

Foundations of Solid Mechanics

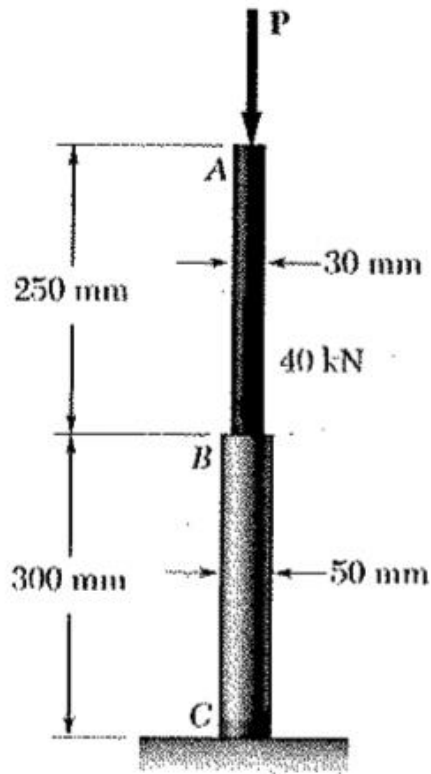
E2: Axial load

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Foundations of Solid Mechanics

Exercise-1

1. Two solid cylindrical rods are jointed at B and loaded as shown. Rod AB is made of steel ($E = 200$ GPa) and rod BC of brass ($E = 105$ GPa). Determine (a) the load P for which the total deformation of the rod is -0.2 mm, (b) the corresponding deflection of point B.



$$\delta_{total} = \delta_{Ac} = \delta_{AB} + \delta_{BC} = -0.2 \text{ mm}$$

$$F_{AB} = P \text{ (compression)}$$

$$F_{BC} = P + 40 \text{ (compression)}$$

$$\delta_{total} = \delta_{AB} + \delta_{BC}$$

$$= \frac{P \cdot l_{AB}}{E_{AB} \cdot A_{AB}} + \frac{(P + 40) \cdot l_{BC}}{E_{BC} \cdot A_{BC}} = 0.2 \text{ mm}$$

$$\rightarrow P = 44.0 \text{ kN}$$

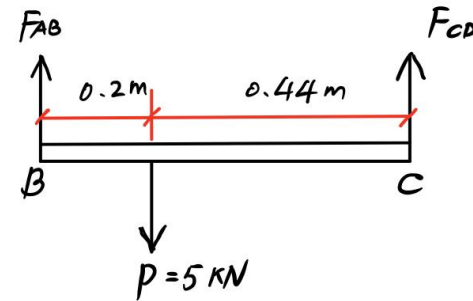
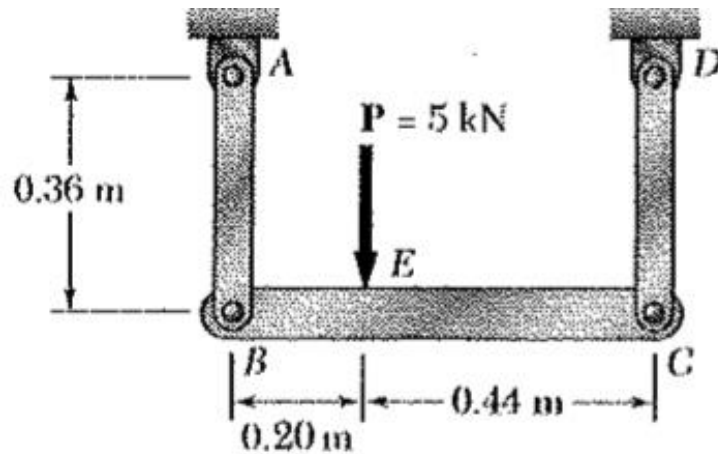
$$\delta_B = \delta_{BC} = \delta_B - \delta_C \quad (\delta_C = 0, C \text{ is fixed})$$

$$= 0.1222 \text{ mm } (\downarrow)$$

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Exercise-2

2. Each of the link AB and CD is made of aluminum ($E = 75 \text{ GPa}$) and has a cross-sectional area of 125 mm^2 . Knowing that they support the rigid member BC, determine the deflection of point E.



Step 1

$$\sum M_C = 0 \rightarrow$$

$$-0.64 \cdot F_{AB} + P \cdot 0.44 = 0$$

$$\rightarrow F_{AB} = 3.4375 \text{ kN}$$

$$\sum M_B = 0 \rightarrow$$

$$0.64 \cdot F_{CD} - 0.2 \cdot P = 0$$

$$\rightarrow F_{CD} = 1.5625 \text{ kN}$$

Step 2

$$\delta_B = \frac{F_{AB} \cdot l}{EA} = \frac{3.4375 \times 10^3 \times 0.36}{75 \times 10^9 \times 125 \times 10^{-6}} = 132 \times 10^{-6} \text{ m}$$

$$\delta_C = \frac{F_{CD} \cdot l}{EA} = \frac{1.5625 \times 10^3 \times 0.36}{75 \times 10^9 \times 125 \times 10^{-6}} = 60 \times 10^{-6} \text{ m}$$

Step 3

$$\delta_E = \delta_C + l_{CE} \cdot \theta$$
$$= \delta_C + \frac{l_{CE}}{l_{BC}} (\delta_B - \delta_C)$$
$$= 109.5 \times 10^{-6} \text{ m}$$
$$\theta = \frac{\delta_B - \delta_C}{l_{BC}}$$

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Exercise-3

3. The steel bars shown in below are pin connected to a rigid member. If the applied load on the member is 15kN, determine the force developed in each bar. Bars AB and EF each have a cross-sectional area of 50mm^2 , and the bar CD has a cross-sectional area of 30mm^2 .

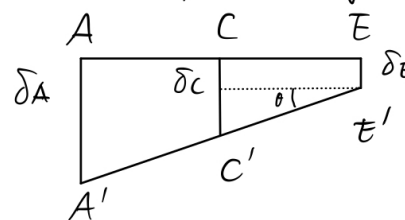
• 3 unknowns : F_{AB} , F_{CD} , F_{EF}

• we need 3 independent equations to solve them

• equilibrium equations can only provide 2 independent equations, which are:

$$\boxed{\sum F_y = 0} \quad (1) \quad \boxed{\sum M_C = 0} \quad (2) \quad (\text{or you can use } \sum M_A = 0, \sum M_E = 0, \dots)$$

• compatibility condition can provide 1 equation



$$\theta = \frac{\delta_A - \delta_E}{L_{AE}} = \frac{\delta_C - \delta_E}{L_{CE}}$$

$$\rightarrow \boxed{\delta_C = \frac{\delta_A + \delta_E}{2}} \quad (3)$$

$$F_A = 9.52 \text{ kN}, \quad F_C = 3.46 \text{ kN}, \quad F_E = 2.02 \text{ kN}$$

