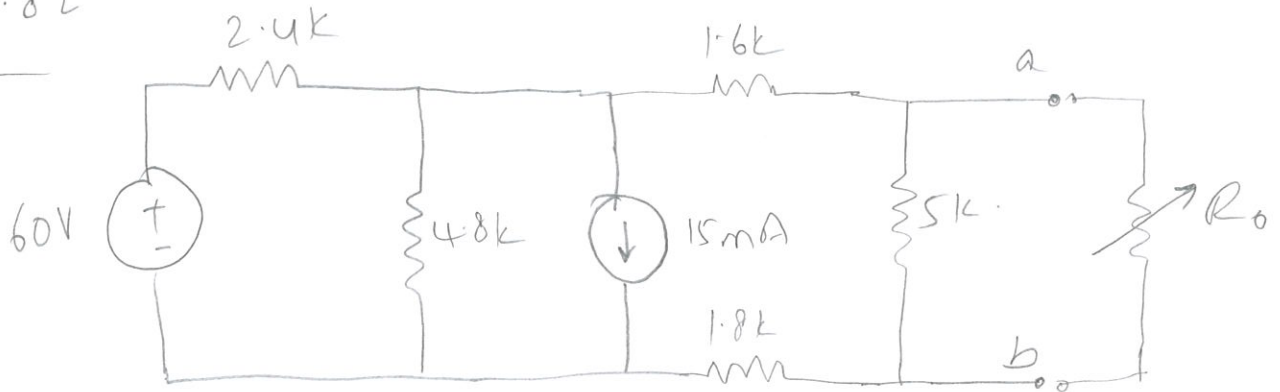


HW Chapter 4, Part B. Solutions

11

Pr 4.82

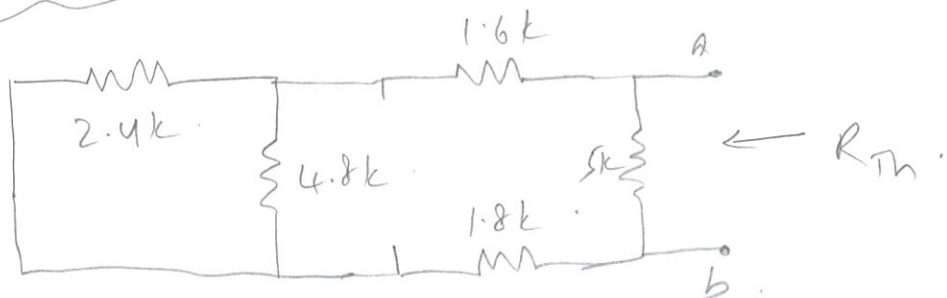


(a) Find the value of R_o for max power

(b) Find the value of max power.

We have to create the Thevenin Equivalent circuit.
i.e. we have to find V_{Th} & R_{Th} .

a). To find R_{Th} ; deactivate the 2 sources:

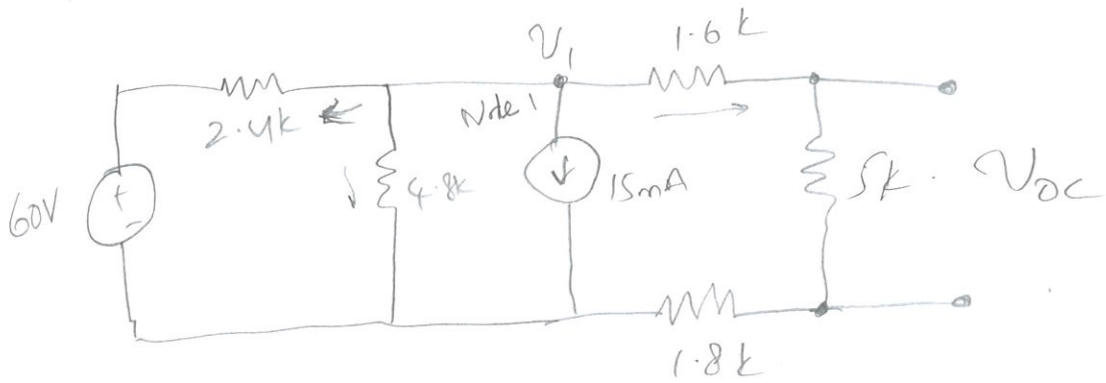


$$\begin{aligned} R_{Th} &= 5k \parallel (1.6k + 1.8k + 2.4k \parallel 4.8k) \\ &= 5k \parallel (3.4k + 1.6k) \\ &= 5k \parallel 5k \end{aligned}$$

$$R_{Th} = \underline{2.5k \Omega}$$

So, R_o for max power is $R_{Th} = \underline{2.5k \Omega}$

b) First, find V_{TH} (V_{oc}).



We can calculate V_{oc} by writing the KCL at Node (1).

Then, we can use voltage divider to find the voltage across the $5k$ resistor.

KCL at
Node 1:

$$\frac{V_1 - 60}{2.4k} + \frac{V_1}{4.8k} + \frac{V_1}{(1.6k + 5k + 1.8k)} + 15 \times 10^{-3} = 0$$

$$\Rightarrow \frac{V_1 - 60}{2.4} + \frac{V_1}{4.8} + \frac{V_1}{8.4} = -15 \times 10^{-3} \times 1000$$

$$\text{So, } \frac{16.8(V_1 - 60) + 8.4V_1 + 4.8V_1}{40.32} = -15$$

$$30V_1 = 403.2$$

$$V_1 = 13.17 \text{ volts}$$

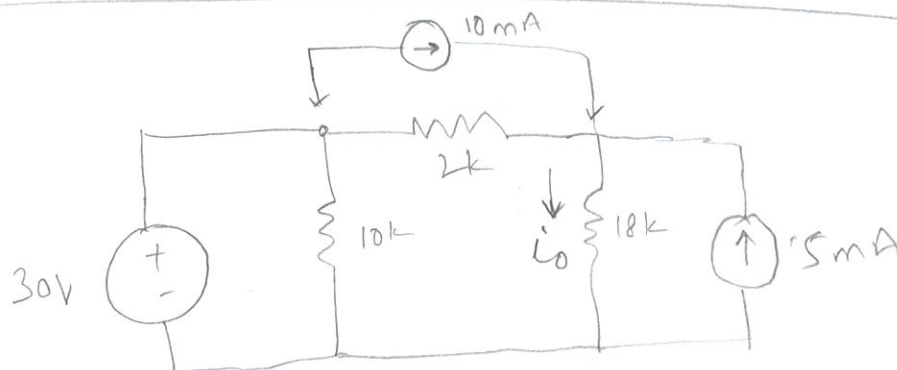
$$\text{Using voltage divider } V_{TH} = V_{oc} = \frac{5k}{(5k + 1.6k + 1.8k)} * 13.17 = \underline{\underline{8 \text{ volts}}}$$

Hence:
$$P_{\max} = \frac{V_{Th}^2}{4R_L}$$

$$= \frac{8^2}{4 \times 2.5 \times 10^3}$$

$$= 6.4 \text{ milliwatts}$$

Pr 4.95



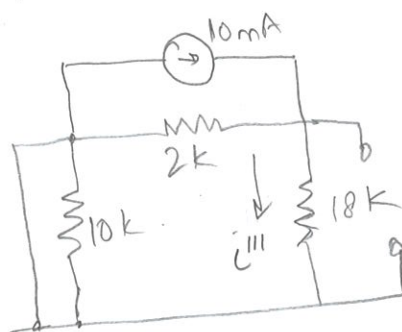
Since there are a total of 3 sources in the network, the current i_o can be written as

$$i_o = i' + i'' + i'''$$

Given that $i' + i'' = 1.5 \text{ mA}$

To find i''' ,

By Superposition we deactivate the other 2 sources.



10k resistor is shorted.

Using the Current-divider formula;

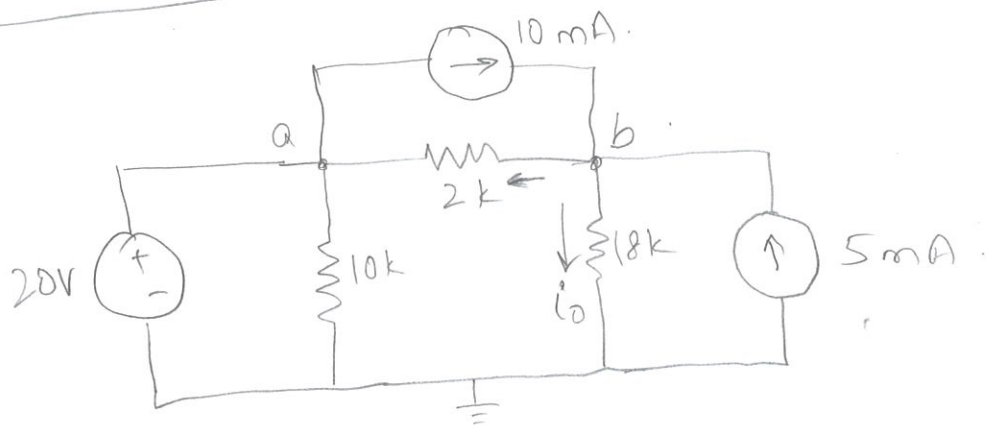
(4)

$$i'' = i_{18k} = \frac{2k * 10mA}{(18k + 2k)} \\ = 1mA$$

Hence, when all 3 sources are attached,

$$i_o = i' + i'' + i''' = 1.5 + 1 \\ = 2.5mA$$

b) With all 3 sources connected:



Writing KCL
at node B:

$$\frac{V_b}{18k} + \frac{V_b - 20}{2k} - 5 \times 10^{-3} - 10 \times 10^{-3} = 0$$

$$\frac{V_b}{18} + \frac{V_b - 20}{2} = 15$$

$$\frac{10V_b}{18} = 15 + 10$$

$$V_b = 45 \text{ volts}$$

$$\text{Hence } i_o = \frac{V_b}{R} = \frac{45}{18k} = 2.5mA$$