

### Homework 1

2.1-1 Using Figure 2.2 as a model, illustrate the operation of INSERTION-SORT on the array

$A = \langle 31, 41, 59, 26, 41, 58 \rangle$

2.1-3

Consider the *searching problem*:

Input: A sequence of  $n$  numbers  $A = \langle a_1, a_2, \dots, a_n \rangle$  and a value  $v$ .

Output: An index  $i$  such that  $v = A[i]$  or the special value NIL if  $v$  does not appear in  $A$ .

Write pseudocode for linear search, which scans through the sequence, looking for  $v$ . Using a loop invariant, prove that your algorithm is correct. Make sure that your loop invariant fulfills the three necessary properties.

2.2-1 Express the function  $n^3 / 1000 - 100n^2 - 100n + 3$  in terms of  $\theta$  notation

2.3-1 Using Figure 2.4 as a model, illustrate the operation of merge sort on the array

$A = \langle 3, 41, 52, 26, 38, 57, 9, 49 \rangle$

*Homework2*

1. Show that the solution of  $T(n) = 2T(\lceil n/2 \rceil) + 1$  is  $O(\lg n)$
2. Solve the recurrence  $T(n) = 2T(\sqrt{n}) + 1$  by making a change of variables. Your solution should be asymptotically tight. Do not worry about whether values are integral.
- 3.(4.4-1) Use a recursion tree to determine a good asymptotic upper bound on the recurrence  $T(n) = 3T(\lfloor n/2 \rfloor) + n$ . Use the substitution method to verify your answer.

4. The recurrence  $T(n) = 7T(n/2) + n^2$  describes the running time of an algorithm A. A competing algorithm  $A'$  has a running time of  $T'(n) = aT'(n/4) + n^2$ . What is the largest integer value for  $a$  such that  $A'$  is asymptotically faster than A?

5.(4.5-3) Use the master method to show that the solution to the binary-search recurrence  $T(n) = T(n/2) + \Theta(1)$  is  $T(n) = \Theta(\lg n)$  (See Exercise 2.3-5 for a description of binary search.)

### *Homework3*

6.1-1 What are the minimum and maximum numbers of elements in a heap of height  $h$ ?

6.2-1 Using Figure 6.2 as a model, illustrate the operation of MAX-HEAPIFY( $A, 3$ ) on the array  $A = \langle 27, 17, 3, 16, 13, 10, 1, 5, 7, 12, 4, 8, 9, 0 \rangle$ .

7.2-2 What is the running time of QUICKSORT when all elements of array  $A$  have the same value ?

8.2-1 Using Figure 8.2 as a model, illustrate the operation of COUNTING-SORT on the array  $A = \langle 6, 0, 2, 0, 1, 3, 4, 6, 1, 3, 2 \rangle$

#### *Homework4*

1. Show how to modify the PRINT\_STATIONS procedure to print out the stations in increasing order of station number. (Hint: Use recursion)

15.2-1 Find an optimal parenthesization of a matrix-chain product whose sequence of dimensions is  $\langle 5, 10, 3, 12, 5, 50, 6 \rangle$ .

15.4-1 Determine an LCS of  $\langle 1, 0, 0, 1, 0, 1, 0, 1 \rangle$  and  $\langle 0, 1, 0, 1, 1, 0, 1, 1, 0 \rangle$

### *Homework5*

24.1-1 Run the Bellman-Ford algorithm on the directed graph of Figure 24.4, using vertex  $z$  as the source. In each pass, relax edges in the same order as in the figure, and show the  $d$  and  $\pi$  values after each pass. Now, change the weight of edge  $(z, x)$  to 4 and run the algorithm again, using  $s$  as the source.

25.1-1 Run SLOW-ALL-PAIRS-SHORTEST-PATHS on the weighted, directed graph of Figure 25.2, showing the matrices that result for each iteration of the loop. Then do the same for FASTER-ALL-PAIRS-SHORTEST-PATHS.

25.2-1 Run the Floyd-Warshall algorithm on the weighted, directed graph of Figure 25.2. Show the matrix  $D^{(k)}$  that results for each iteration of the outer loop.