

**Please note that, this file is just an auxiliary material for reviewing this course, practices and thinking are still necessary to comprehend solid mechanics.**

**Please don't simply recite them, but try to understand the essence of each formula and think about in which case you can use it.**

### ① axial load

normal stress:  $\sigma_n = \frac{F}{A}$

normal strain:  $\epsilon_n = \frac{\Delta l}{l}$

axial deformation:  $\delta = \frac{Fl}{EA}$

thermal deformation:  $\delta_t = \Delta T \cdot \alpha \cdot l$

### ② torsion

polar moment of inertia  $J = \begin{cases} \frac{\pi}{2} \cdot C^4, & \text{solid} \\ \frac{\pi}{2} (C_o^4 - C_i^4), & \text{hollow} \end{cases}$

shear stress under torsion:  $\tau = \frac{T \cdot C}{J}$

twist angle:  $\varphi = \frac{T \cdot l}{J \cdot G}$

### ③ analysis of beam

$\begin{cases} \text{BMD} \\ \text{SFD} \end{cases} \rightarrow \text{Pay attention to the sign of } M \& Q$

geometric properties:  $I = I_s + A d^2$

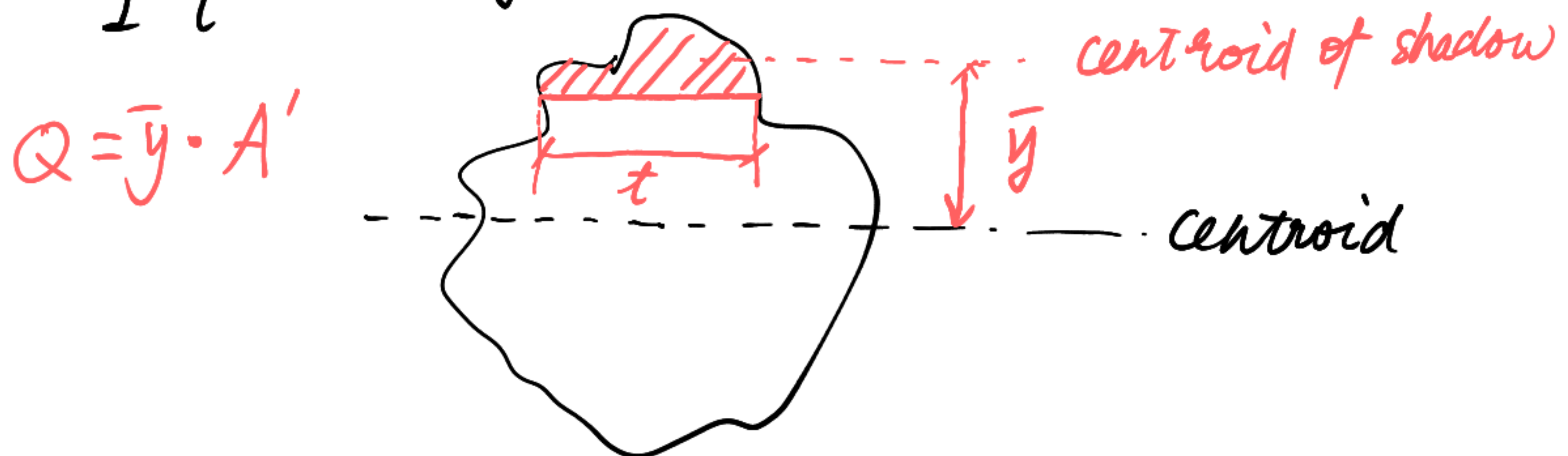
$\uparrow$   
about its self centroid axis

normal stress under bending moment:

$$\sigma_n = \frac{M}{I} \cdot y \quad (\text{Pay attention to the value of } y, \text{ depends on which stress you determine})$$

shear stress under shear force:

$$\tau = \frac{V \cdot Q}{I \cdot t} \quad (\text{Pay attention to } Q \text{ and } t)$$



#### ④ plane-stress transformation

pay attention to the sign of  $\sigma$  and  $\tau$

$$\sigma_{\max, \min} = \frac{\sigma_x + \sigma_y}{2} \pm \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + \tau_x^2}$$

$$\tau_{\max} = \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + \tau_x^2}$$

$$\sigma_{\text{ave}} = \frac{\sigma_x + \sigma_y}{2}$$

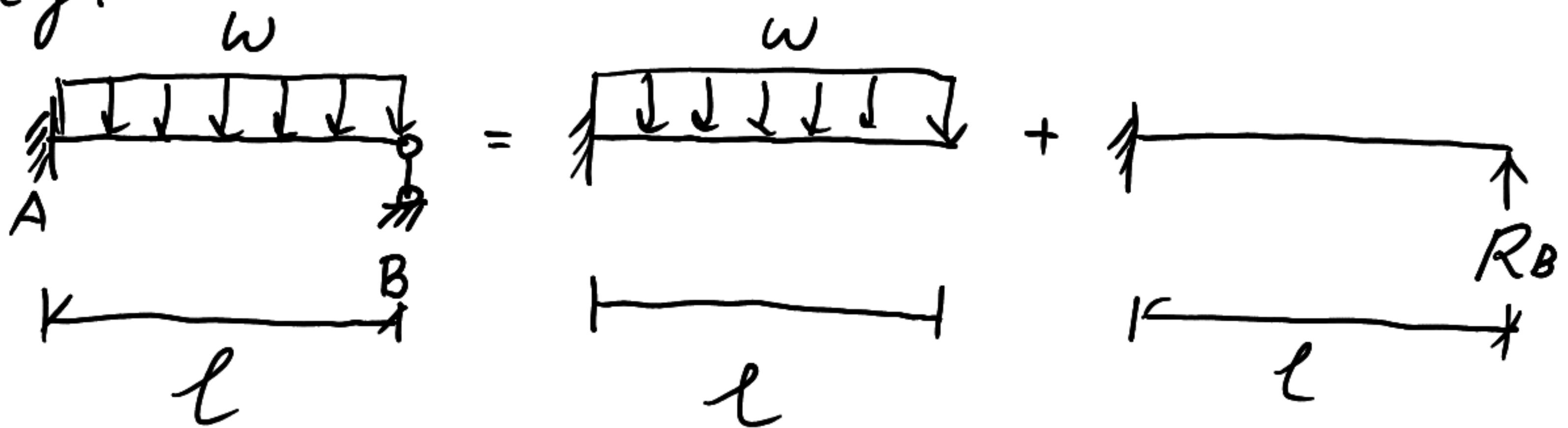
⑤ deflection of beam & statically indeterminate beam

$$M(x) = -EI y'' = -EI \frac{d^2 y}{dx^2}$$

integral constant  $C_1, C_2, \dots, C_n$  are determined by using boundary condition and continuity condition.

Optional method to solve statically indeterminate beam is using principle of superposition.

eg.



⑥ buckling

$$P_{cr} = \frac{\pi^2 EI}{l_e^2} \quad (\text{Pay attention to } I \text{ and } l_e)$$