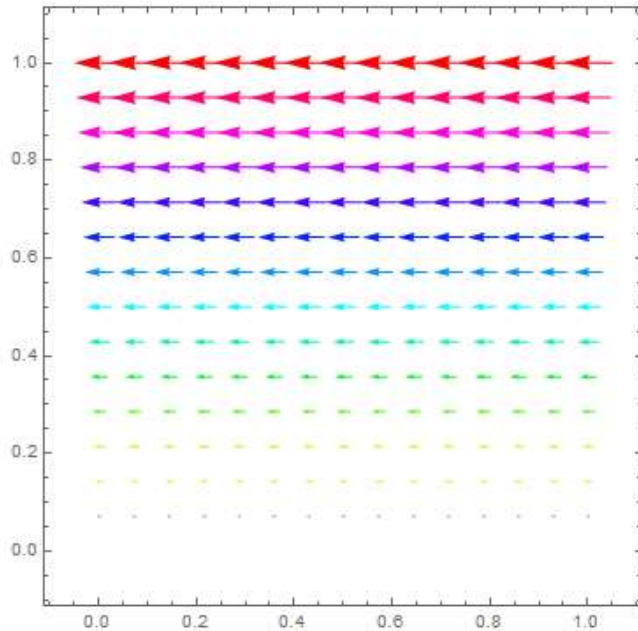
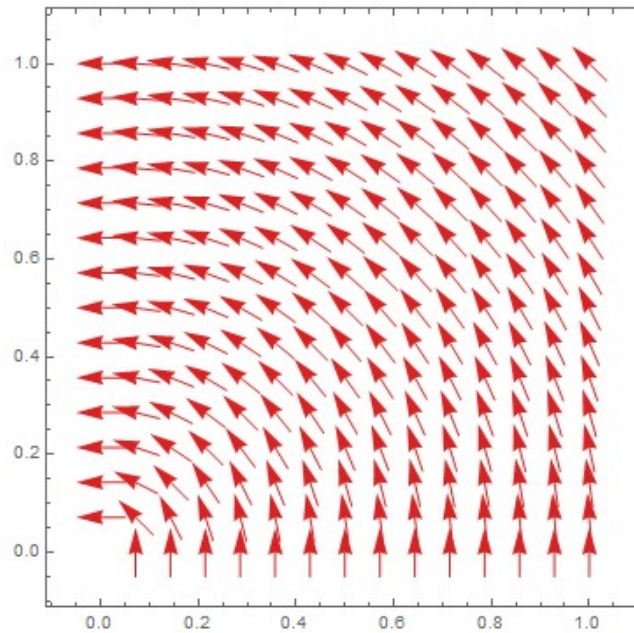


Week	Dates	Book chapters	Topic
1	March 1–4	1 and 2	Electromagnetic model, field concepts. Vector algebra, vector analysis.
2	March 8–11	3	Electrostatics. Coulomb's law, scalar potential, electric dipole, permittivity, conductors and insulators, capacitance, electrostatic energy and forces.
3	March 15–18	4 and 5	Static electric currents, Ohm's law, conductivity. Magnetostatics, Biot-Savart's law, vector potential, permeability, magnetic dipole, inductance.
4	March 22–25	6	Faraday's law, Maxwell equations for dynamic electromagnetic fields. Complex representation of time-harmonic fields.
5	March 29 – April 1	7	Plane waves in lossless and lossy media. Attenuation of waves, Wave reflection from planar interfaces. Brewster angle.
6	April 6–8	(8,9) 10	Electromagnetic radiation. Fields generated by a Hertzian dipole.

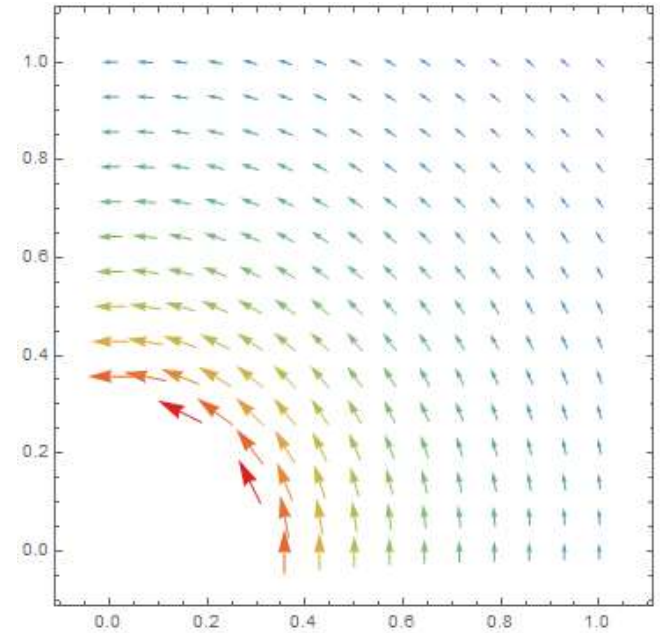
Is there curl?



$$\mathbf{F}_1 = -y \mathbf{a}_x$$

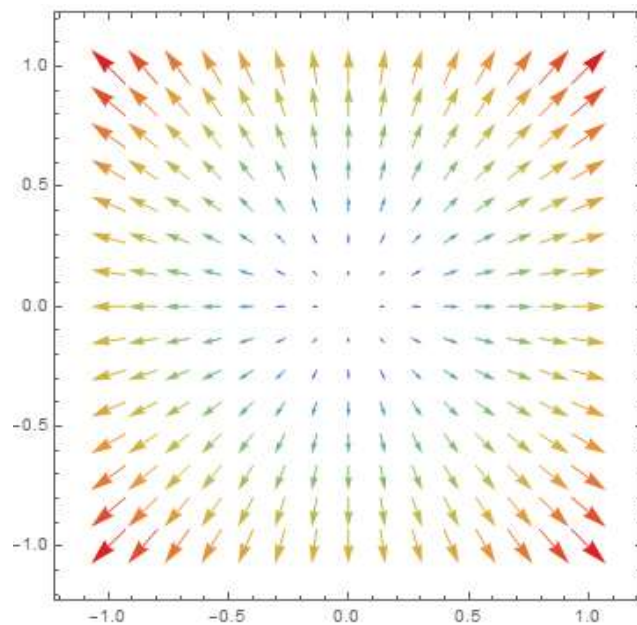


$$\mathbf{F}_2 = \mathbf{a}_\phi$$



$$\mathbf{F}_3 = \frac{\mathbf{a}_\phi}{r}$$

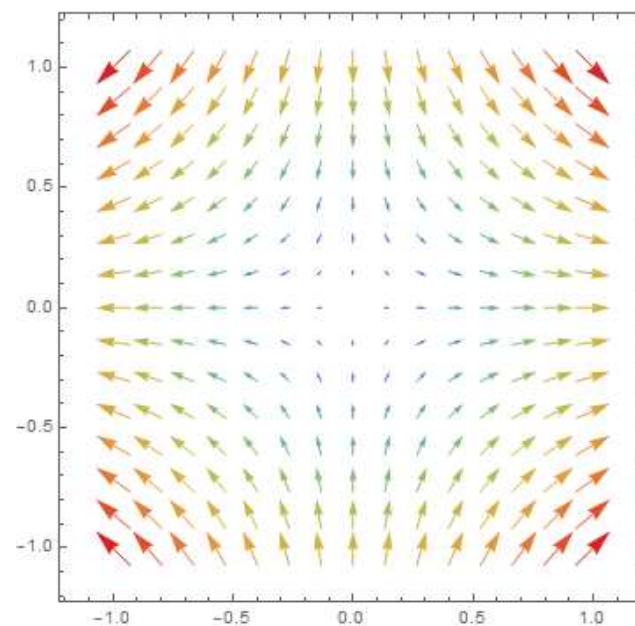
$$\mathbf{A}_1 = x\mathbf{a}_x + y\mathbf{a}_y$$



$$\nabla \cdot \mathbf{A}_1 = 2$$

$$\nabla \times \mathbf{A}_1 = 0$$

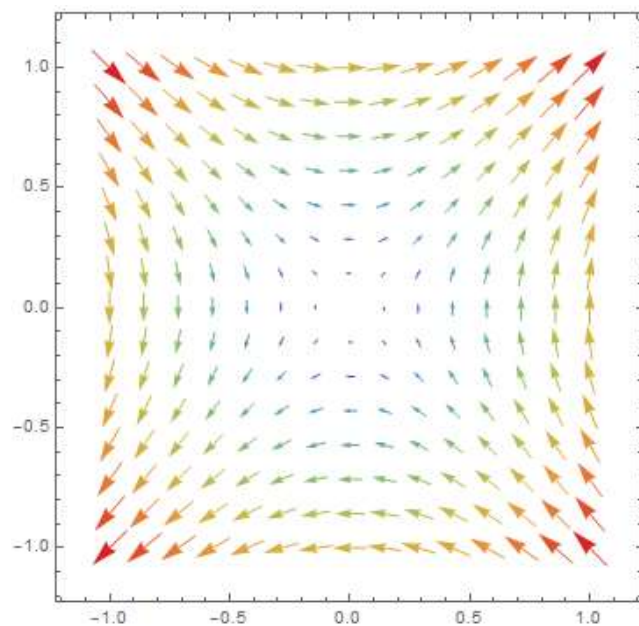
$$\mathbf{A}_2 = x\mathbf{a}_x - y\mathbf{a}_y$$



$$\nabla \cdot \mathbf{A}_2 = 0$$

$$\nabla \times \mathbf{A}_2 = 0$$

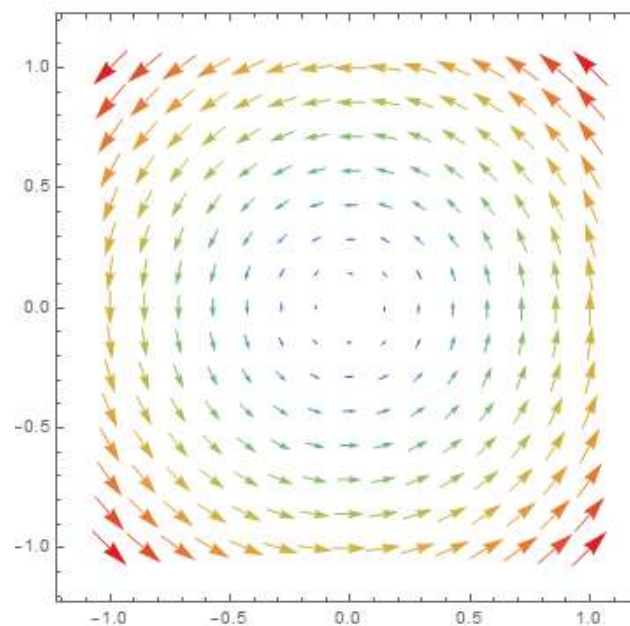
$$\mathbf{A}_3 = y \mathbf{a}_x + x \mathbf{a}_y$$



$$\nabla \cdot \mathbf{A}_3 = 0$$

$$\nabla \times \mathbf{A}_3 = 0$$

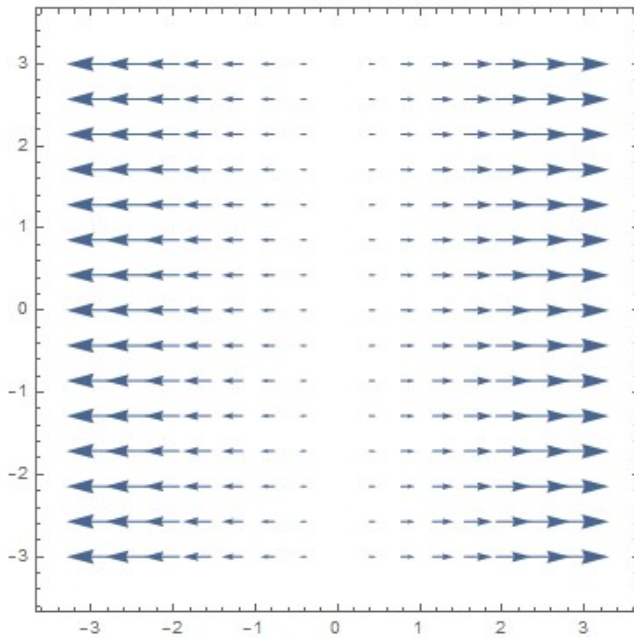
$$\mathbf{A}_4 = -y \mathbf{a}_x + x \mathbf{a}_y$$



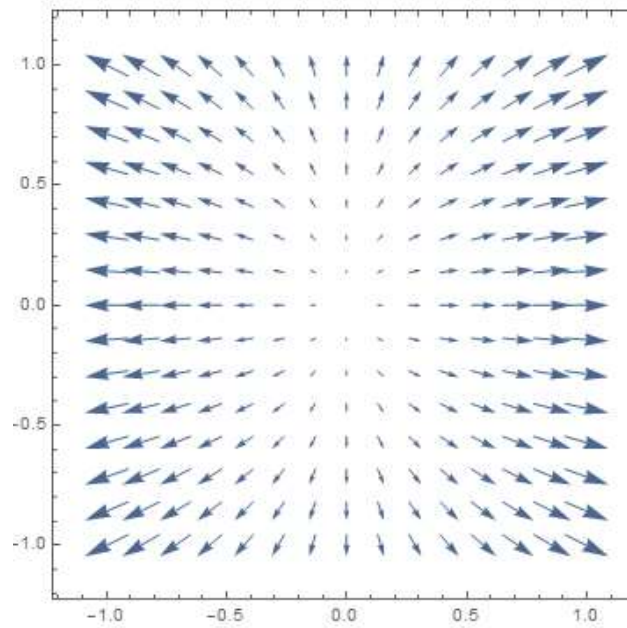
$$\nabla \cdot \mathbf{A}_4 = 0$$

$$\nabla \times \mathbf{A}_4 = 2 \mathbf{u}_z$$

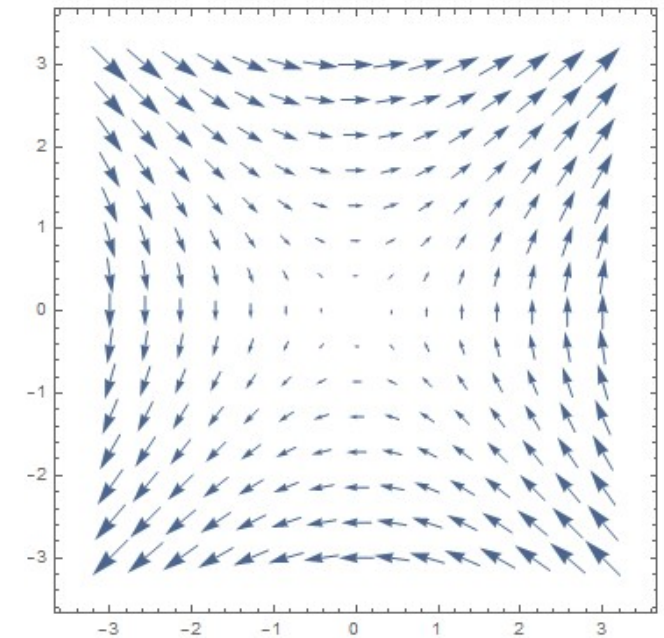
What about divergence?



$$\mathbf{D}_1 = x \mathbf{a}_x$$

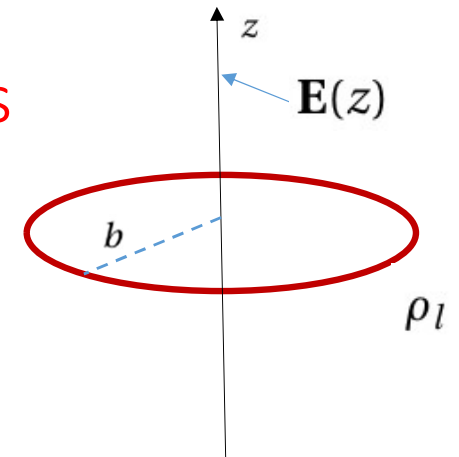
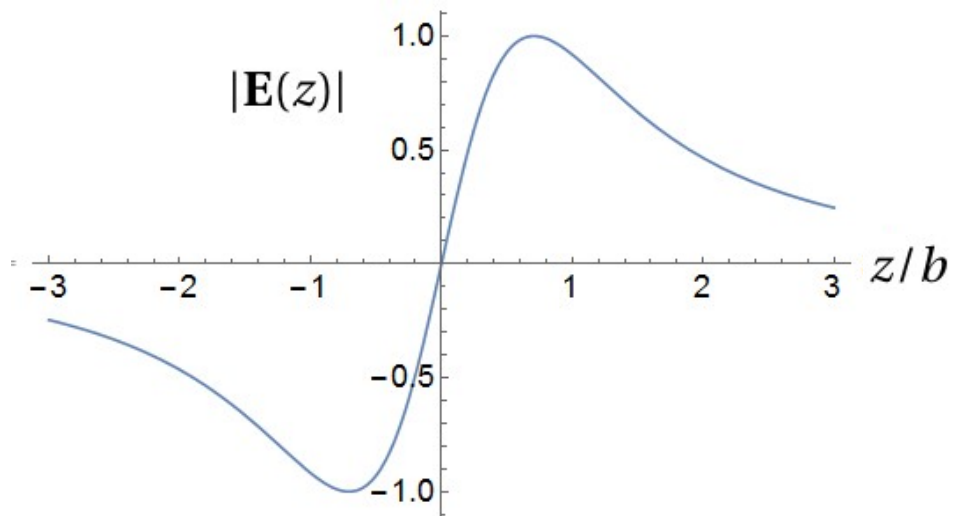


$$\mathbf{D}_2 = 2x \mathbf{a}_x + y \mathbf{a}_y$$



$$\mathbf{D}_3 = y \mathbf{a}_x + x \mathbf{a}_y$$

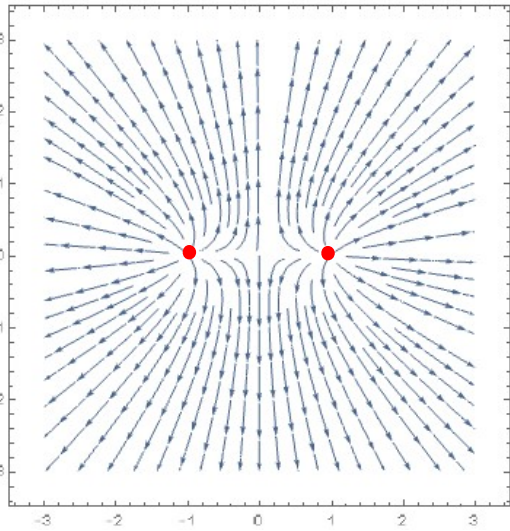
Field of a circular line charge on the symmetry axis



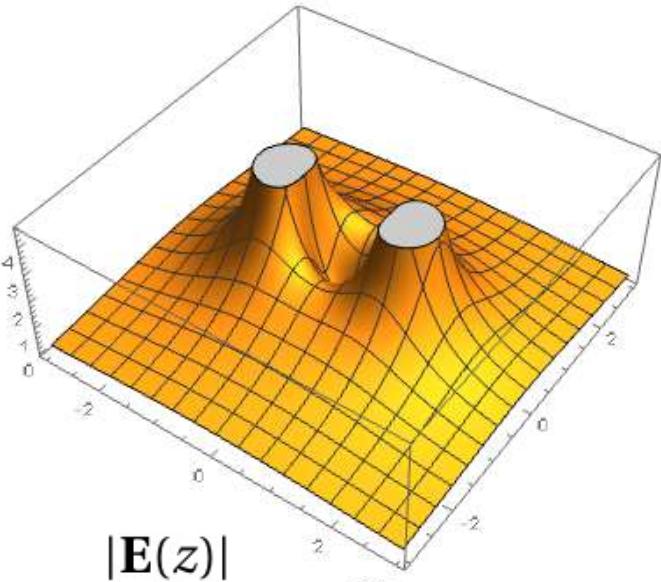
$$\mathbf{E}(z) = \mathbf{a}_z \frac{Q}{4\pi\epsilon_0} \frac{z}{(z^2 + b^2)^{3/2}}$$

$$Q = (2\pi b)\rho_l$$

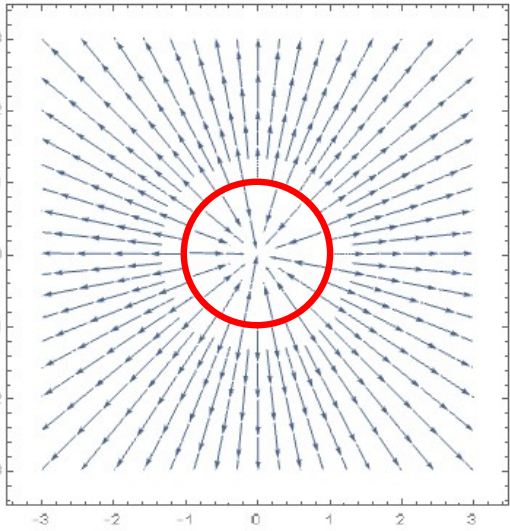
Field of circular line charge everywhere (elliptic integrals!)



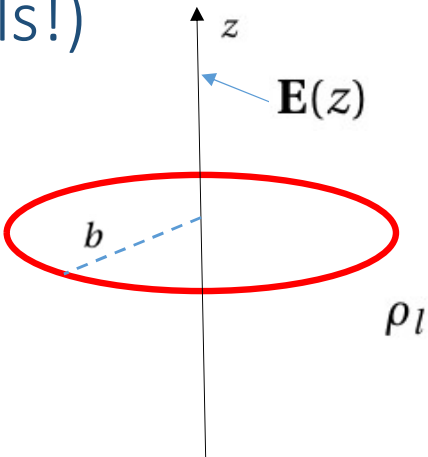
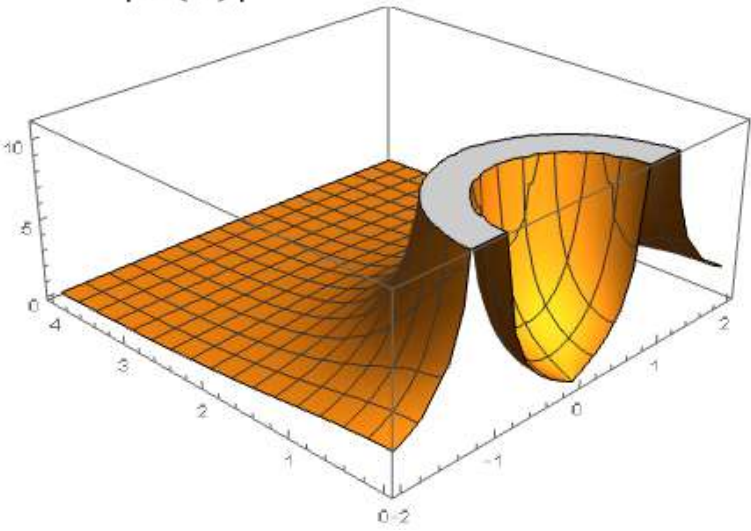
zx plane



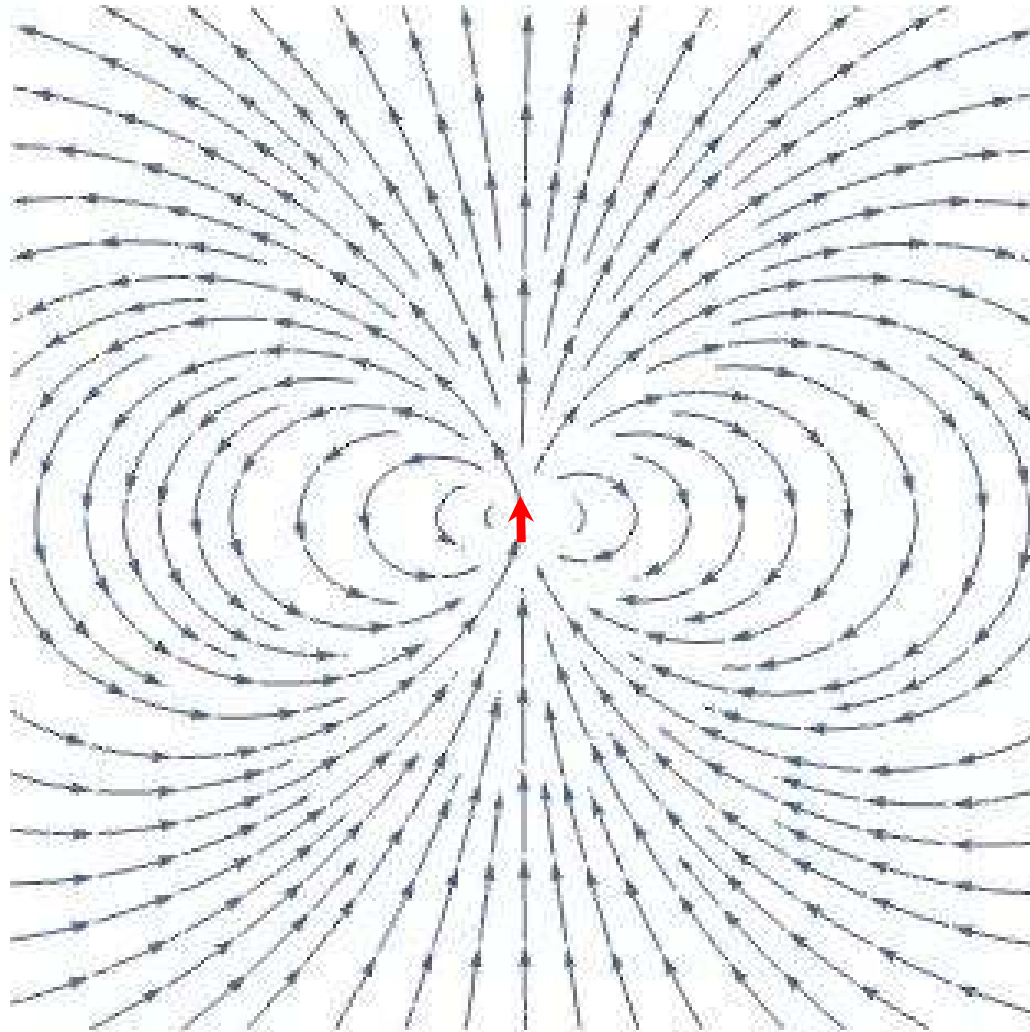
$|\mathbf{E}(z)|$



xy plane



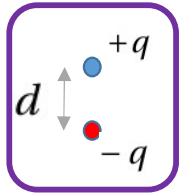
$$\mathbf{p} = \mathbf{a}_z qd = \mathbf{a}_z p$$



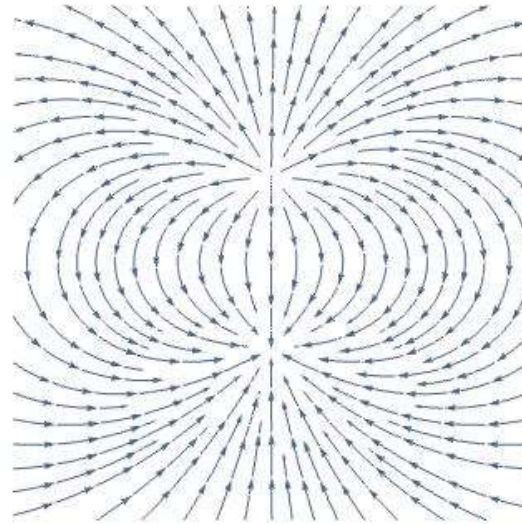
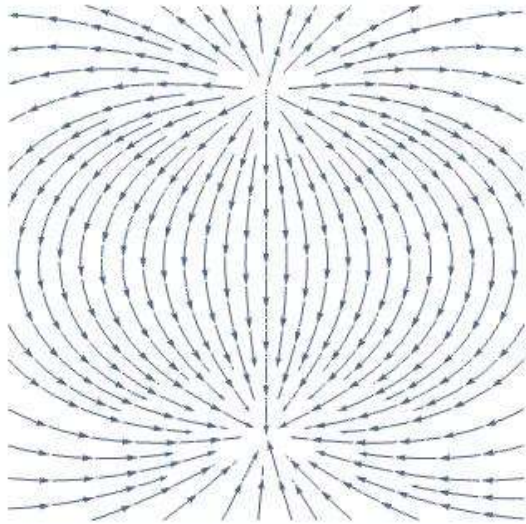
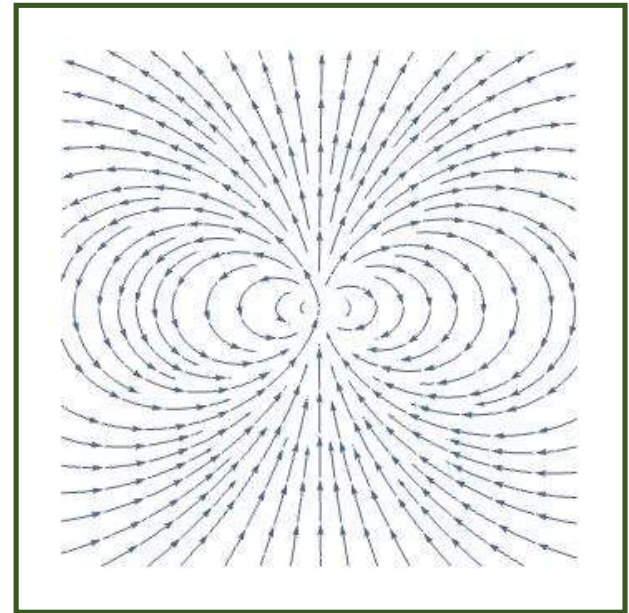
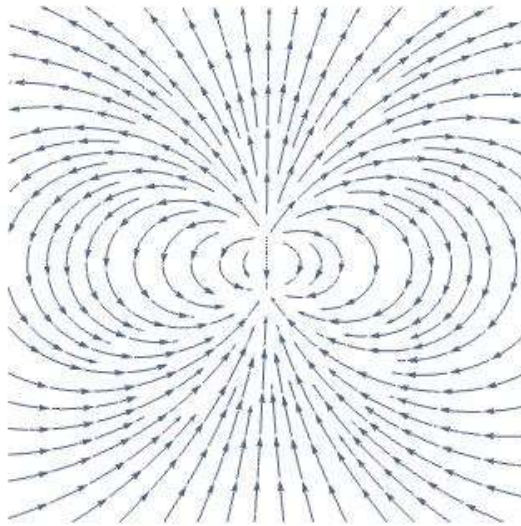
$$V(\mathbf{R}) = \frac{\mathbf{p} \cdot \mathbf{a}_R}{4\pi\epsilon_0 R^2}$$

$$\mathbf{E}(\mathbf{R}) = \frac{p}{4\pi\epsilon_0 R^3} (\mathbf{a}_R 2 \cos \theta + \mathbf{a}_\theta \sin \theta)$$

Two point charges
or a dipole?



\uparrow
 $\mathbf{p} = \mathbf{a}_z qd$



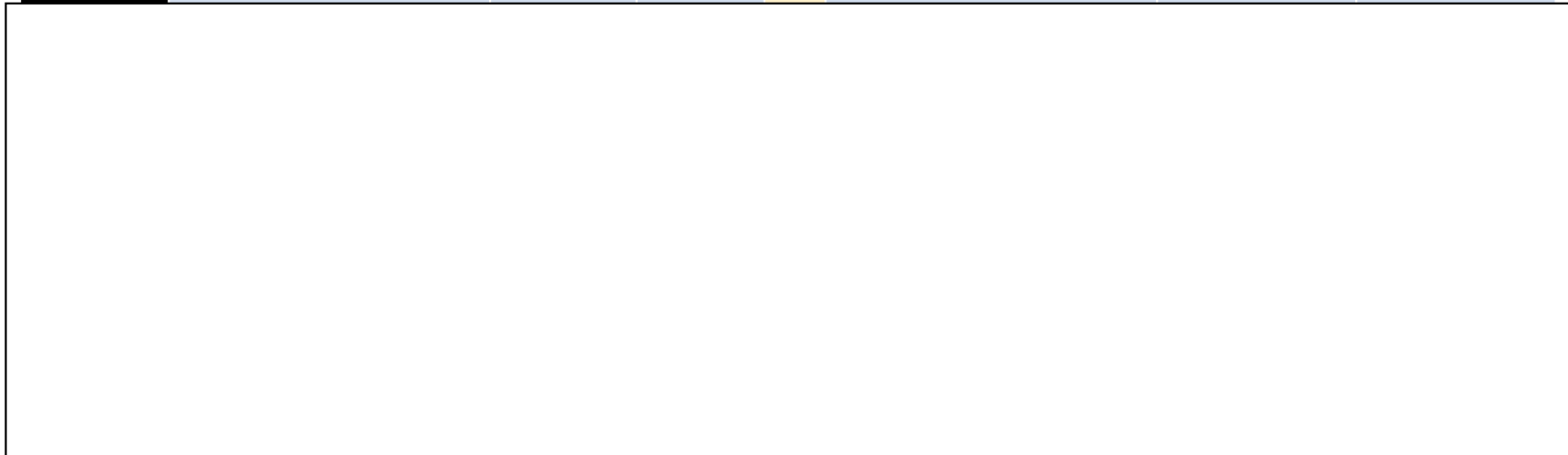
About the accuracy of the Taylor series

x	$\frac{1}{1+x}$	$1-x$	error		$\sqrt{1+x}$	$1+\frac{x}{2}$	error
-----	-----------------	-------	-------	--	--------------	-----------------	-------



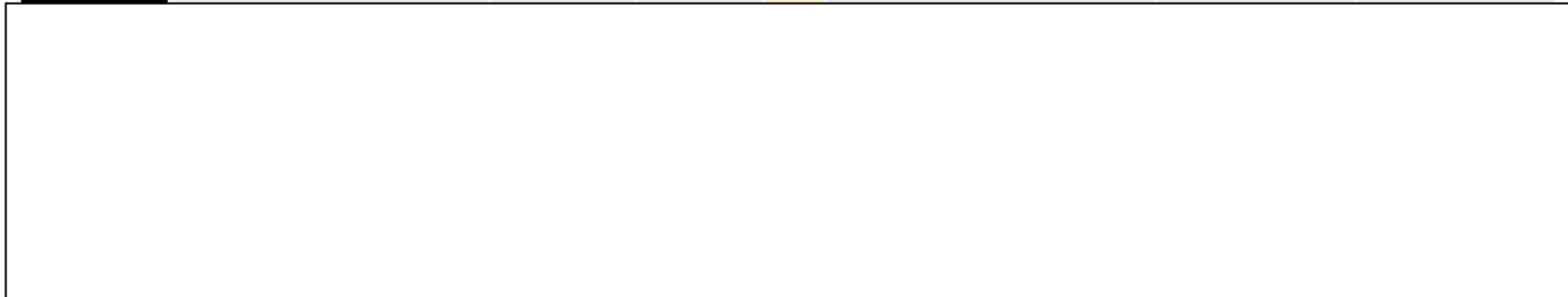
About the accuracy of the Taylor series

x	$\frac{1}{1+x}$	$1-x$	error		$\sqrt{1+x}$	$1+\frac{x}{2}$	error
0,1	0,90909090909	0,9	1 %		1,0488088482	1,05	0,114 %



About the accuracy of the Taylor series

x	$\frac{1}{1+x}$	$1-x$	error		$\sqrt{1+x}$	$1+\frac{x}{2}$	error
0,1	0,90909090909	0,9	1 %		1,0488088482	1,05	0,114 %
0,01	0,99009900990	0,99	10^{-4}		1,0049875621	1,005	$1,24 \cdot 10^{-5}$



About the accuracy of the Taylor series

x	$\frac{1}{1+x}$	$1-x$	error		$\sqrt{1+x}$	$1+\frac{x}{2}$	error
0,1	0,90909090909	0,9	1 %		1,0488088482	1,05	0,114 %
0,01	0,99009900990	0,99	10^{-4}		1,0049875621	1,005	$1,24 \cdot 10^{-5}$
0,001	0,99900099900	0,999	10^{-6}		1,0004998751	1,0005	$1.25 \cdot 10^{-7}$

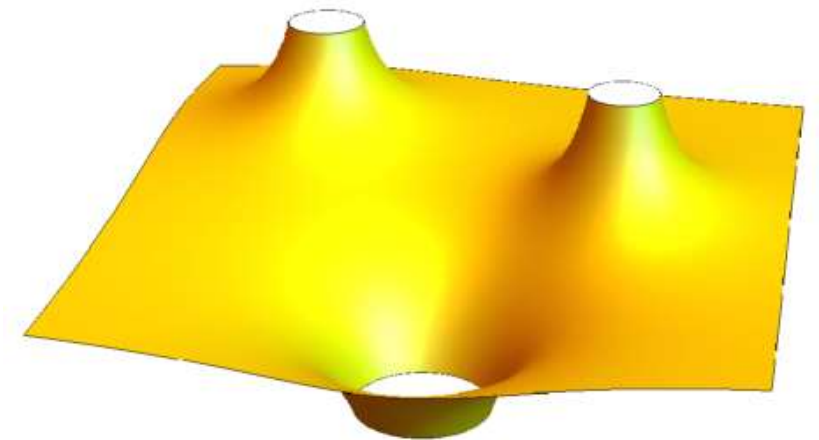
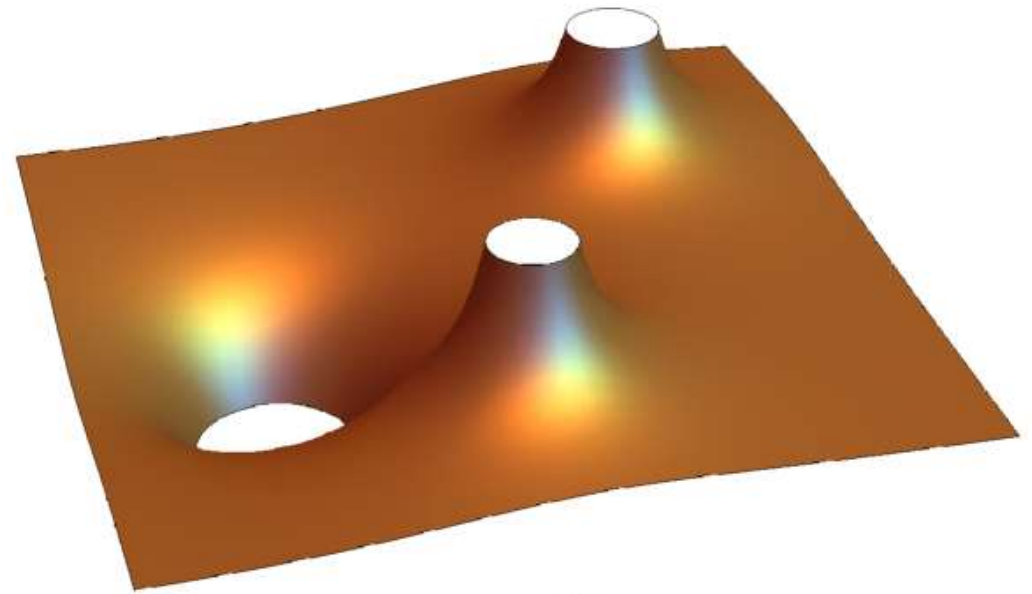
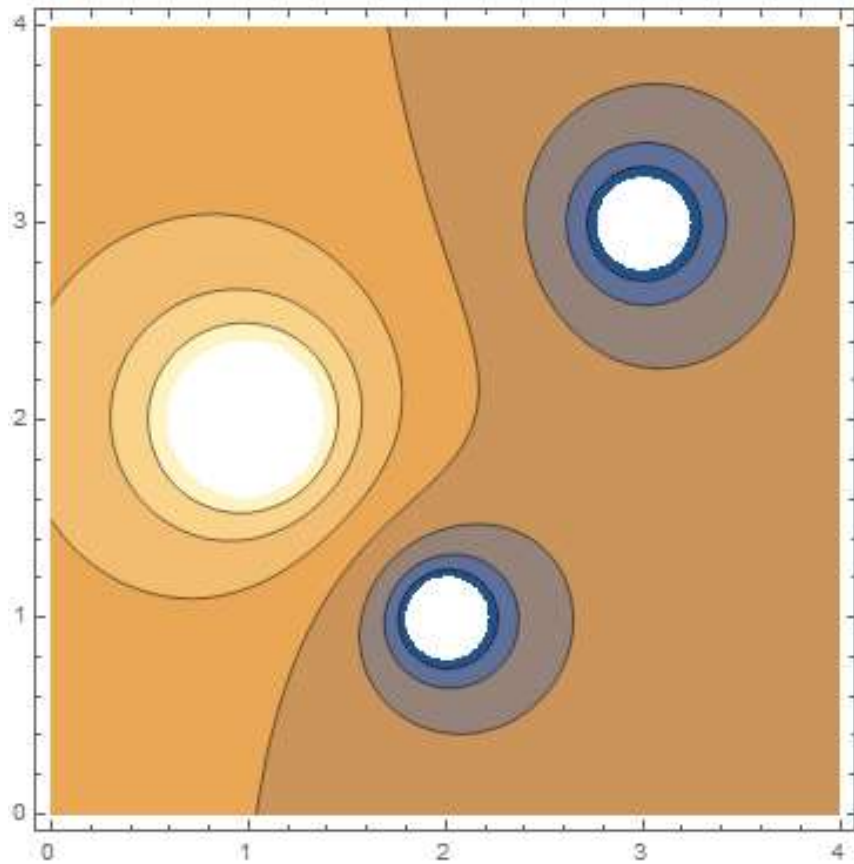
--

About the accuracy of the Taylor series

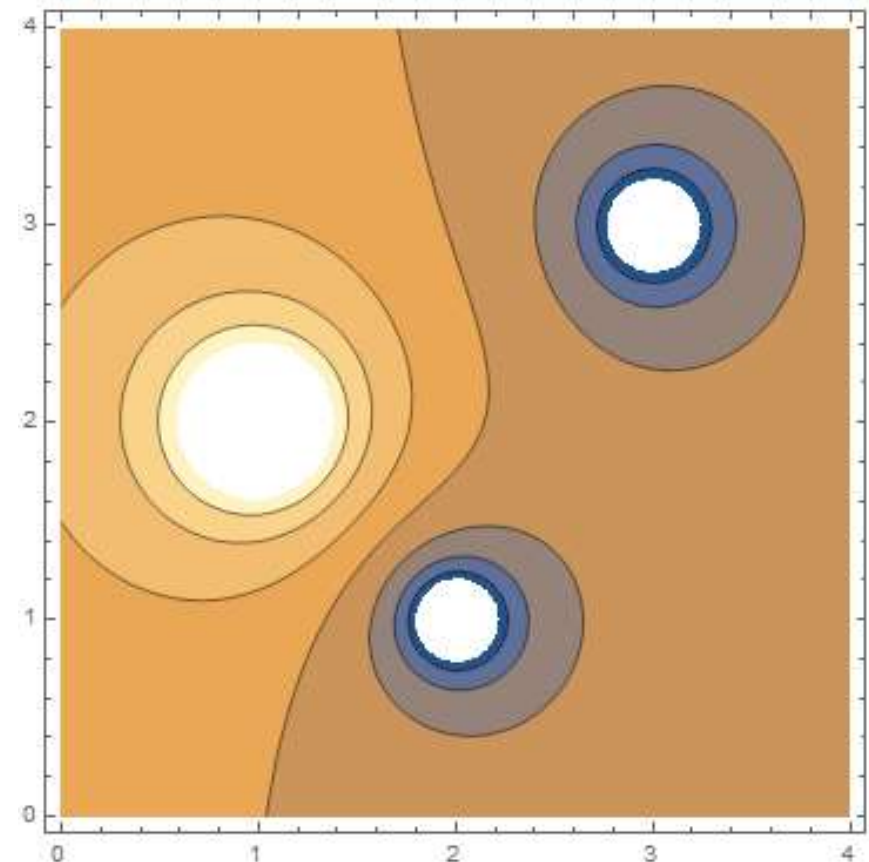
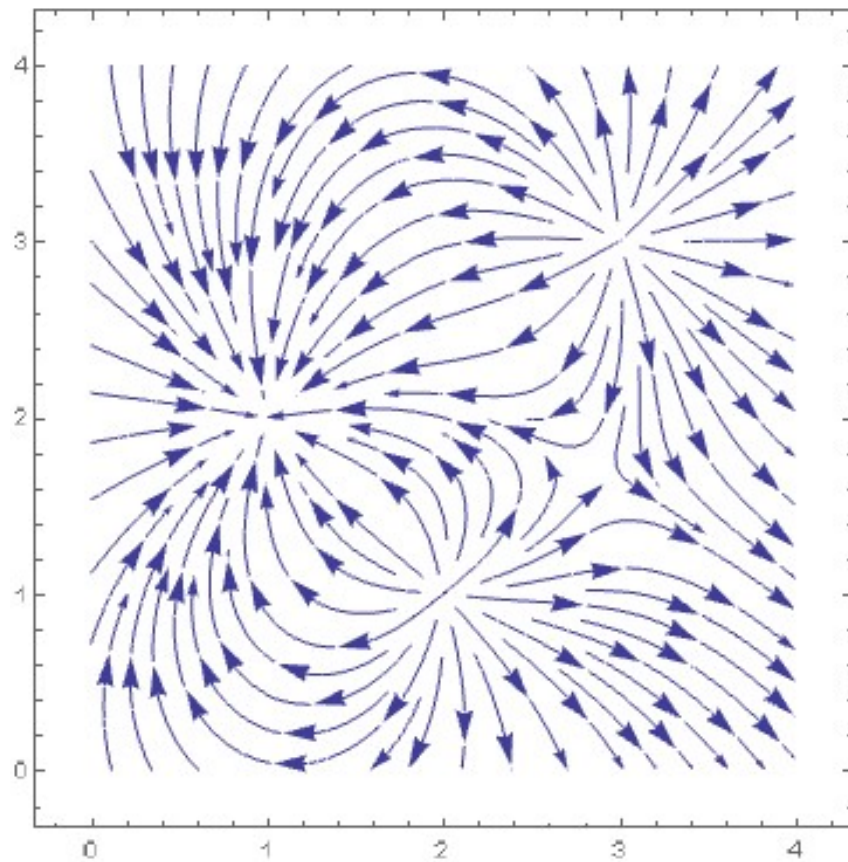
x	$\frac{1}{1+x}$	$1-x$	error		$\sqrt{1+x}$	$1+\frac{x}{2}$	error
0,1	0,90909090909	0,9	1 %		1,0488088482	1,05	0,114 %
0,01	0,99009900990	0,99	10^{-4}		1,0049875621	1,005	$1,24 \cdot 10^{-5}$
0,001	0,99900099900	0,999	10^{-6}		1,0004998751	1,0005	$1.25 \cdot 10^{-7}$
0,0001	0,999900009999	0,9999	10^{-8}		1,0000499988	1,00005	$1.25 \cdot 10^{-9}$

About the accuracy of the Taylor series

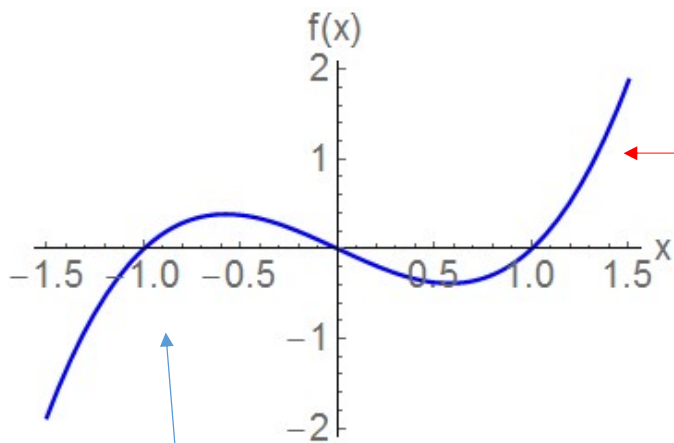
x	$\frac{1}{1+x}$	$1-x$	error		$\sqrt{1+x}$	$1+\frac{x}{2}$	error
0,1	0,90909090909	0,9	1 %		1,0488088482	1,05	0,114 %
0,01	0,99009900990	0,99	10^{-4}		1,0049875621	1,005	$1,24 \cdot 10^{-5}$
0,001	0,99900099900	0,999	10^{-6}		1,0004998751	1,0005	$1.25 \cdot 10^{-7}$
0,0001	0,999900009999	0,9999	10^{-8}		1,0000499988	1,00005	$1.25 \cdot 10^{-9}$



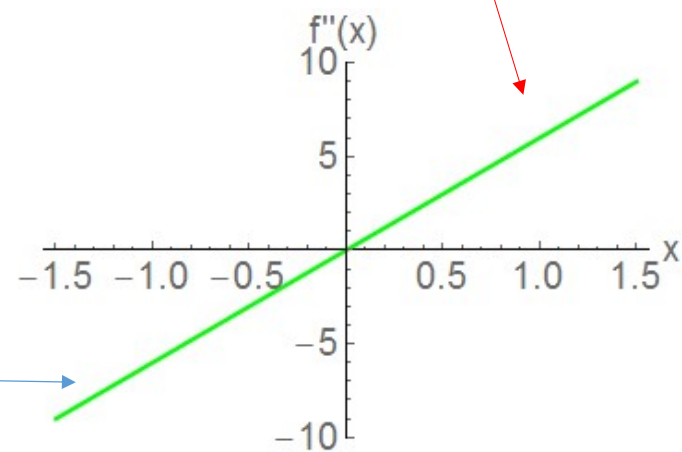
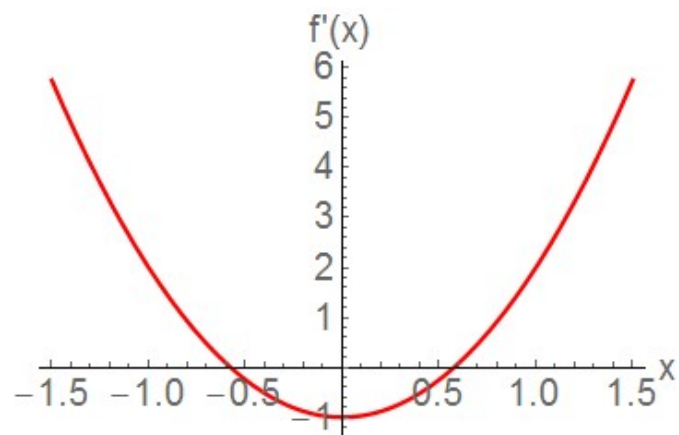
Three point charges: $+1[C]$ & $+1[C]$ & $-2[C]$



Three point charges: $+1[C]$ & $+1[C]$ & $-2[C]$



positive curvature



negative curvature

