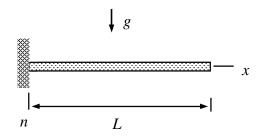
Assignment 1 (2p)

Find the stress resultants of the plate strip of length L, width H, and thickness t which is loaded by its own weight. Density of the plate material is ρ . Assume that the resultants do not depend on y. Use the plate equilibrium equations in the Cartesian system



$$\left\{ \frac{\partial N_{xx}}{\partial x} + \frac{\partial N_{xy}}{\partial y} + b_x \\ \frac{\partial N_{yy}}{\partial y} + \frac{\partial N_{xy}}{\partial x} + b_y \right\} = 0 \text{ and } \begin{cases} \frac{\partial Q_x}{\partial x} + \frac{\partial Q_y}{\partial y} + b_n \\ \frac{\partial M_{xx}}{\partial x} + \frac{\partial M_{xy}}{\partial y} - Q_x \\ \frac{\partial M_{yy}}{\partial y} + \frac{\partial M_{xy}}{\partial x} - Q_y \end{cases} = 0 \text{ in } (0, L) \times (0, H).$$

Solution

In plate strip problem, the resultants do not depend on y and $Q_y = N_{xy} = M_{xy} = 0$. The differential equations that are not satisfied automatically and their boundary conditions at the free end simplify to

$$= 0$$
 in $(0,L)$ and $= 0$ at $x = L$
 $= 0$ in $(0,L)$ and $= 0$ at $x = L$
 $= 0$ in $(0,L)$ and $= 0$ at $x = L$

Solutions to the stress resultants are

$$N_{xx}(x) = \underline{\hspace{1cm}},$$
 $Q_x(x) = \underline{\hspace{1cm}},$
 $M_{xx}(x) = \underline{\hspace{1cm}},$