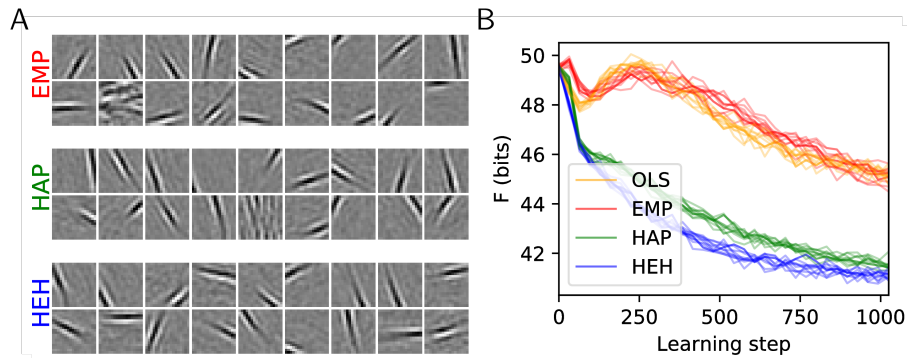
In [39]:

```
%%tikz -f pdf --save {fname}.pdf
\draw[white, fill=white] (0.\linewidth,0) rectangle (1.\linewidth, .382\linewidth) ;
\draw [anchor=north west] (.0\linewidth, .382\linewidth) node {\includegraphics[width=.5\linewidth]{}}
\draw [anchor=north west] (.5\linewidth, .382\linewidth) node {\includegraphics[width=.5\linewidth]{}}
\begin{scope}[font=\bf\sffamily\large]
\draw [anchor=west,fill=white] (.0\linewidth, .382\linewidth) node [above right=-3mm] {\$\\mat}
\draw [anchor=west,fill=white] (.53\linewidth, .382\linewidth) node [above right=-3mm] {\$\\ma}
\end{scope}
```

In [40]:

```
!convert -density {dpi_export} {fname}.pdf {fname}.jpg
!convert -density {dpi_export} {fname}.pdf {fname}.png
#!convert -density {dpi_export} -resize 5400 -units pixelsperinch -flatten -compress lzw
Image(fname + '.png')
```

Out[40]:



```
!echo "width=" ; convert {fname}.tiff -format "%[fx:w]" info: !echo ", \nheight="
; convert {fname}.tiff -format "%[fx:h]" info: !echo ", \nunit=" ; convert
{fname}.tiff -format "%U" info:!identify {fname}.tiff
```

figure 4: Convolutional Neural Network

In [41]:

```
fname = 'figure_CNN'
```

In [42]:

```
from CHAMP.DataLoader import LoadData
from CHAMP.DataTools import LocalContrastNormalization, FilterInputData, GenerateMask
from CHAMP.Monitor import DisplayDico, DisplayConvergenceCHAMP, DisplayWhere

import os
datapath = os.path.join("/tmp", "database")
path = os.path.join(datapath, "Face_DataBase")
TrSet, TeSet = LoadData('Face', path, decorrelate=False, resize=(65, 65))

# MP Parameters
nb_dico = 20
width = 9
dico_size = (width, width)
l0 = 20
seed = 42
# Learning Parameters
eta = .05
nb_epoch = 500

TrSet, TeSet = LoadData('Face', path, decorrelate=False, resize=(65, 65))
N_TrSet, _, _, _ = LocalContrastNormalization(TrSet)
Filtered_L_TrSet = FilterInputData(
    N_TrSet, sigma=0.25, style='Custom', start_R=15)
```

```

mask = GenerateMask(full_size=(nb_dico, 1, width, width), sigma=0.8, style='Gaussian')

from CHAMP.CHAMP_Layer import CHAMP_Layer

from CHAMP.DataTools import SaveNetwork, LoadNetwork
homeo_methods = ['None', 'HAP']

for homeo_method, eta_homeo in zip(homeo_methods, [0., 0.0025]):
    fname = 'cache_dir_CNN/CHAMP_low_' + homeo_method + '.pkl'
    try:
        L1_mask = LoadNetwork(loading_path=fname)
    except:
        L1_mask = CHAMP_Layer(l0_sparseness=l0, nb_dico=nb_dico,
                               dico_size=dico_size, mask=mask, verbose=1)
        dico_mask = L1_mask.TrainLayer(
            Filtered_L_TrSet, eta=eta, eta_homeo=eta_homeo, nb_epoch=nb_epoch, seed=seed)
        SaveNetwork(Network=L1_mask, saving_path=fname)

```

panel A: plotting some dictionaries¶

In [43]:

```

pname = '/tmp/panel_A' #pname = fname + '_A'

subplotpars = dict( left=0.042, right=1., bottom=0., top=1., wspace=0.05,
hspace=0.05,) fig, axs = plt.subplots(2, 1, figsize=(fig_width/2, fig_width/(1+phi)),
gridspec_kw=subplotpars) for ax, color, homeo_method in zip(axs.ravel(),
['black', 'green'], homeo_methods): ax.axis(c=color, lw=2, axisbg='w')
ax.set_facecolor('w') fname = 'cache_dir/CHAMP_low_' + homeo_method
+ '.pkl' L1_mask = LoadNetwork(loading_path=fname) fig, ax = Display-
Dico(L1_mask.dictionary, fig=fig, ax=ax) # ax.set_ylabel(homeo_method)
ax.text(-8, 7*dim_graph[0], homeo_method, fontsize=12, color=color, rota-
tion=90)#, backgroundcolor='white' for ext in FORMATS: fig.savefig(pname +
ext, dpi=dpi_export)

```

In [44]:

```

subplotpars = dict( left=0.042, right=1., bottom=0., top=1., wspace=0.05, hspace=0.05,)

for color, homeo_method in zip(['black', 'green'], homeo_methods):
    #fig, axs = plt.subplots(1, 1, figsize=(fig_width/2, fig_width/(1+phi)), gridspec_kw=sub-
    fname = 'cache_dir_CNN/CHAMP_low_' + homeo_method + '.pkl'
    L1_mask = LoadNetwork(loading_path=fname)
    fig, ax = DisplayDico(L1_mask.dictionary)
    # ax.set_ylabel(homeo_method)
    #for ax in list(axs):
    #    ax.axis(c=color, lw=2, axisbg='w')

```

```

# ax.set_facecolor('w')
ax[0].text(-4, 3, homeo_method, fontsize=8, color=color, rotation=90)#, backgroundcolor=
plt.tight_layout( pad=0., w_pad=0., h_pad=.0)

```

```

for ext in FORMATS: fig.savefig(pname + '_' + homeo_method + ext, dpi=dpi_export)
<Figure size 576x28.8 with 0 Axes>

```



```

<Figure size 576x28.8 with 0 Axes>

```



panel B: quantitative comparison¶

In [45]:

```

pname = '/tmp/panel_B' #fname + '_B'

from shl_scripts import time_plot variable = 'F' alpha = .3 subplotpars =
dict(left=0.2, right=.95, bottom=0.2, top=.95)#, wspace=0.05, hspace=0.05,)
fig, axs = plt.subplots(2, 1, figsize=(fig_width/2, fig_width/(1+phi)), grid-
spec_kw=subplotpars) for ax, color, homeo_method in zip(axs, ['black', 'green'],
homeo_methods): print(ax, axs) fname = 'cache_dir_CNN/CHAMP_low_'
+ homeo_method + '.pkl' L1_mask = LoadNetwork(loading_path=fname)
fig, ax = DisplayConvergenceCHAMP(L1_mask, to_display=['histo'],
fig=fig, ax=ax) ax.axis(c=color, lw=2, axisbg='w') ax.set_facecolor('w') #
ax.set_ylabel(homeo_method) #ax.text(-8, 7*dim_graph[0], homeo_method,
fontsize=12, color=color, rotation=90)#, backgroundcolor='white' for ext in
FORMATS: fig.savefig(pname + ext, dpi=dpi_export) if DEBUG: Image(pname
+'.png')

```

In [46]:

```

from shl_scripts import time_plot
variable = 'F'
alpha = .3
subplotpars = dict(left=0.2, right=.95, bottom=0.2, top=.95)#, wspace=0.05, hspace=0.05,)

for color, homeo_method in zip(['black', 'green'], homeo_methods):
    #fig, axs = plt.subplots(1, 1, figsize=(fig_width/2, fig_width/(1+phi)), gridspec_kw=sub
    fname = 'cache_dir_CNN/CHAMP_low_' + homeo_method + '.pkl'
    L1_mask = LoadNetwork(loading_path=fname)
    fig, ax = DisplayConvergenceCHAMP(L1_mask, to_display=['histo'], color=color)
    ax.axis(c=color, lw=2, axisbg='w')

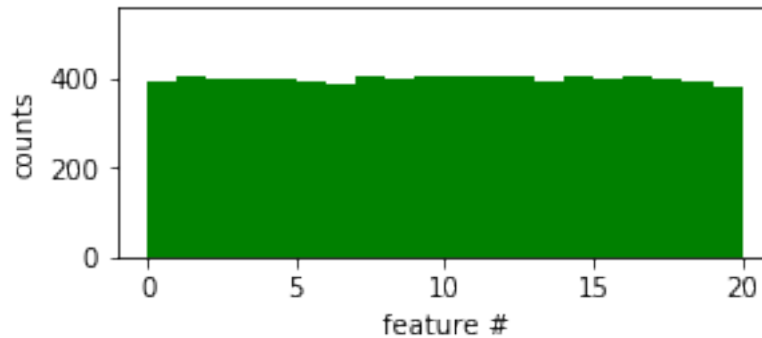
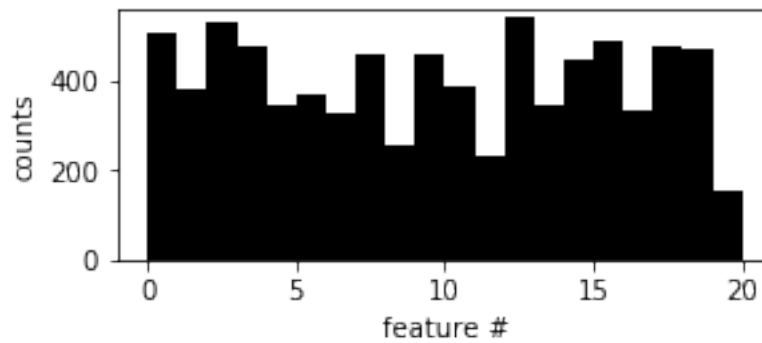
```

```

ax.set_facecolor('w')
ax.set_ylabel('counts')
ax.set_xlabel('feature #')
ax.set_ylim(0, 560)
#ax.text(-8, 7*dim_graph[0], homeo_method, fontsize=12, color=color, rotation=90)#, backg
#ax[0].text(-8, 3, homeo_method, fontsize=12, color=color, rotation=90)#, backgroundcol

for ext in FORMATS: fig.savefig(pname + '_' + homeo_method + ext, dpi=dpi_export)
if DEBUG: Image(pname + '.png')

```



Montage of the subplots¶

In [47]:

```
%ls -ltr /tmp/panel_*
```

```

-rw-r--r-- 1 laurentperrinet wheel 72275 Sep 28 13:13 /tmp/panel_A.pdf
-rw-r--r-- 1 laurentperrinet wheel 84631 Sep 28 13:13 /tmp/panel_A.png
-rw-r--r-- 1 laurentperrinet wheel 22106 Sep 28 13:13 /tmp/panel_B.pdf
-rw-r--r-- 1 laurentperrinet wheel 532305 Sep 28 13:13 /tmp/panel_B.png
-rw-r--r-- 1 laurentperrinet wheel 27370 Sep 28 13:13 /tmp/panel_A_None.pdf
-rw-r--r-- 1 laurentperrinet wheel 18909 Sep 28 13:13 /tmp/panel_A_None.png

```

```
-rw-r--r--@ 1 laurentperrinet wheel 26909 Sep 28 13:13 /tmp/panel_A_HAP.pdf
-rw-r--r-- 1 laurentperrinet wheel 16431 Sep 28 13:13 /tmp/panel_A_HAP.png
-rw-r--r-- 1 laurentperrinet wheel 8816 Sep 28 13:13 /tmp/panel_B_None.pdf
-rw-r--r-- 1 laurentperrinet wheel 39035 Sep 28 13:13 /tmp/panel_B_None.png
-rw-r--r-- 1 laurentperrinet wheel 8813 Sep 28 13:13 /tmp/panel_B_HAP.pdf
-rw-r--r-- 1 laurentperrinet wheel 38743 Sep 28 13:13 /tmp/panel_B_HAP.png
```

In [48]:

```
fname
```

Out[48]:

```
'figure_CNN'
```

In [49]:

```
382+191
```

Out[49]:

```
573
```

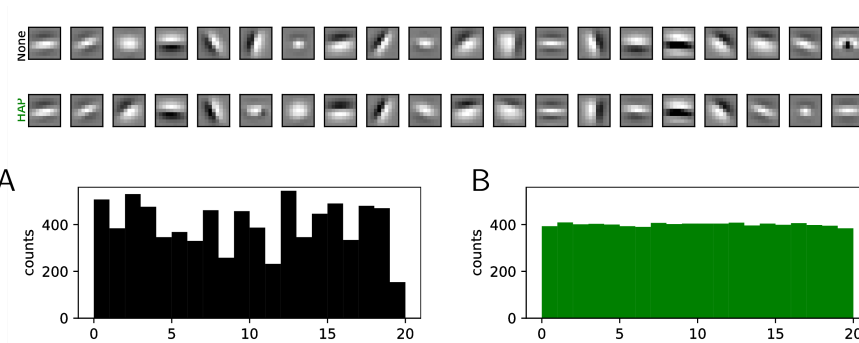
In [50]:

```
%\tikz -f pdf --save {fname}.pdf
\draw[white, fill=white] (0.\linewidth,0) rectangle (1.\linewidth, .382\linewidth) ;
\draw [anchor=north west] (.0\linewidth, .375\linewidth) node {\includegraphics[width=.95\linewidth]{figure_CNN.png}};
\draw [anchor=north west] (.0\linewidth, .300\linewidth) node {\includegraphics[width=.95\linewidth]{figure_CNN.png}};
\draw [anchor=north west] (.0\linewidth, .191\linewidth) node {\includegraphics[width=.45\linewidth]{figure_CNN.png}};
\draw [anchor=north west] (.5\linewidth, .191\linewidth) node {\includegraphics[width=.45\linewidth]{figure_CNN.png}};
\begin{scope}[font=\bf\sffamily\large]
%\draw [anchor=west,fill=white] (.0\linewidth, .382\linewidth) node [above right=-3mm] {$\mathcal{M}$};
\draw [anchor=west,fill=white] (.0\linewidth, .191\linewidth) node [above right=-3mm] {$\mathcal{M}$};
\draw [anchor=west,fill=white] (.53\linewidth, .191\linewidth) node [above right=-3mm] {$\mathcal{M}$};
\end{scope}
```

In [51]:

```
!convert -density {dpi_export} {fname}.pdf {fname}.jpg
!convert -density {dpi_export} {fname}.pdf {fname}.png
#!convert -density {dpi_export} -resize 5400 -units pixelsperinch -flatten -compress lzw
Image(fname +'.png')
```

Out[51]:



```
!echo "width=" ; convert {fname}.tiff -format "%[fx:w]" info: !echo ", \nheight="
; convert {fname}.tiff -format "%[fx:h]" info: !echo ", \nunit=" ; convert
{fname}.tiff -format "%U" info:!identify {fname}.tiff
```

coding¶

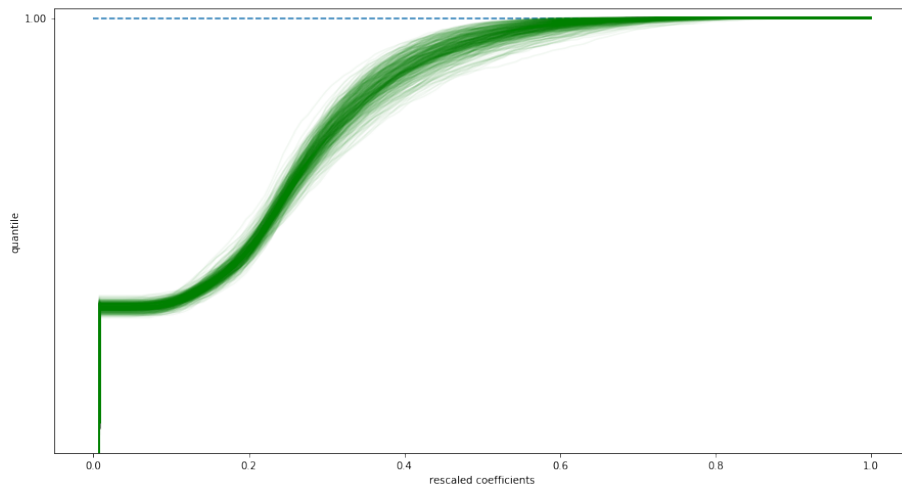
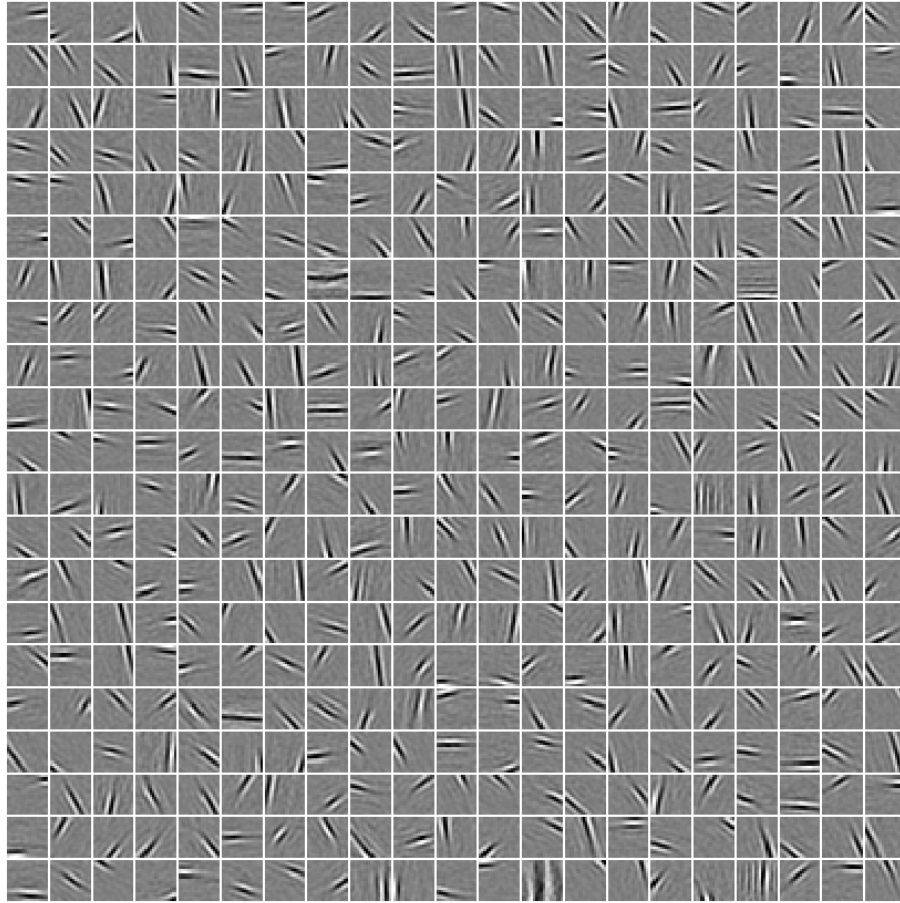
The learning itself is done via a gradient descent but is highly dependent on the coding / decoding algorithm. This belongs to a another function (in the shl_encode.py script)

Supplementary controls¶

starting a learning¶

In [52]:

```
shl = SHL(**opts)
list_figures = ['show_dico', 'show_Pcum', 'time_plot_F']
dico = shl.learn_dico(data=data, list_figures=list_figures, matname=tag + '_vanilla')
```



In [53]:

```
print('size of dictionary = (number of filters, size of imagelets) = ', dico.dictionary.shape)
print('average of filters = ', dico.dictionary.mean(axis=1).mean(),
      '+/-' , dico.dictionary.mean(axis=1).std())
SE = np.sqrt(np.sum(dico.dictionary**2, axis=1))
print('average energy of filters = ', SE.mean(), '+/-' , SE.std())

size of dictionary = (number of filters, size of imagelets) = (441, 324)
average of filters = -3.1637286525674506e-05 +/- 0.0010915831873405475
average energy of filters = 1.0 +/- 3.884971301458624e-17

[autoreload of IPython.core.ultratb failed: Traceback (most recent call last):
  File "/usr/local/lib/python3.6/site-packages/IPython/extensions/autoreload.py", line 245,
    if py_filename in self.failed:
  File "/usr/local/lib/python3.6/site-packages/IPython/extensions/autoreload.py", line 368,
    module.__dict__['__name__'] = old_name
  File "/usr/local/Cellar/python/3.6.5_1/Frameworks/Python.framework/Versions/3.6/lib/python3.6/importlib.py", line 366, in reload
    return importlib.reload(module)
  File "/usr/local/Cellar/python/3.6.5_1/Frameworks/Python.framework/Versions/3.6/lib/python3.6/importlib/_bootstrap.py", line 219, in _bootstrap._exec(spec, module)
  File "<frozen importlib._bootstrap>", line 618, in _exec
  File "<frozen importlib._bootstrap_external>", line 678, in exec_module
  File "<frozen importlib._bootstrap>", line 219, in _call_with_frames_removed
  File "/usr/local/lib/python3.6/site-packages/IPython/core/ultratb.py", line 128, in <module>
    import IPython.utils.colorable as colorable
AttributeError: module 'IPython' has no attribute 'utils'
]
```

getting help¶

In [54]:

help(shl)

Help on SHL in module shl_scripts.shl_experiments object:

```
class SHL(builtins.object)
|   Base class to define SHL experiments:
|       - initialization
|       - coding and learning
|       - visualization
|       - quantitative analysis
|
|   Methods defined here:
|
|   __init__(self, height=256, width=256, patch_width=18, N_patches=65536, datapath='../data')
|       Initialize self. See help(type(self)) for accurate signature.
```

```

| code(self, data, dico, coding_algorithm='mp', matname=None, P_cum=None, fit_tol=None, 10
|
| decode(self, sparse_code, dico)
|
| get_data(self, matname=None, patch_width=None)
|
| learn_dico(self, dictionary=None, precision=None, P_cum=None, data=None, matname=None, 1
|
| plot_error(self, dico, **fig_kwargs)
|
| plot_variance(self, sparse_code, **fig_kwargs)
|
| plot_variance_histogram(self, sparse_code, **fig_kwargs)
|
| show_Pcum(self, dico, title=None, verbose=False, n_yticks=21, alpha=0.05, c='g', **fig_l
|
| show_dico(self, dico, data=None, title=None, **fig_kwargs)
|
| show_dico_in_order(self, dico, data=None, title=None, **fig_kwargs)
|
| time_plot(self, dico, variable='kurt', N_nosample=1, **fig_kwargs)
|
| -----
| Data descriptors defined here:
|
| __dict__
|     dictionary for instance variables (if defined)
|
| __weakref__
|     list of weak references to the object (if defined)

```

In [55]:

```
help(dico)
```

Help on SparseHebbianLearning in module shl_scripts.shl_learn object:

```

class SparseHebbianLearning(builtins.object)
|   Sparse Hebbian learning
|
|   Finds a dictionary (a set of atoms) that can best be used to represent data
|   using a sparse code.
|
|   Parameters
|   -----
|

```

```

| n_dictionary : int,
|     Number of dictionary elements to extract
|
| eta : float or dict
|     Gives the learning parameter for the homeostatic gain.
|
| n_iter : int,
|     total number of iterations to perform
|
| eta_homeo : float
|     Gives the learning parameter for the homeostatic gain.
|
| alpha_homeo : float
|     Gives the smoothing exponent for the homeostatic gain
|     If equal to 1 the homeostatic learning rule learns a linear relation to
|     variance.
|
| dictionary : array of shape (n_dictionary, n_pixels),
|     initial value of the dictionary for warm restart scenarios
|     Use ``None`` for a new learning.
|
| fit_algorithm : {'mp', 'lars', 'cd'}
|     see sparse_encode
|
| batch_size : int,
|     The number of samples to take in each batch.
|
| l0_sparseness : int, ``0.1 * n_pixels`` by default
|     Number of nonzero coefficients to target in each column of the
|     solution. This is only used by `algorithm='lars'`, `algorithm='mp'` and
|     `algorithm='omp'`.
|
| fit_tol : float, 1. by default
|     If `algorithm='lasso_lars'` or `algorithm='lasso_cd'`, `fit_tol` is the
|     penalty applied to the L1 norm.
|     If `algorithm='threshold'`, `fit_tol` is the absolute value of the
|     threshold below which coefficients will be squashed to zero.
|     If `algorithm='mp'` or `algorithm='omp'`, `fit_tol` is the tolerance
|     parameter: the value of the reconstruction error targeted. In this case,
|     it overrides `l0_sparseness`.
|
| verbose :
|     degree of verbosity of the printed output
|
| Attributes
| -----

```

```

| dictionary : array, [n_dictionary, n_pixels]
|     dictionary extracted from the data
|
|
| Notes
| -----
|
| **References:**
|
| Olshausen BA, Field DJ (1996).
| Emergence of simple-cell receptive field properties by learning a sparse code for natural
| Nature, 381: 607-609. (http://redwood.berkeley.edu/bruno/papers/nature-paper.pdf)
|
| Olshausen BA, Field DJ (1997)
| Sparse Coding with an Overcomplete Basis Set: A Strategy Employed by V1?
| Vision Research, 37: 3311-3325. (http://redwood.berkeley.edu/bruno/papers/VR.pdf)
|
| See also
| -----
| http://scikit-learn.org/stable/auto\_examples/decomposition/plot\_image\_denoising.html
|
| Methods defined here:
|
| __init__(self, fit_algorithm, dictionary=None, precision=None, eta=0.003, beta1=0.9, beta2=0.999)
|     Initialize self. See help(type(self)) for accurate signature.
|
| fit(self, X, y=None)
|     Fit the model from data in X.
|
|     Parameters
|     -----
|
|     X: array-like, shape (n_samples, n_pixels)
|         Training vector, where n_samples is the number of samples
|         and n_pixels is the number of features.
|
|     Returns
|     -----
|
|     self : object
|         Returns the instance itself.
|
| transform(self, X, algorithm=None, l0_sparseness=None, fit_tol=None, alpha_MP=None)
|     Fit the model from data in X.
|
|     Parameters
|     -----
|
|     X: array-like, shape (n_samples, n_pixels)
|         Training vector, where n_samples is the number of samples

```

```

|         and n_pixels is the number of features.
|
|     Returns
|     -----
|     self : object
|         Returns sparse code.
|
|     -----
|     Data descriptors defined here:
|
|     __dict__
|         dictionary for instance variables (if defined)
|
|     __weakref__
|         list of weak references to the object (if defined)
|
|     -----
|     Data and other attributes defined here:
|
|     __slotnames__ = []

```

loading a database¶

Loading patches, with or without mask:

In []:

```

N_patches = 12
from shl_scripts.shl_tools import show_data

for i, (do_mask, label) in enumerate(zip([False, True], ['Without mask', 'With mask'])):
    data_ = SHL(DEBUG_DOWNSCALE=1, verbose=0, N_patches=N_patches, n_image=1, do_mask=do_mask)
    fig, axs = show_data(data_)
    axs[0].set_ylabel(label)
    plt.show()

```

Testing different algorithms¶

In [56]:

```

fig, ax = None, None

for algorithm in ['lasso_lars', 'lasso_cd', 'lars', 'omp', 'mp']: # 'threshold',
    opts_ = opts.copy()
    opts_.update(homeo_method='None', learning_algorithm=algorithm, verbose=0)
    shl = SHL(**opts_)
    dico= shl.learn_dico(data=data, list_figures=[],

```

```

matname=tag + ' - algorithm={}'.format(algorithm)
fig, ax = shl.time_plot(dico, variable='F', fig=fig, ax=ax, label=algorithm)

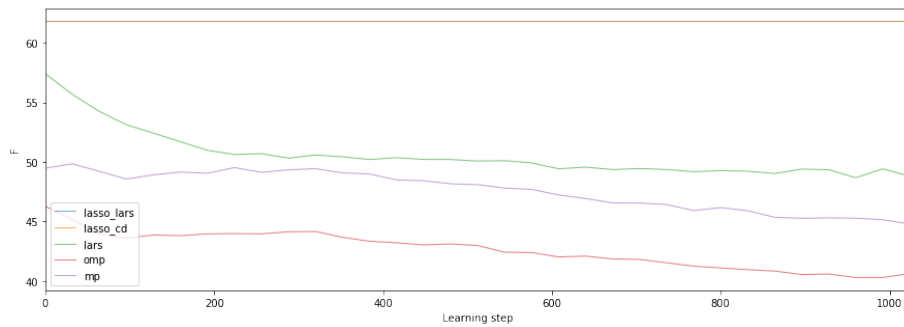
```

```
ax.legend()
```

ERROR! Session/line number was not unique in database. History logging moved to new session

Out[56]:

```
<matplotlib.legend.Legend at 0x146eaea20>
```



Testing two different dictionary initialization strategies¶

White Noise Initialization + Learning

In [57]:

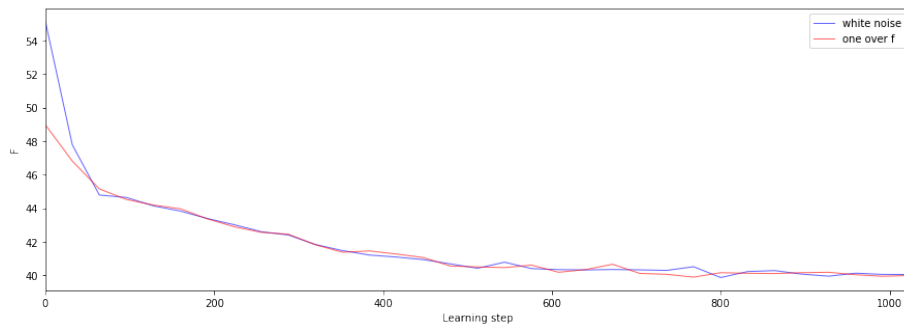
```

shl = SHL(one_over_F=False, **opts)
dico_w = shl.learn_dico(data=data, matname=tag + '_WHITE', list_figures=[])
shl = SHL(one_over_F=True, **opts)
dico_1oF = shl.learn_dico(data=data, matname=tag + '_OVF', list_figures=[])
fig_error, ax_error = None, None
fig_error, ax_error = shl.time_plot(dico_w, variable='F', fig=fig_error, ax=ax_error, color='b')
fig_error, ax_error = shl.time_plot(dico_1oF, variable='F', fig=fig_error, ax=ax_error, color='r')
#ax_error.set_ylim((0, .65))
ax_error.legend(loc='best')

```

Out[57]:

```
<matplotlib.legend.Legend at 0x1468d6048>
```

Testing two different learning rates strategies¶

We use by default the strategy of ADAM, see <https://arxiv.org/pdf/1412.6980.pdf>

In []:

```
shl = SHL(beta1=0., **opts)
dico_fixed = shl.learn_dico(data=data, matname=tag + '_fixed', list_figures=[])
shl = SHL(**opts)
dico_default = shl.learn_dico(data=data, matname=tag + '_default', list_figures=[])
fig_error, ax_error = None, None
fig_error, ax_error = shl.time_plot(dico_fixed, variable='F', fig=fig_error, ax=ax_error, co
fig_error, ax_error = shl.time_plot(dico_default, variable='F', fig=fig_error, ax=ax_error,
#ax_error.set_ylim((0, .65))
ax_error.legend(loc='best')
```

Perspectives¶

Convolutional neural networks¶

In []:

```
from CHAMP.DataLoader import LoadData
from CHAMP.DataTools import LocalContrastNormalization, FilterInputData, GenerateMask
from CHAMP.Monitor import DisplayDico, DisplayConvergenceCHAMP, DisplayWhere

import os
home = os.getenv('HOME')
datapath = os.path.join("/tmp", "database")
path = os.path.join(datapath, "Face_DataBase")
TrSet, TeSet = LoadData('Face', path, decorrelate=False, resize=(65, 65))
to_display = TrSet[0][0, 0:10, :, :, :]
print('Size=', TrSet[0].shape)
DisplayDico(to_display)
```

Training on a face database¶

In []:

```
# MP Parameters
nb_dico = 20
width = 9
dico_size = (width, width)
l0 = 20
seed = 42
# Learning Parameters
eta = .05
nb_epoch = 500

TrSet, TeSet = LoadData('Face', path, decorrelate=False, resize=(65, 65))
N_TrSet, _, _, _ = LocalContrastNormalization(TrSet)
Filtered_L_TrSet = FilterInputData(
    N_TrSet, sigma=0.25, style='Custom', start_R=15)
to_display = Filtered_L_TrSet[0][0, 0:10, :, :, :]
DisplayDico(to_display)

mask = GenerateMask(full_size=(nb_dico, 1, width, width), sigma=0.8, style='Gaussian')
DisplayDico(mask)
```

Training the ConvMP Layer with homeostasis¶

In []:

```
from CHAMP.CHAMP_Layer import CHAMP_Layer

from CHAMP.DataTools import SaveNetwork, LoadNetwork
fname = 'cache_dir_CNN/CHAMP_low_None.pkl'
try:
    L1_mask = LoadNetwork(loading_path=fname)
except:
    L1_mask = CHAMP_Layer(l0_sparseness=l0, nb_dico=nb_dico,
                          dico_size=dico_size, mask=mask, verbose=2)
    dico_mask = L1_mask.TrainLayer(
        Filtered_L_TrSet, eta=eta, nb_epoch=nb_epoch, seed=seed)
    SaveNetwork(Network=L1_mask, saving_path=fname)

DisplayDico(L1_mask.dictionary)
DisplayConvergenceCHAMP(L1_mask, to_display=['error', 'histo'])
DisplayWhere(L1_mask.where)
```

Training the ConvMP Layer with homeostasis¶

In []:

```

fname = 'cache_dir_CNN/CHAMP_low_HAP.pkl'
try:
    L1_mask = LoadNetwork(loading_path=fname)
except:

    # Learning Parameters
    eta_homeo = 0.0025
    L1_mask = CHAMP_Layer(l0_sparseness=10, nb_dico=nb_dico,
                          dico_size=dico_size, mask=mask, verbose=1)
    dico_mask = L1_mask.TrainLayer(
        Filtered_L_TrSet, eta=eta, eta_homeo=eta_homeo, nb_epoch=nb_epoch, seed=seed)
    SaveNetwork(Network=L1_mask, saving_path=fname)

DisplayDico(L1_mask.dictionary)
DisplayConvergenceCHAMP(L1_mask, to_display=['error', 'histo'])
DisplayWhere(L1_mask.where)

```

Reconstructing the input image¶

```

In [ ]:

from CHAMP.DataTools import Rebuilt
import torch
rebuilt_image = Rebuilt(torch.FloatTensor(L1_mask.code), L1_mask.dictionary)
DisplayDico(rebuilt_image[0:10, :, :, :])

```

Training the ConvMP Layer with higher-level filters¶

We train higher-level feature vectors by forcing the network to :

- learn bigger filters,
- represent the information using a bigger dictionary (higher sparseness)
- represent the information with less features (higher sparseness)

```

In [ ]:

fname = 'cache_dir_CNN/CHAMP_high_None.pkl'
try:
    L1_mask = LoadNetwork(loading_path=fname)
except:

    nb_dico = 60
    width = 19
    dico_size = (width, width)
    l0 = 5
    mask = GenerateMask(full_size=(nb_dico, 1, width, width), sigma=0.8, style='Gaussian')
    # Learning Parameters
    eta_homeo = 0.0

```

```

eta = .05
nb_epoch = 500
# learn
L1_mask = CHAMP_Layer(l0_sparseness=10, nb_dico=nb_dico,
                      dico_size=dico_size, mask=mask, verbose=0)
dico_mask = L1_mask.TrainLayer(
    Filtered_L_TrSet, eta=eta, eta_homeo=eta_homeo, nb_epoch=nb_epoch, seed=seed)
SaveNetwork(Network=L1_mask, saving_path=fname)

DisplayDico(L1_mask.dictionary)
DisplayConvergenceCHAMP(L1_mask, to_display=['error', 'histo'])
DisplayWhere(L1_mask.where)

In [ ]:

fname = 'cache_dir_CNN/CHAMP_high_HAP.pkl'
try:
    L1_mask = LoadNetwork(loading_path=fname)
except:

    nb_dico = 60
    width = 19
    dico_size = (width, width)
    l0 = 5
    mask = GenerateMask(full_size=(nb_dico, 1, width, width), sigma=0.8, style='Gaussian')
    # Learning Parameters
    eta_homeo = 0.0025
    eta = .05
    nb_epoch = 500
    # learn
    L1_mask = CHAMP_Layer(l0_sparseness=10, nb_dico=nb_dico,
                          dico_size=dico_size, mask=mask, verbose=0)
    dico_mask = L1_mask.TrainLayer(
        Filtered_L_TrSet, eta=eta, eta_homeo=eta_homeo, nb_epoch=nb_epoch, seed=seed)
    SaveNetwork(Network=L1_mask, saving_path=fname)

DisplayDico(L1_mask.dictionary)
DisplayConvergenceCHAMP(L1_mask, to_display=['error', 'histo'])
DisplayWhere(L1_mask.where)

```

Training on MNIST database¶

```

fname = 'cache_dir/CHAMP_MNIST_HAP.pkl'
try: L1_mask = LoadNetwork(loading_path=fname)
except: path = os.path.join(datapath, "MNISTtorch")
TrSet, TeSet = LoadData('MNIST', data_path=path)
N_TrSet, __, __, __ = LocalContrastNormalization(TrSet)
Filtered_L_TrSet

```

```
= FilterInputData( N_TrSet, sigma=0.25, style='Custom', start_R=15)
nb_dico = 60 width = 7 dico_size = (width, width) l0 = 15 # Learning
Parameters eta_homeo = 0.0025 eta = .05 nb_epoch = 500 # learn L1_mask
= CHAMP_Layer(l0_sparseness=l0, nb_dico=nb_dico, dico_size=dico_size,
mask=mask, verbose=2) dico_mask = L1_mask.TrainLayer( Filtered_L_TrSet,
eta=eta, eta_homeo=eta_homeo, nb_epoch=nb_epoch, seed=seed) SaveNet-
work(Network=L1_mask, saving_path=fname) DisplayDico(L1_mask.dictionary)
DisplayConvergenceCHAMP(L1_mask, to_display=['error', 'histo']) Display-
Where(L1_mask.where)
```

Computational details ¶

caching simulation data ¶

A convenience script to run and cache most learning items in this notebooks:

In []:

```
!ls -l {shl.cache_dir}/{tag}*
#!rm {shl.cache_dir}/{tag}*lock*
#!rm {shl.cache_dir}/{tag}*
#!ls -l {shl.cache_dir}/{tag}*
```

In []:

```
%%writefile model.py
#!/usr/bin/env python3
# -*- coding: utf-8 -*-
tag = 'ICLR'
from shl_scripts.shl_experiments import SHL, prun
# pre-loading data
datapath = '.././SparseHebbianLearning/database'
opts = dict(eta=0.0033, eta_homeo=0.05, alpha_homeo=2.5, cache_dir='cache_dir_42', datapath=
shl = SHL(**opts)
data = shl.get_data(matname=tag)

# running main simulations
# Figure 1 & 3
N_cv = 10
homeo_methods = ['None', 'OLS', 'HEH', 'HAP', 'EMP']
seed = 42

# running in parallel on a multi-core machine
import sys
try:
    n_jobs = sys.argv[2]
except:
```

```

n_jobs = 4
n_jobs = 9
n_jobs = 10
n_jobs = 35
n_jobs = 1

list_figures = []

from shl_scripts.shl_experiments import SHL_set
for homeo_method in homeo_methods:
    opts_ = opts.copy()
    opts_.update(homeo_method=homeo_method)
    experiments = SHL_set(opts_, tag=tag + '_' + homeo_method, N_scan=N_cv)
    experiments.run(variables=['seed'], n_jobs=n_jobs, verbose=0)

# Figure 2-B
variables = ['eta', 'alpha_homeo', 'eta_homeo', 'l0_sparseness']

variables = ['eta', 'alpha_homeo', 'eta_homeo']

for homeo_method in homeo_methods:
    opts_ = opts.copy()
    opts_.update(homeo_method=homeo_method)
    experiments = SHL_set(opts_, tag=tag + '_' + homeo_method)
    experiments.run(variables=variables, n_jobs=n_jobs, verbose=0)

# Annex X.X
for algorithm in ['lasso_lars', 'lasso_cd', 'lars', 'omp', 'mp']: # 'threshold',
    opts_ = opts.copy()
    opts_.update(homeo_method='None', learning_algorithm=algorithm, verbose=0)
    shl = SHL(**opts_)
    dico= shl.learn_dico(data=data, list_figures=[],
                        matname=tag + ' - algorithm={}'.format(algorithm))

In [ ]:

#%run model.py

```

Version used¶

```

In [ ]:

%load_ext version_information
%version_information numpy, shl_scripts

```

version control¶

In []:

```
!git status
```

In []:

```
!git pull
```

In []:

```
!git commit -am' {tag} : re-running notebooks'
```

In []:

```
!git push
```

exporting the notebook¶

In []:

```
!jupyter nbconvert Annex.ipynb
```

In []:

```
#!jupyter-nbconvert --template report --to pdf Annex.ipynb
```

In []:

```
!pandoc Annex.html -o Annex.pdf
```

In []:

```
!zip Annex.zip Annex.html
```

Done. Thanks for your attention!