

Domanda 1

Risposta corretta

Punteggio ottenuto
1,00 su 1,00Contrassegna
domanda

Let X be a random variable following a Normal distribution with mean = -5.01 and variance = 3.52 , what is the probability that $X > -3.44$?

Scegli un'alternativa:

- ☒ a. `pnorm(-3.44, -5.01, 1.88, lower.tail = FALSE)`; 0.20
- ☐ b. `pnorm(-3.44, -5.01, 3.52, lower.tail = TRUE)`; 0.67
- ☐ c. `pnorm(-3.44, -5.01, 3.52, lower.tail = FALSE)`; 0.33
- ☐ d. `pnorm(-3.44, -5.01, 1.88, lower.tail = TRUE)`; 0.80

- a. True
- b. False
- c. False
- d. False

La risposta corretta è: `pnorm(-3.44, -5.01, 1.88, lower.tail = FALSE)`; 0.20**Domanda 2**

Risposta errata

Punteggio ottenuto
-0,33 su 1,00Contrassegna
domanda

The interval $(\hat{\theta} - z_{1-\alpha/2}\sqrt{V(\hat{\theta})}; \hat{\theta} + z_{1-\alpha/2}\sqrt{V(\hat{\theta})})$ for the parameter θ of a statistical model is obtained, where $z_{1-\alpha/2}$ is the $1 - \alpha/2$ quantile of a standard normal distribution. Which of the following sentences is true:

Scegli un'alternativa:

- ☐ a. The probability that such a random interval contains the value θ is $1-\alpha$.
- ☐ b. The parameter θ is not contained in the interval with probability $1 - \alpha$.
- ☒ c. The parameter θ is contained in the interval with probability $1 - \alpha$.
- ☐ d. The interval obtained is larger if the value α is larger.

- a. TRUE
- b. FALSE
- c. FALSE
- d. FALSE

La risposta corretta è: The probability that such a random interval contains the value θ is $1-\alpha$.

Domanda 5

Risposta corretta

Punteggio ottenuto
1,00 su 1,00Contrassegna
domanda

The asymptotic distribution for the MLE (maximum likelihood estimator) for a binomial distribution with parameter p is:

Scegli un'alternativa:

- ☐ a. $\hat{p} \sim \mathcal{N}\left(0, \frac{p(1-p)}{n}\right)$
- ☒ b. $\hat{p} \sim \mathcal{N}\left(p, \frac{p(1-p)}{n}\right)$
- ☐ c. $\hat{p} \sim \mathcal{N}(p, p(1-p))$
- ☐ d. $\hat{p} \sim \mathcal{N}(p, np(1-p))$

✓ TRUE

- a. FALSE
- b. TRUE
- c. FALSE
- d. FALSE

La risposta corretta è: $\hat{p} \sim \mathcal{N}\left(p, \frac{p(1-p)}{n}\right)$ **Domanda 6**

Risposta corretta

Punteggio ottenuto
1,00 su 1,00Contrassegna
domanda

Given a sample $y = (y_1, y_2, \dots, y_{10})$ from a $\mathcal{N}(\mu, \sigma^2)$, we want to test the null hypothesis $H_0 : \mu = 0$ against the alternative $H_1 : \mu \neq 0$ at level $\alpha = 0.05$. Suppose we find: $t_{obs} = \sqrt{10} \bar{y} / s = 4.72$. Then, which is the right R code to compute the test's p -value?

Scegli un'alternativa:

- ☐ a. `1-pt(q=4.72, df = 9, lower.tail = FALSE)`
- ☐ b. `pt(q=4.72, df = 10, lower.tail = TRUE)`
- ☒ c. `2*pt(q=4.72, df = 9, lower.tail = FALSE)` ✓ TRUE
- ☐ d. `dt(x=4.72, df = 9)`

- a. FALSE
- b. FALSE
- c. TRUE
- d. FALSE

La risposta corretta è: `2*pt(q=4.72, df = 9, lower.tail = FALSE)`

Domanda 4

Risposta corretta

Punteggio ottenuto
1,00 su 1,00Contrassegna
domanda

Consider the following random sample of 14 cats that collects their weight in kilograms

```
c(4.31, 5.19, 3.37, 4.42, 4.82, 4.02, 5.62, 5.47, 4.38, 6.38,  
3.97, 5.85, 5.35, 5.81)
```

Assume that the random variable weight of cats follows a Normal distribution with mean μ , compute the observed significance level to verify the following hypotheses:

 $H_0: \mu \geq 5$ $H_1: \mu < 5$

```
> n <- length(cat)  
> stat.test.H0 <- (mean(cat)-5)/sqrt(var(cat)/n)  
> stat.test.H0
```

```
[1] -0.3188786
```

Scegli un'alternativa:

- ☒ a. `pt(stat.test.H0, df = n-1)` ✓ TRUE
- ☐ b. `pnorm(stat.test.H0)`
- ☐ c. `pt(stat.test.H0, df = n-1, lower.tail = FALSE)`
- ☐ d. `pnorm(stat.test.H0, lower.tail = FALSE)`

- a. TRUE
- b. FALSE
- c. FALSE
- d. FALSE

La risposta corretta è: `pt(stat.test.H0, df = n-1)`

Domanda 3

Risposta corretta

Punteggio ottenuto

1,00 su 1,00

Contrassegna
domanda

The following code computes:

```
> R <- 1000
> n <- 10
> p <- 0.5
> alpha <- 0.01
> TF <- c()
> for(i in 1:R){
+   p.hat <- mean(rbinom(n,1,p))
+   TF[i] <- (p.hat + qnorm(alpha/2)*sqrt(p.hat*(1-p.hat)/n) < p &
+             p.hat + qnorm(1-alpha/2)*sqrt(p.hat*(1-p.hat)/n) > p)
+ }
> mean(TF)
```

Scegli un'alternativa:

- ☐ a. the nominal level of a confidence interval
- ☒ b. the empirical coverage of a confidence interval ✓ TRUE
- ☐ c. an estimate of the parameter of interest p
- ☐ d. the margin of error of a confidence interval

- a. FALSE
- b. TRUE
- c. FALSE
- d. FALSE

La risposta corretta è: the empirical coverage of a confidence interval