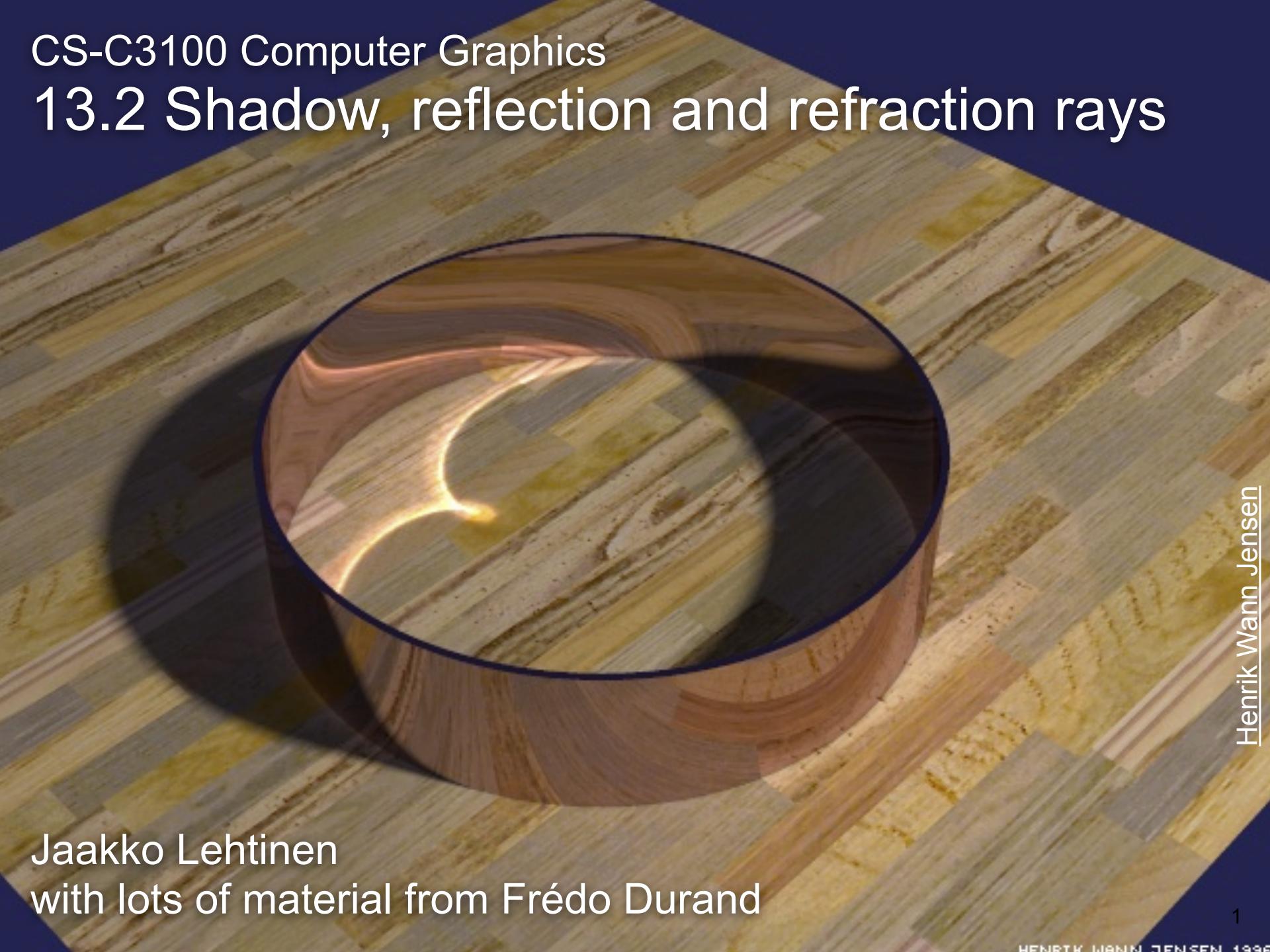


13.2 Shadow, reflection and refraction rays



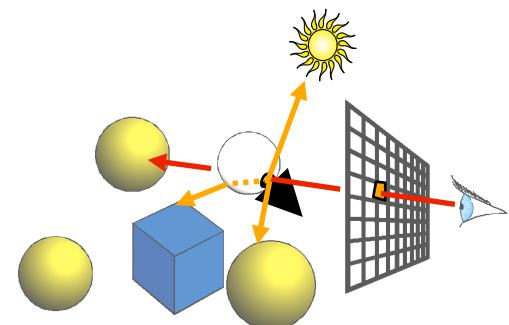
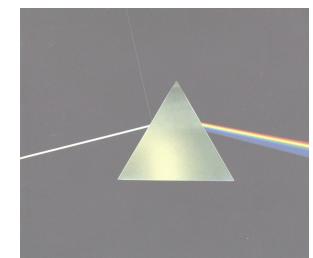
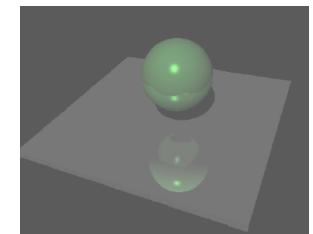
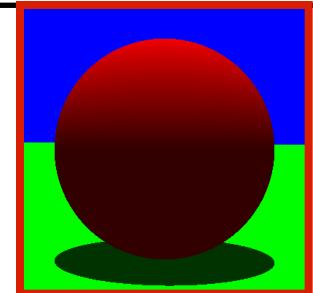
Jaakko Lehtinen
with lots of material from Frédo Durand

In This Video

- Using the ray tracer for..
 - Shadows
 - With an important optimization
 - Reflections
 - Only perfect mirrors for now
 - Refractions
 - The Snell-Descartes law and refractive indices

Using a Ray Tracer for..

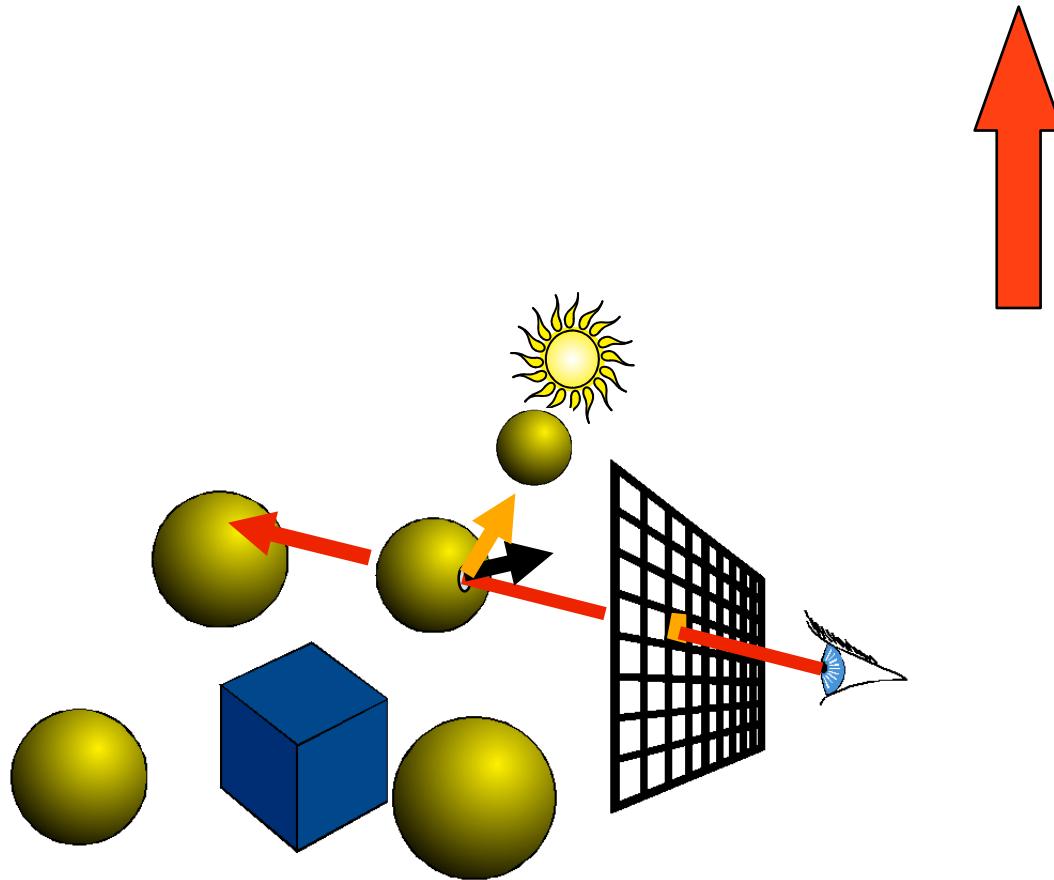
- Shadows
- Reflection
- Refraction
- Recursive Ray Tracing
 - “Hall of mirrors”



How Can We Add Shadows?

$$I = k_d \max(0, \mathbf{L} \cdot \mathbf{N}) V(\mathbf{L})$$

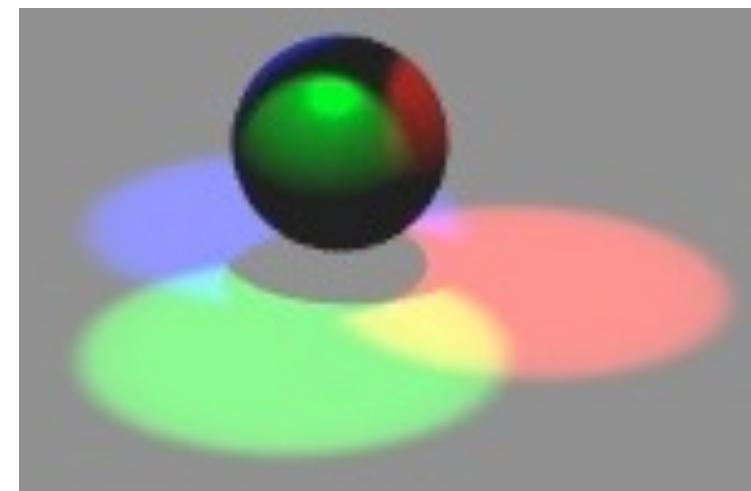
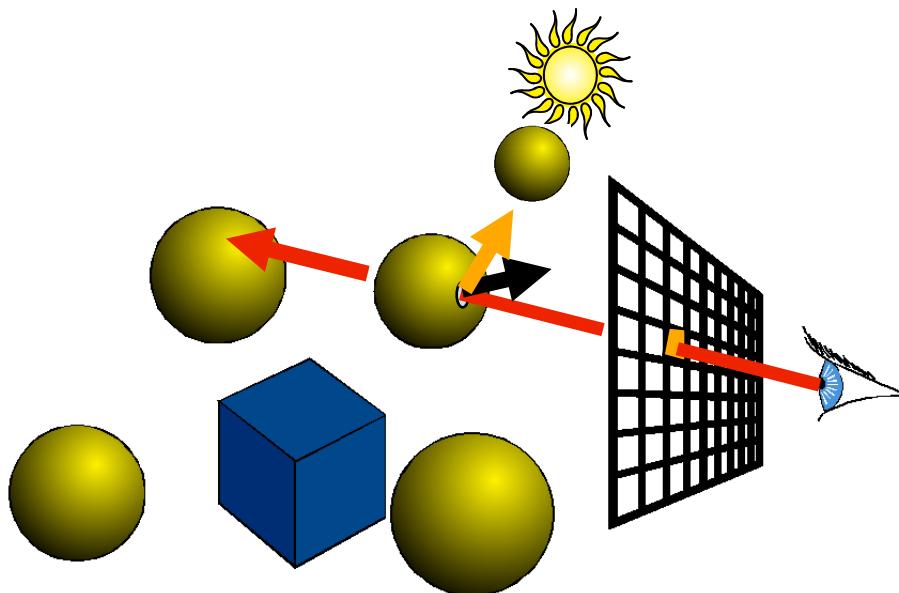
direct
lighting



How Can We Add Shadows?

```
color = ambient*hit->getMaterial()->getDiffuseColor()
for every light
    Ray ray2(hitPoint, directionToLight)
    Hit hit2(distanceToLight, NULL, NULL)
    For every object
        object->intersect(ray2, hit2, 0)
        if (hit2->getT() = distanceToLight)
            color += hit->getMaterial()->Shade
                (ray, hit, directionToLight, lightColor)
return color
```

ambient = k_a
diffuseColor = k_d



Problem: Self-Shadowing

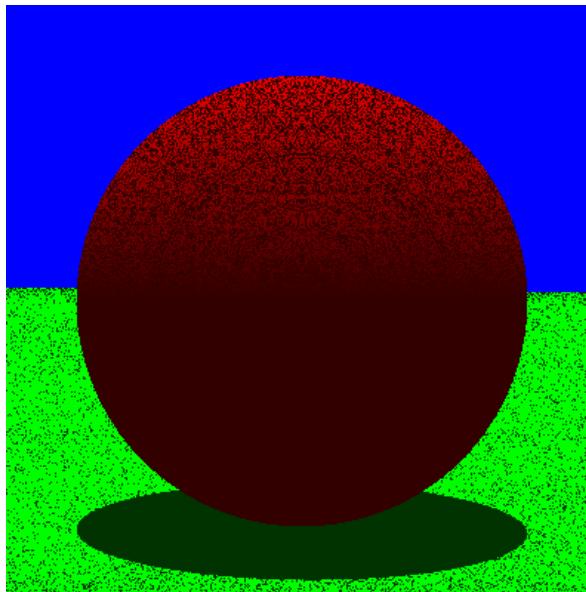
```
color = ambient*hit->getMaterial()->getDiffuseColor()
for every light
    Ray ray2(hitPoint, directionToLight)
    Hit hit2(distanceToLight, NULL, NULL)
    For every object
        object->intersect(ray2, hit2, 0)
        if (hit2->getT() = distanceToLight)
            color += hit->getMaterial()->Shade
                            (ray, hit, directionToLight, lightColor)
return color
```

Problem: Self-Shadowing

```
color = ambient*hit->getMaterial()->getDiffuseColor()
for every light
    Ray ray2(hitPoint, directionToLight)
    Hit hit2(distanceToLight, NULL, NULL)
    For every object
        object->intersect(ray2, hit2, epsilon)
        if (hit2->getT() = distanceToLight)
            color += hit->getMaterial()->Shade
                            (ray, hit, directionToLight, lightColor)
return color
```

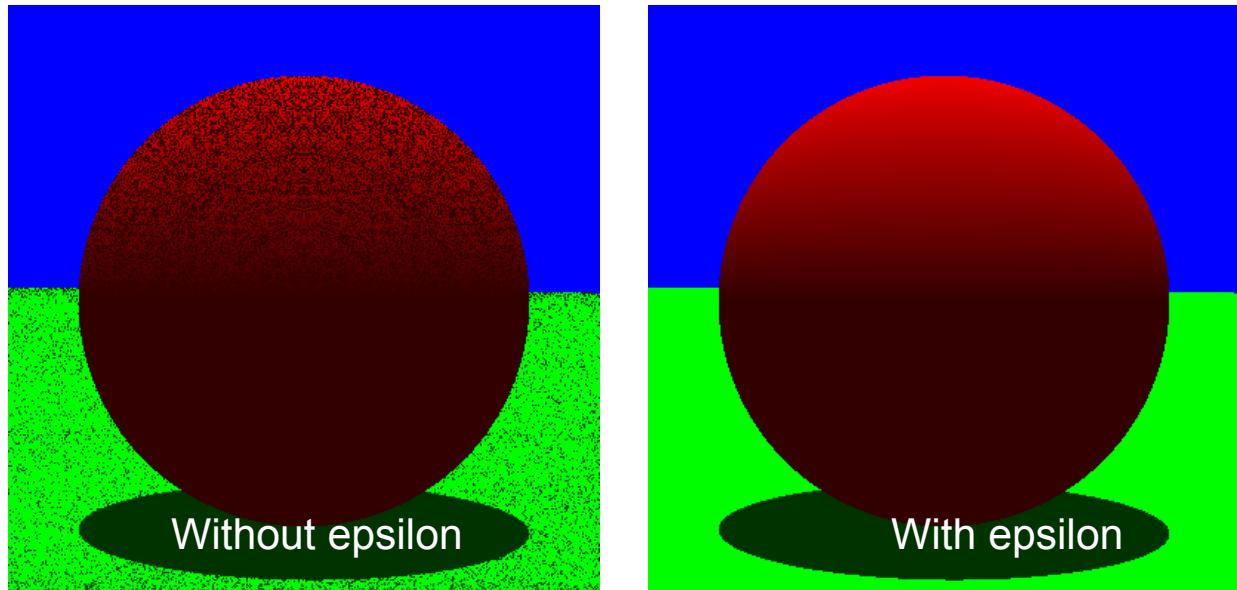
Problem: Self-Shadowing

```
color = ambient*hit->getMaterial()->getDiffuseColor()
for every light
    Ray ray2(hitPoint, directionToLight)
    Hit hit2(distanceToLight, NULL, NULL)
    For every object
        object->intersect(ray2, hit2, epsilon)
        if (fabs(hit2->getT() - distanceToLight) < epsilon)
            color += hit->getMaterial()->Shade
                (ray, hit, directionToLight, lightColor)
return color
```



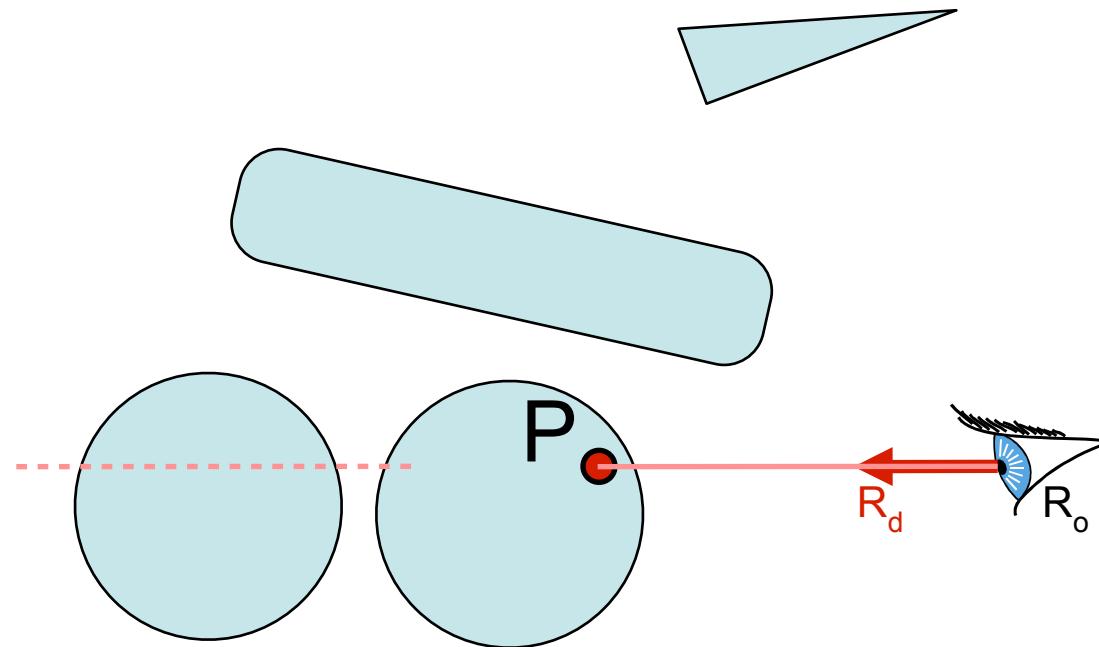
Problem: Self-Shadowing

```
color = ambient*hit->getMaterial()->getDiffuseColor()
for every light
    Ray ray2(hitPoint, directionToLight)
    Hit hit2(distanceToLight, NULL, NULL)
    For every object
        object->intersect(ray2, hit2, epsilon)
        if (fabs(hit2->getT() - distanceToLight) < epsilon)
            color += hit->getMaterial()->Shade
                (ray, hit, directionToLight, lightColor)
return color
```



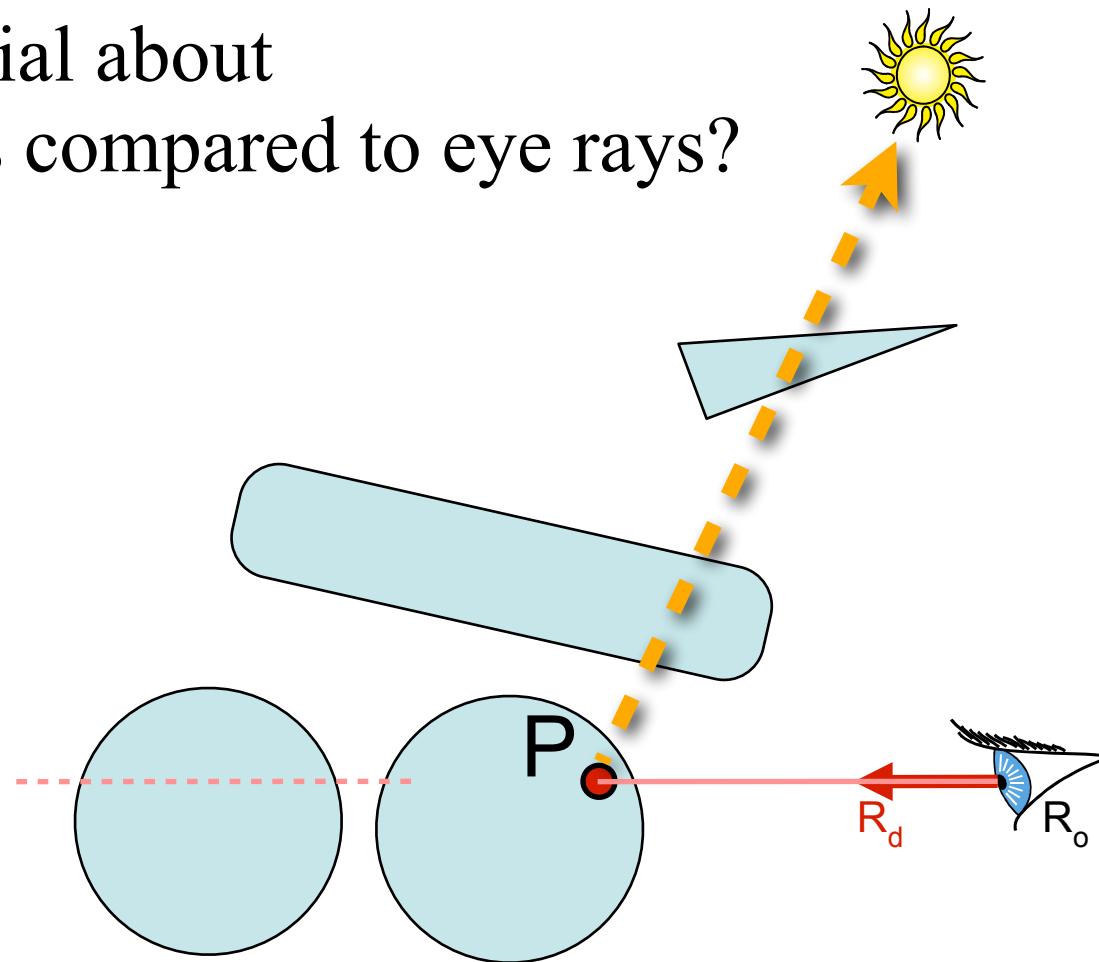
Let's Think About Shadow Rays

- What's special about shadow rays compared to eye rays?



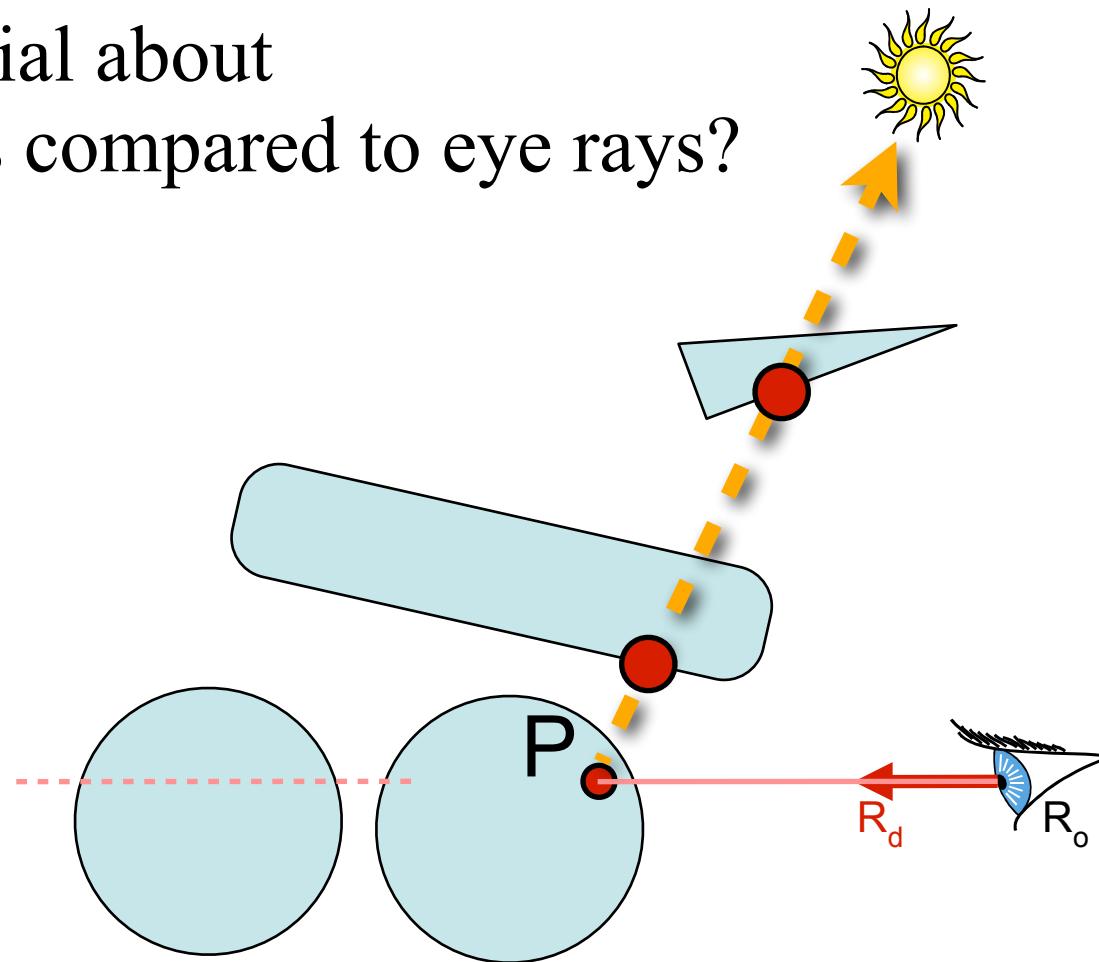
Let's Think About Shadow Rays

- What's special about shadow rays compared to eye rays?



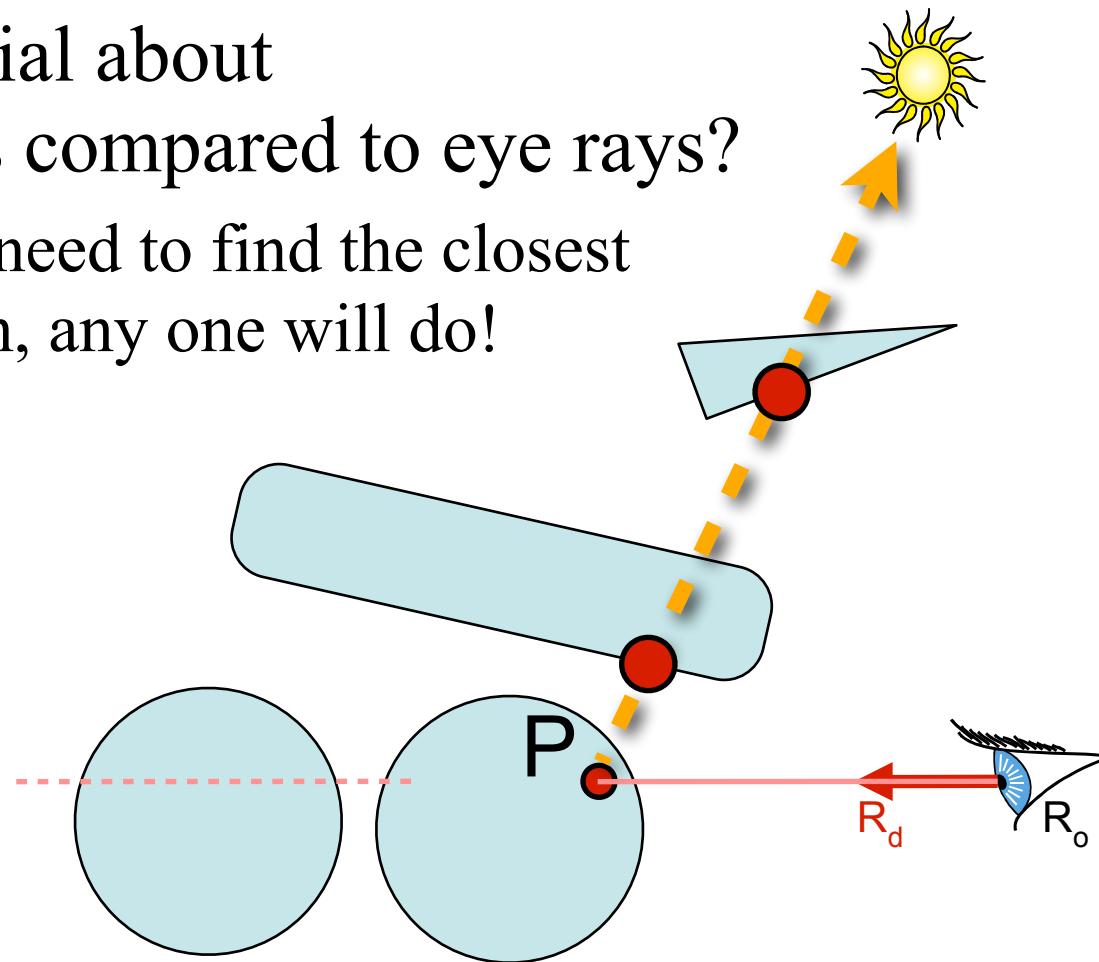
Let's Think About Shadow Rays

- What's special about shadow rays compared to eye rays?

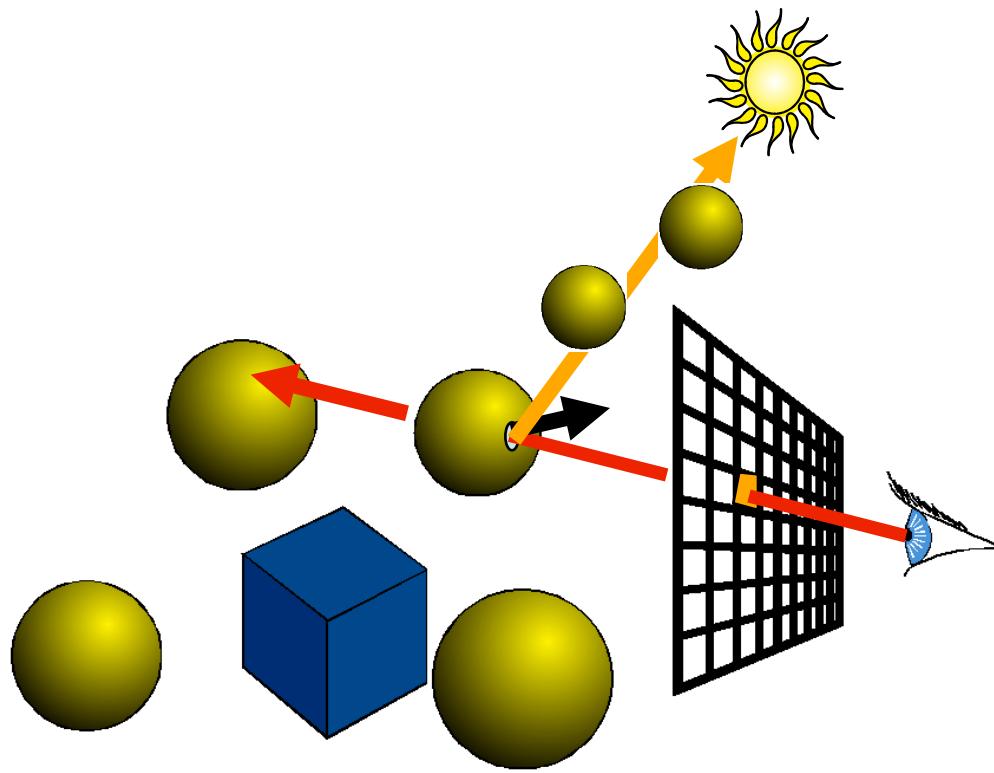


Let's Think About Shadow Rays

- What's special about shadow rays compared to eye rays?
 - We do not need to find the closest intersection, any one will do!

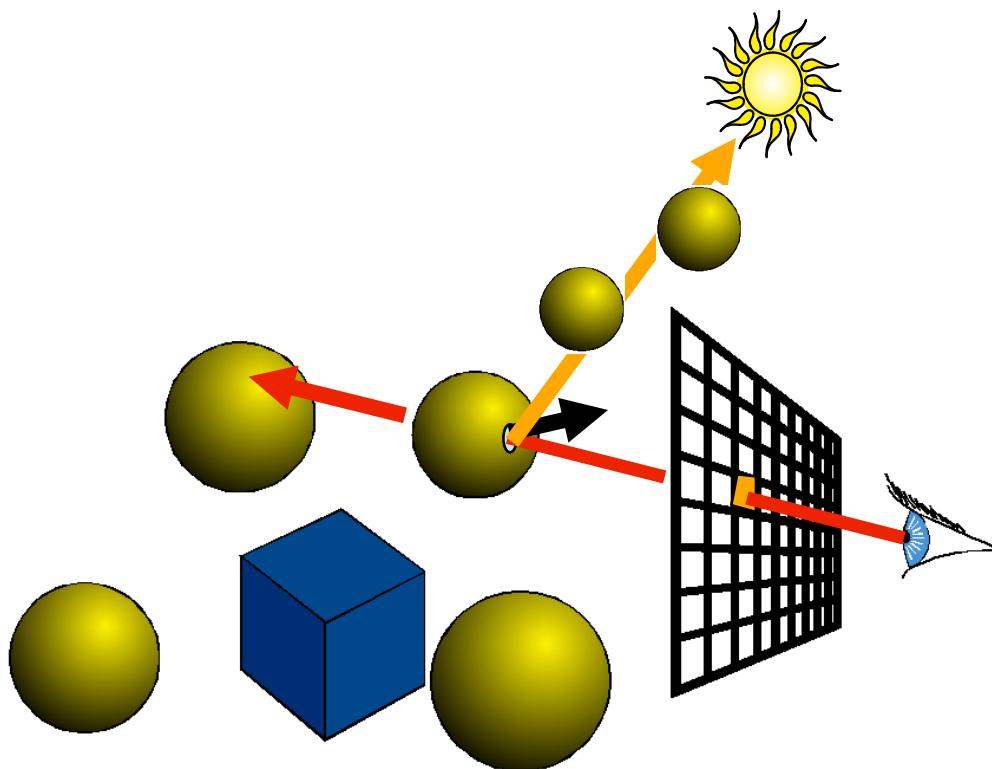


Shadow Optimization



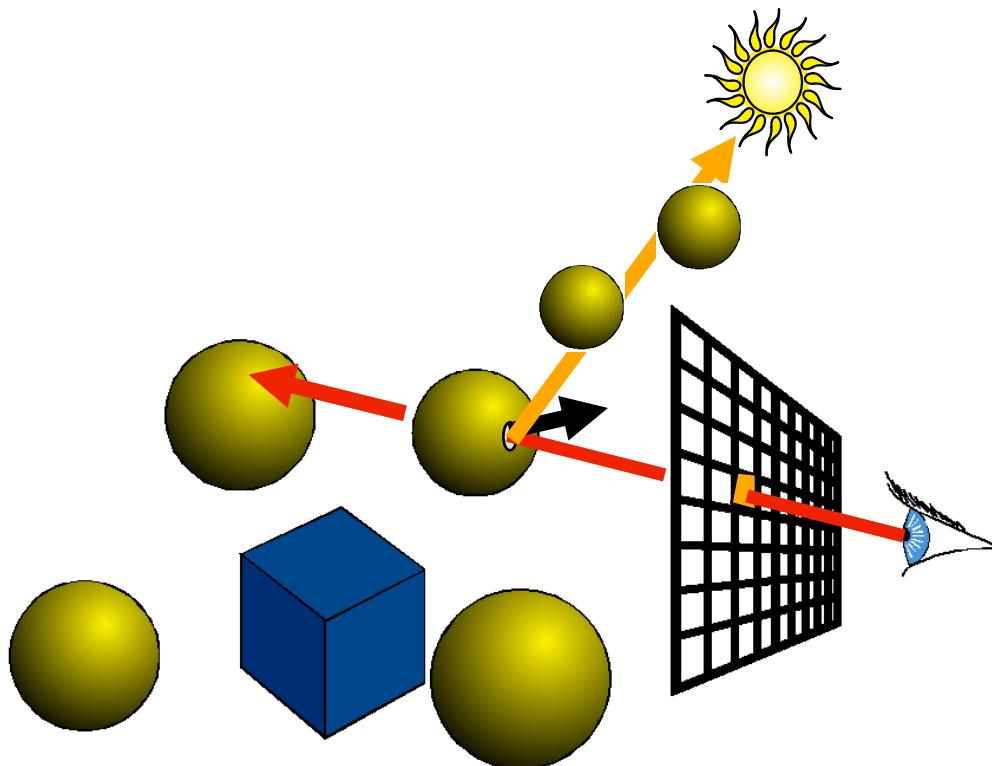
Shadow Optimization

- We only want to know whether there is an intersection, *not* which one is closest



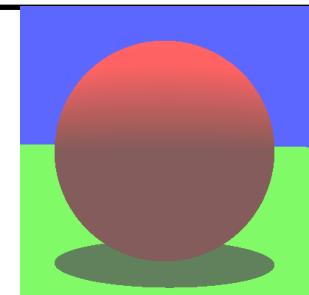
Shadow Optimization

- We only want to know whether there is an intersection, *not* which one is closest
- Special routine `Object3D::intersectShadowRay()`
 - Stops at first intersection found

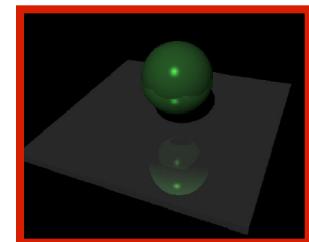


Using a Ray Tracer for..

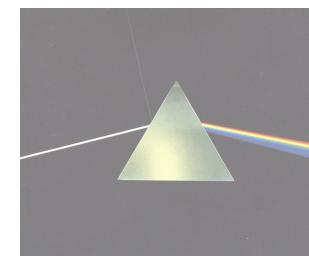
- Shadows



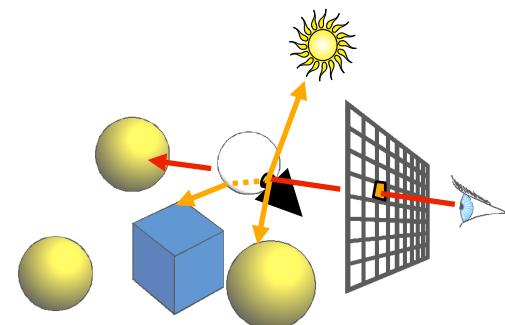
- Reflection



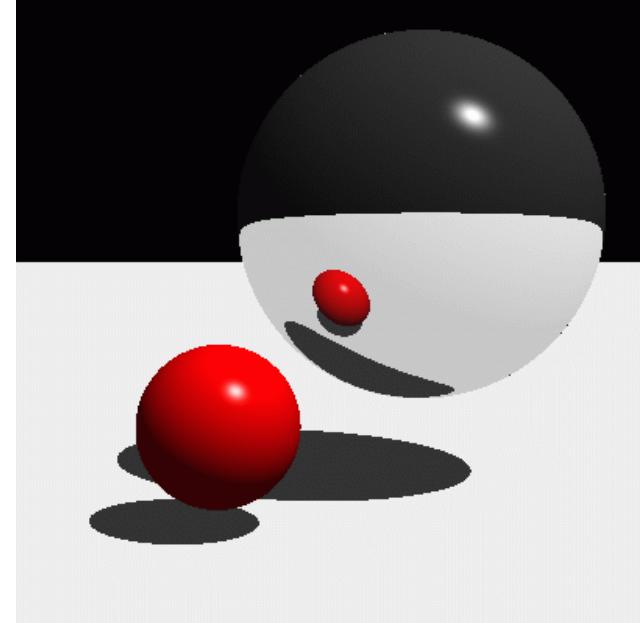
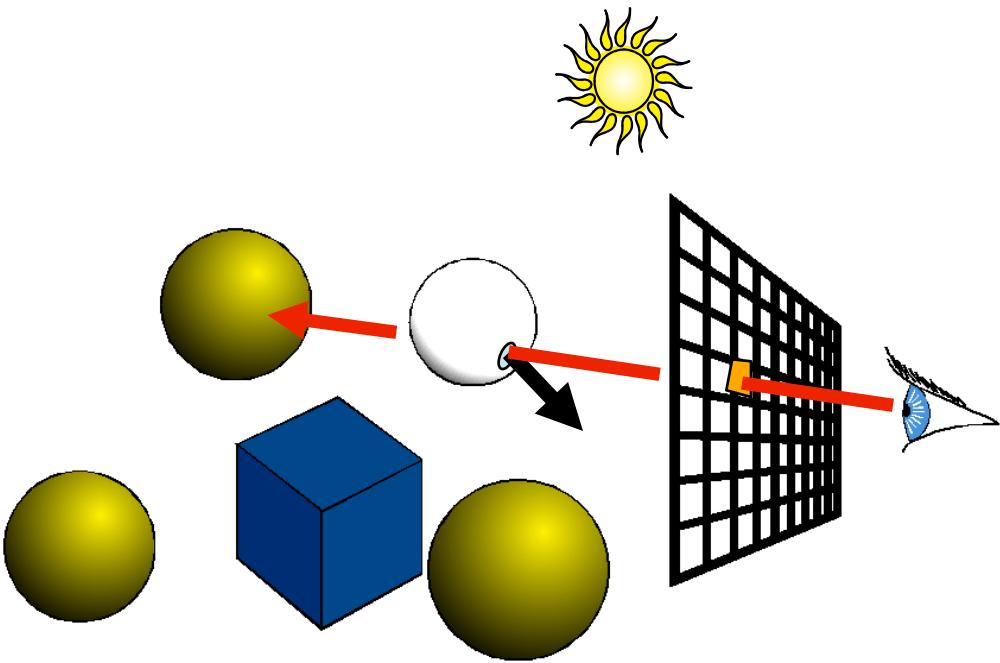
- Refraction



- Recursive Ray Tracing

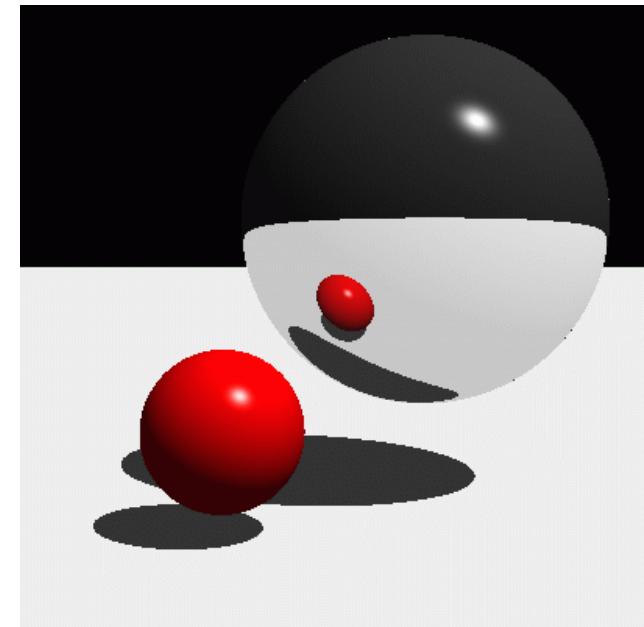
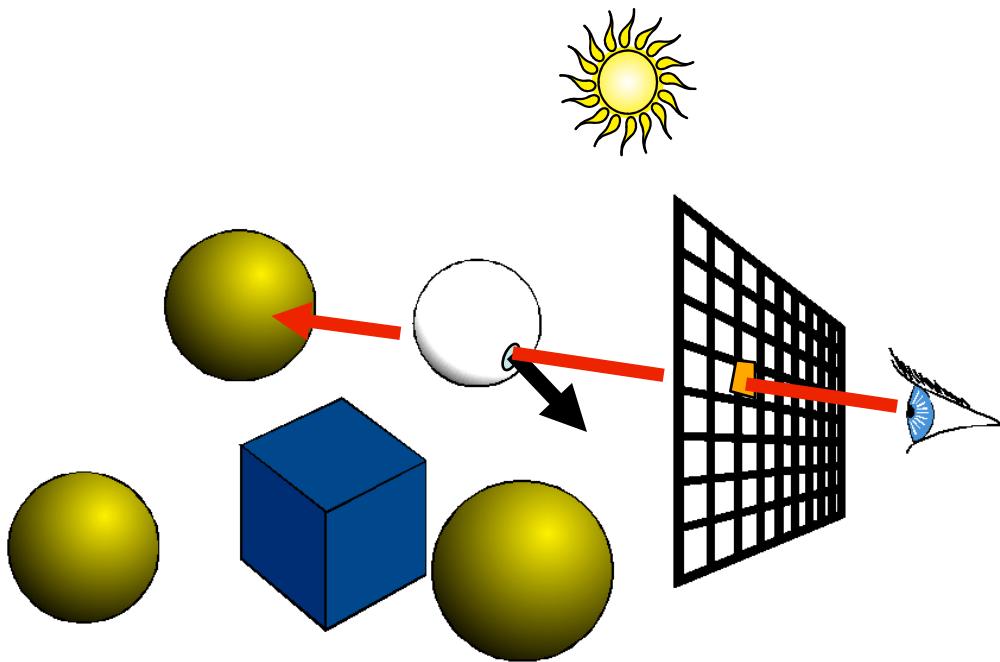


Mirror Reflection



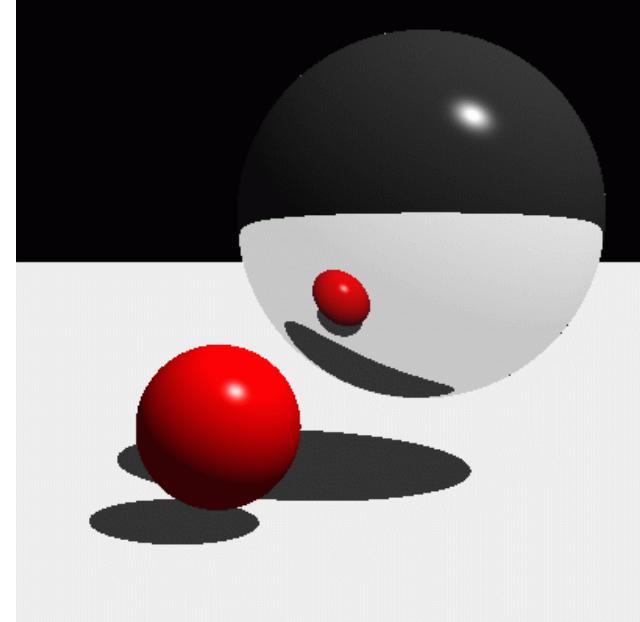
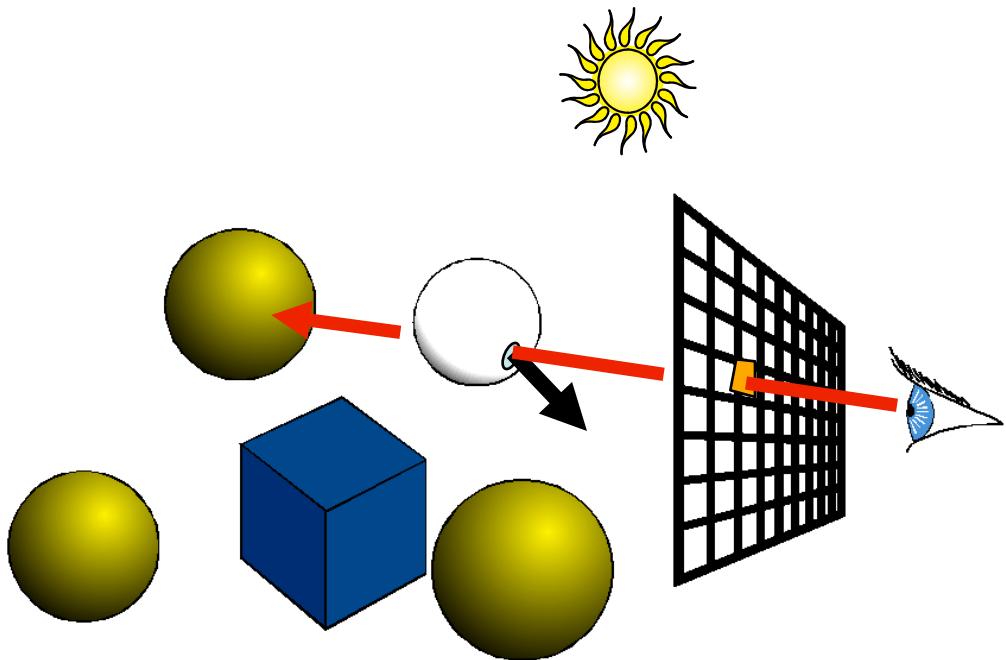
Mirror Reflection

- Cast ray symmetric with respect to the normal



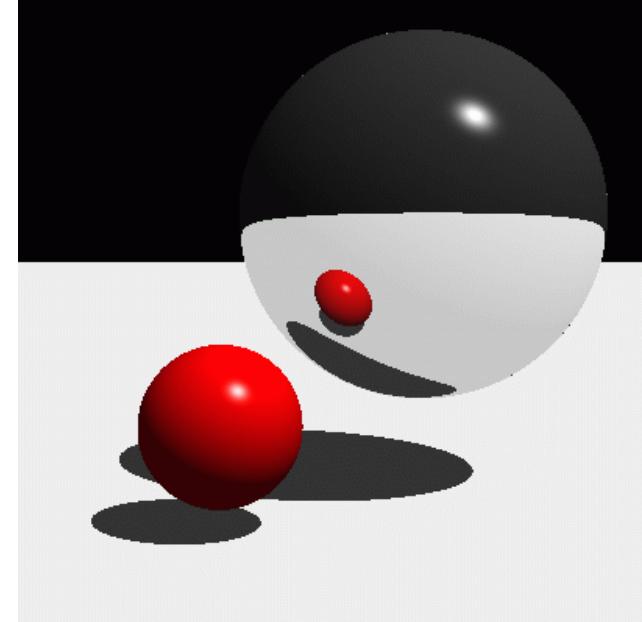
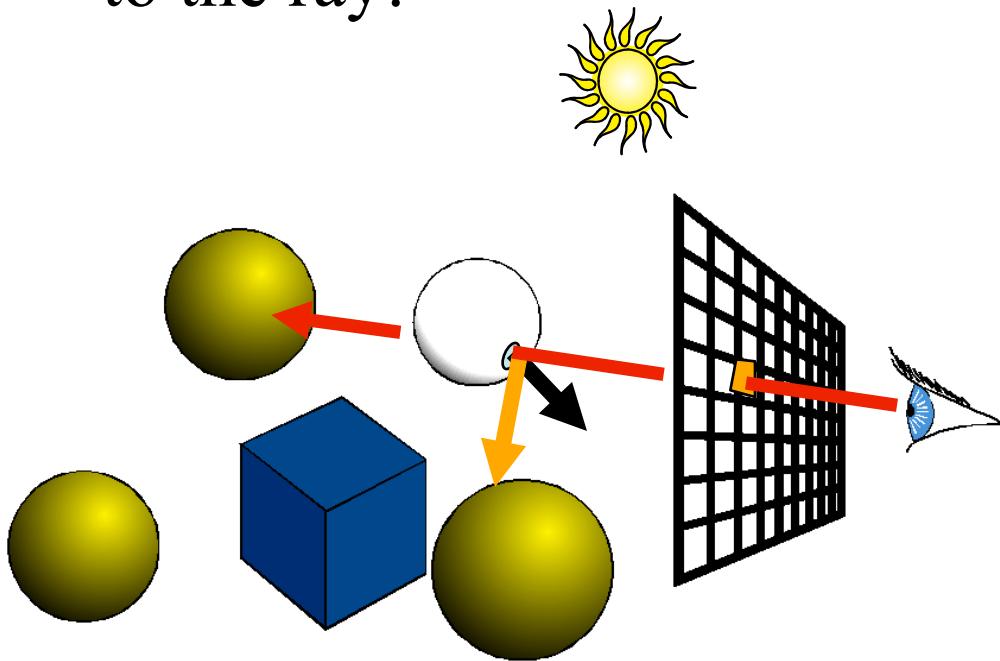
Mirror Reflection

- Cast ray symmetric with respect to the normal
- Multiply by reflection coefficient k_s (color)



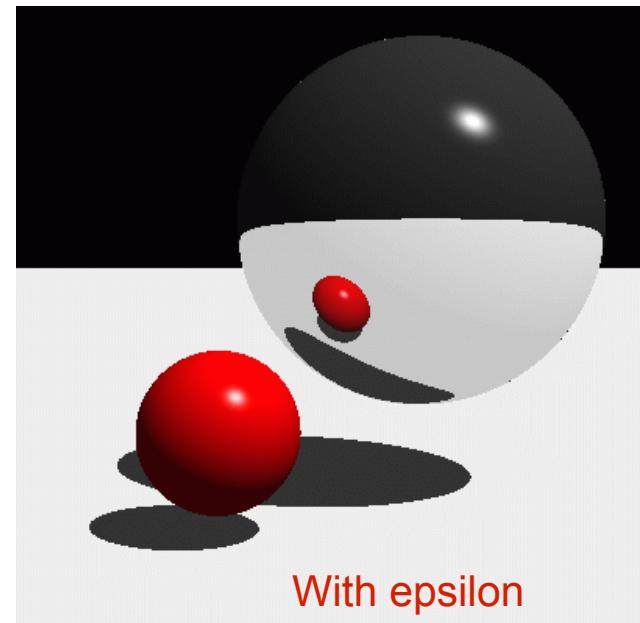
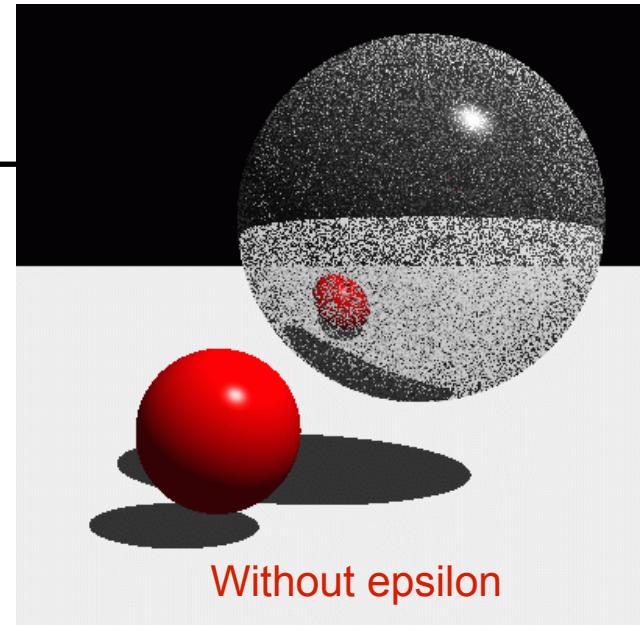
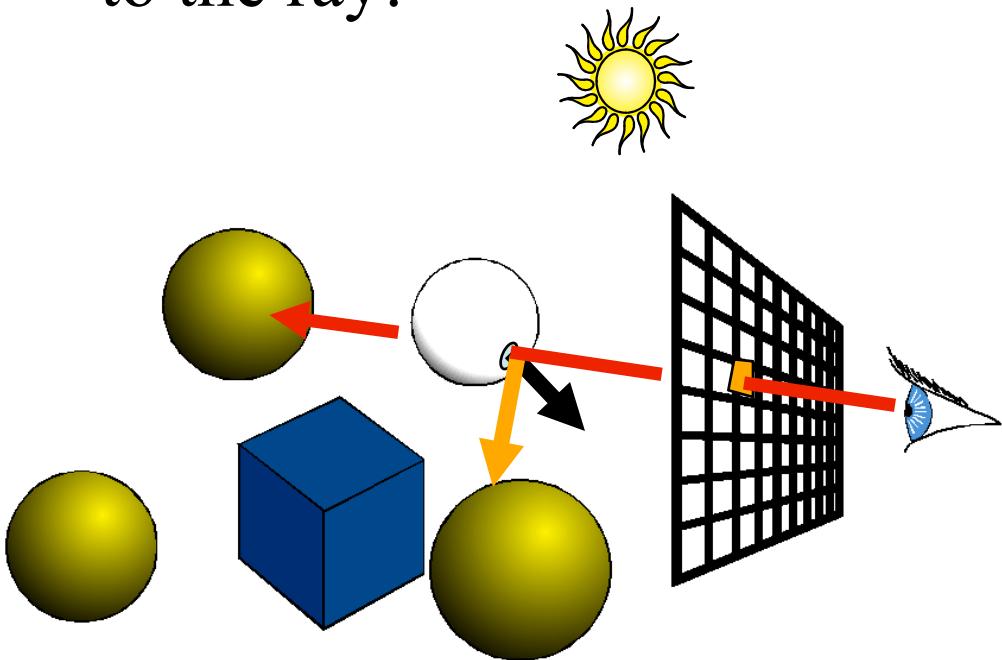
Mirror Reflection

- Cast ray symmetric with respect to the normal
- Multiply by reflection coefficient k_s (color)
- Don't forget to add epsilon to the ray!

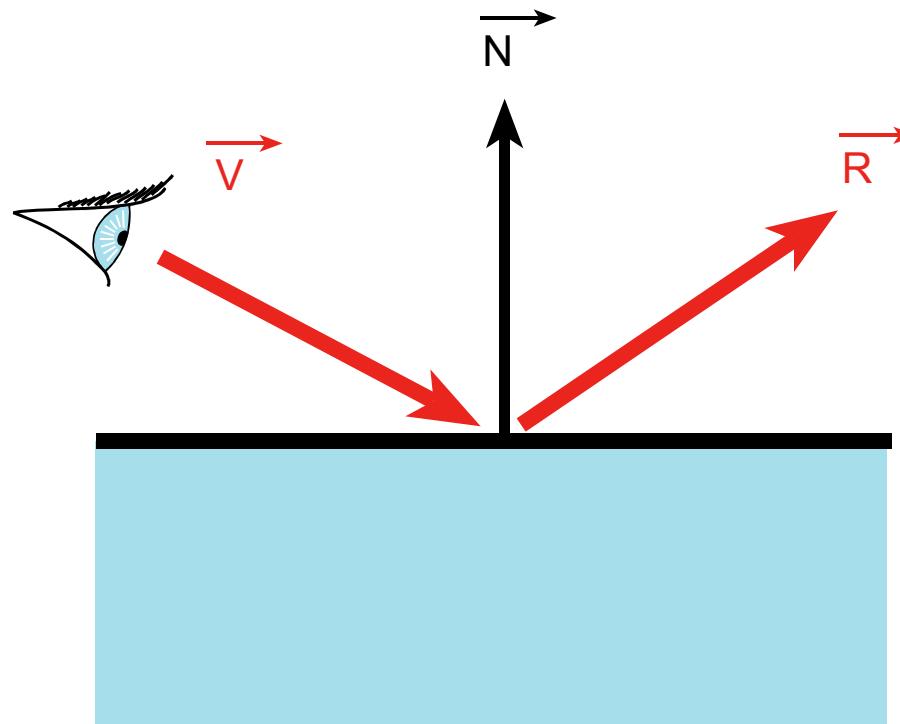


Mirror Reflection

- Cast ray symmetric with respect to the normal
- Multiply by reflection coefficient k_s (color)
- Don't forget to add epsilon to the ray!

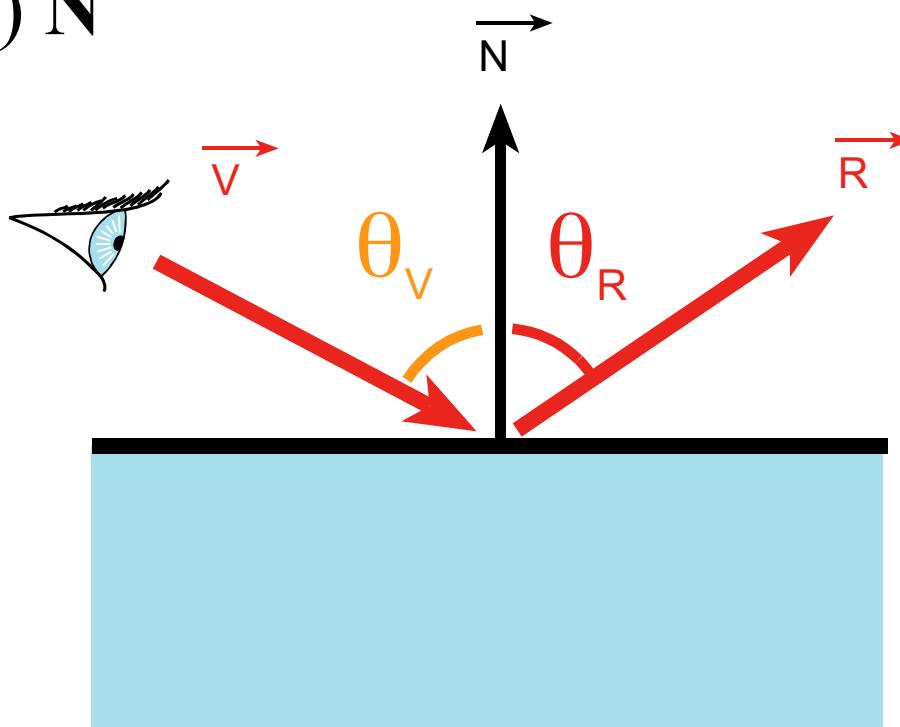


Perfect Mirror Reflection



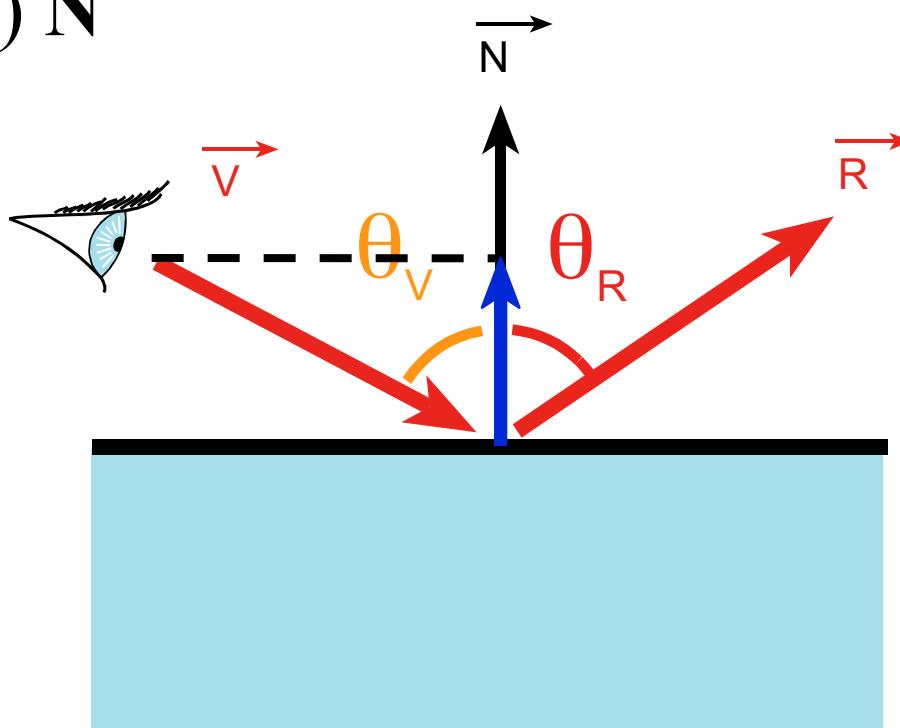
Perfect Mirror Reflection

- Reflection angle = view angle
 - Normal component is negated
 - Remember particle collisions?
- $\mathbf{R} = \mathbf{V} - 2 (\mathbf{V} \cdot \mathbf{N}) \mathbf{N}$



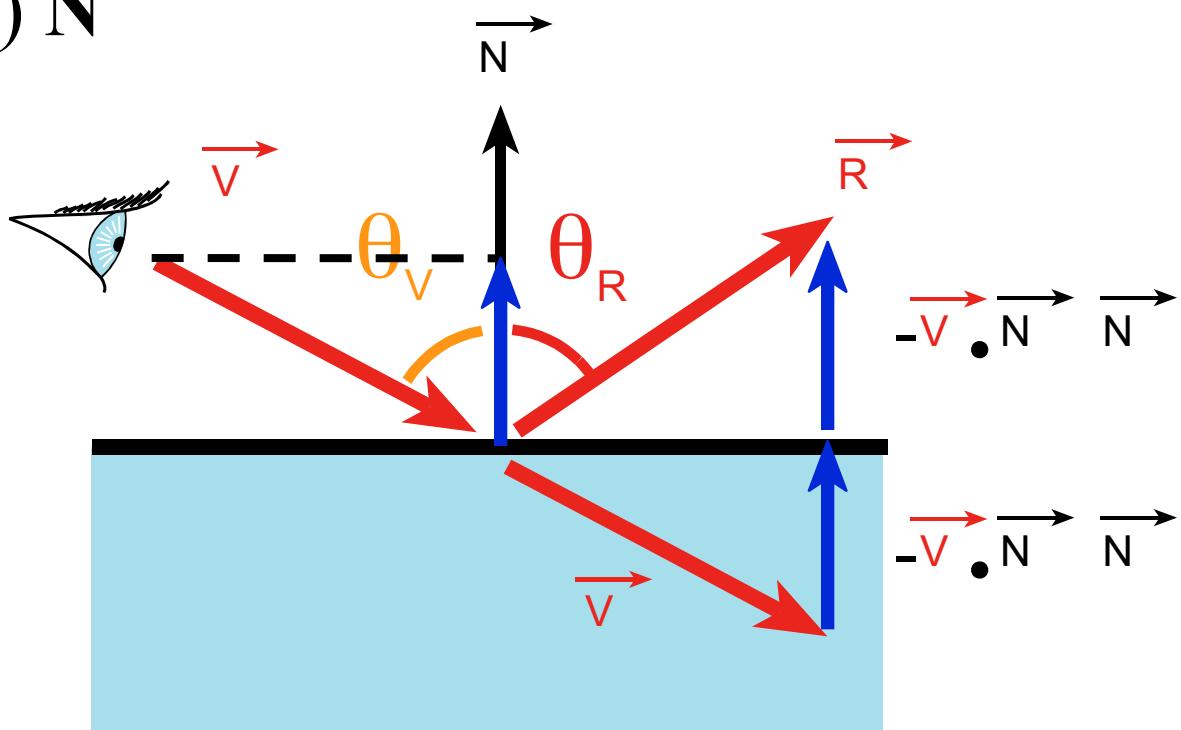
Perfect Mirror Reflection

- Reflection angle = view angle
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- $\mathbf{R} = \mathbf{V} - 2 (\mathbf{V} \cdot \mathbf{N}) \mathbf{N}$



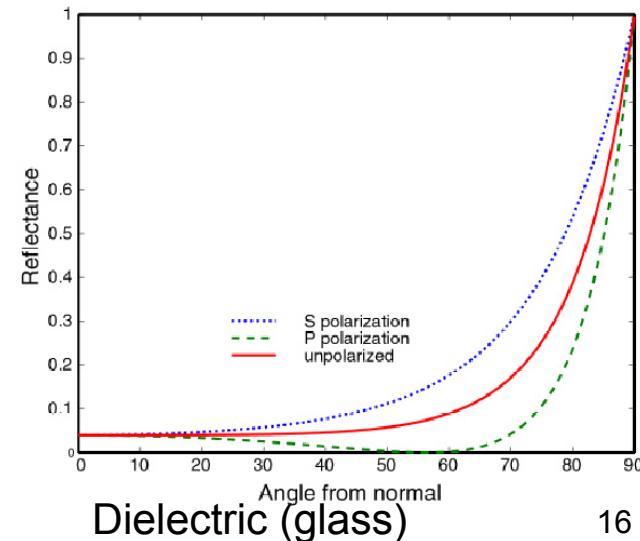
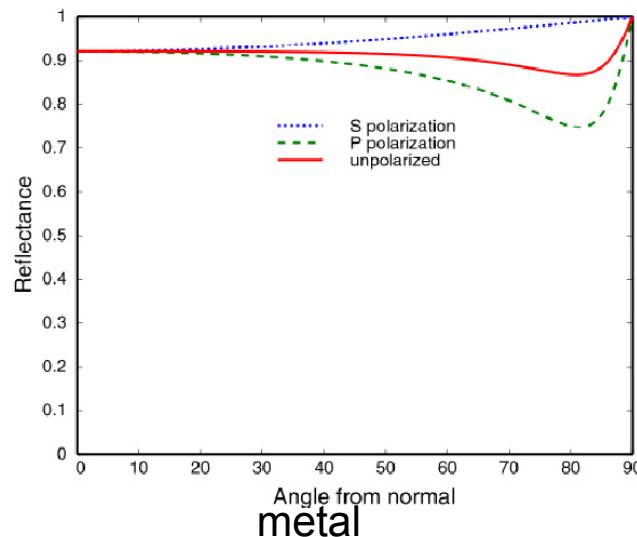
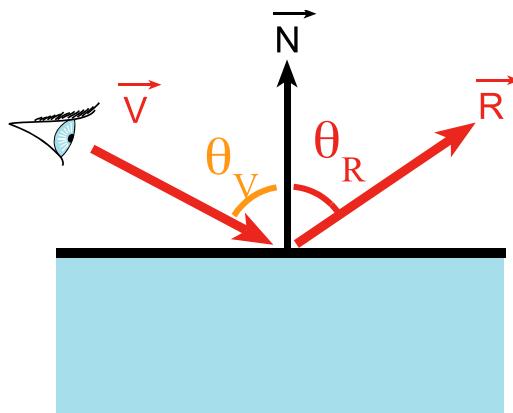
Perfect Mirror Reflection

- Reflection angle = view angle
 - Normal component is negated
 - Remember particle collisions?
- $\mathbf{R} = \mathbf{V} - 2 (\mathbf{V} \cdot \mathbf{N}) \mathbf{N}$



Amount of Reflection

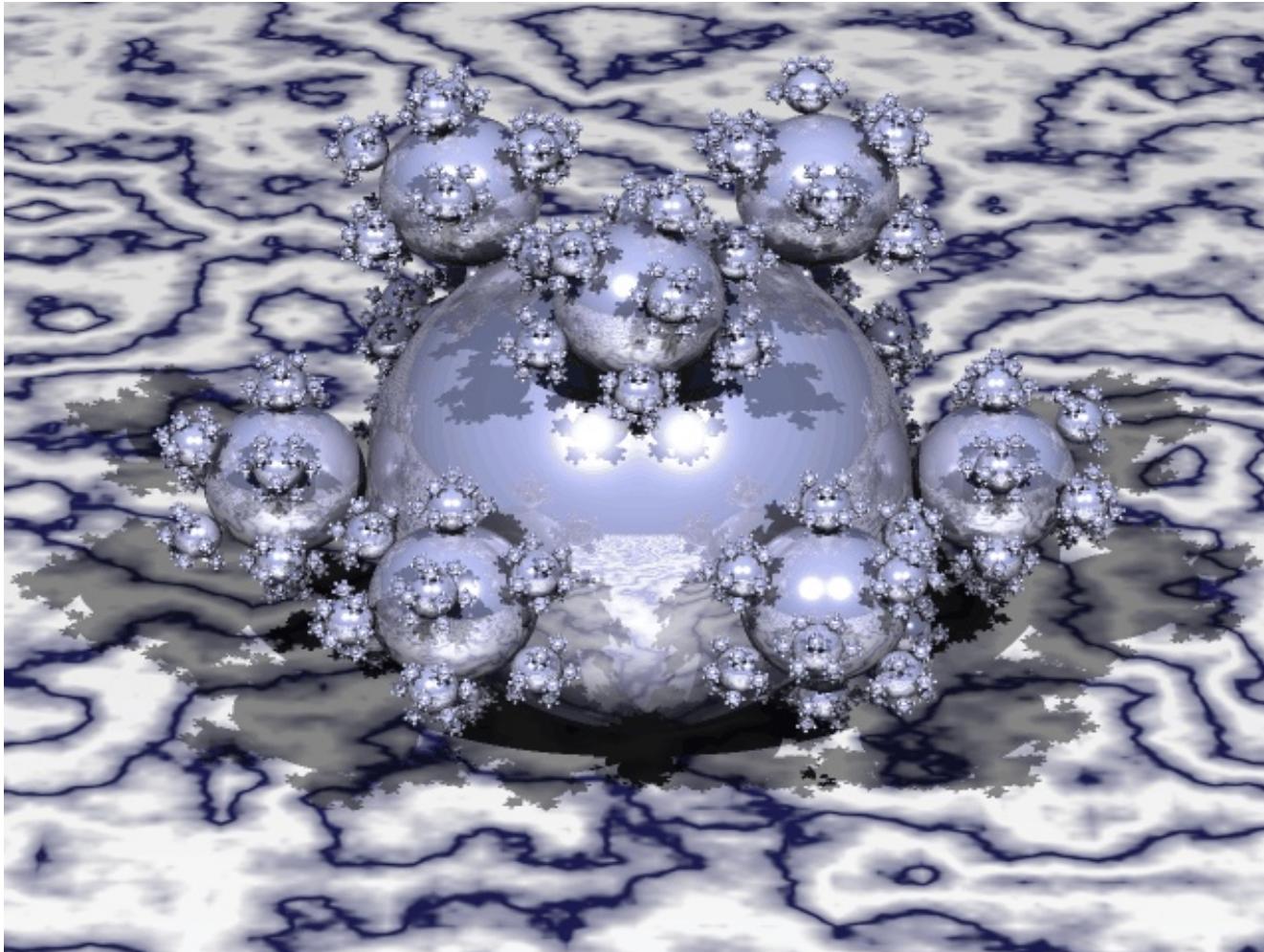
- Traditional ray tracing (hack)
 - Constant k_s
- More realistic
 - Fresnel reflection term (more reflection at grazing angle)
 - Schlick's approximation: $R(\theta) = R_0 + (1-R_0)(1-\cos \theta)^5$
- Fresnel makes a big difference!



Questions?

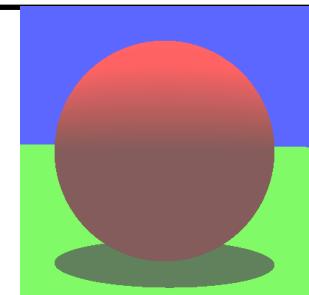
“Sphereflake” fractal

Henrik Wann Jensen

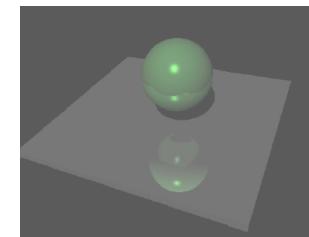


Using a Ray Tracer for..

- Shadows



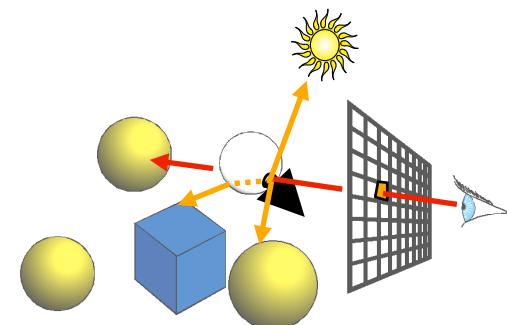
- Reflection



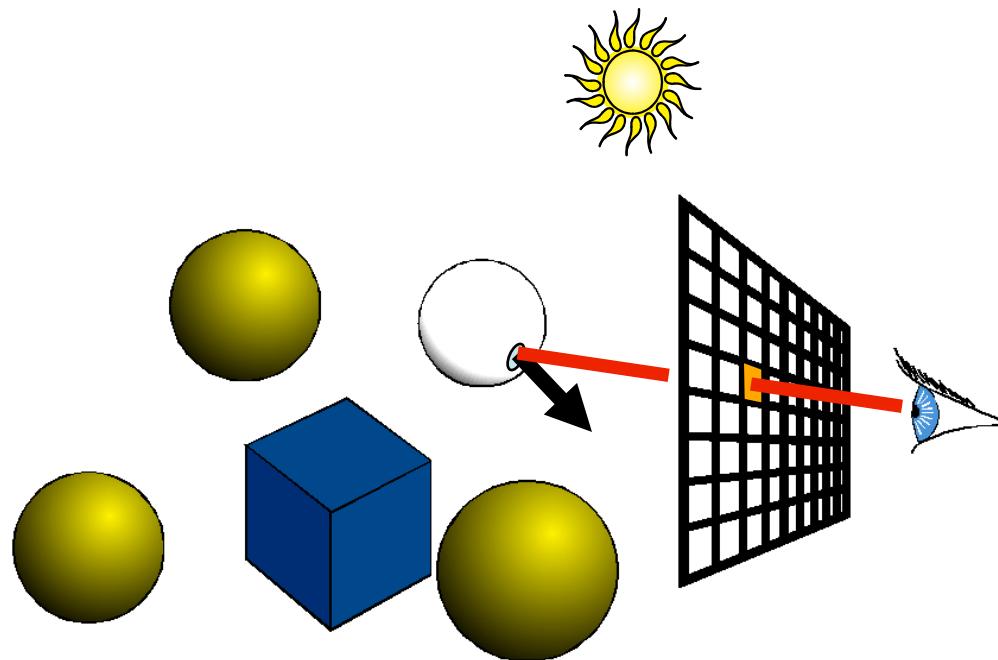
- Refraction



- Recursive Ray Tracing

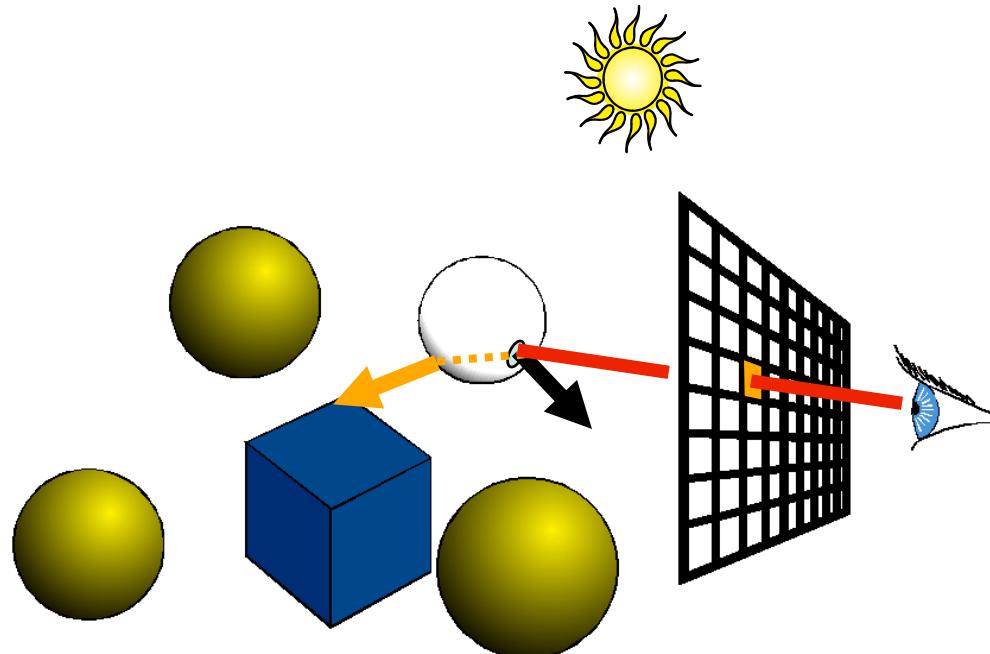


Transparency (Refraction)

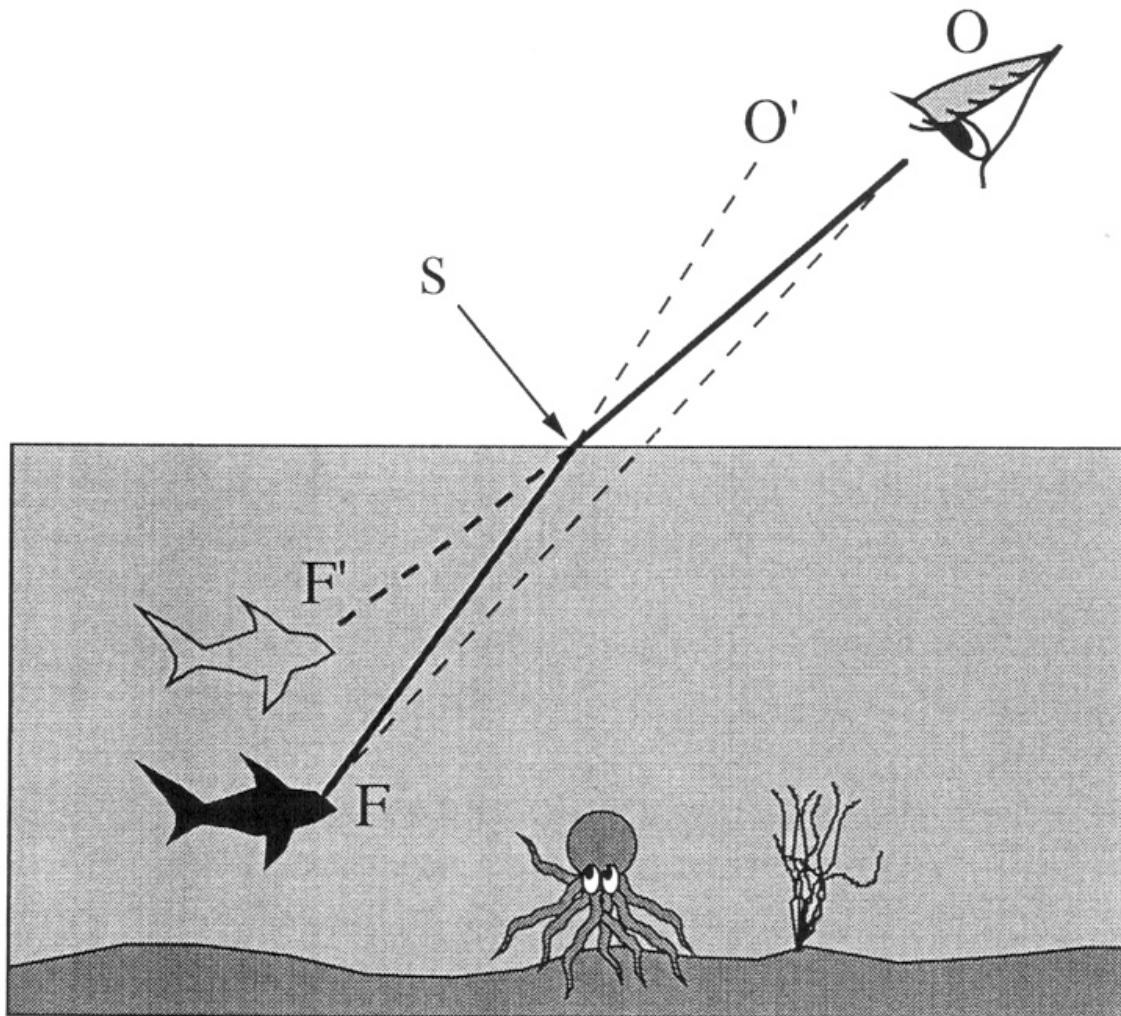


Transparency (Refraction)

- Cast ray in refracted direction
- Multiply by transparency coefficient k_t (color)

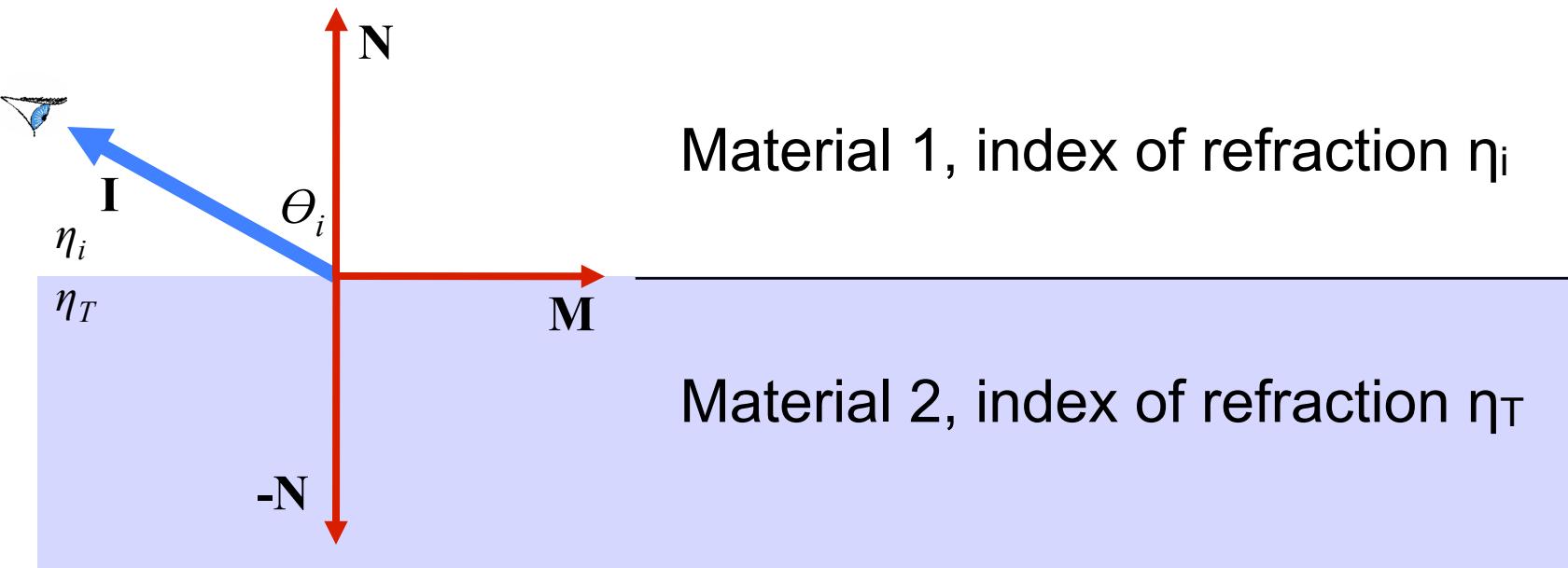


Qualitative Refraction

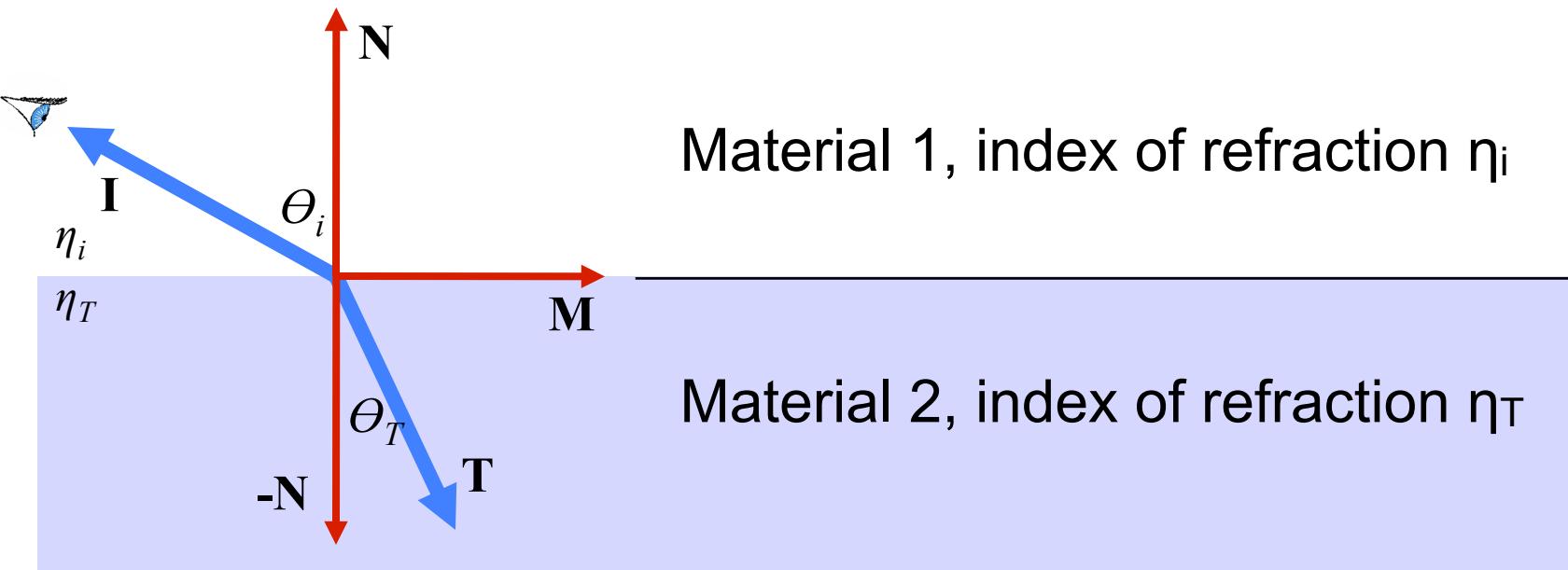


From “Color and Light in Nature” by Lynch and Livingston

Refraction

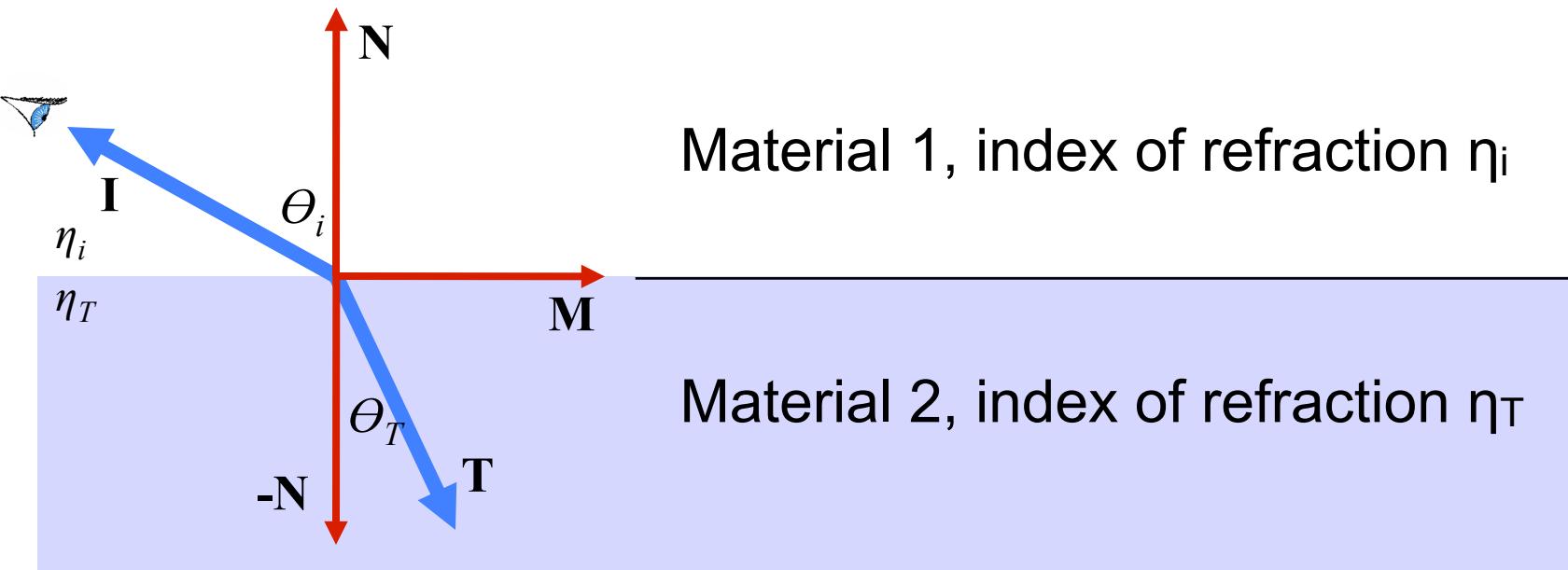


Refraction



Refracted direction **T**?

Refraction



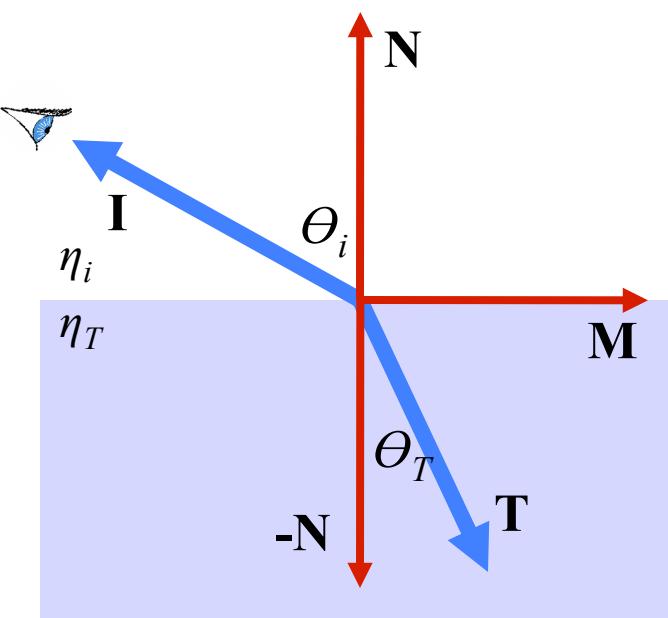
Snell-Descartes Law:

$$\frac{\sin \Theta_i}{\sin \Theta_T} = \frac{\eta_T}{\eta_i} = \eta_r$$

Refracted direction T?

Relative index of refraction

Refraction

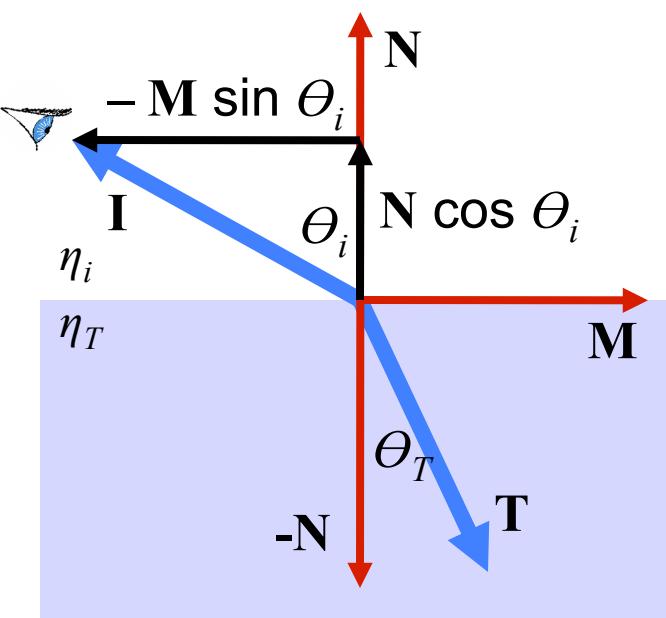


$$\mathbf{I} = \mathbf{N} \cos \theta_i - \mathbf{M} \sin \theta_i$$
$$\mathbf{M} = (\mathbf{N} \cos \theta_i - \mathbf{I}) / \sin \theta_i$$

Snell-Descartes Law:

$$\frac{\sin \theta_i}{\sin \theta_T} = \frac{\eta_T}{\eta_i} = \eta_r$$

Refraction



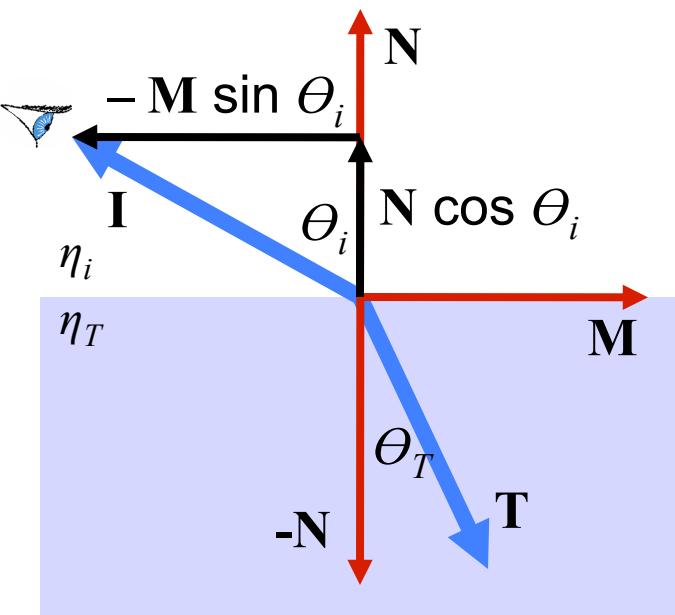
$$\mathbf{I} = \mathbf{N} \cos \theta_i - \mathbf{M} \sin \theta_i$$

$$\mathbf{M} = (\mathbf{N} \cos \theta_i - \mathbf{I}) / \sin \theta_i$$

Snell-Descartes Law:

$$\frac{\sin \theta_i}{\sin \theta_T} = \frac{\eta_T}{\eta_i} = \eta_r$$

Refraction



$$\mathbf{I} = \mathbf{N} \cos \theta_i - \mathbf{M} \sin \theta_i$$

$$\mathbf{M} = (\mathbf{N} \cos \theta_i - \mathbf{I}) / \sin \theta_i$$

$$\mathbf{T} = -\mathbf{N} \cos \theta_T + \mathbf{M} \sin \theta_T$$

Plug M

$$= -\mathbf{N} \cos \theta_T + (\mathbf{N} \cos \theta_i - \mathbf{I}) \sin \theta_T / \sin \theta_i$$

$$= -\mathbf{N} \cos \theta_T + (\mathbf{N} \cos \theta_i - \mathbf{I}) \eta_r$$

let's get rid of
the cos & sin

$$= [\eta_r \cos \theta_i - \cos \theta_T] \mathbf{N} - \eta_r \mathbf{I}$$

$$= [\eta_r \cos \theta_i - \sqrt{1 - \sin^2 \theta_T}] \mathbf{N} - \eta_r \mathbf{I}$$

$$= [\eta_r \cos \theta_i - \sqrt{1 - \eta_r^2 \sin^2 \theta_i}] \mathbf{N} - \eta_r \mathbf{I}$$

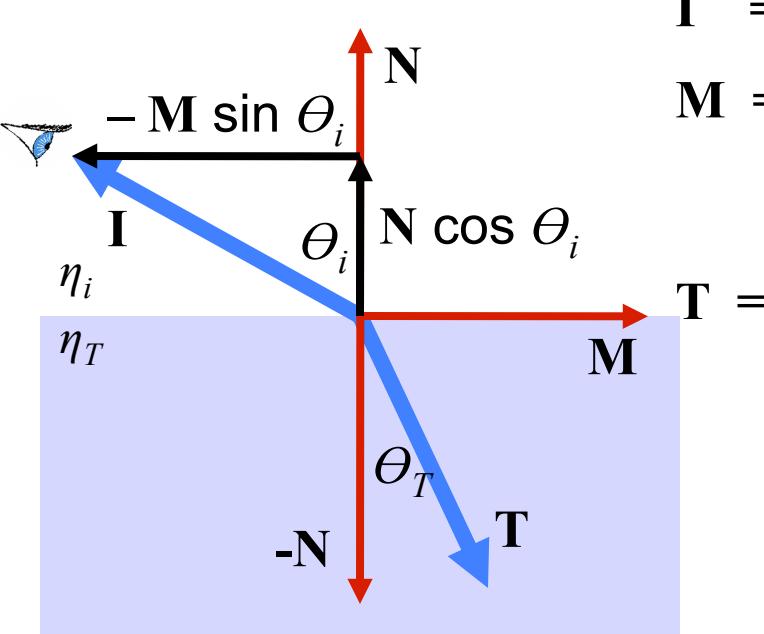
$$= [\eta_r \cos \theta_i - \sqrt{1 - \eta_r^2 (1 - \cos^2 \theta_i)}] \mathbf{N} - \eta_r \mathbf{I}$$

$$= [\eta_r (\mathbf{N} \cdot \mathbf{I}) - \sqrt{1 - \eta_r^2 (1 - (\mathbf{N} \cdot \mathbf{I})^2)}] \mathbf{N} - \eta_r \mathbf{I}$$

Snell-Descartes Law:

$$\frac{\sin \theta_i}{\sin \theta_T} = \frac{\eta_T}{\eta_i} = \eta_r$$

Refraction



$$I = N \cos \theta_i - M \sin \theta_i$$
$$M = (N \cos \theta_i - I) / \sin \theta_i$$

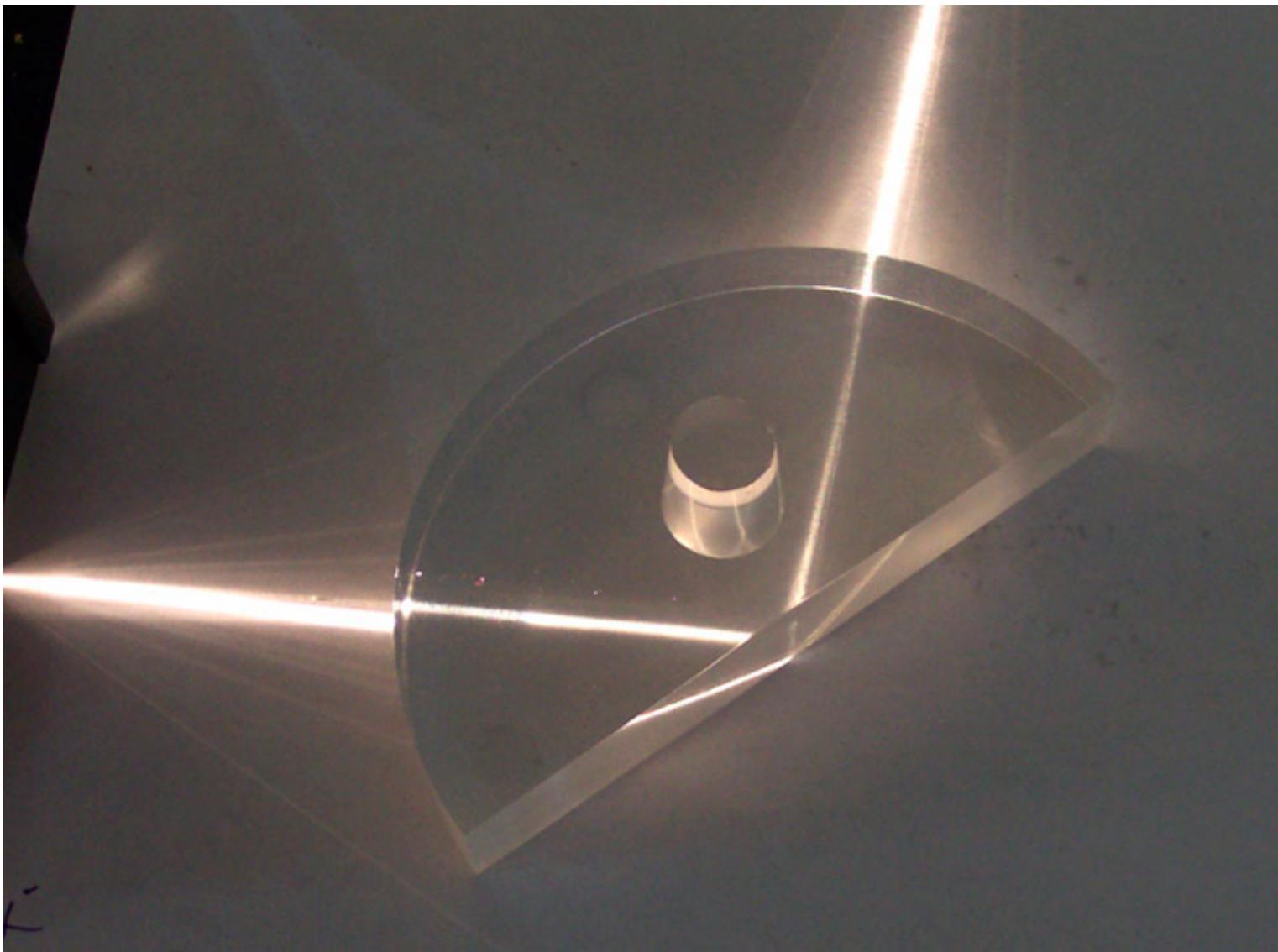
- **Total internal reflection** when the square root is imaginary (no refraction, just reflection)
- Don't forget to normalize T !

Snell-Descartes Law:

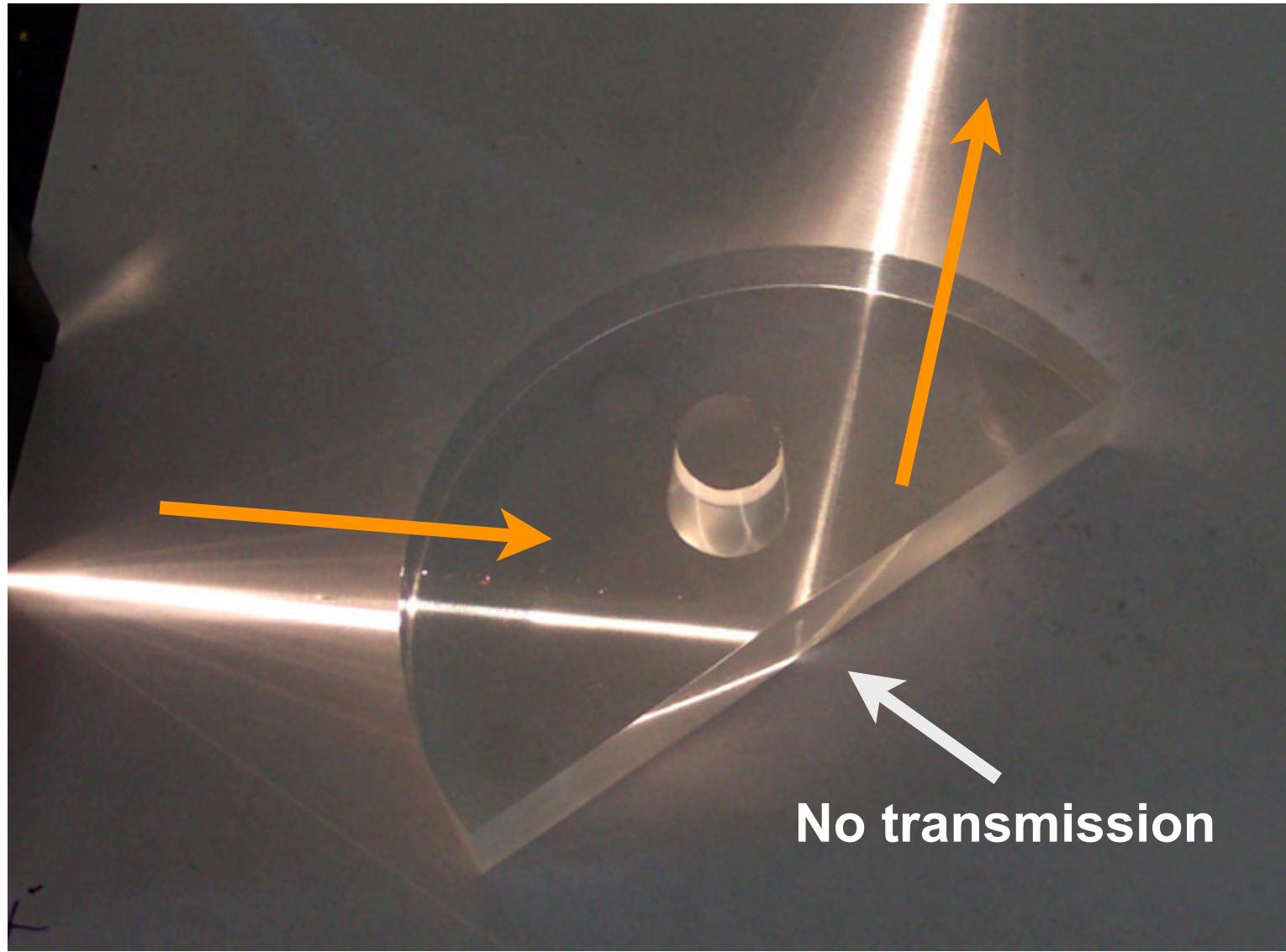
$$\frac{\sin \Theta_i}{\sin \Theta_T} = \frac{\eta_T}{\eta_i} = \eta_r = [\eta_r (\mathbf{N} \cdot \mathbf{I}) - \sqrt{1 - \eta_r^2 (1 - (\mathbf{N} \cdot \mathbf{I})^2)}] \mathbf{N} - \eta_r \mathbf{I}$$

Total Internal Reflection

Wikipedia user Fir0002



Total Internal Reflection



Wikipedia user Fir0002

No transmission

Total Internal Reflection



Fig. 3.7A The optical manhole. From under water, the entire celestial hemisphere is compressed into a circle only 97.2° across. The dark boundary defining the edges of the manhole is not sharp due to surface waves. The rays are analogous to the crepuscular type seen in hazy air, Section 1.9. (Photo by D. Granger)

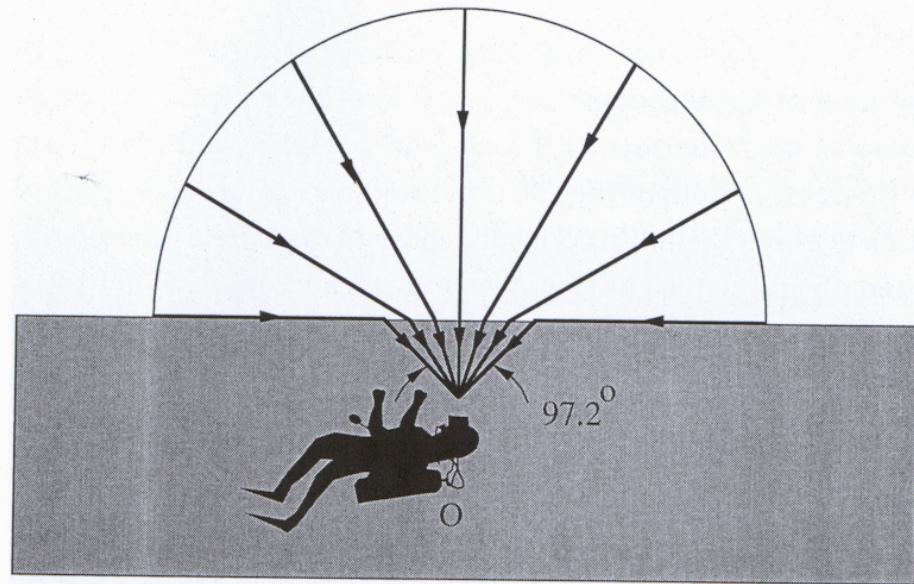
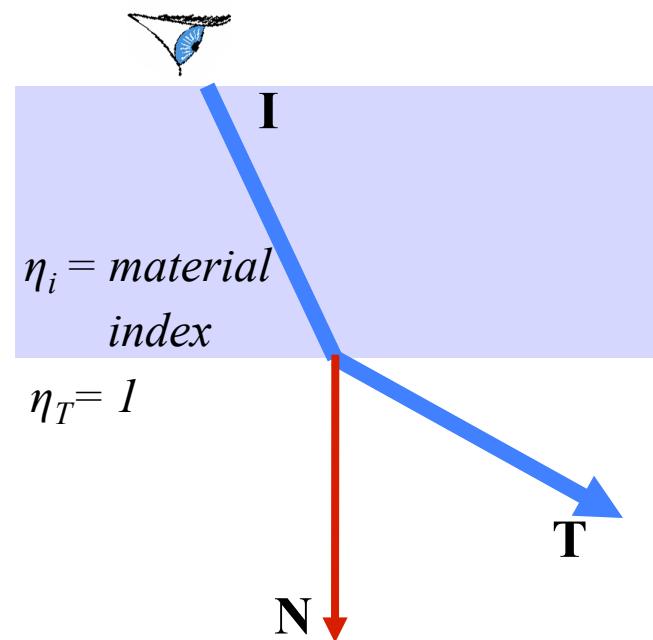
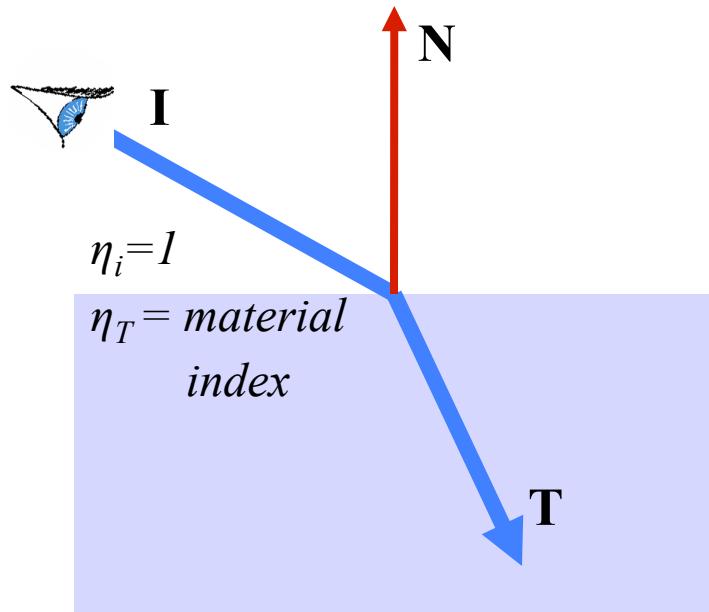


Fig. 3.7B The optical manhole. Light from the horizon (angle of incidence = 90°) is refracted downward at an angle of 48.6° . This compresses the sky into a circle with a diameter of 97.2° instead of its usual 180° .

From “Color and Light in Nature” by Lynch and Livingston

Refraction & Sidedness of Objects

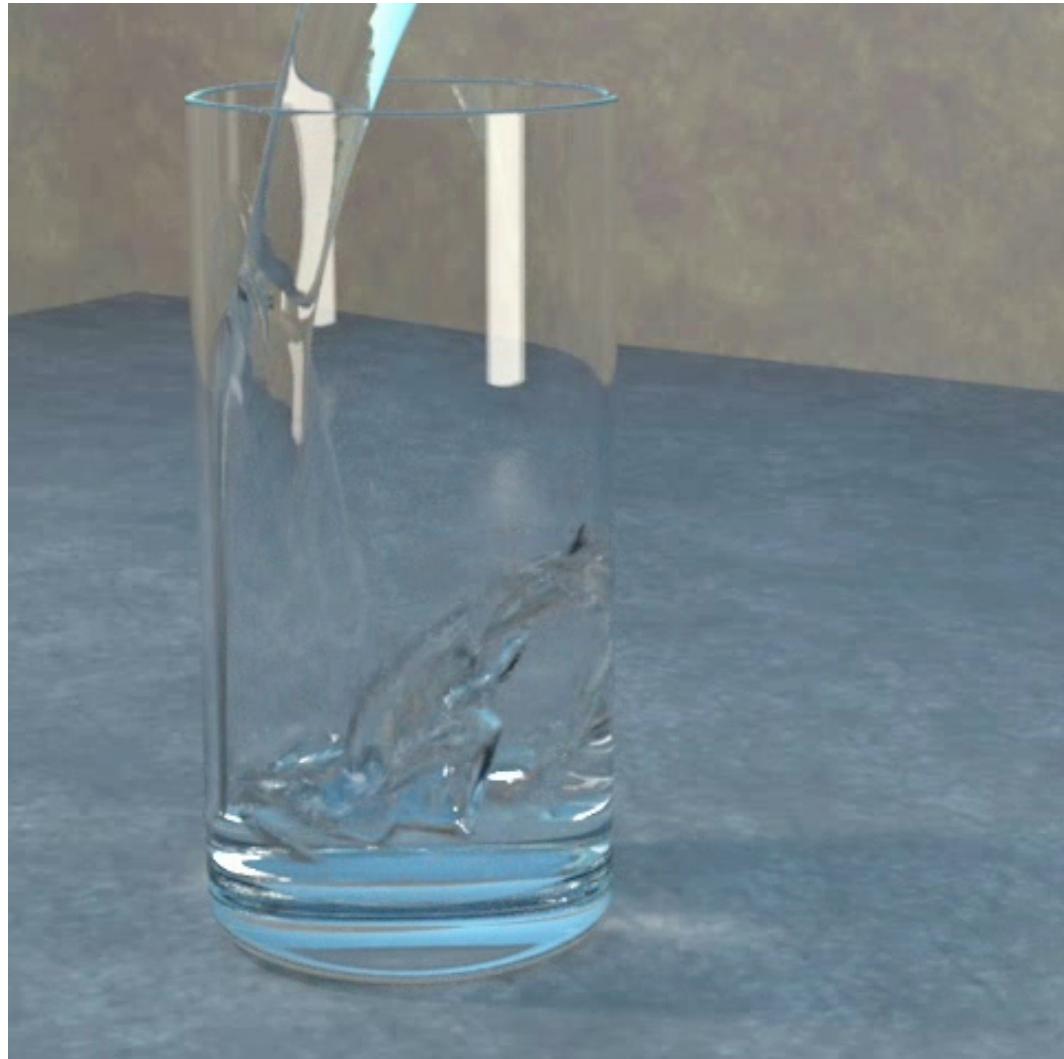
- Make sure you know whether you're entering or leaving the transmissive material:



- Note: We won't ask you to trace rays through intersecting transparent objects :-)

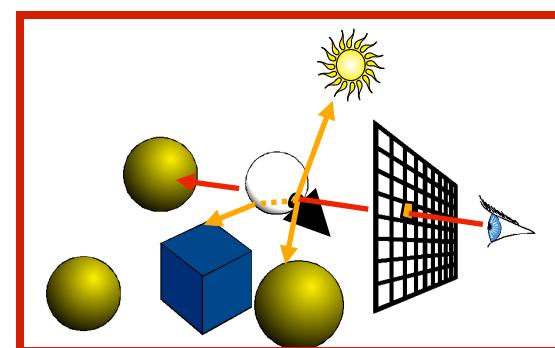
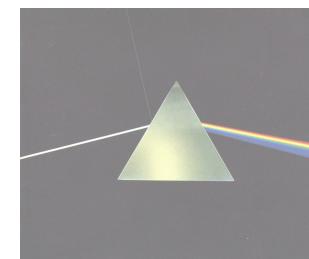
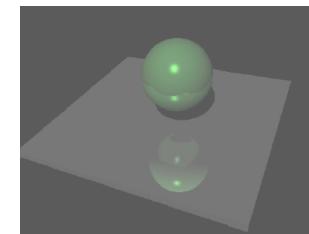
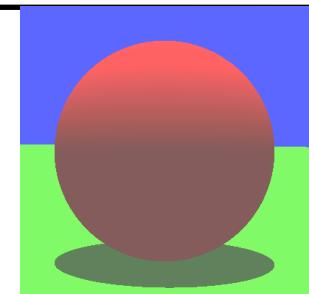
Cool Refraction Demo

- Enright, D.,
Marschner, S.
and Fedkiw, R.,
SIGGRAPH
2002
- Physical fluid simulation combined with ray traced rendering

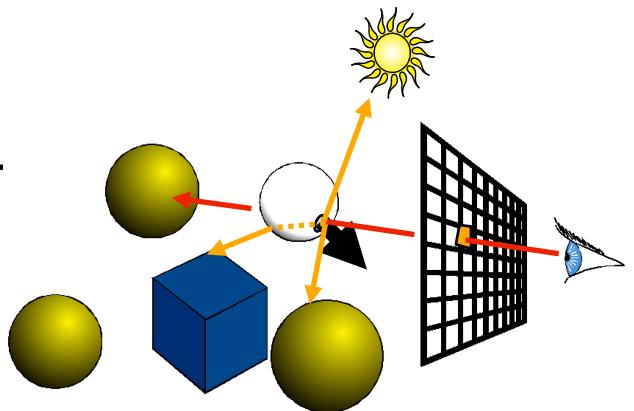


Using a Ray Tracer for..

- Shadows
- Reflection
- Refraction
- Recursive Ray Tracing

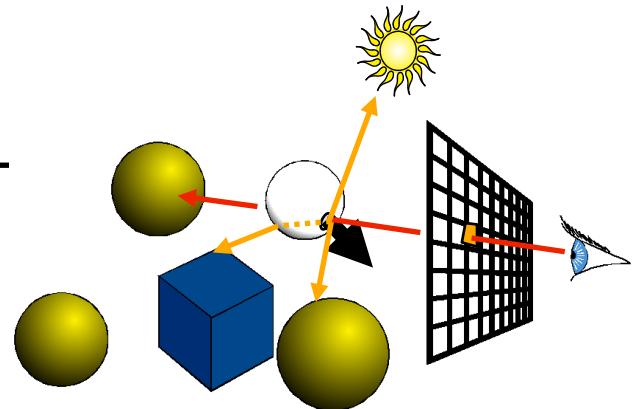


Recap: Ray Tracing



Recap: Ray Tracing

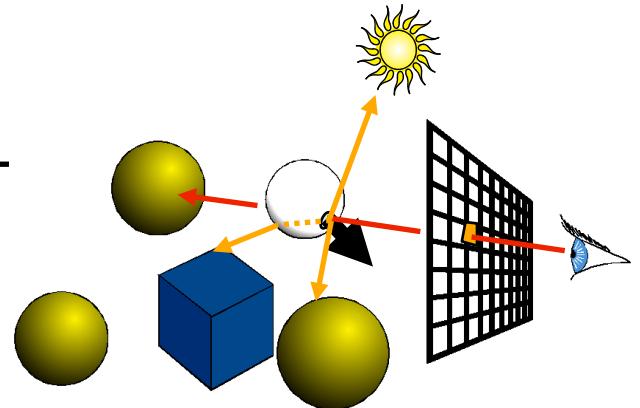
trace ray



Recap: Ray Tracing

trace ray

Intersect all objects

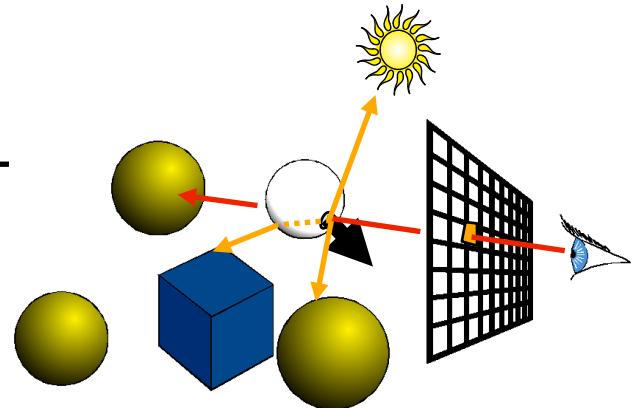


Recap: Ray Tracing

trace ray

Intersect all objects

color = ambient term



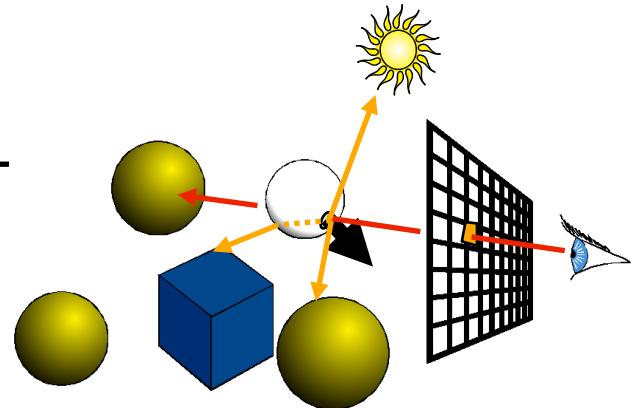
Recap: Ray Tracing

trace ray

Intersect all objects

color = ambient term

For every light



Recap: Ray Tracing

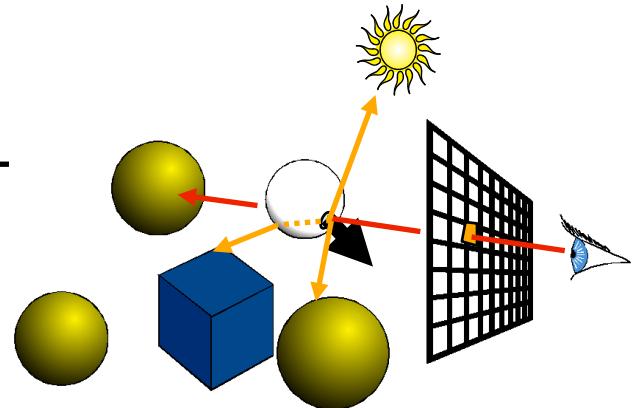
trace ray

Intersect all objects

color = ambient term

For every light

cast shadow ray



Recap: Ray Tracing

trace ray

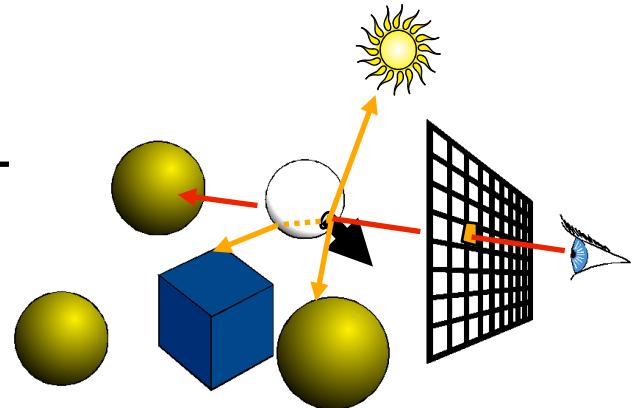
Intersect all objects

color = ambient term

For every light

cast shadow ray

color += local shading term



Recap: Ray Tracing

trace ray

Intersect all objects

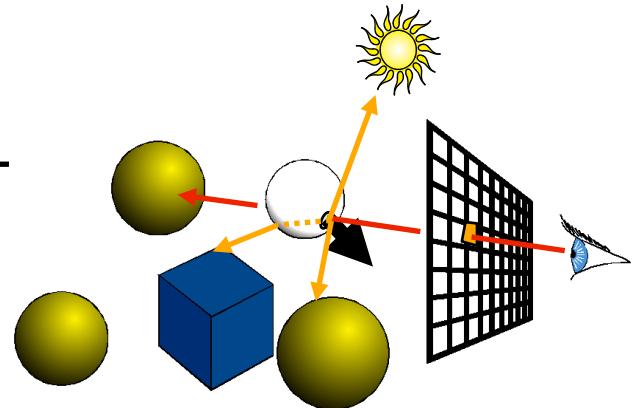
color = ambient term

For every light

cast shadow ray

color += local shading term

If mirror



Recap: Ray Tracing

trace ray

Intersect all objects

color = ambient term

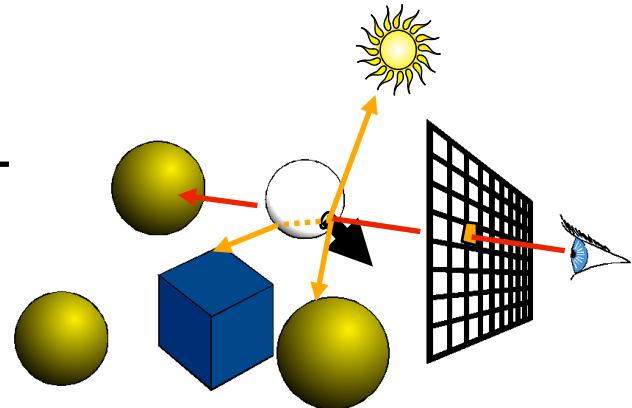
For every light

cast shadow ray

color += local shading term

If mirror

color += color_{refl} *



Recap: Ray Tracing

trace ray

Intersect all objects

color = ambient term

For every light

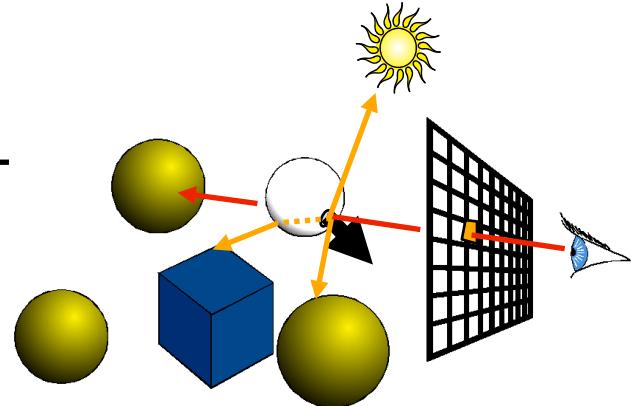
cast shadow ray

color += local shading term

If mirror

color += color_{refl} *

trace reflected ray



Recap: Ray Tracing

trace ray

Intersect all objects

color = ambient term

For every light

cast shadow ray

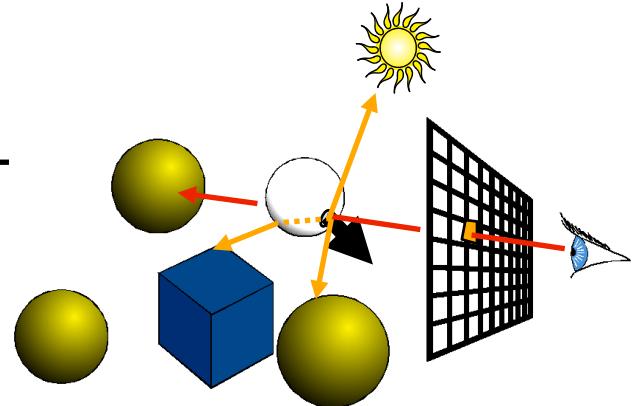
color += local shading term

If mirror

color += color_{refl} *

trace reflected ray

If transparent



Recap: Ray Tracing

trace ray

Intersect all objects

color = ambient term

For every light

cast shadow ray

color += local shading term

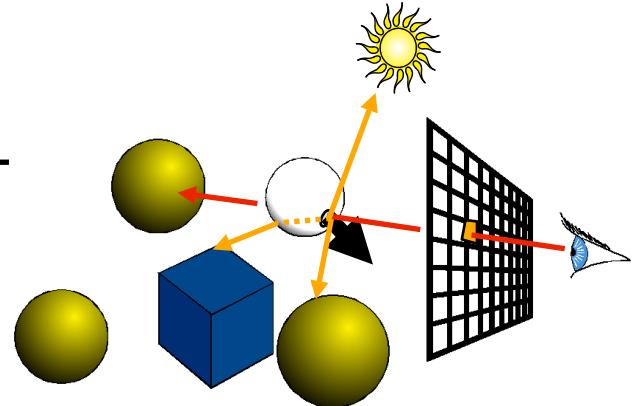
If mirror

color += color_{refl} *

trace reflected ray

If transparent

color += color_{trans} *



Recap: Ray Tracing

trace ray

Intersect all objects

color = ambient term

For every light

cast shadow ray

color += local shading term

If mirror

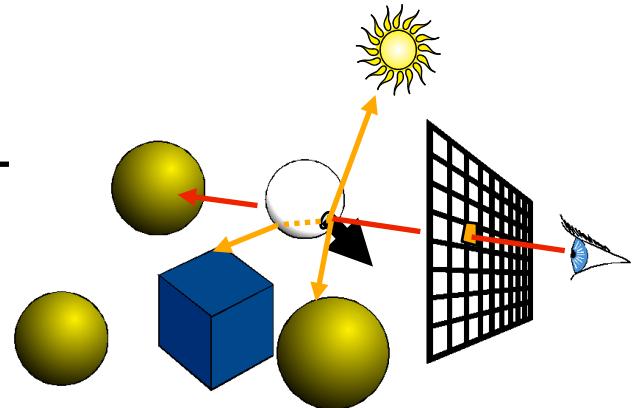
color += color_{refl} *

trace reflected ray

If transparent

color += color_{trans} *

trace transmitted ray



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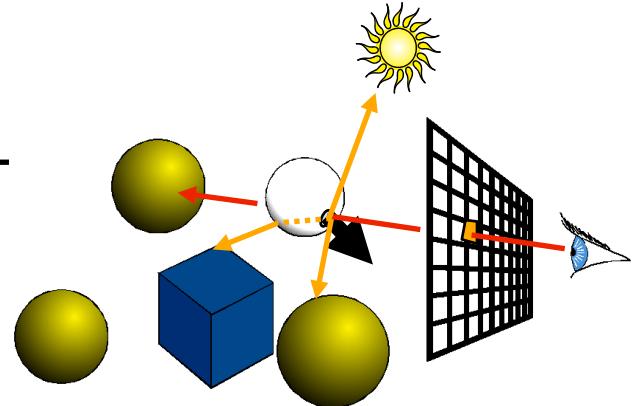
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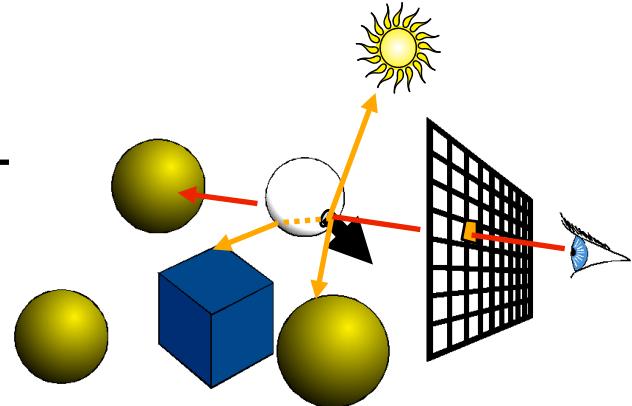
trace reflected ray

If transparent

color += color_{trans} *

trace transmitted ray

- *Does it ever end?*



Recap: Ray Tracing

trace ray

Intersect all objects

color = ambient term

For every light

cast shadow ray

color += local shading term

If mirror

color += color_{refl} *

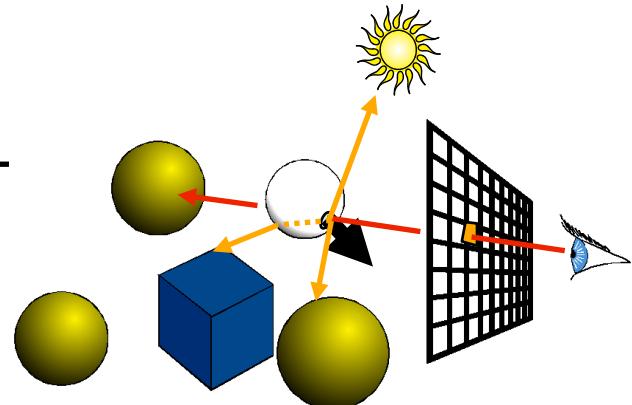
trace reflected ray

If transparent

color += color_{trans} *

trace transmitted ray

- *Does it ever end?*



Recap: Ray Tracing

trace ray

Intersect all objects

color = ambient term

For every light

cast shadow ray

color += local shading term

If mirror

color += color_{refl} *

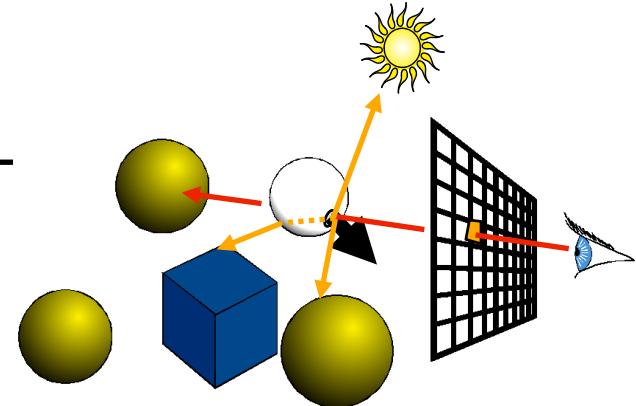
trace reflected ray

If transparent

color += color_{trans} *

trace transmitted ray

- *Does it ever end?*



Recap: Ray Tracing

trace ray

Intersect all objects

color = ambient term

For every light

cast shadow ray

color += local shading term

If mirror

color += color_{refl} *

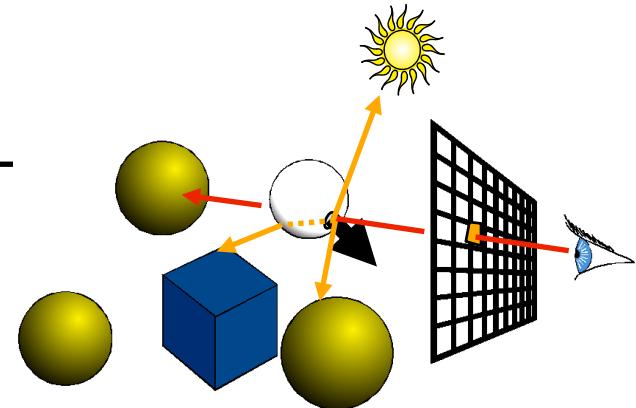
trace reflected ray

If transparent

color += color_{trans} *

trace transmitted ray

- *Does it ever end?*



Stopping criteria:

Recap: Ray Tracing

trace ray

Intersect all objects

color = ambient term

For every light

cast shadow ray

color += local shading term

If mirror

color += color_{refl} *

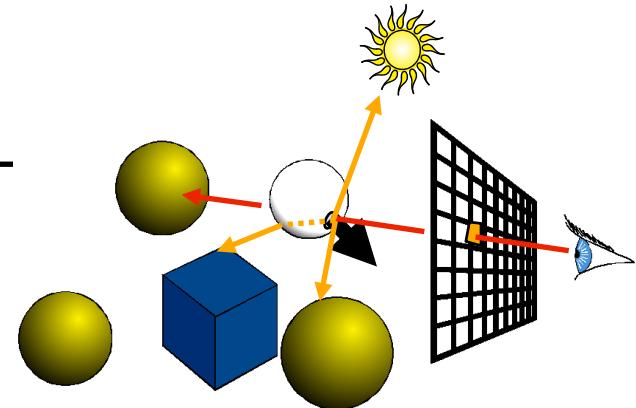
trace reflected ray

If transparent

color += color_{trans} *

trace transmitted ray

- *Does it ever end?*



Stopping criteria:

- Recursion depth
 - Stop after a number of bounces

Recap: Ray Tracing

trace ray

Intersect all objects

color = ambient term

For every light

cast shadow ray

color += local shading term

If mirror

color += color_{refl} *

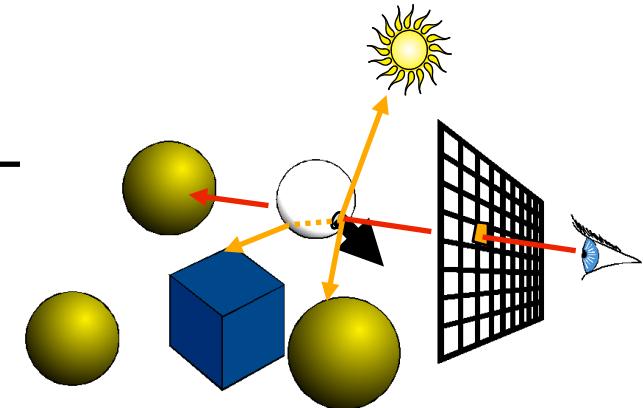
trace reflected ray

If transparent

color += color_{trans} *

trace transmitted ray

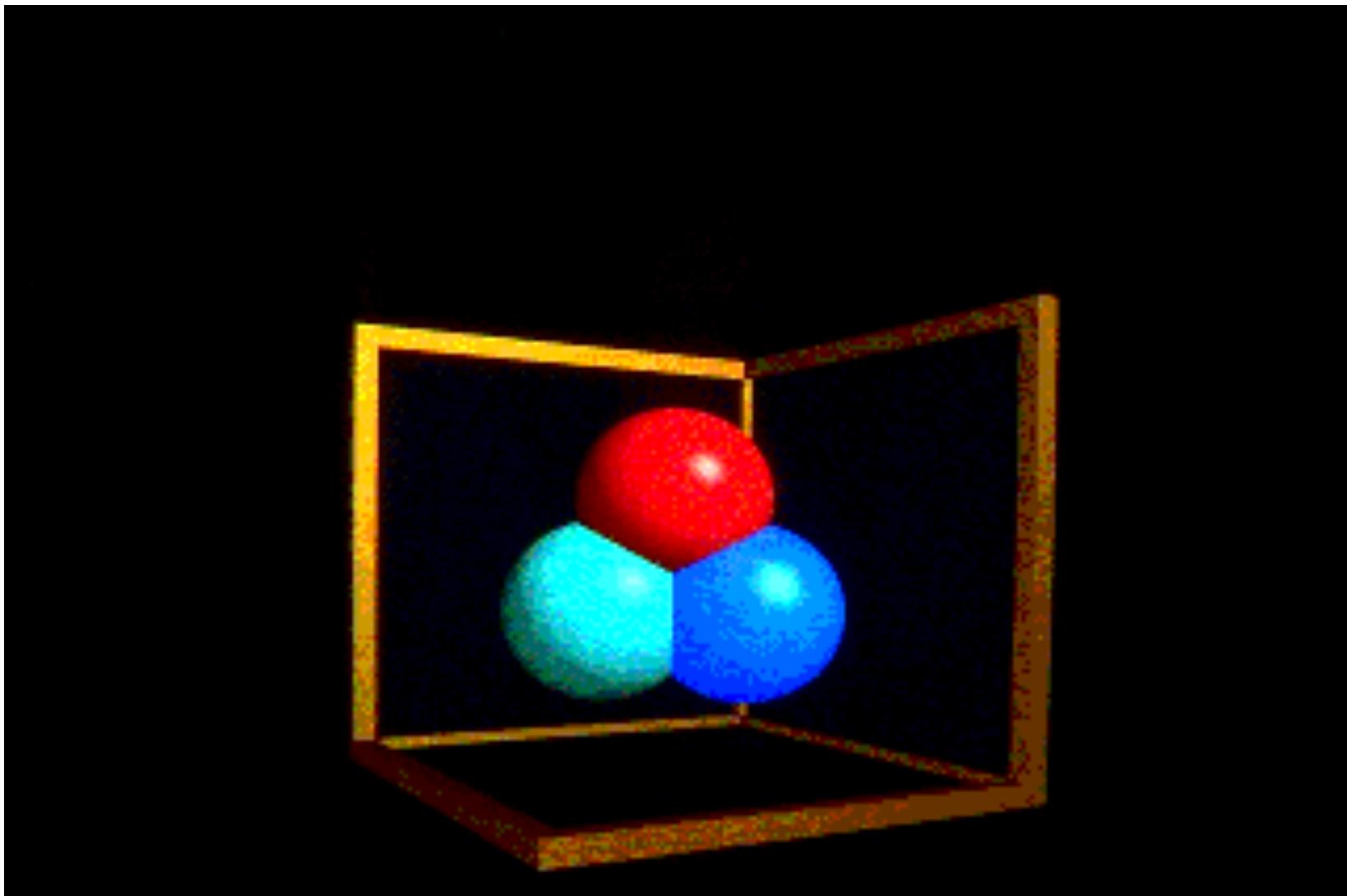
- *Does it ever end?*



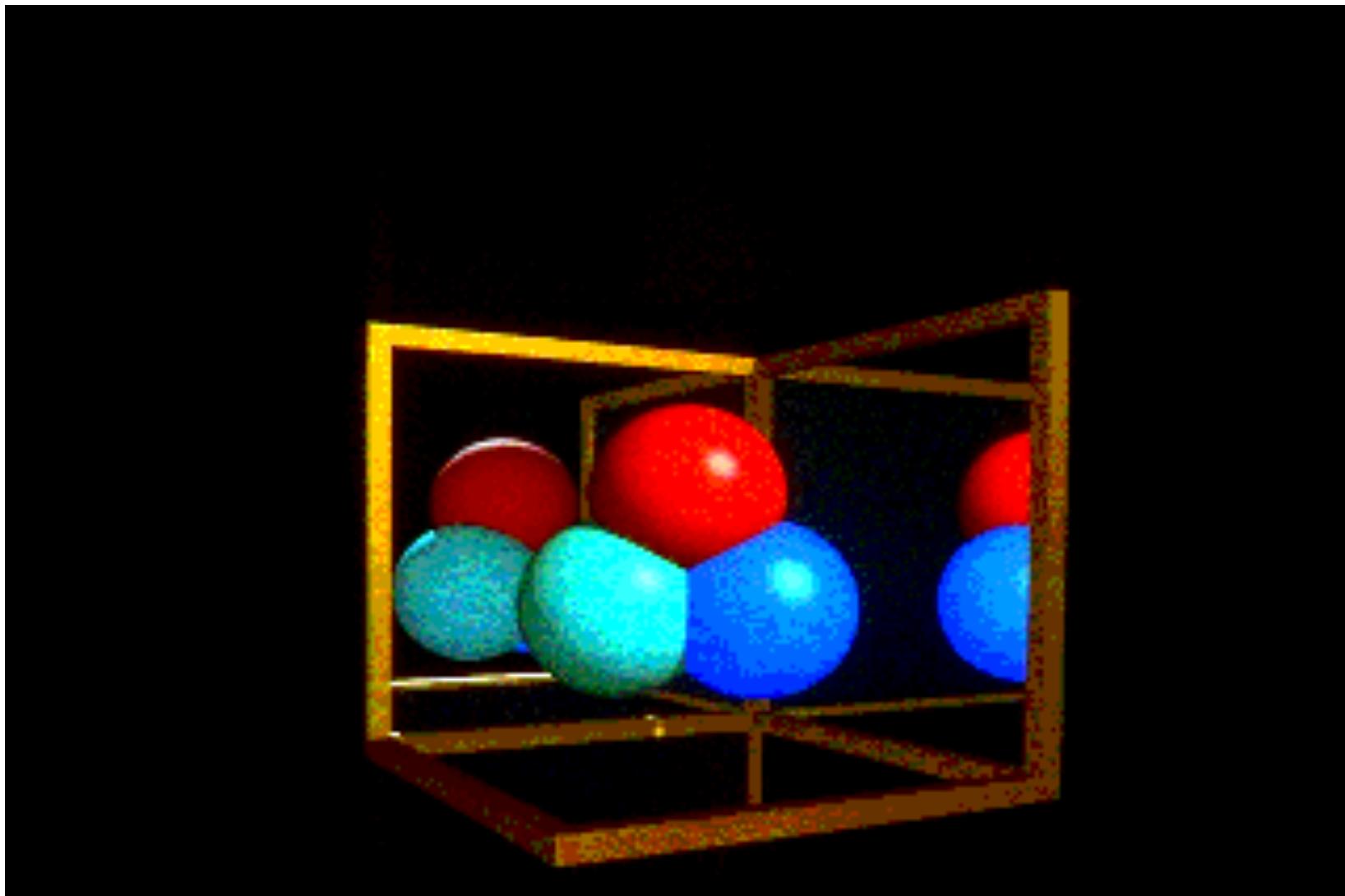
Stopping criteria:

- Recursion depth
 - Stop after a number of bounces
- Ray contribution
 - Stop if reflected / transmitted contribution becomes too small

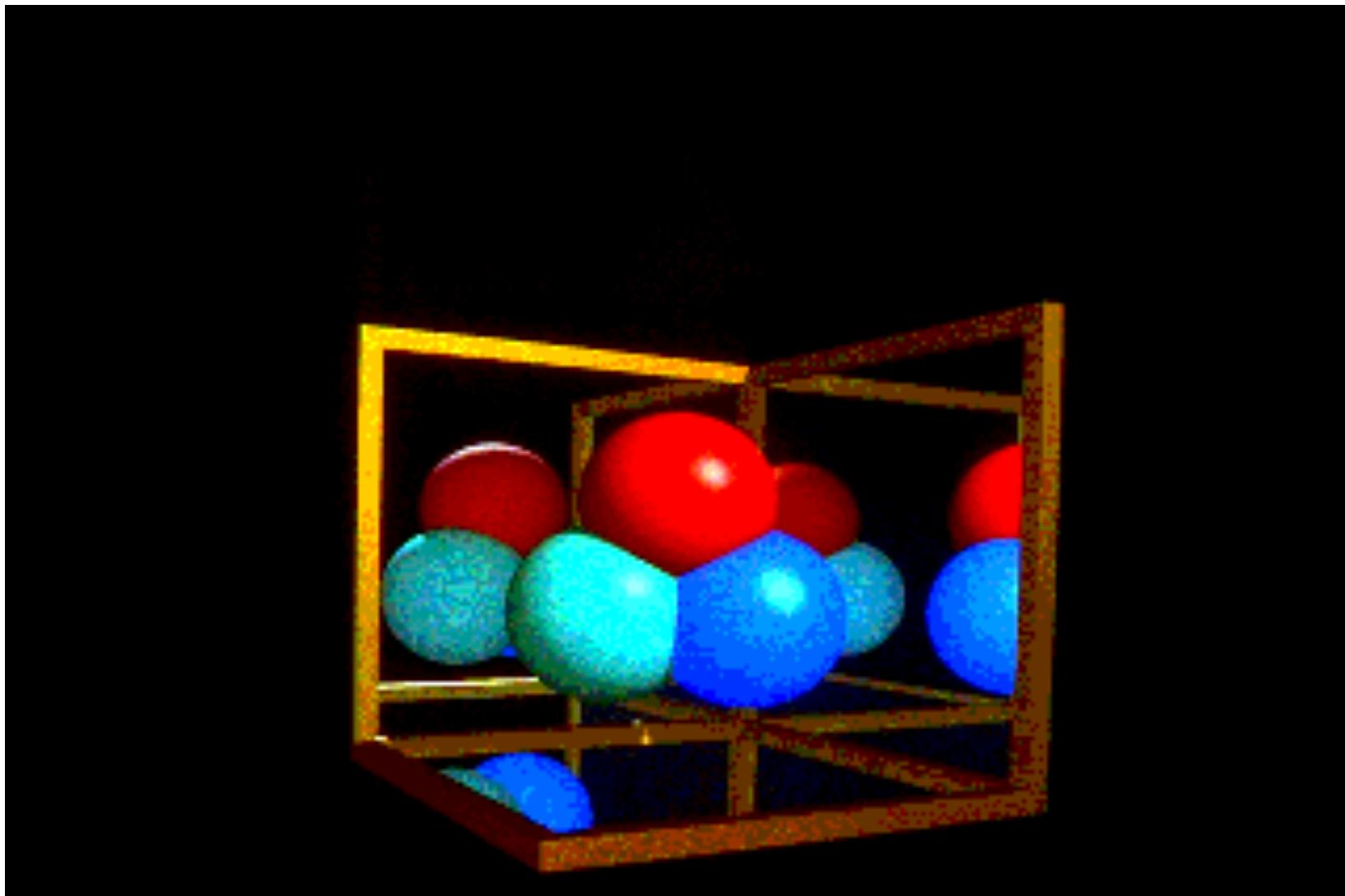
Recursion For Reflection: None



Recursion For Reflection: 1

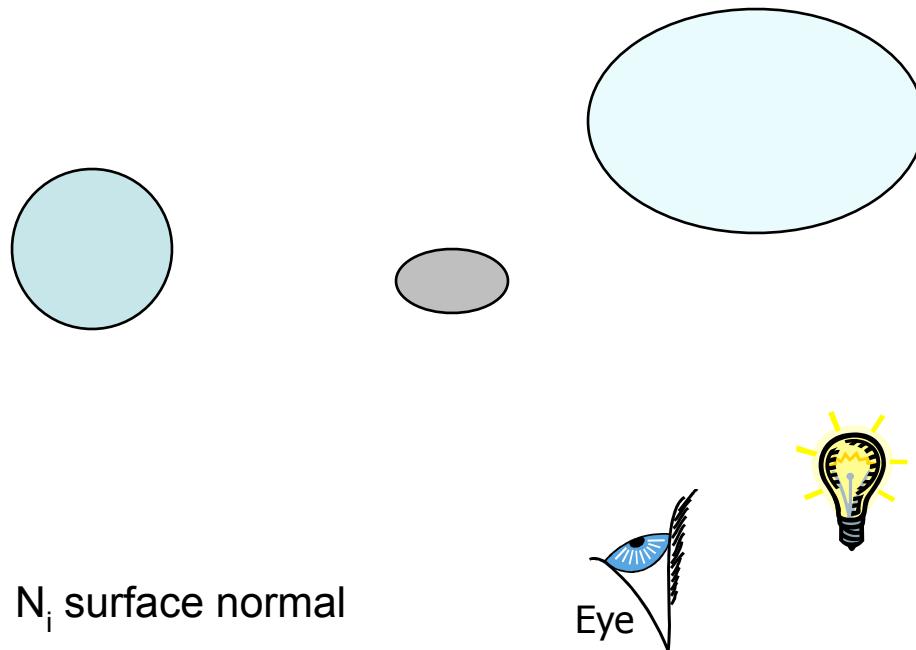


Recursion For Reflection: 2



The Ray Tree

Eye



N_i surface normal

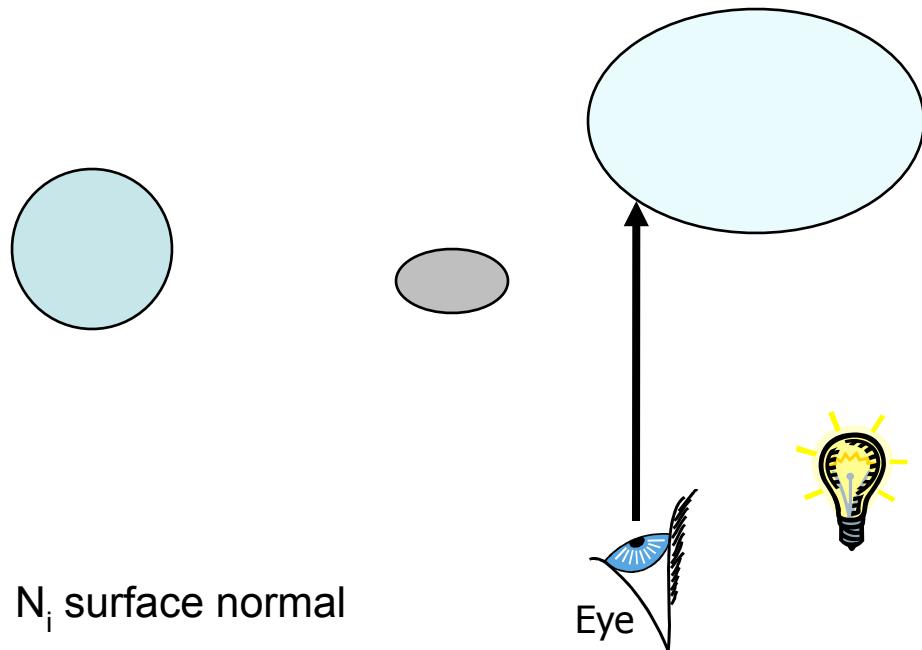
R_i reflected ray

L_i shadow ray

T_i transmitted (refracted) ray

The Ray Tree

Eye



N_i surface normal

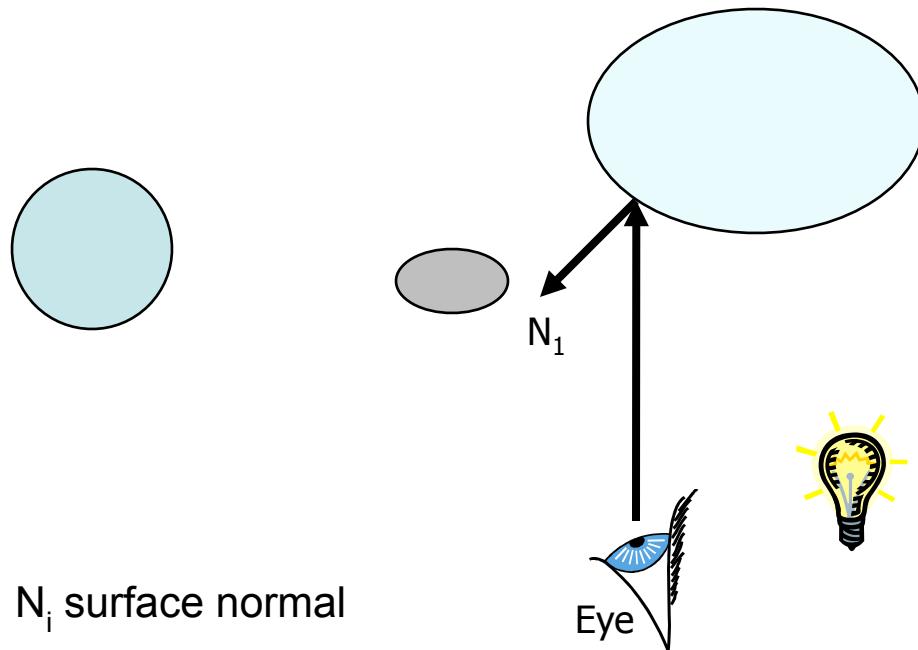
R_i reflected ray

L_i shadow ray

T_i transmitted (refracted) ray

The Ray Tree

Eye



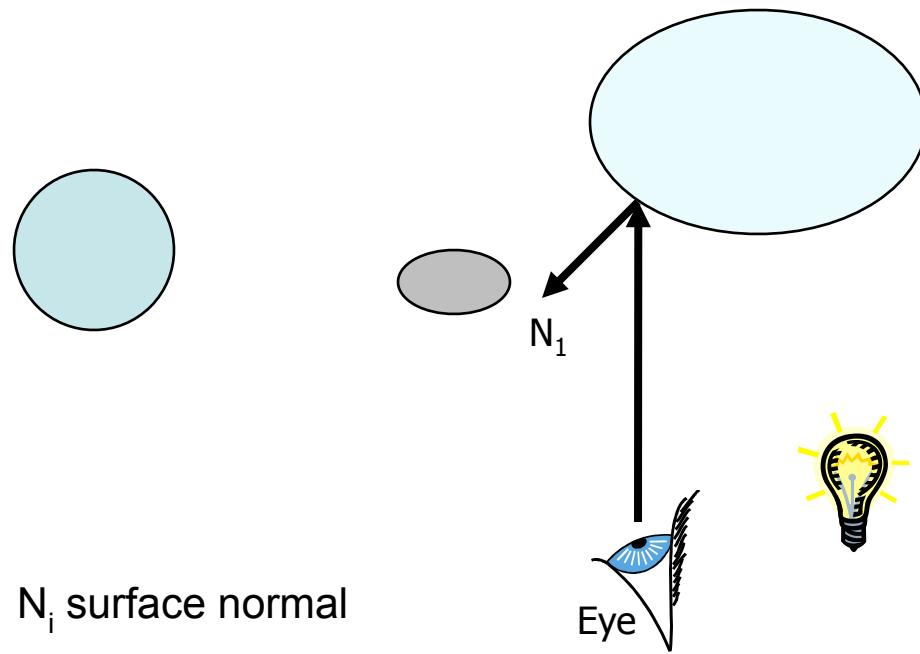
N_i surface normal

R_i reflected ray

L_i shadow ray

T_i transmitted (refracted) ray

The Ray Tree



N_i surface normal

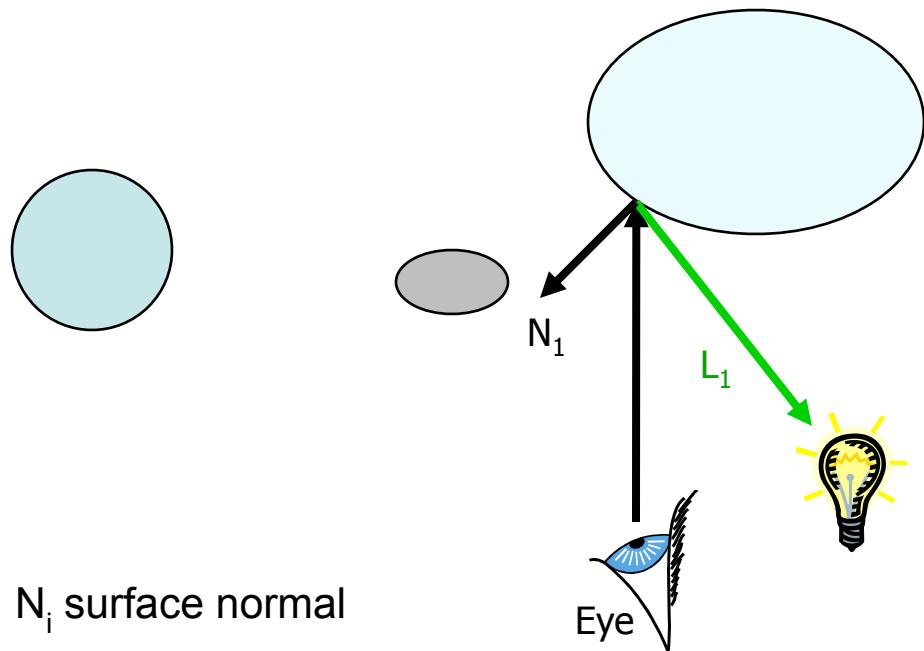
R_i reflected ray

L_i shadow ray

T_i transmitted (refracted) ray

Eye

The Ray Tree

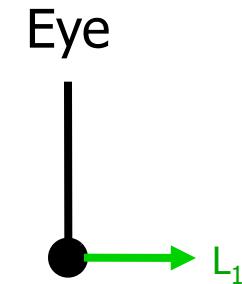


N_i surface normal

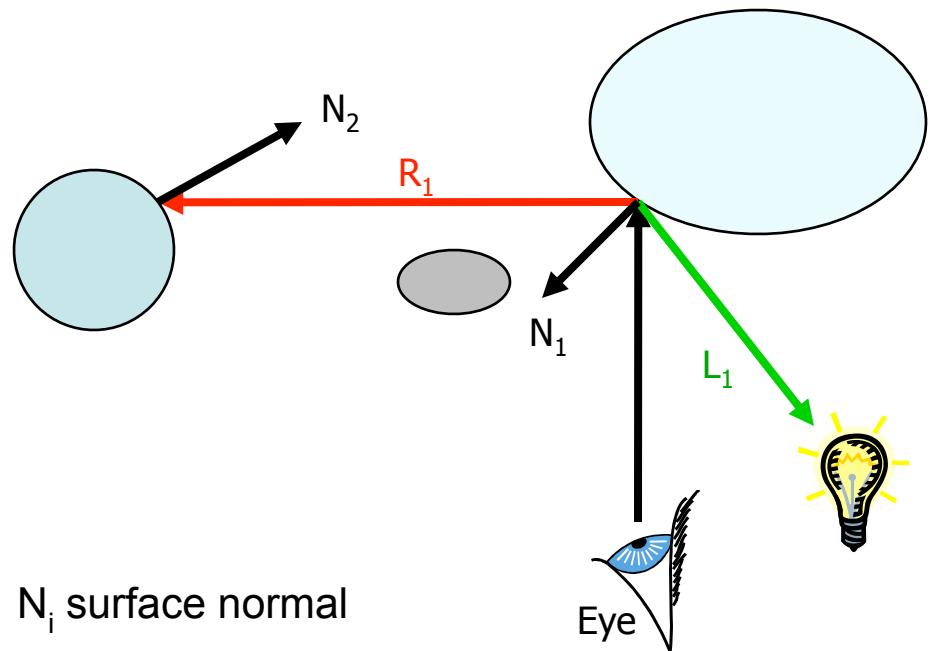
R_i reflected ray

L_i shadow ray

T_i transmitted (refracted) ray



The Ray Tree

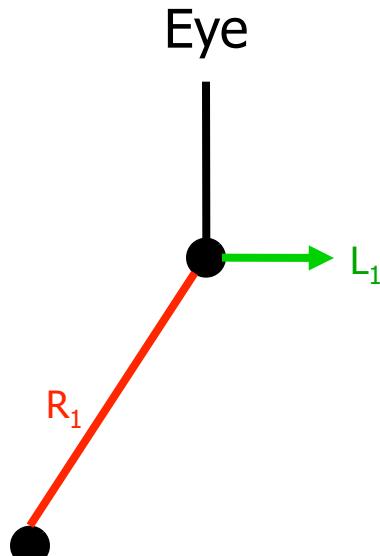


N_i surface normal

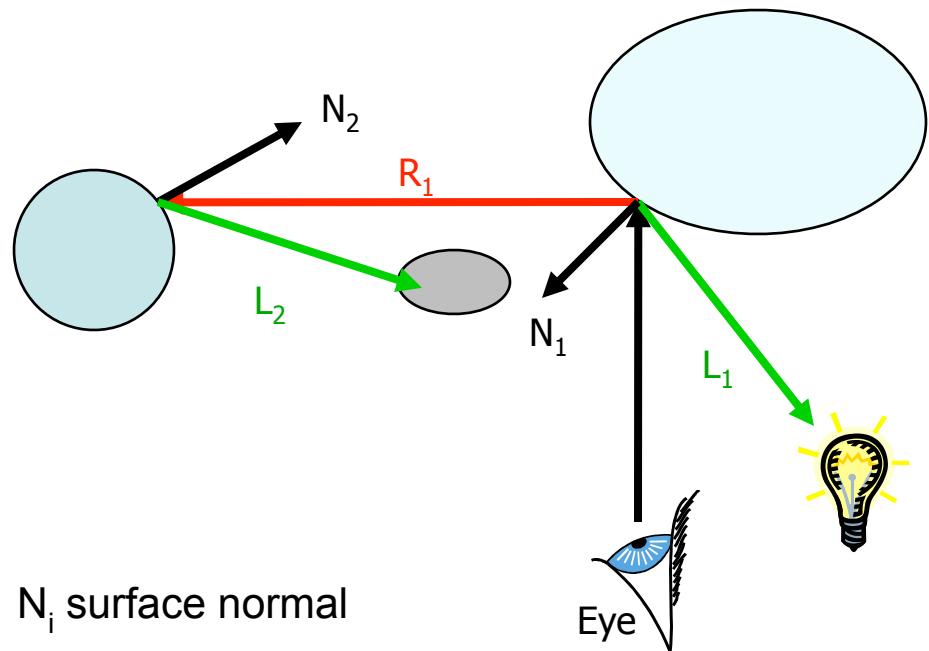
R_i reflected ray

L_i shadow ray

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The Ray Tree

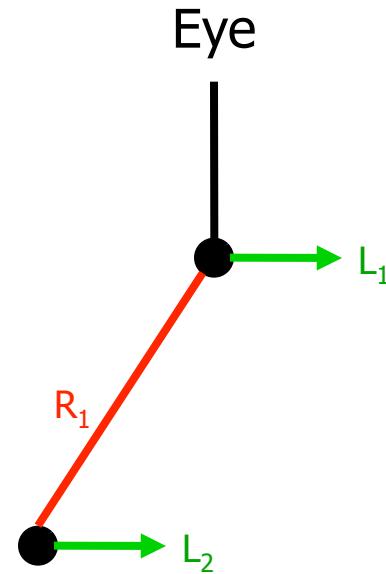


N_i surface normal

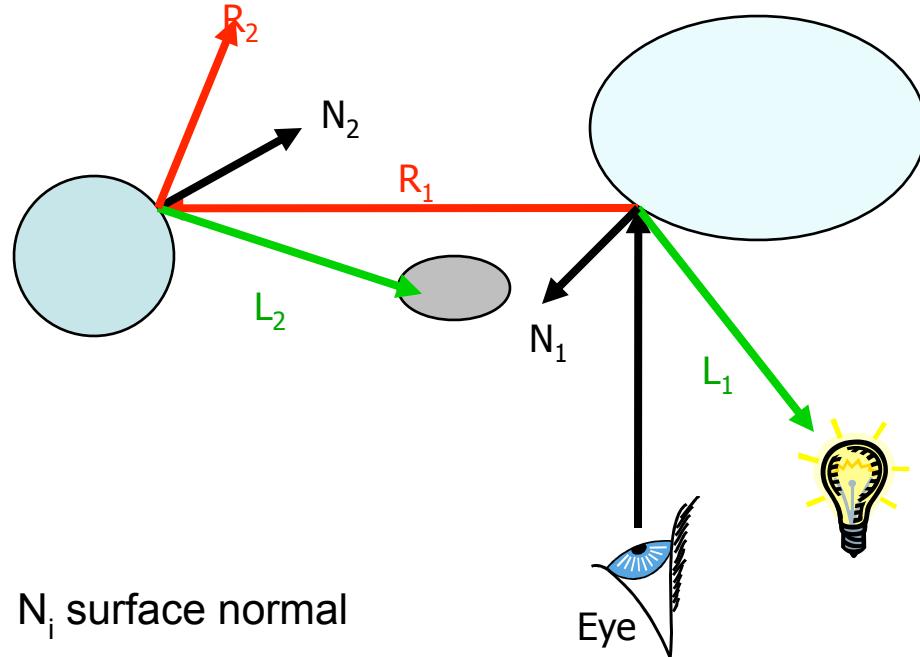
R_i reflected ray

L_i shadow ray

T_i transmitted (refracted) ray



The Ray Tree

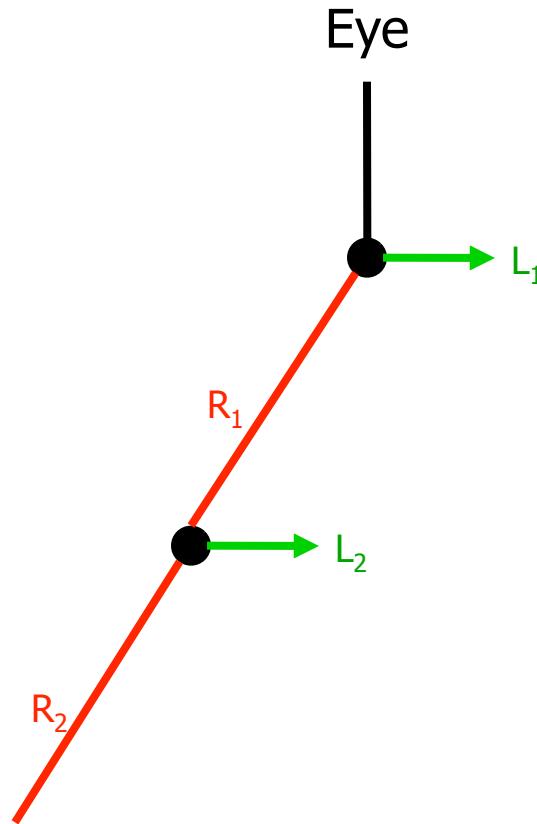


N_i surface normal

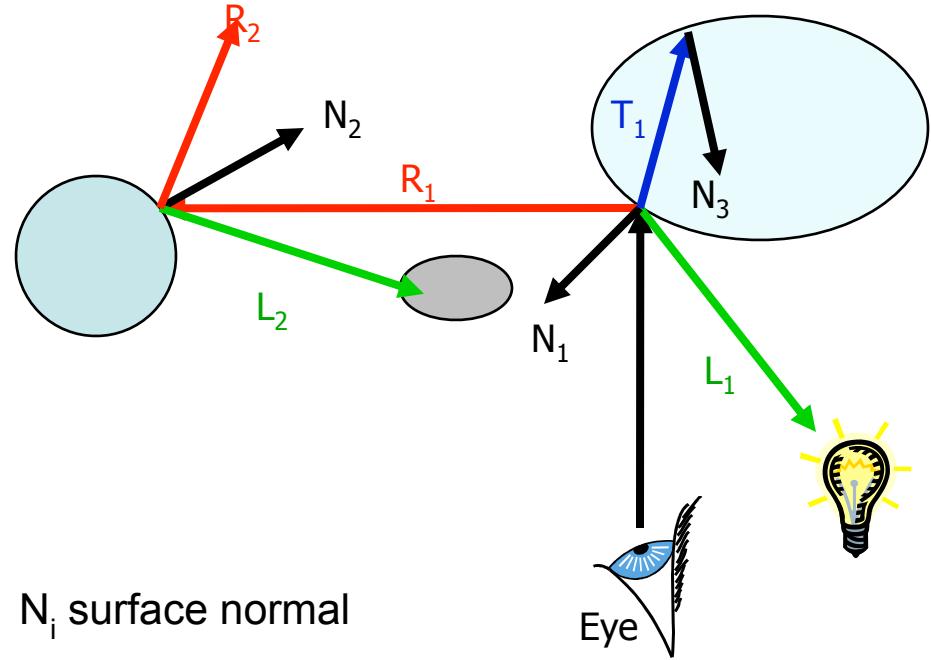
R_i reflected ray

L_i shadow ray

T_i transmitted (refracted) ray



The Ray Tree

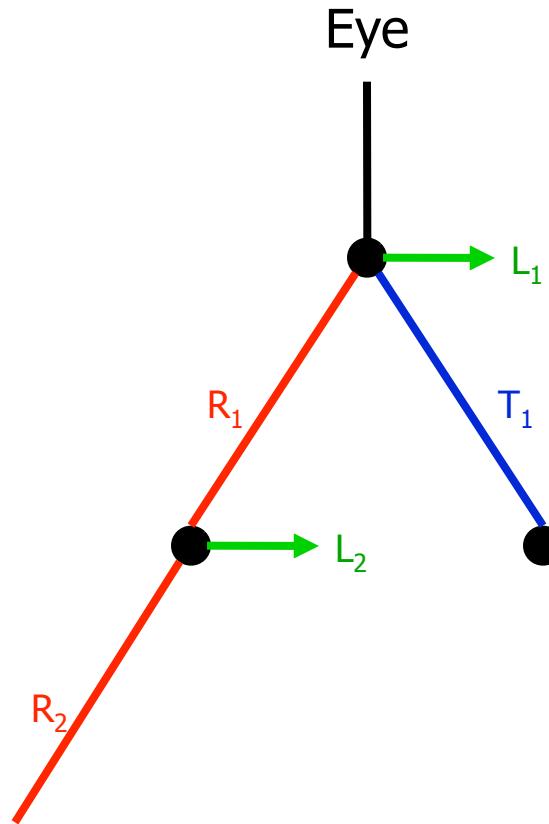


N_i surface normal

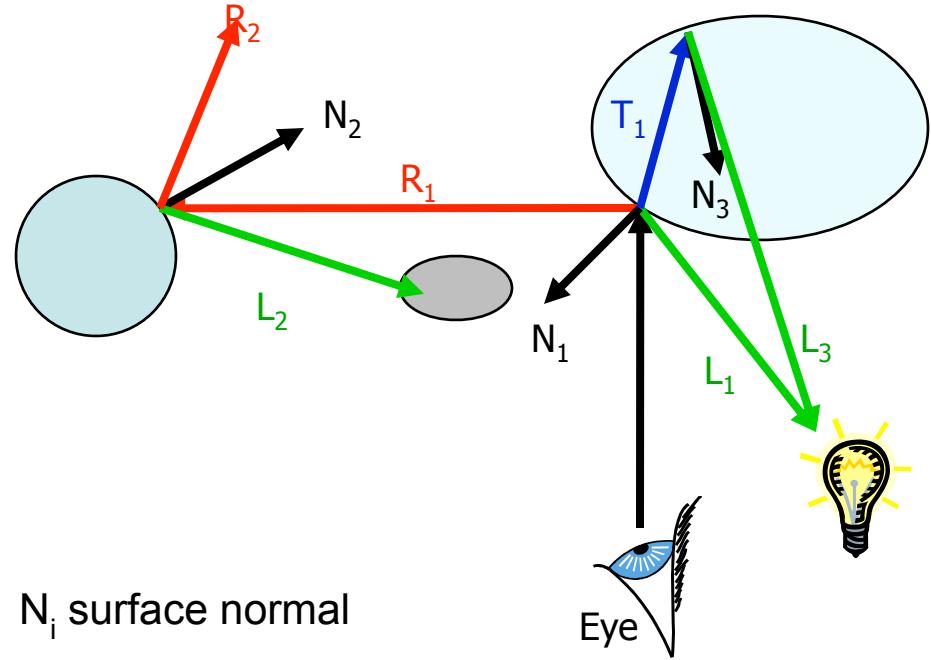
R_i reflected ray

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The Ray Tree

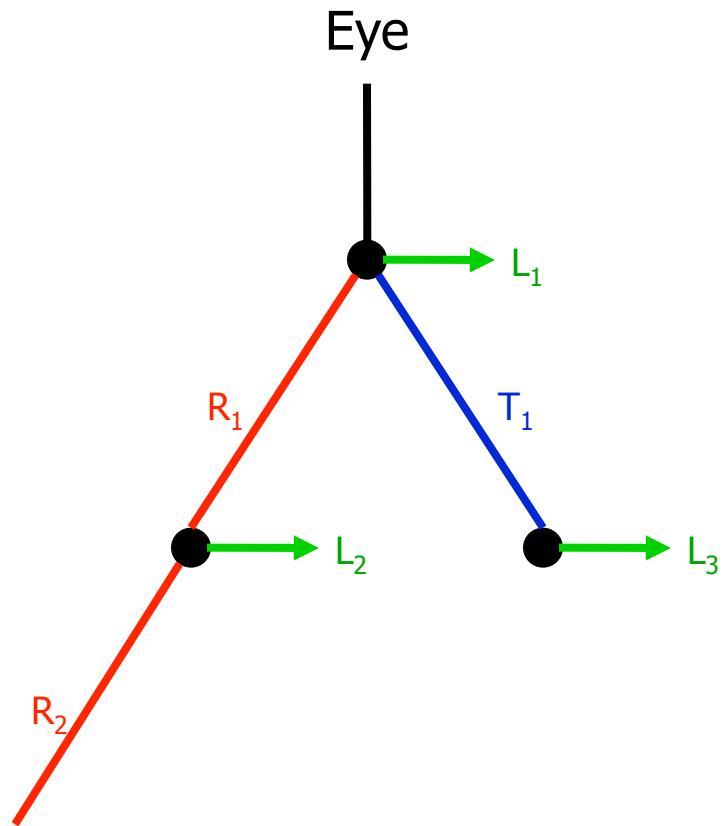


N_i surface normal

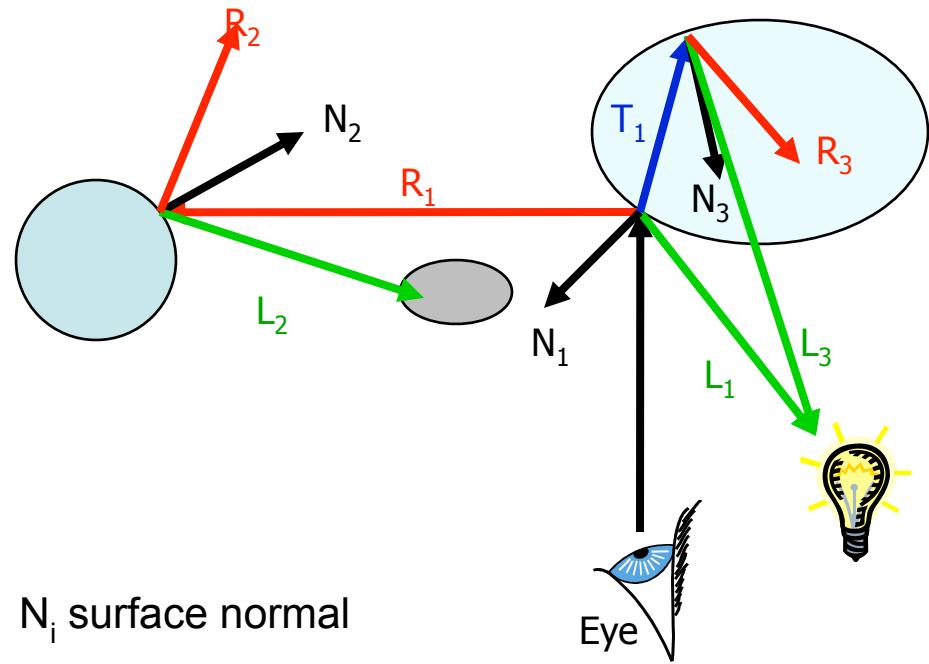
R_i reflected ray

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T_i transmitted (refracted) ray



The Ray Tree

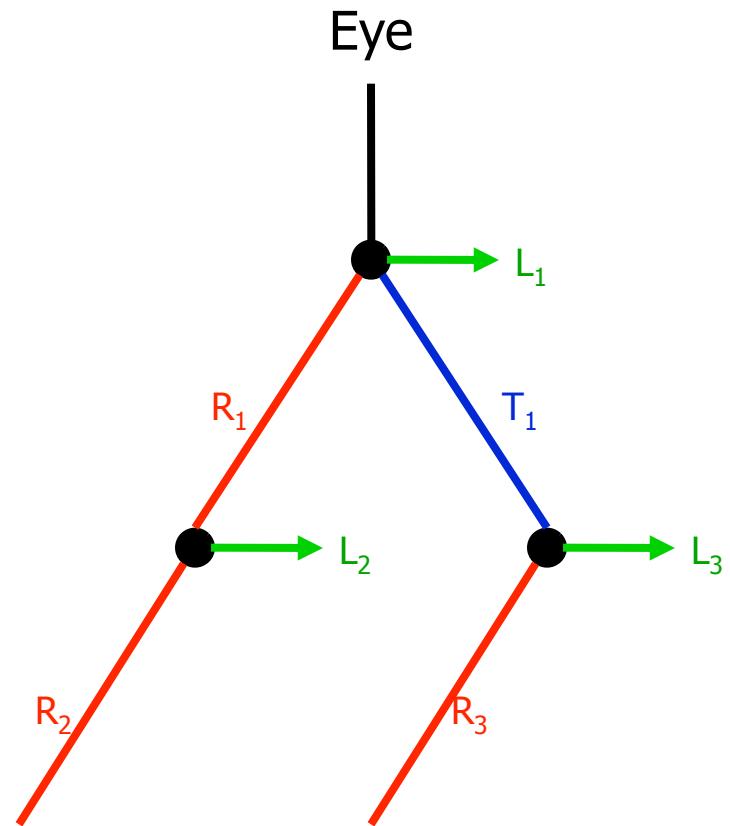


N_i surface normal

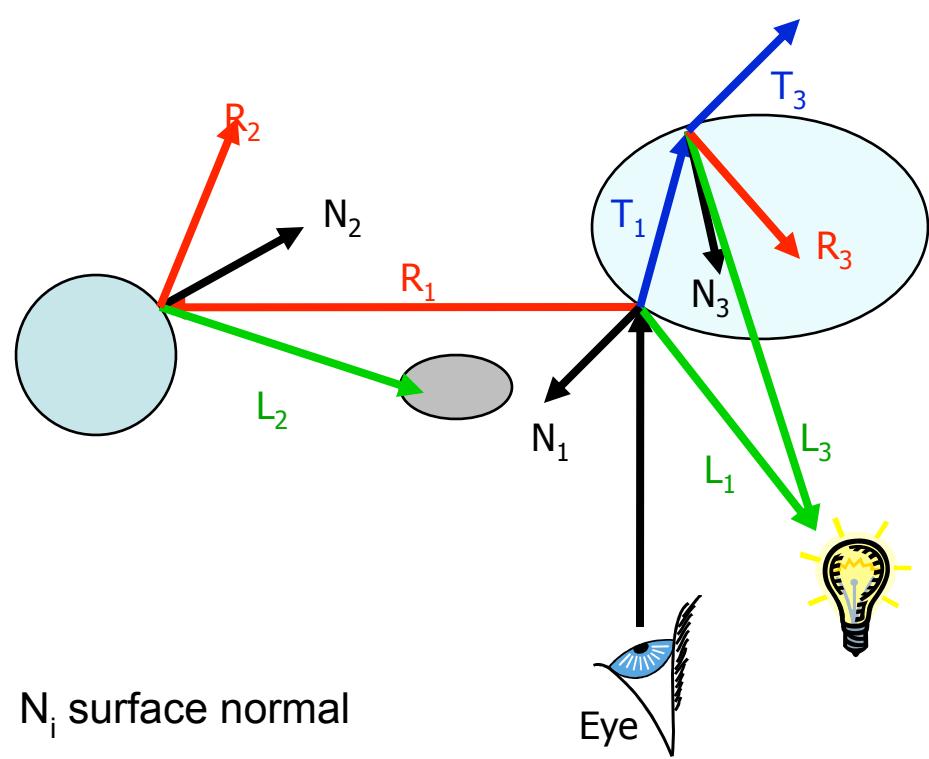
R_i reflected ray

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The Ray Tree

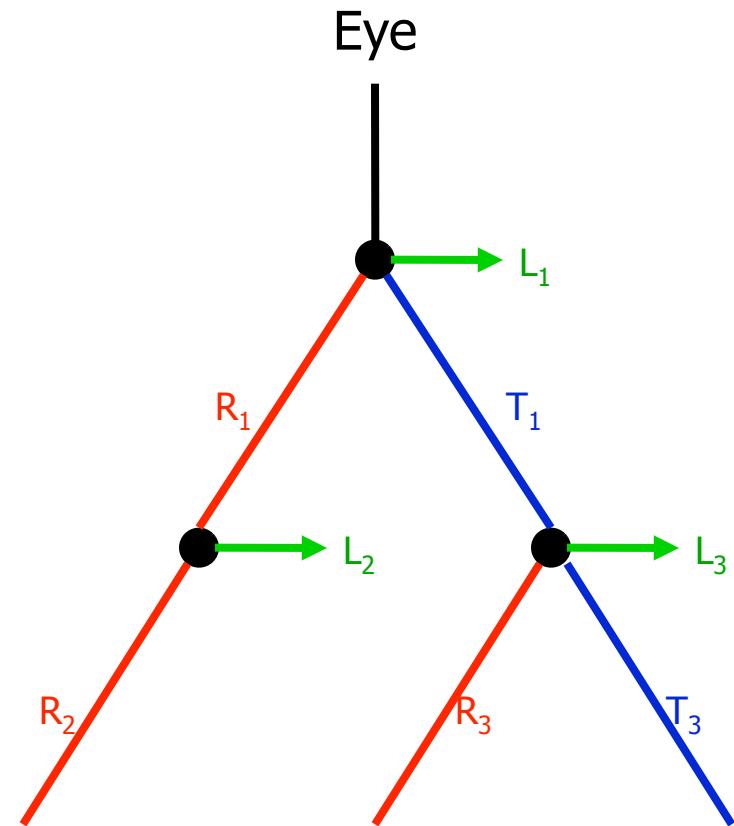


N_i surface normal

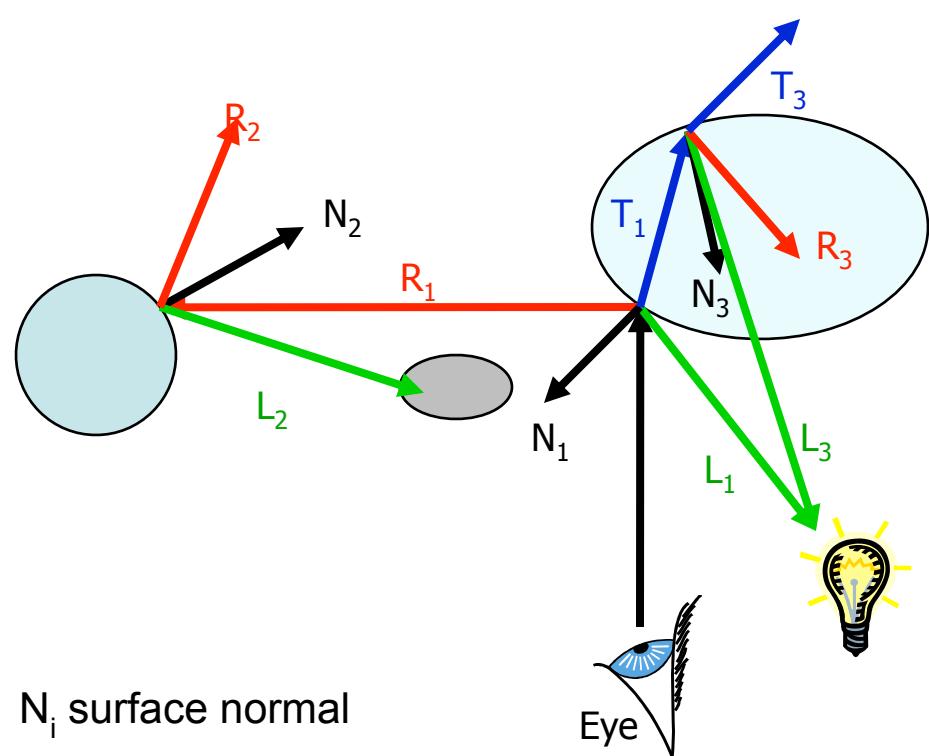
R_i reflected ray

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T_i transmitted (refracted) ray



The Ray Tree

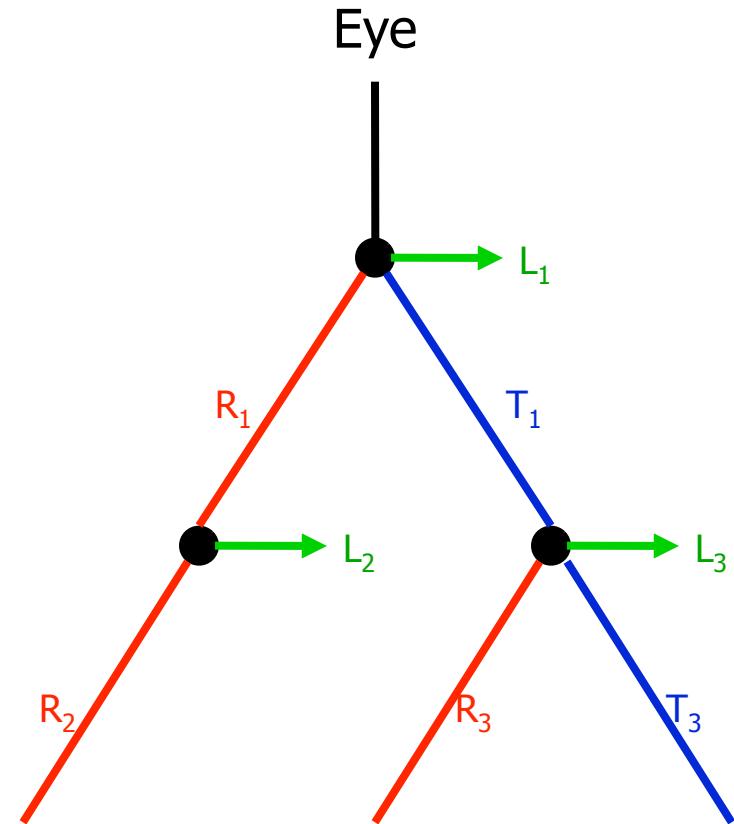


N_i surface normal

R_i reflected ray

L_i shadow ray

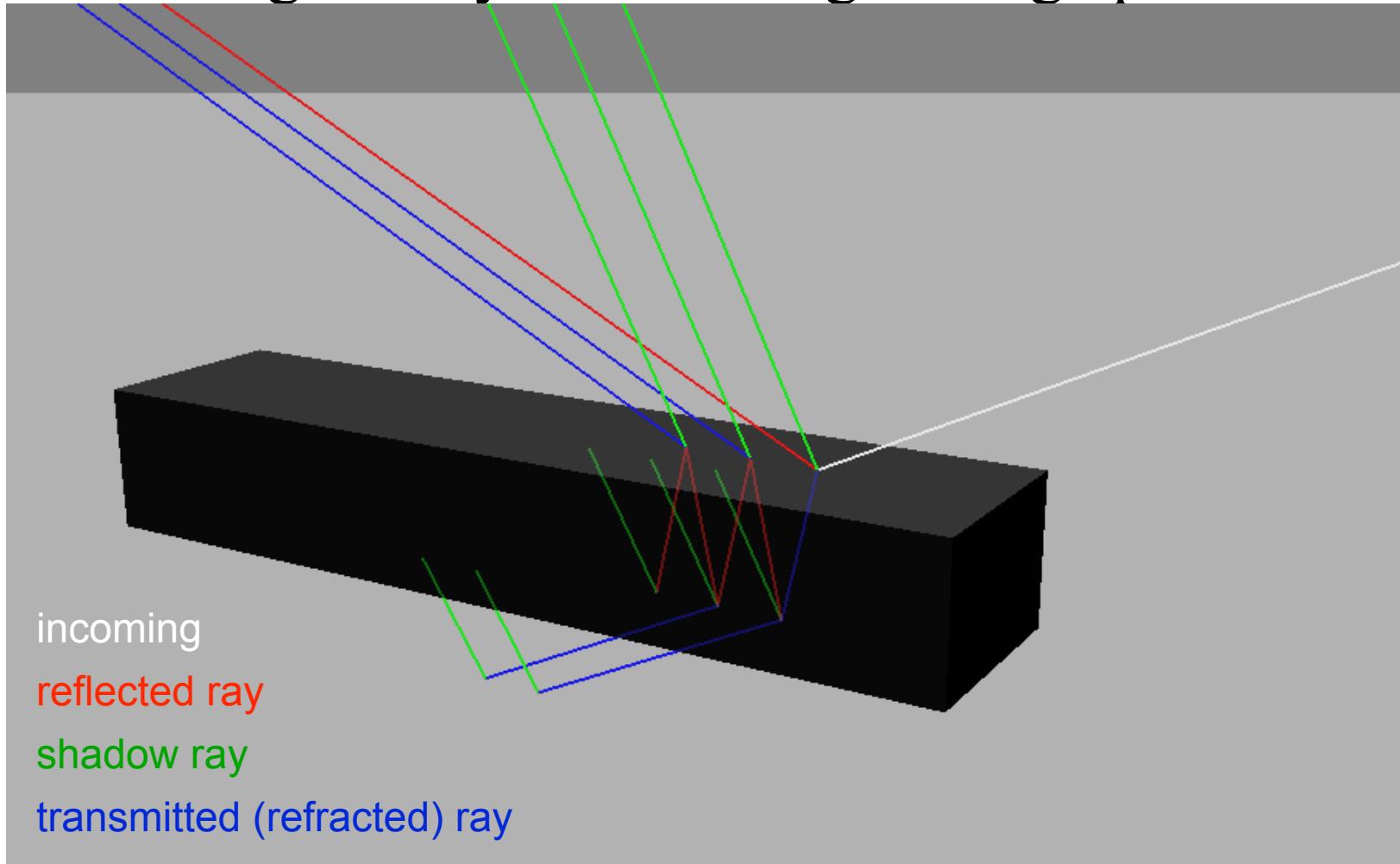
T_i transmitted (refracted) ray



Complexity?

Ray tree

- Visualizing the ray tree for single image pixel



Ray tree

This gets pretty complicated pretty fast!

- Visualizing the ray tree for single image pixel

