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# CS-C3100 Computer Graphics

## 4.2 Subdivision Surfaces

# Representing Surfaces

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- Triangle meshes ✓
  - Surface analogue of polylines, this is what GPUs draw
- Tensor Product Splines (previous video)
  - Surface analogue of spline curves
- **Subdivision surfaces (this video)**
- Implicit surfaces
  - $f(x,y,z)=0$
- Procedural
  - e.g. surfaces of revolution, generalized cylinder
- From volume data (medical images, etc.)

# In This Video

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- Subdivision for curves and surfaces
- Loop subdivision for triangle meshes

# Issues with Spline Patches

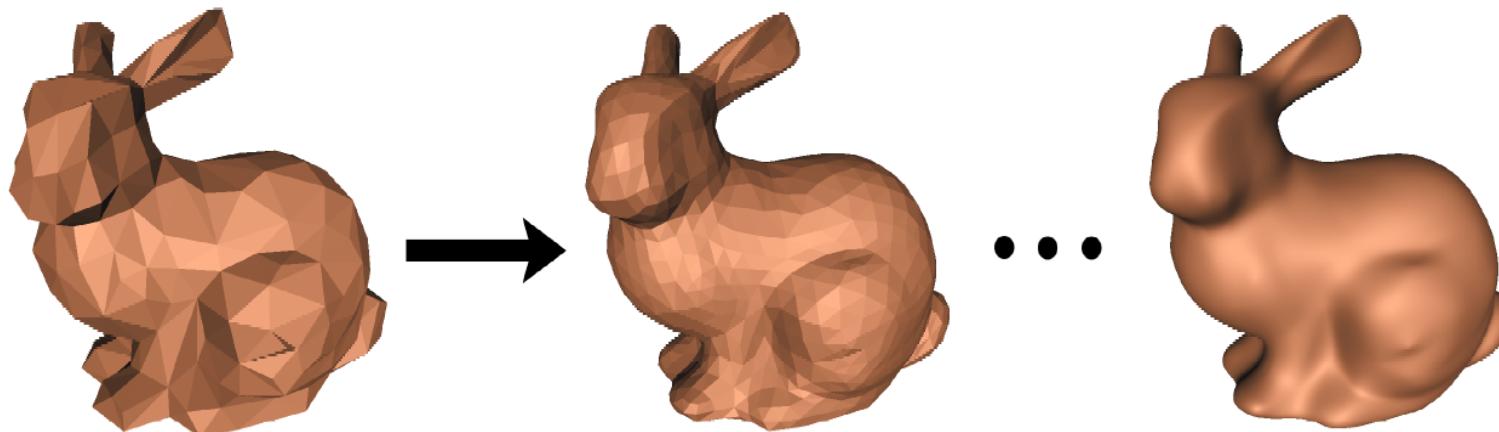
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- Regular connectivity only (square patches)
- Hard to ensure smoothness across boundaries
- Subdivision surfaces turn meshes into smooth surfaces through a recursive subdivision rule
  - Can use regular mesh modelling tools
  - Intuitive control
  - Smoothness built in (with some caveats)

# Subdivision Surfaces

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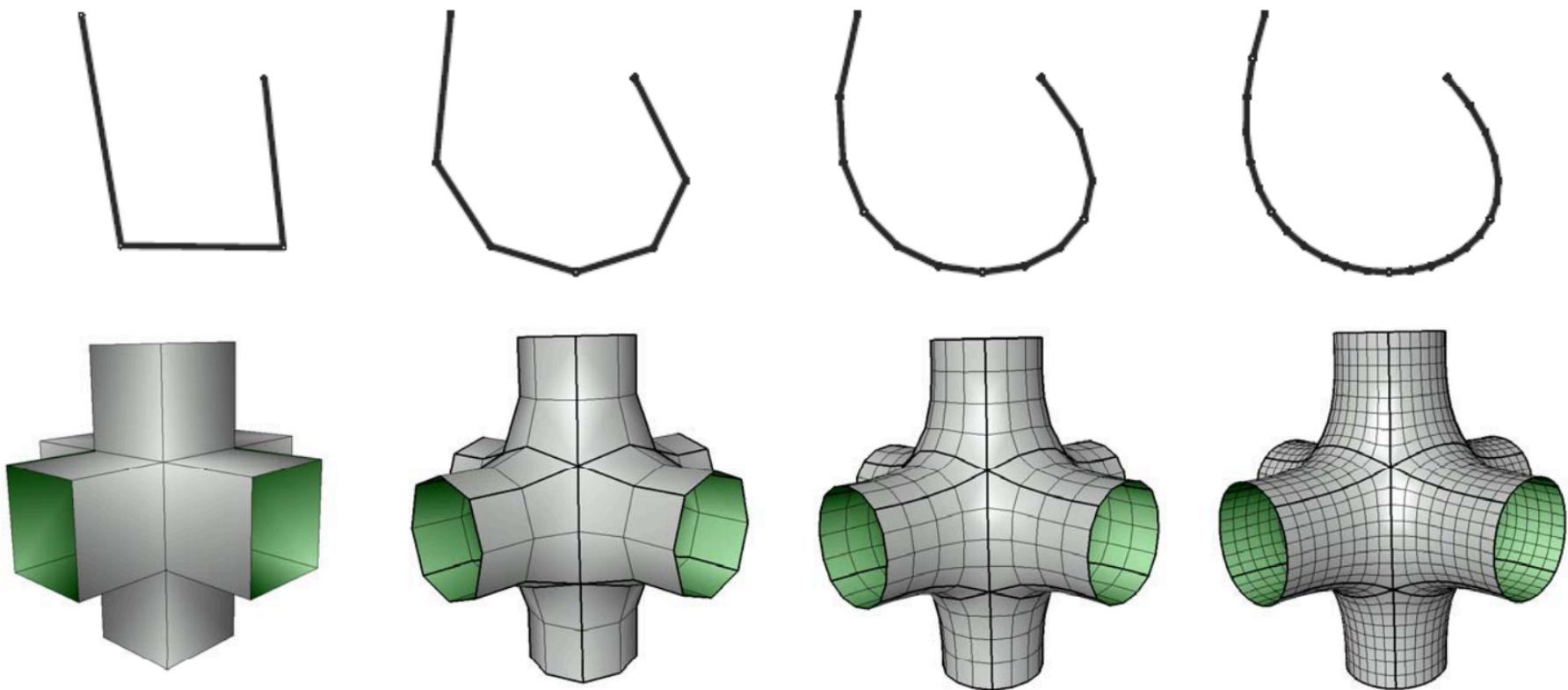
- Start with polygonal mesh
- Subdivide into larger number of polygons, smooth result after each subdivision
  - Lots of ways to do this.
- The limit surface is smooth!



# Subdividing curves vs. Surfaces

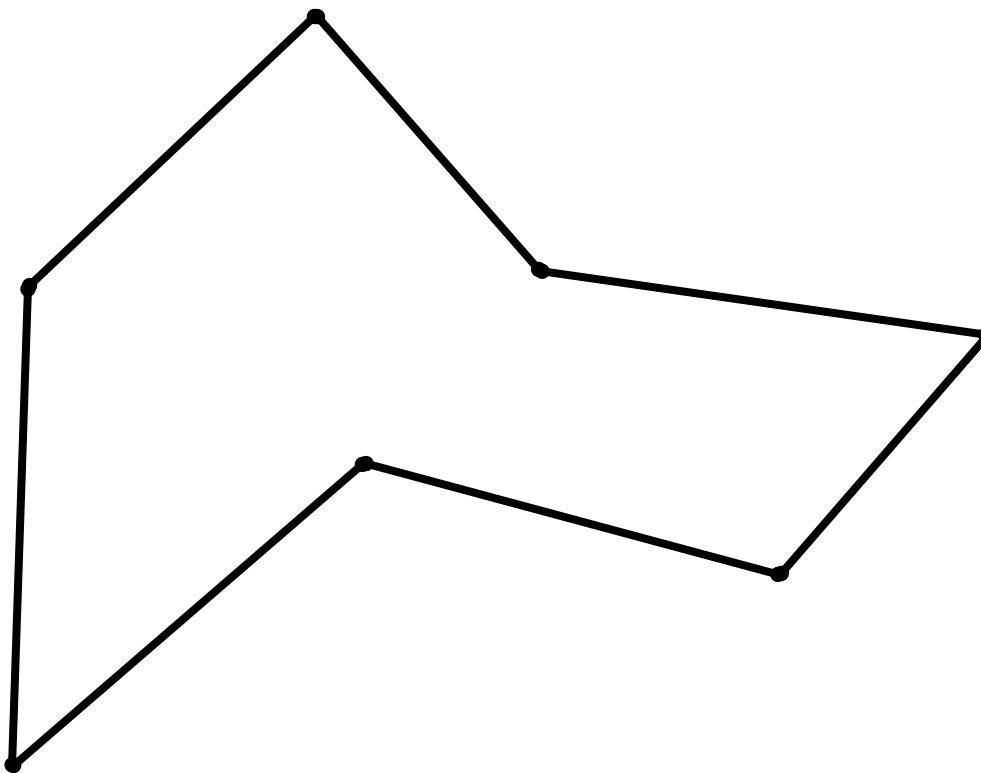
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Image from Mirela Ben-Chen's Geometry Processing Algorithms class (Stanford)



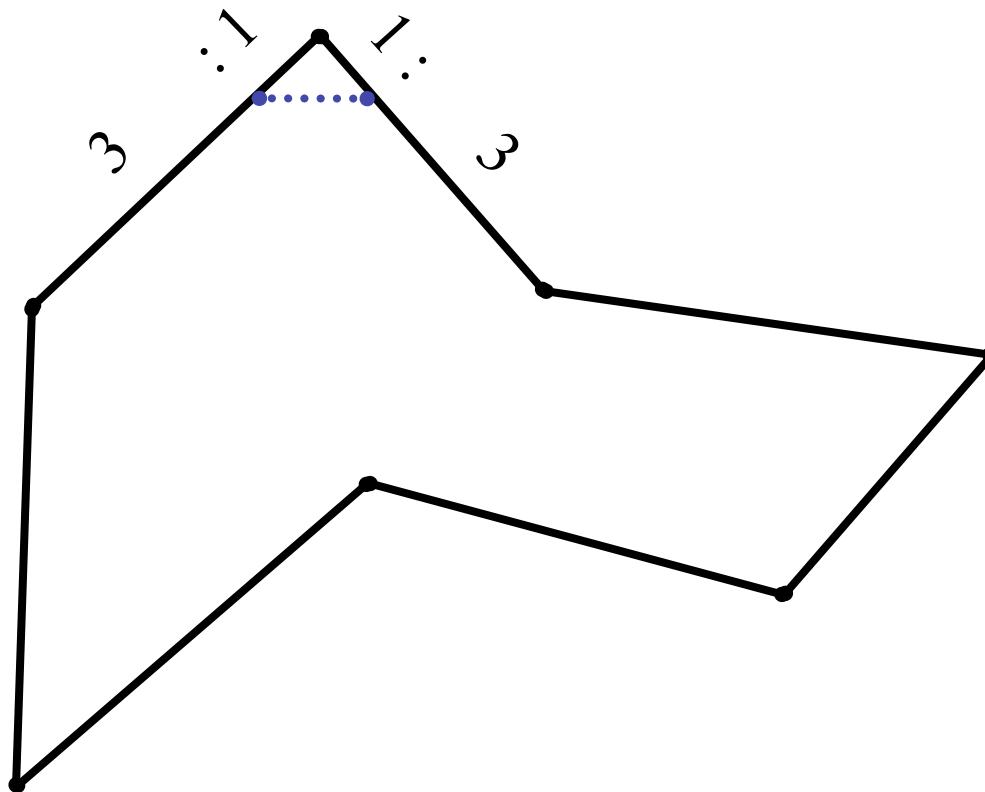
# Corner Cutting

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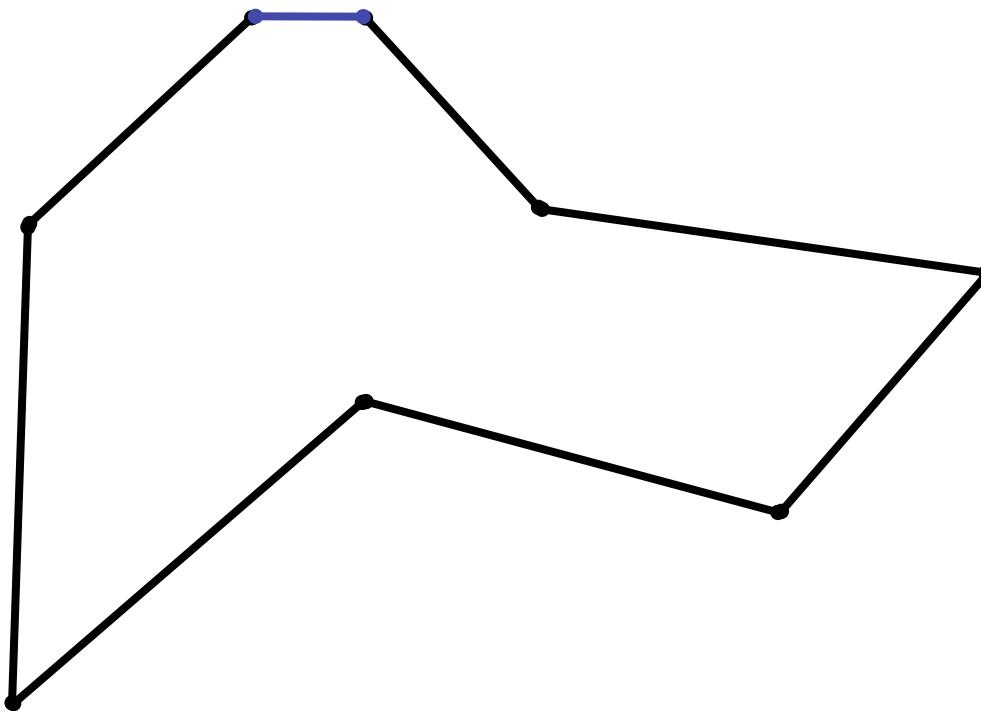
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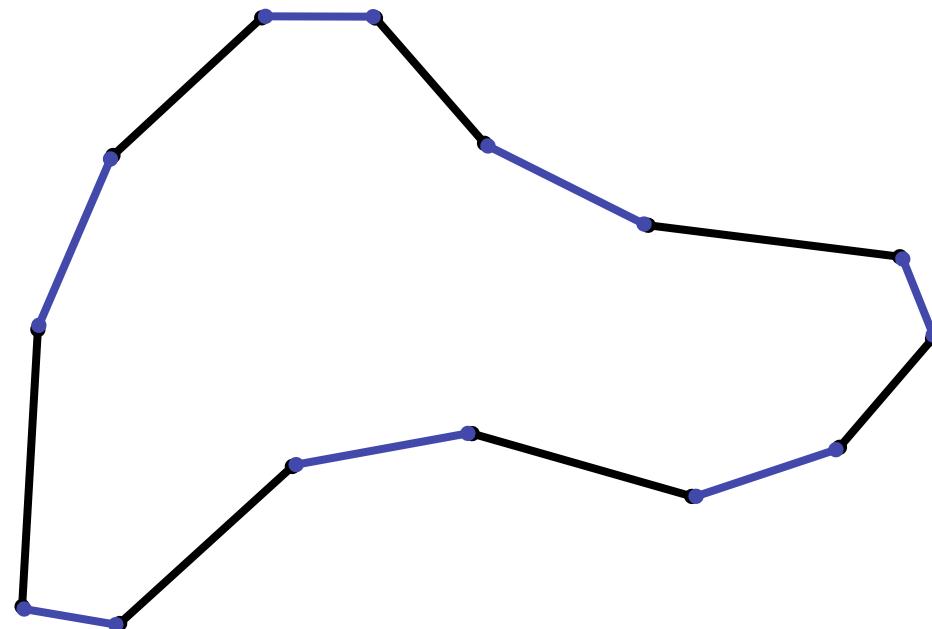
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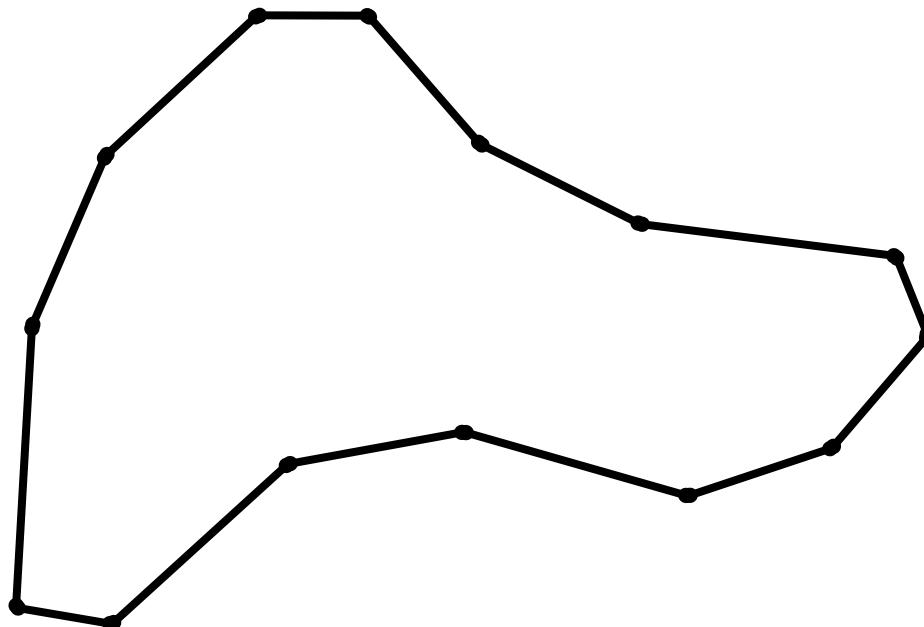
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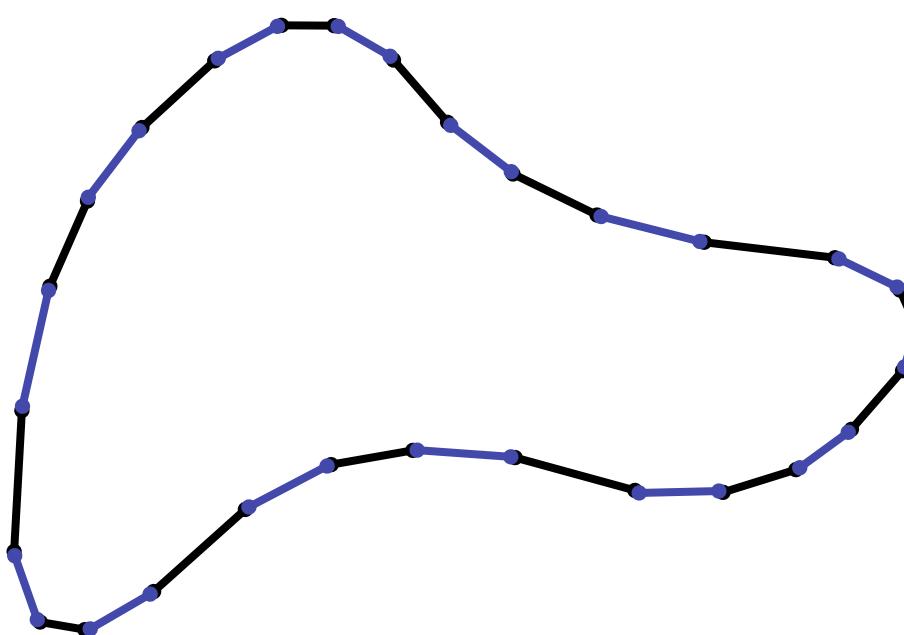
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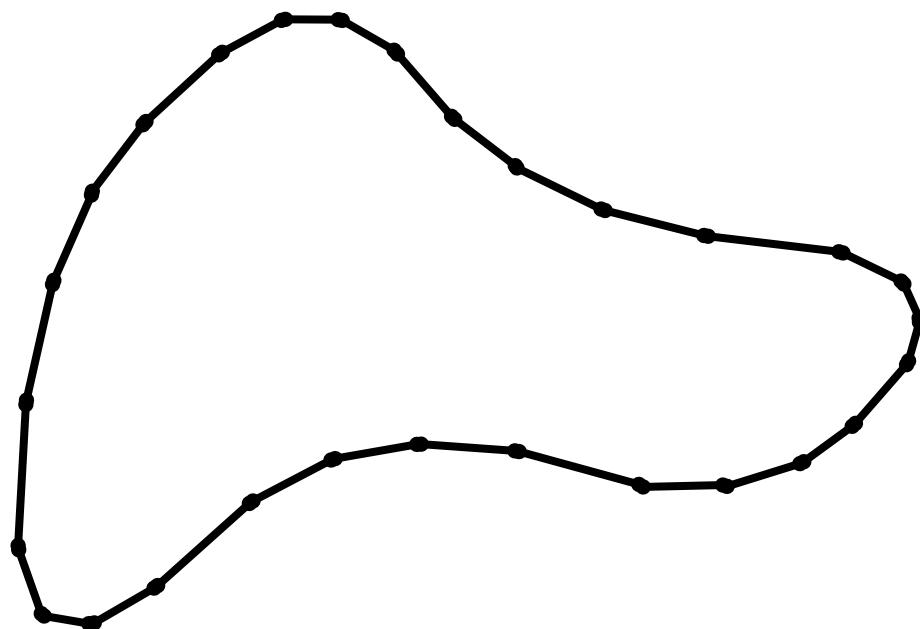
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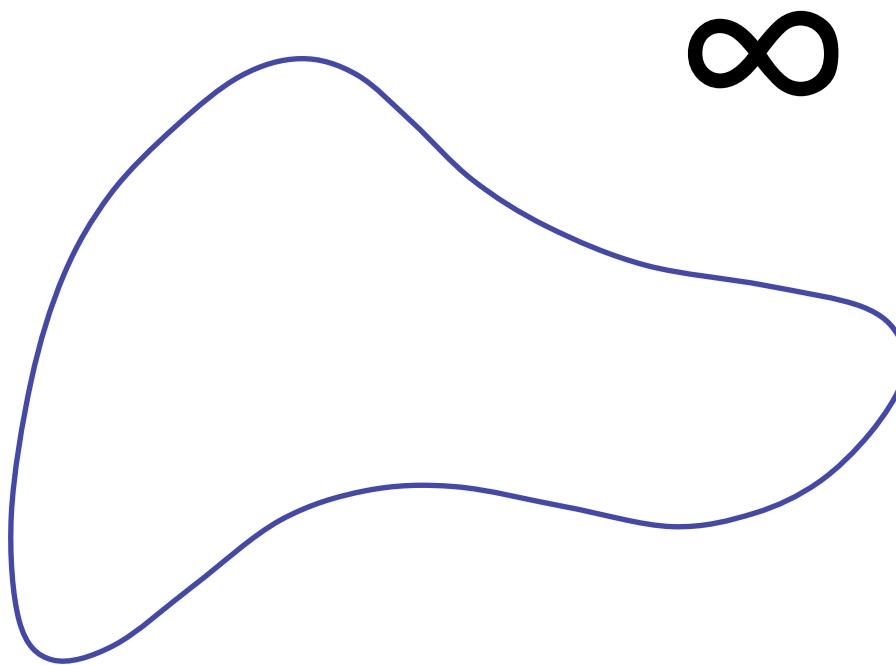
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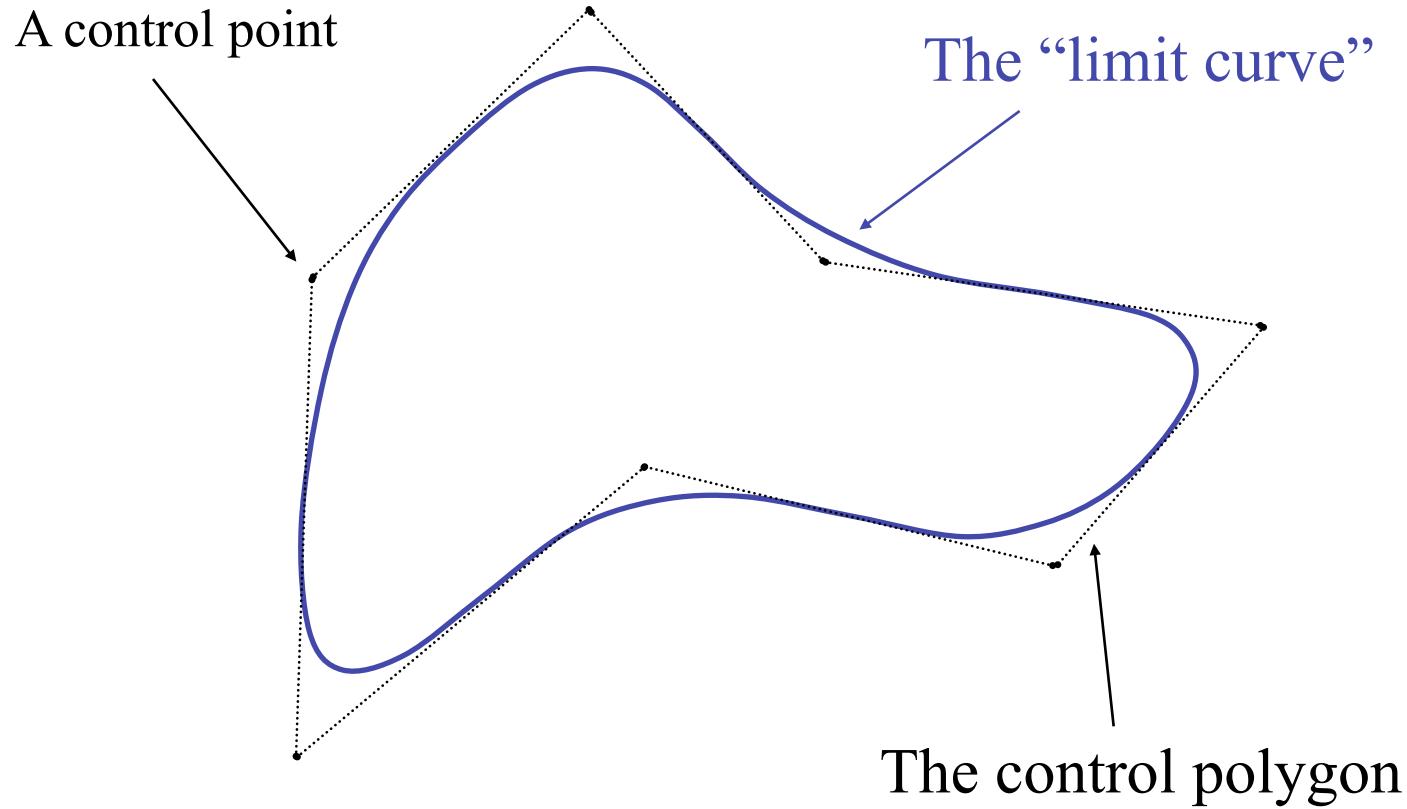
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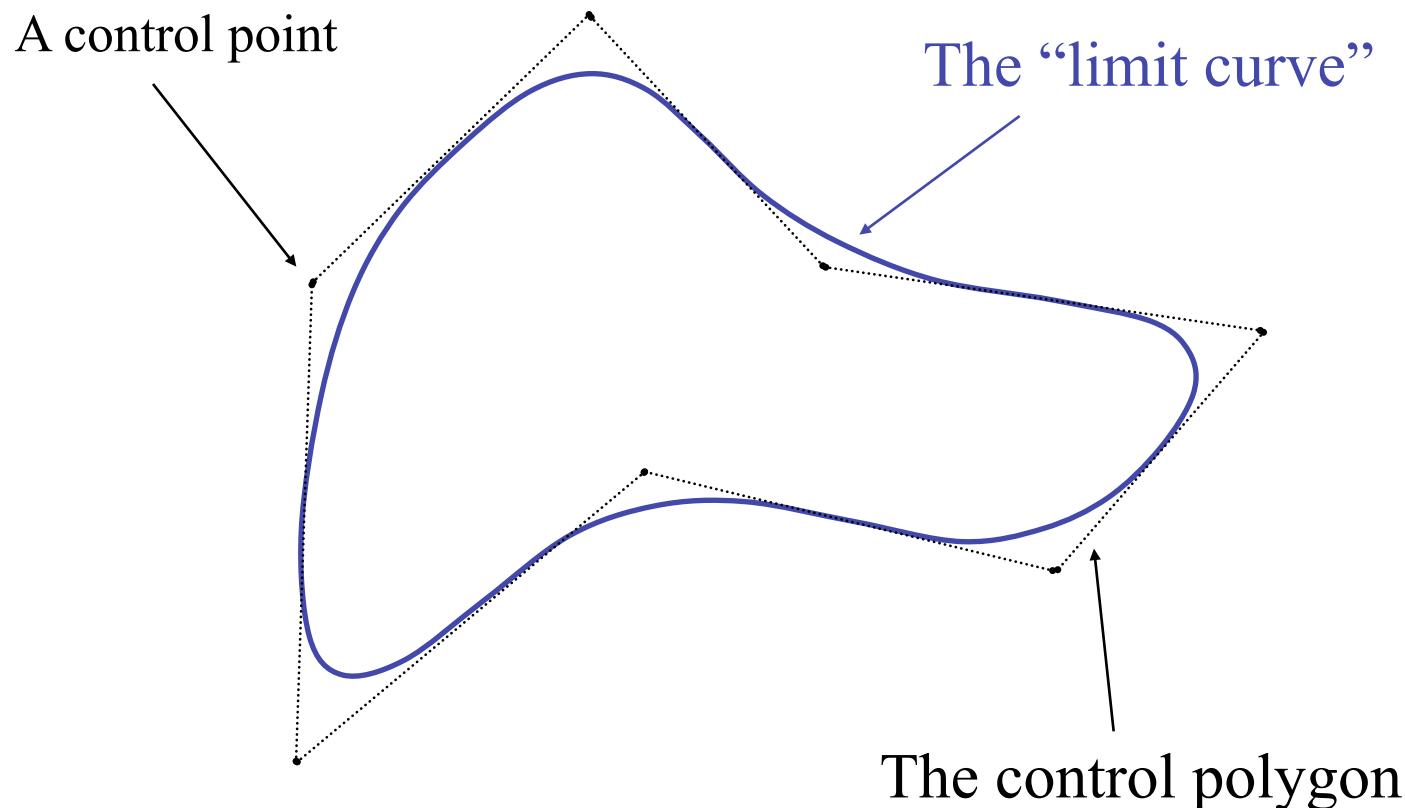
# Corner Cutting

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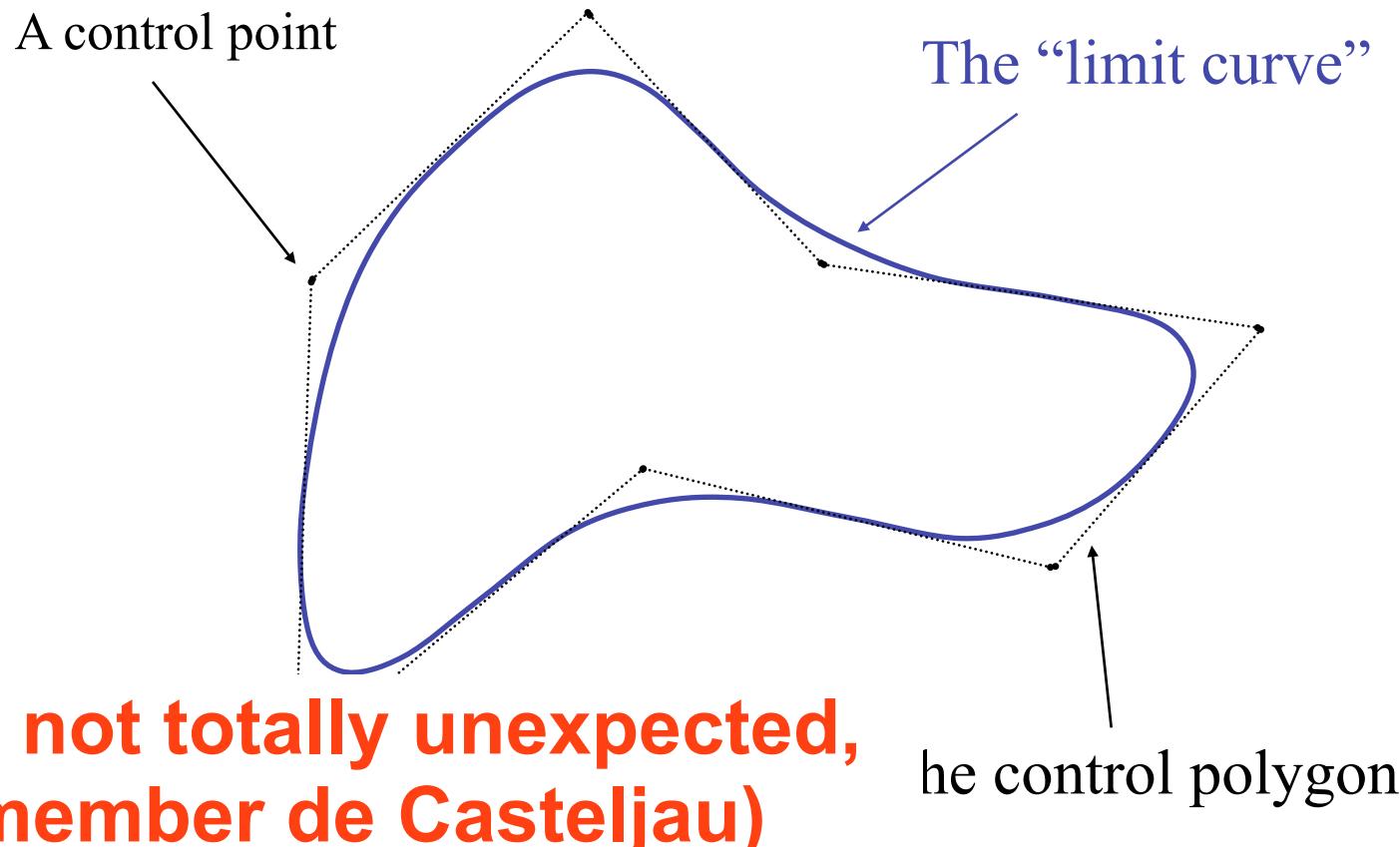
# Corner Cutting

It turns out corner cutting (Chaikin's Algorithm) produces a quadratic B-Spline curve! (Magic!)



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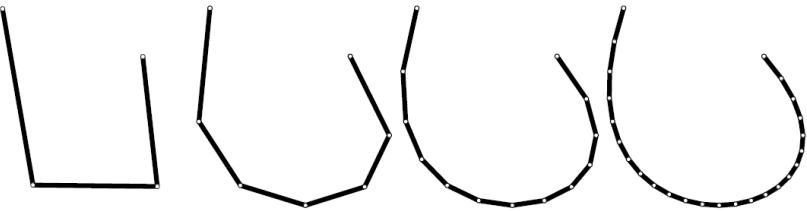
(Well, not totally unexpected,  
remember de Casteljau)

the control polygon

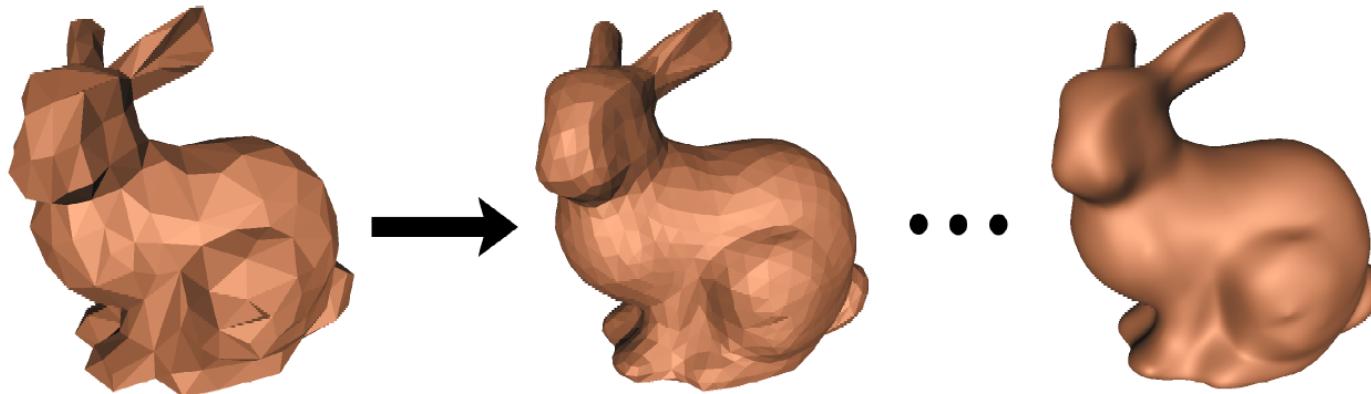
# Subdivision Curves and Surfaces

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- Idea: cut corners to smooth
- Add points and compute weighted average of neighbors
- Same for surfaces
  - Special case for irregular vertices
    - vertex with more or less than 6 neighbors in a triangle mesh



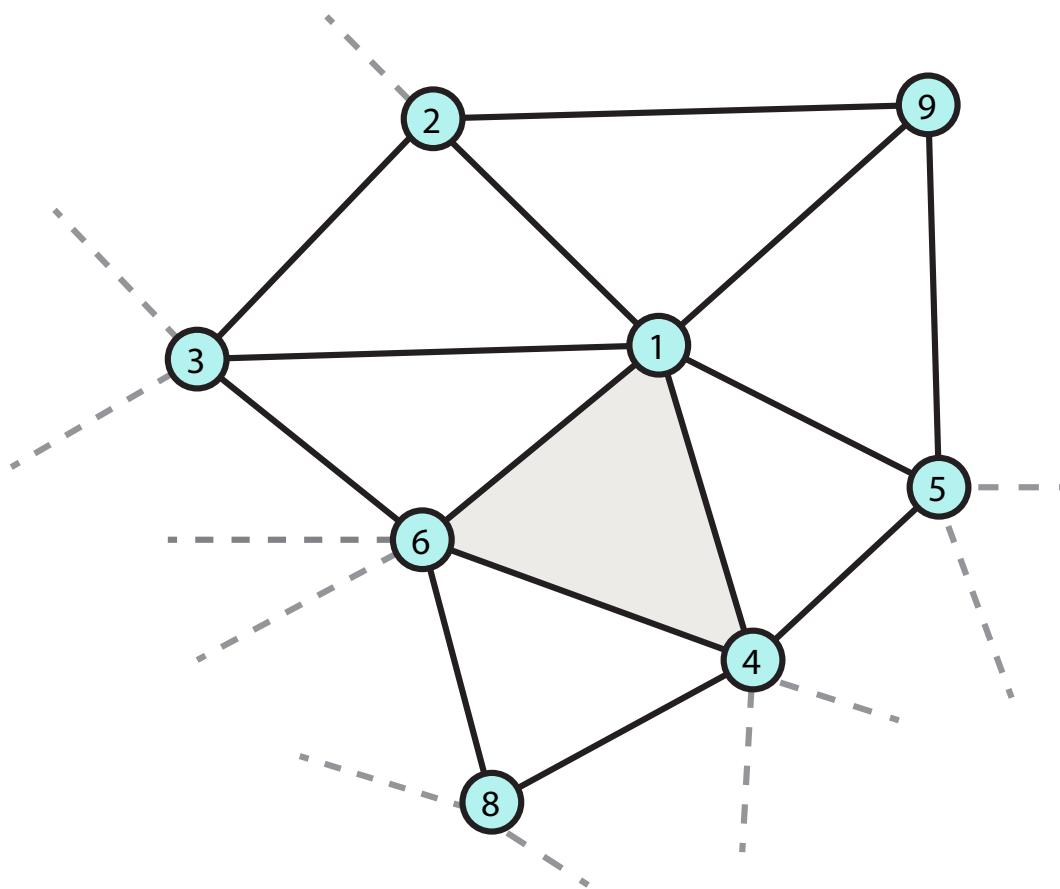
Warren et al.



# Assignment 2: Loop Subdivision

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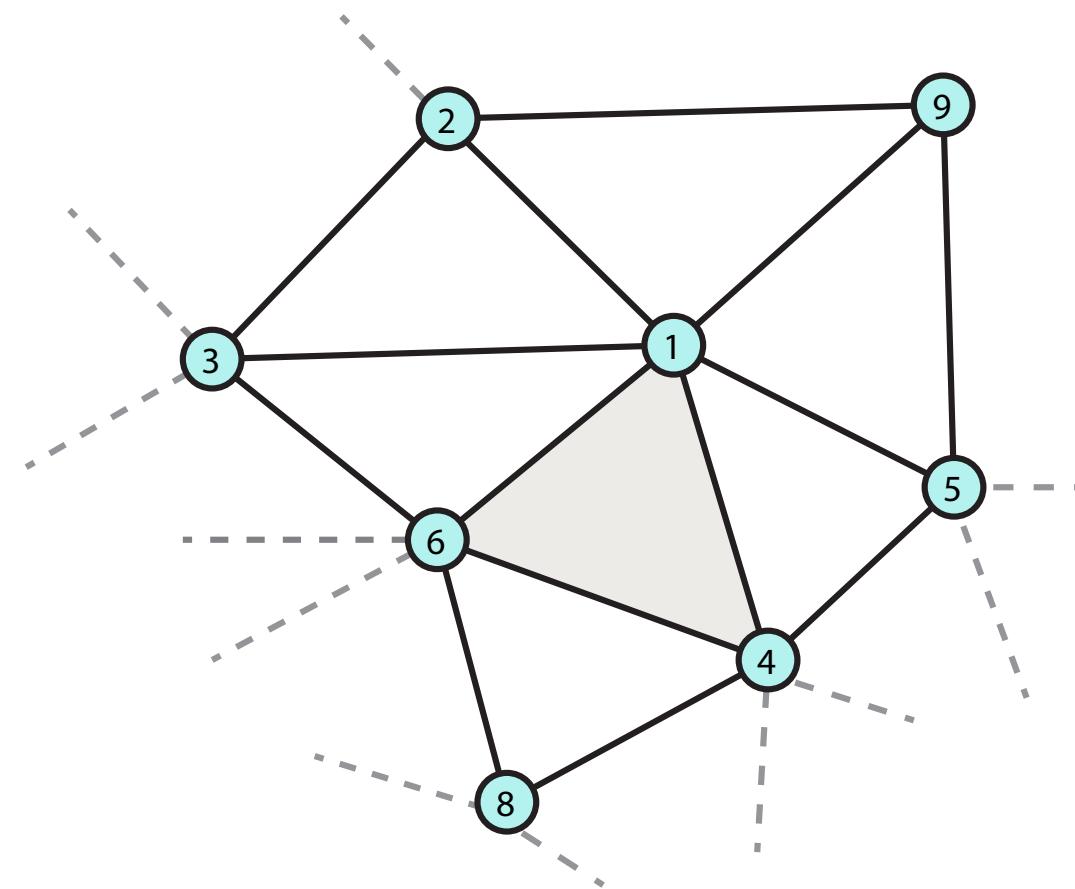
- (After Charles Loop, now with NVIDIA Research)



# Assignment 2: Loop Subdivision

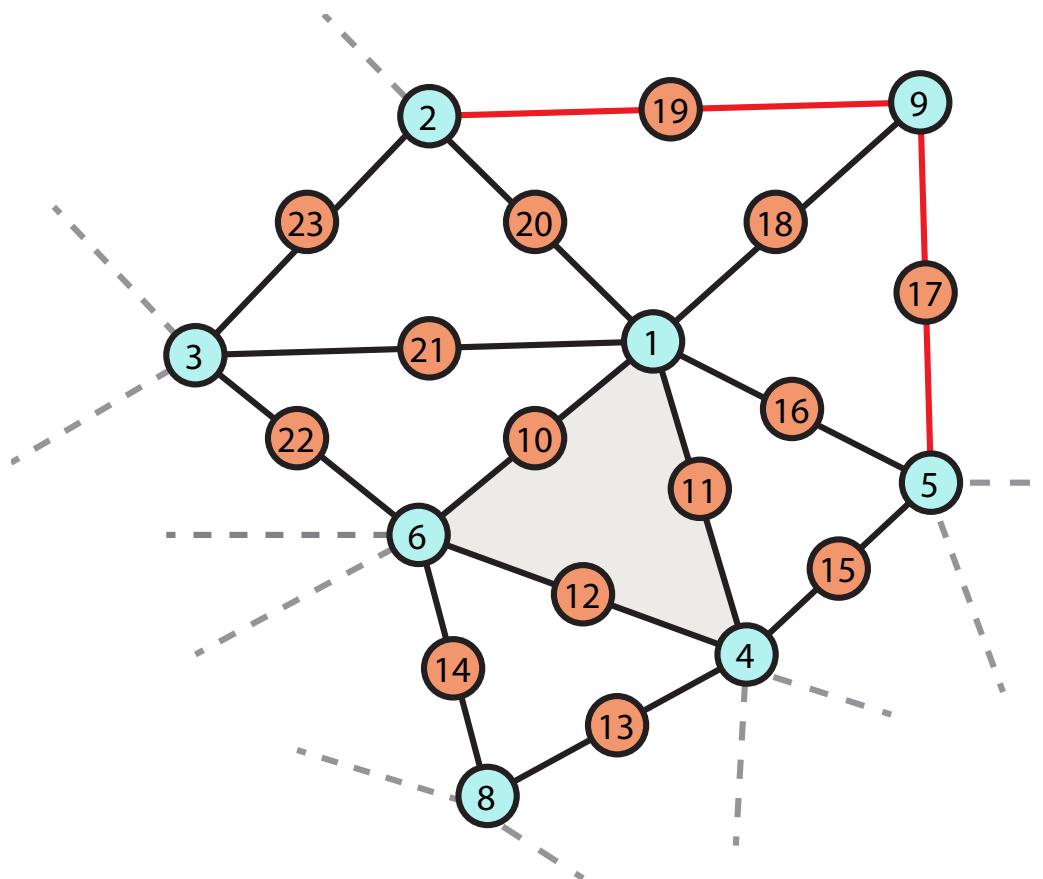
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- The input mesh



# Assignment 2: Loop Subdivision

- First step: each input edge gets a new vertex



Vertex from input mesh

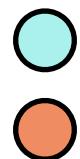
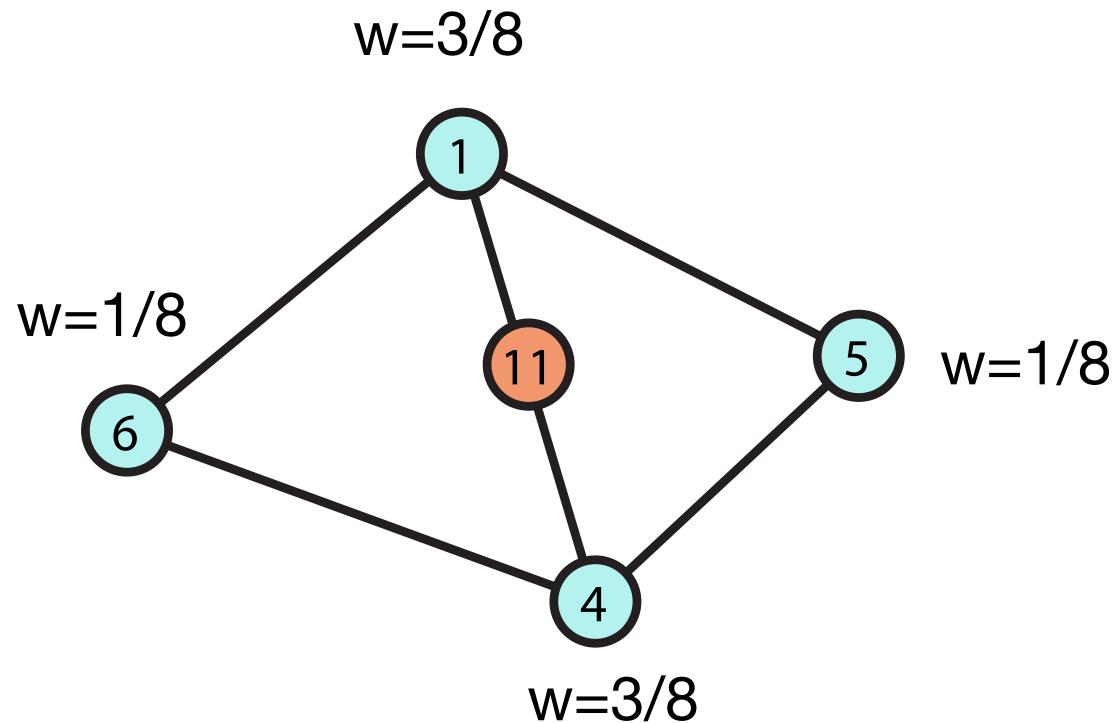


Newly-introduced vertex

# Assignment 2: Loop Subdivision

- Then compute positions for new vertices
  - Weighted combinations of the connected *old* vertices
  - Need adjacency information (details in handout)

$$p_{11} = \frac{1}{8} p_5 + \frac{1}{8} p_6 + \frac{3}{8} p_1 + \frac{3}{8} p_4$$



Vertex from input mesh



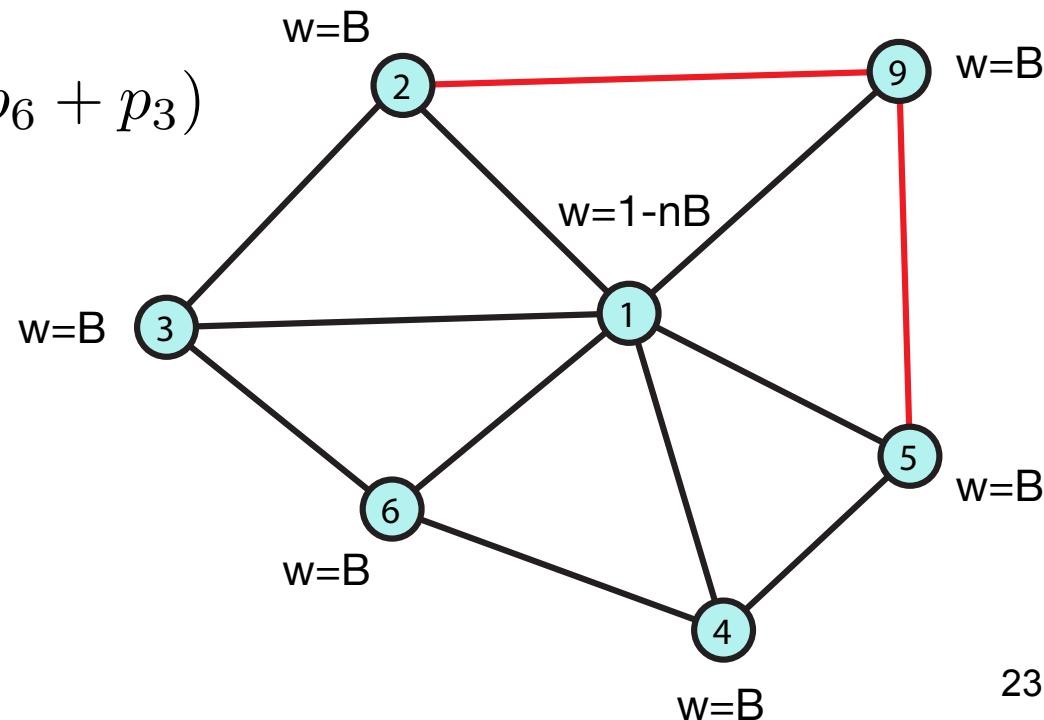
Newly-introduced vertex

# Assignment 2: Loop Subdivision

- Then compute new positions for all *old* vertices!
  - Again weighted combinations of nearby *old* vertices
  - Need to find all  $n$  connected vertices

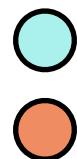
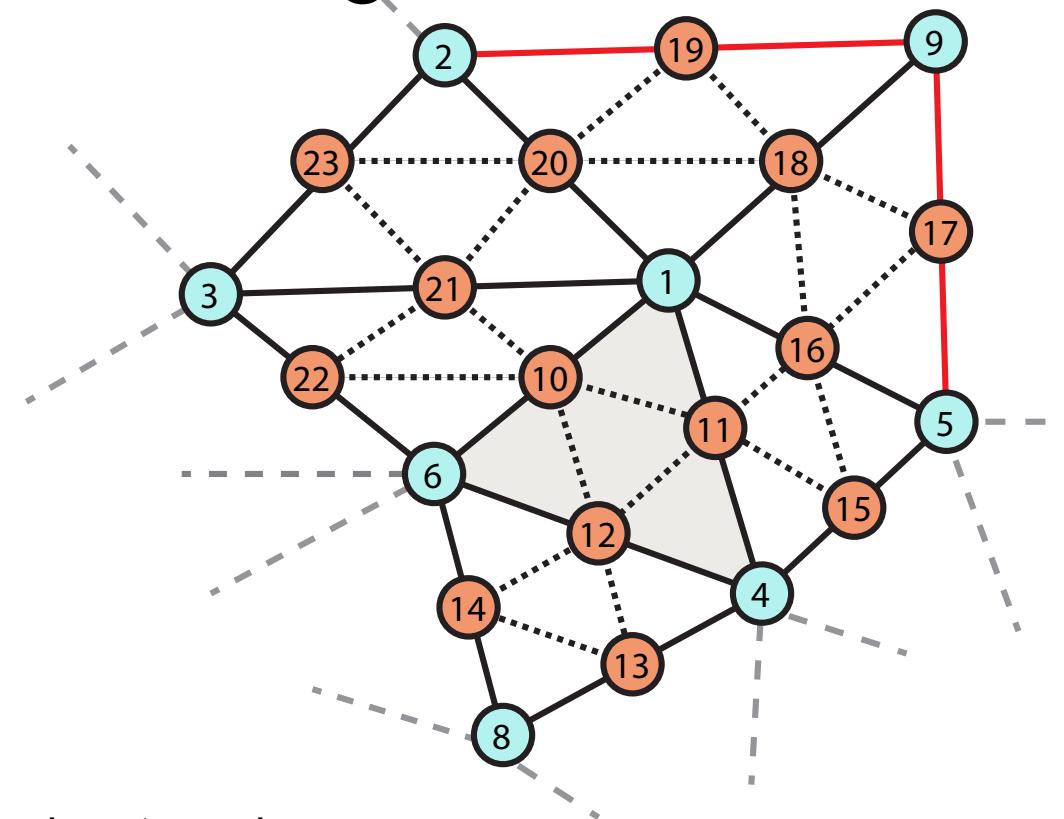
$$p'_1 = (1 - nB) p_1 + B(p_2 + p_9 + p_5 + p_4 + p_6 + p_3)$$

$$B = \begin{cases} \frac{3}{8n}, & n > 3 \\ \frac{3}{16}, & n = 3 \end{cases}$$



# Assignment 2: Loop Subdivision

- Finally, split all input triangles into four: remove old triangle, insert 4 new triangles



Vertex from input mesh

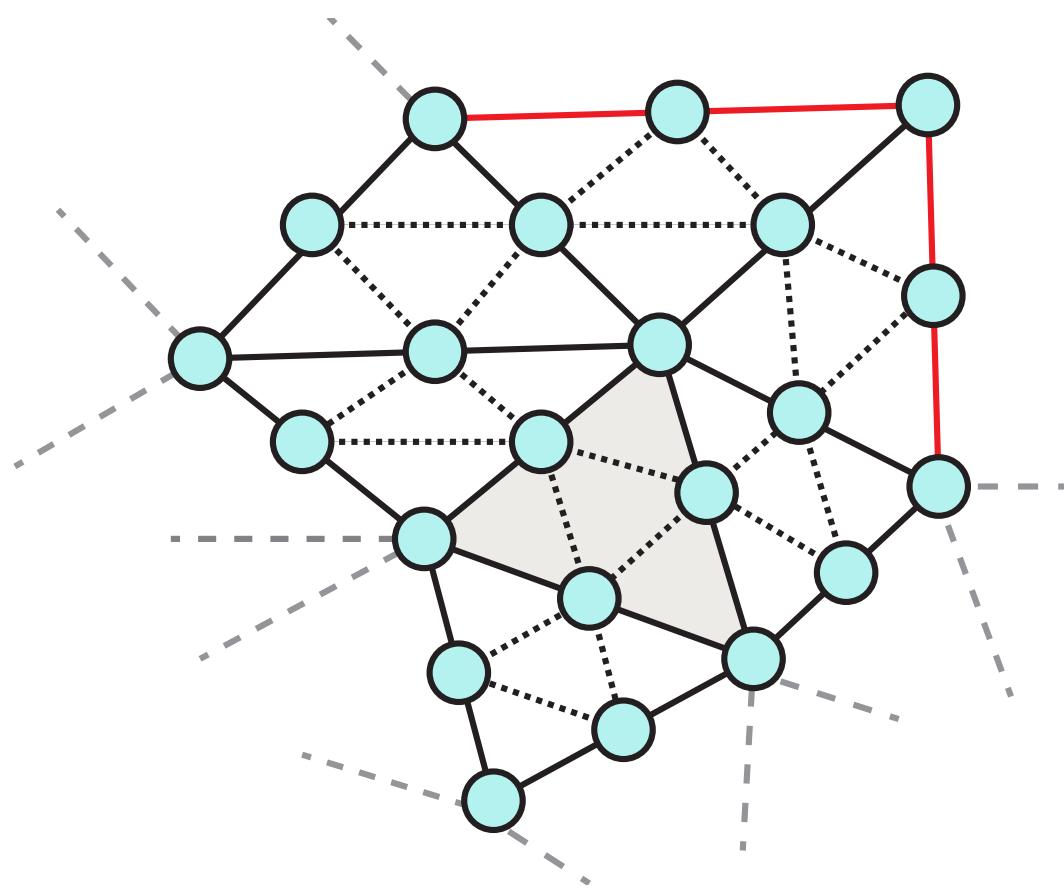


Newly-introduced vertex

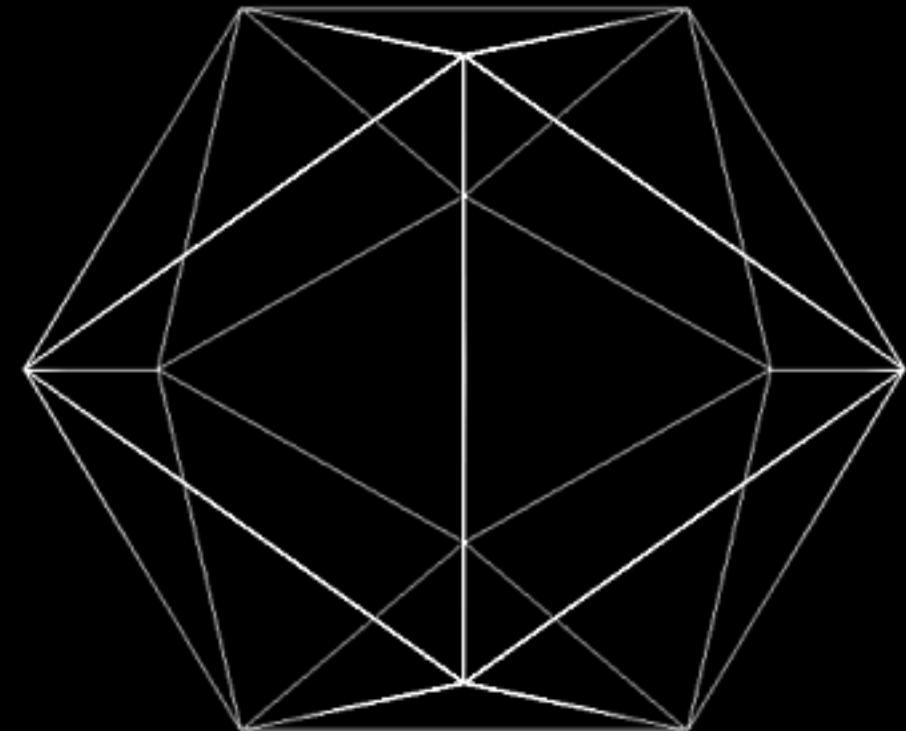
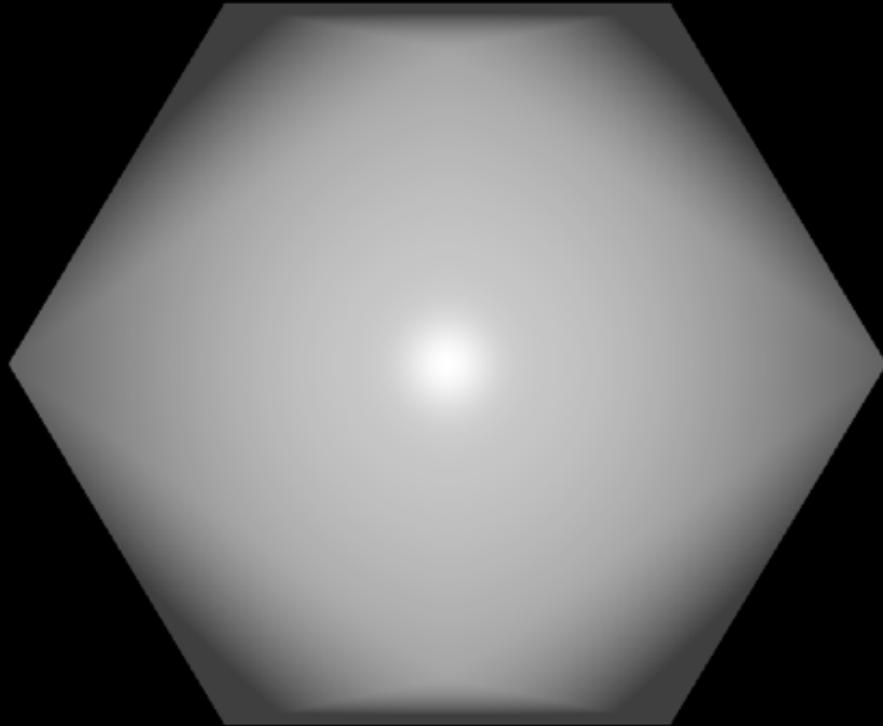
# Assignment 2: Loop Subdivision

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- This becomes the new base mesh for next round

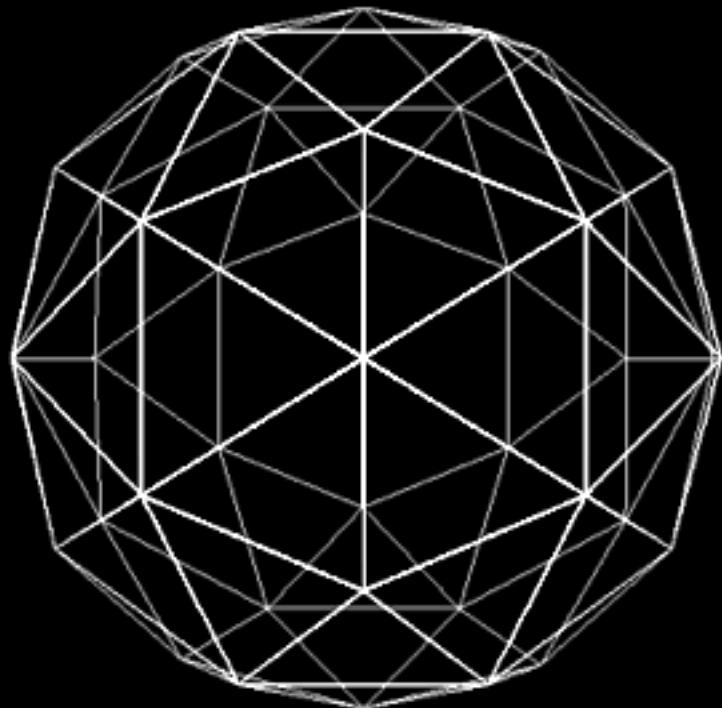
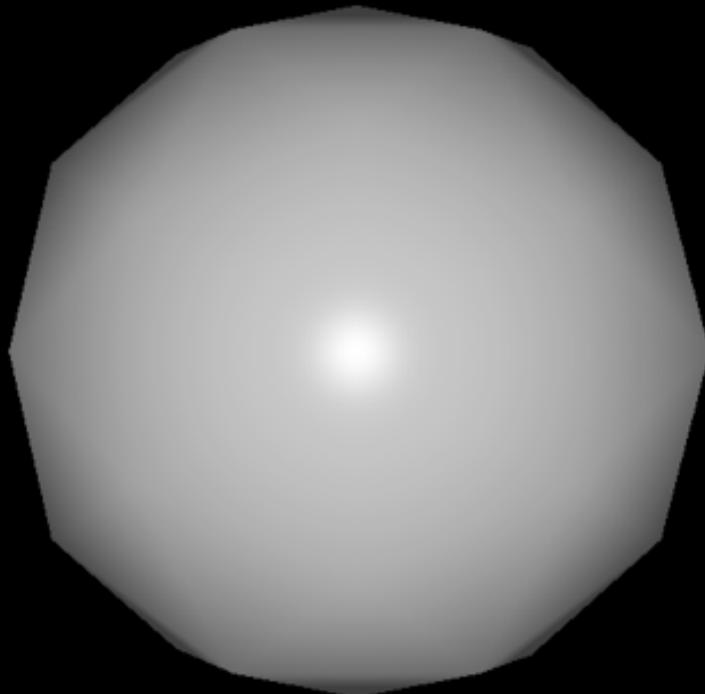


# Assignment 2: Loop Subdivision



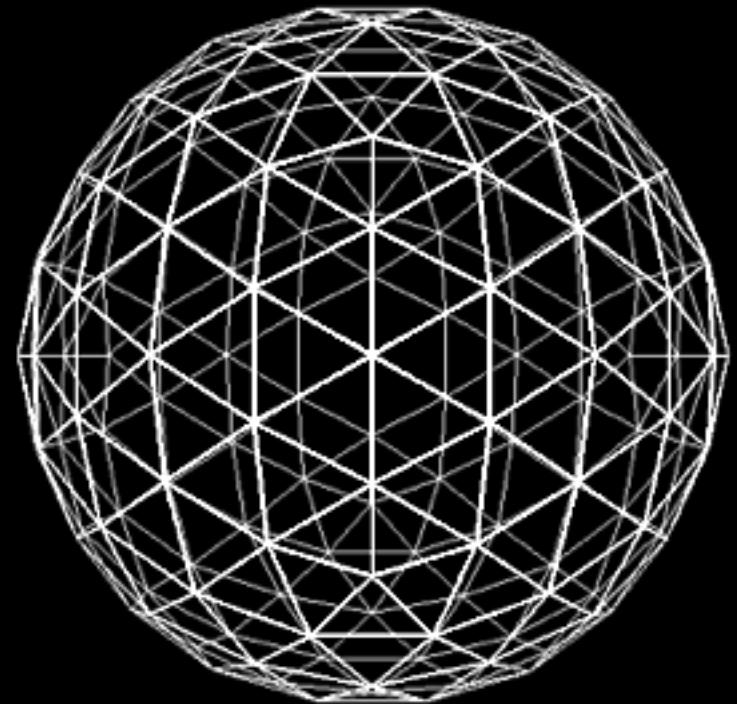
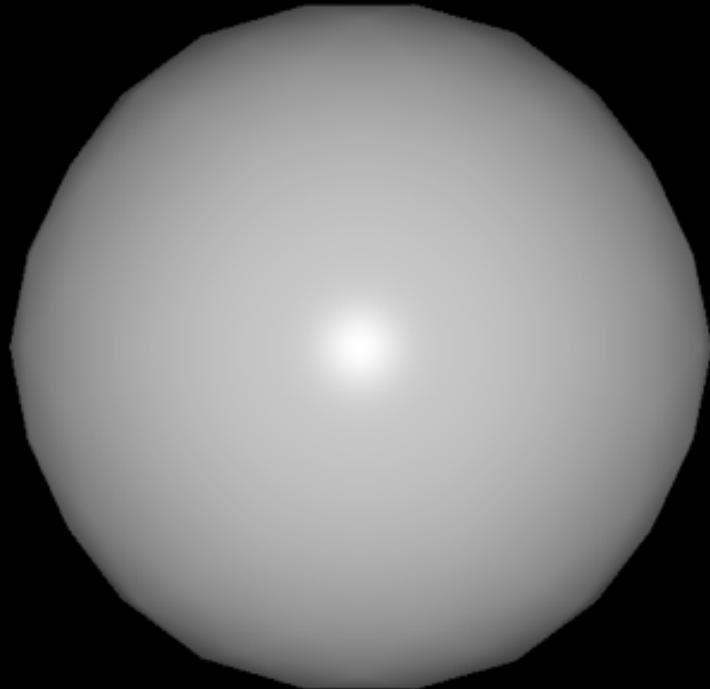
Input mesh

# Assignment 2: Loop Subdivision



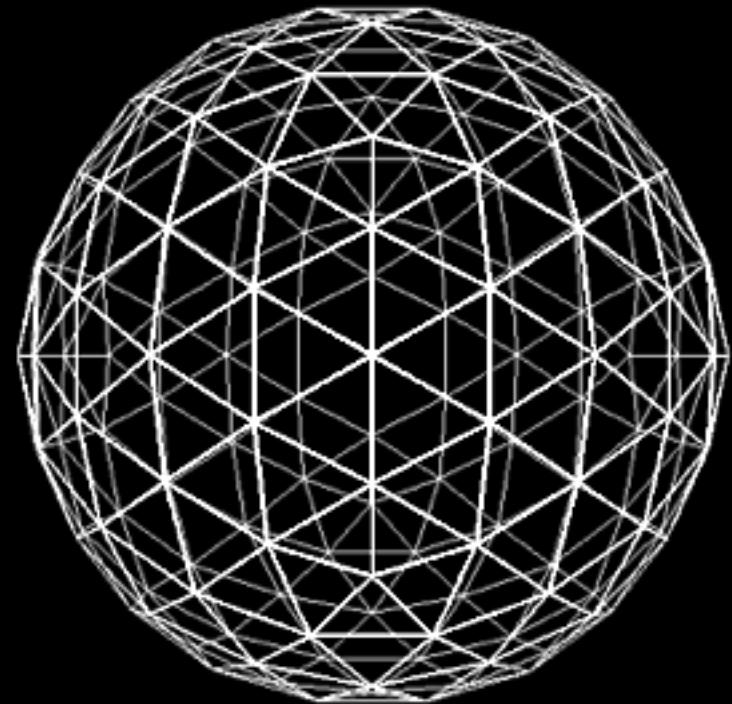
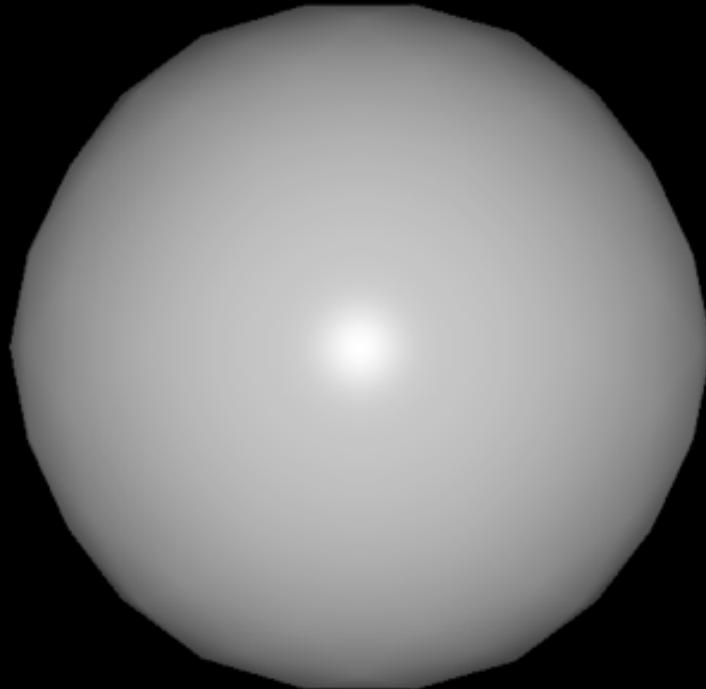
1st level of subdivision

# Assignment 2: Loop Subdivision



2nd level of subdivision

# Assignment 2: Loop Subdivision



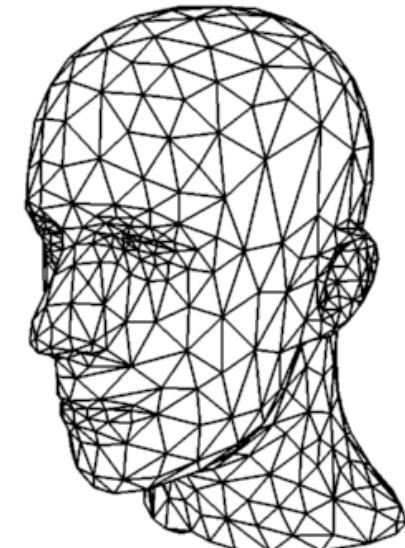
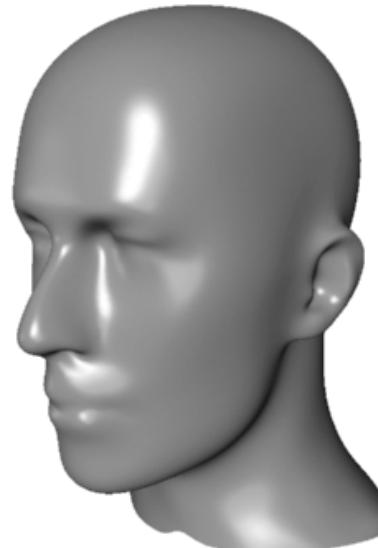
2nd level of subdivision

etc.

# Flavors of Subdivision Surfaces

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- Catmull-Clark
  - Quads and triangles
  - Generalizes bicubics to arbitrary topology!
- Loop, Butterfly
  - Triangles
- Doo-Sabin,  $\sqrt{3}$ , biquartic...
  - and a whole host of others
- Used **everywhere** in movie and game modeling!
- See <http://www.cs.nyu.edu/~dzorin/sig00course/>

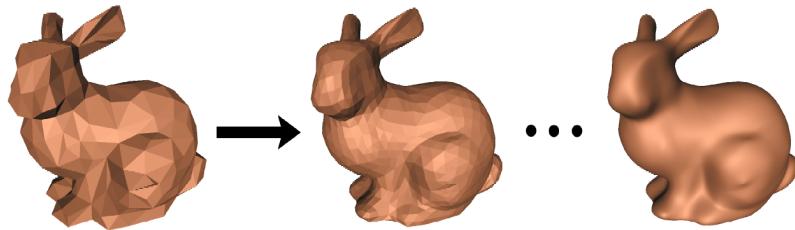


Leif Kobbelt

# Subdivision Curves and Surfaces

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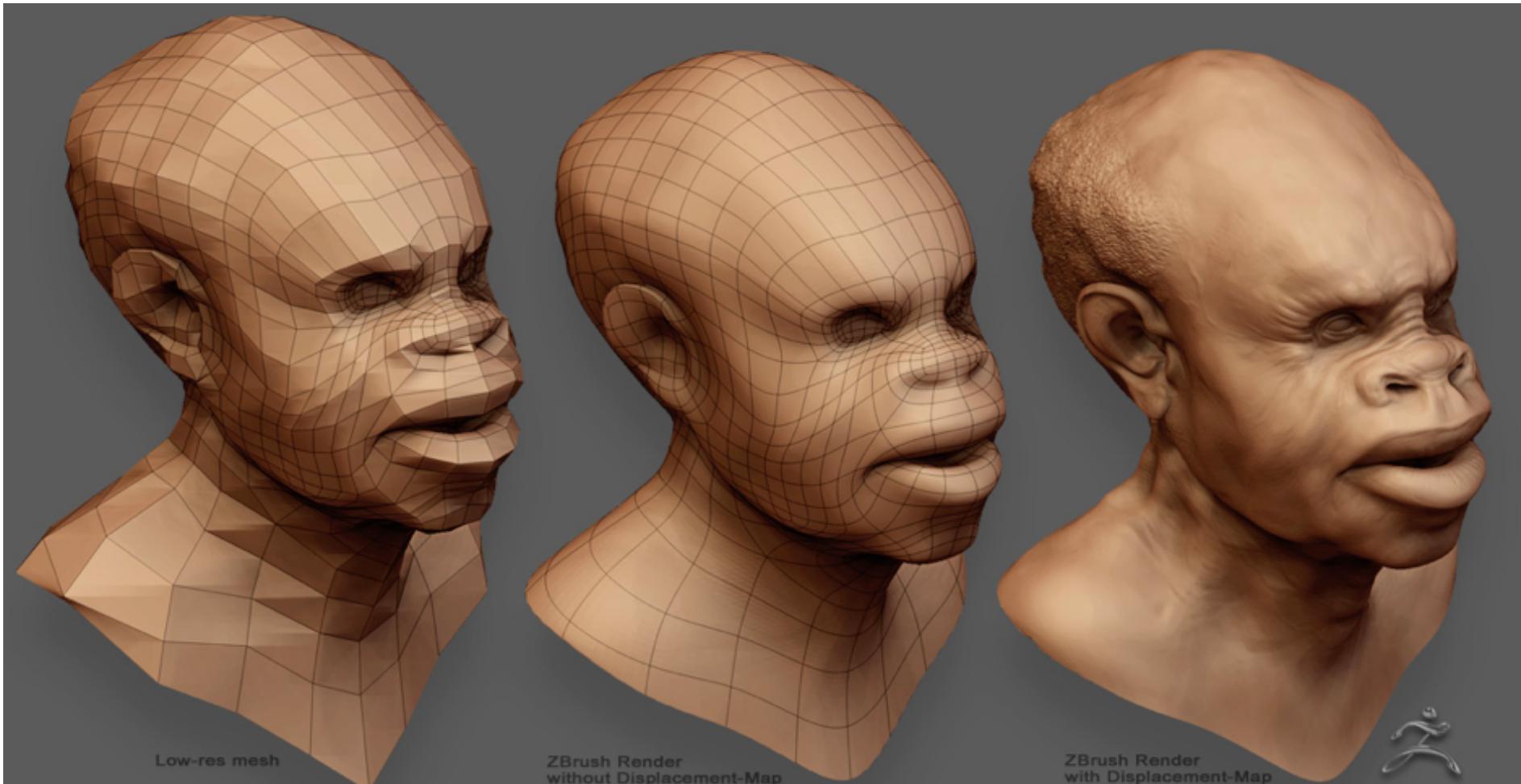
- Advantages
  - Arbitrary topology
  - Smooth at boundaries
  - Level of detail, scalable
  - Simple representation
  - Numerical stability, well-behaved meshes
  - Code simplicity
- Little disadvantage:
  - Procedural definition
  - Not parametric, not implicit
  - Tricky at special vertices



Warren et al.

# Subdivision + Displacement

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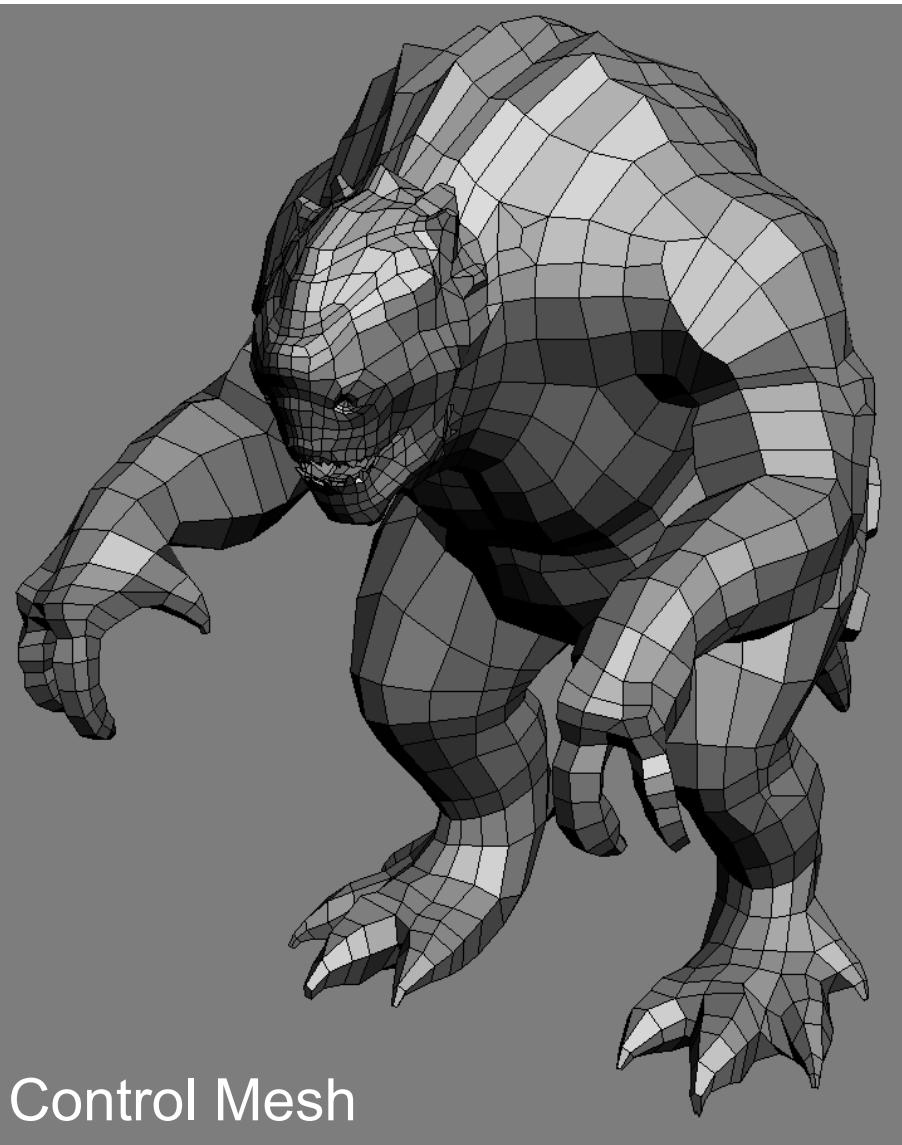


# Subdivision + Displacement

Epic Games



Final Model



Control Mesh

# ZBrush Modeling Session

- <http://www.youtube.com/watch?v=i8lIvWN8ZmQ>

