



Aalto University  
School of Engineering

**MEC-E8006 Fatigue of Structures**

# **Lecture 9: Influence of residual stresses**

# Course contents

| Week |                      | Description  |
|------|----------------------|--|
| 43   | <b>Lecture 1-2</b>   | <b>Fatigue phenomenon and fatigue design principles</b>                                    |
|      | Assignment 1         | Fatigue Damage process, design principle and Rainflow counting – dl after week 43          |
| 44   | <b>Lecture 3-4</b>   | <b>Stress-based fatigue assessment</b>   |
|      | Assignment 2         | Fatigue life estimation using stress-based approach – dl after week 44                     |
| 45   | <b>Lecture 5-6</b>   | <b>Strain-based fatigue assessment</b>   |
|      | Assignment 3         | Fatigue crack initiation life by strain-based approach – dl after week 46                  |
| 46   | <b>Lectures 7-8</b>  | <b>Fracture mechanics -based assessment</b>  |
|      | Assignment 4         | Fatigue crack propagation life by fracture mechanics – dl after week 46                    |
| 47   | <b>Lectures 9-10</b> | <b>Fatigue assessment of welded structures and residual stress effect</b>                  |
|      | Assignment 5         | Fatigue life estimation of welded joint – dl after week 48                                 |
| 48   | <b>Lecture 11-12</b> | <b>Multiaxial fatigue and statistic of fatigue testing</b>                                 |
|      | Assignment 6         | Fatigue life estimation for multiaxial loading and statistical analysis – dl after week 48 |
| 49   | <b>Exam</b>          | <b>Course exam</b>   |
|      | Project work         | Delivery of final project (optional) – dl on week 50                                       |

# Learning outcomes

## After the lecture, you

- understand the reasons for residual stresses
- understand the effect of residual stress on fatigue strength
- can define the affecting mechanics

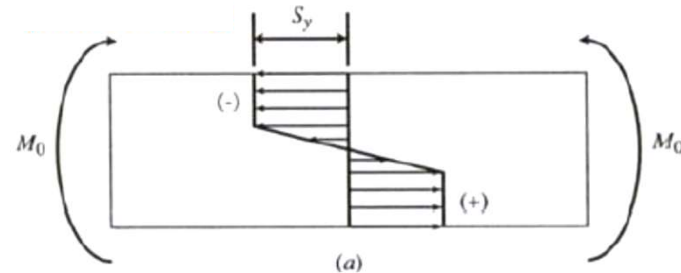
# Contents

- **Residual stress and their influence on fatigue strength**
- **Methods inducing residual stresses**
- **Residual stress in welded joints**
- **Determination of residual stress and its consideration in fatigue analysis**

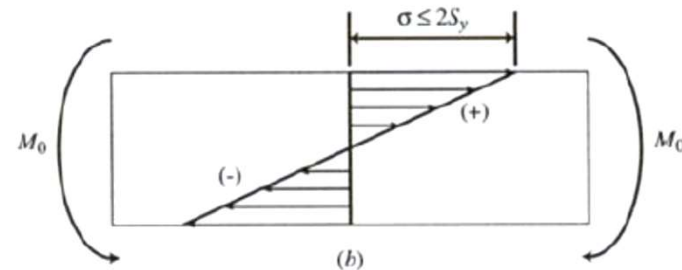
# Definition of residual stresses

## Case example: Plate inelastic bending

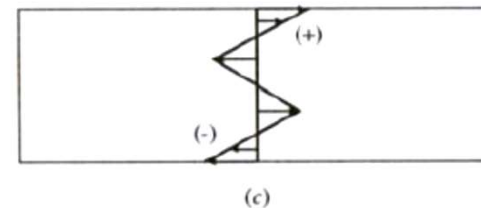
Stress distribution during inelastic bending; positive moment is applied so that upper and lower surface yield



Elastic spring back stress distribution; elastic recovery during unloading



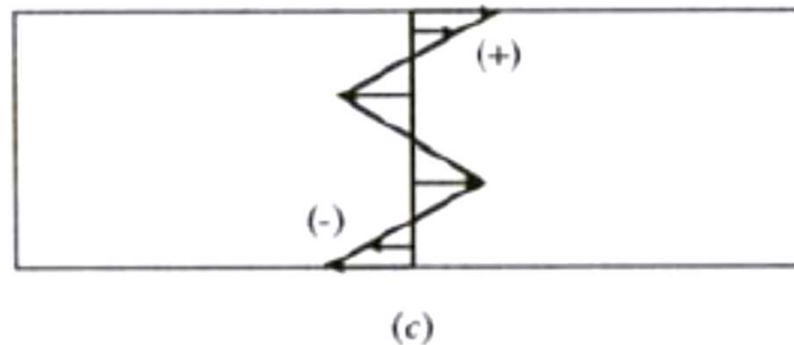
The sum of the inelastic and elastic spring back stress distribution; plate has zero external load, and self-equilibrating **residual stresses** ( $\Sigma M=0$ ,  $\Sigma F=0$ )



# Definition of residual stresses

**Residual stresses are in equilibrium within a part, without any external load**

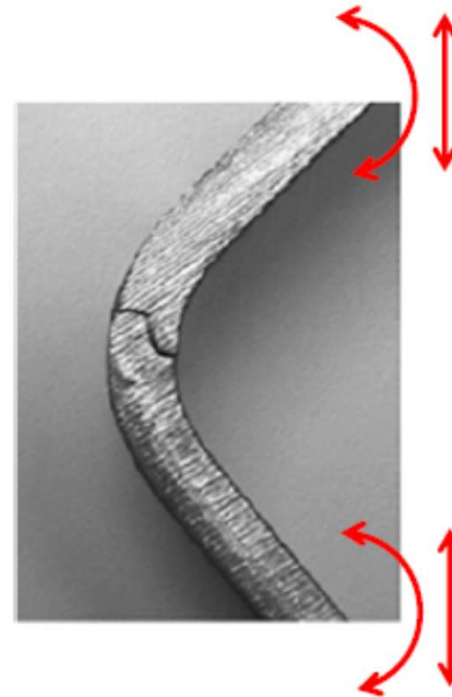
- They are called residual stresses because they remain from a previous operation
- Residual stresses exist in most manufactured parts



# Influence of residual stresses

In fatigue, residual stresses influence on

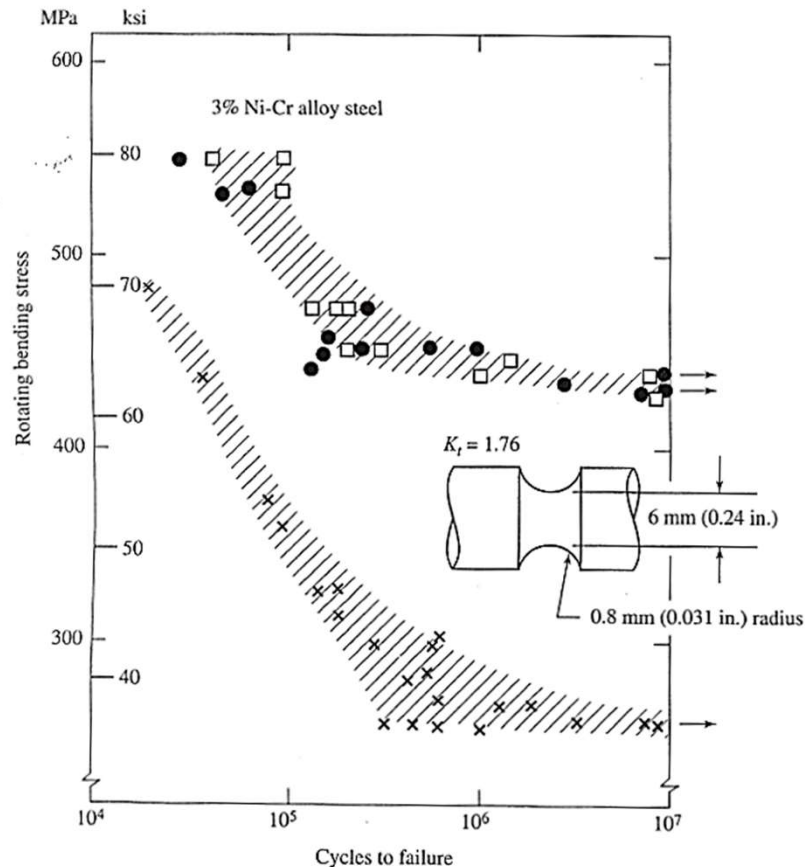
- the number of cycles needed to form a crack,
- the growth rate of cracks, and
- the direction of crack propagation



**Positive or negative**

# Influence of residual stresses

## Example: Ni-Cr alloy steel (rotating bending)



Three different surface conditions

- Smooth
- (x) Notched
- Notched shot-peened

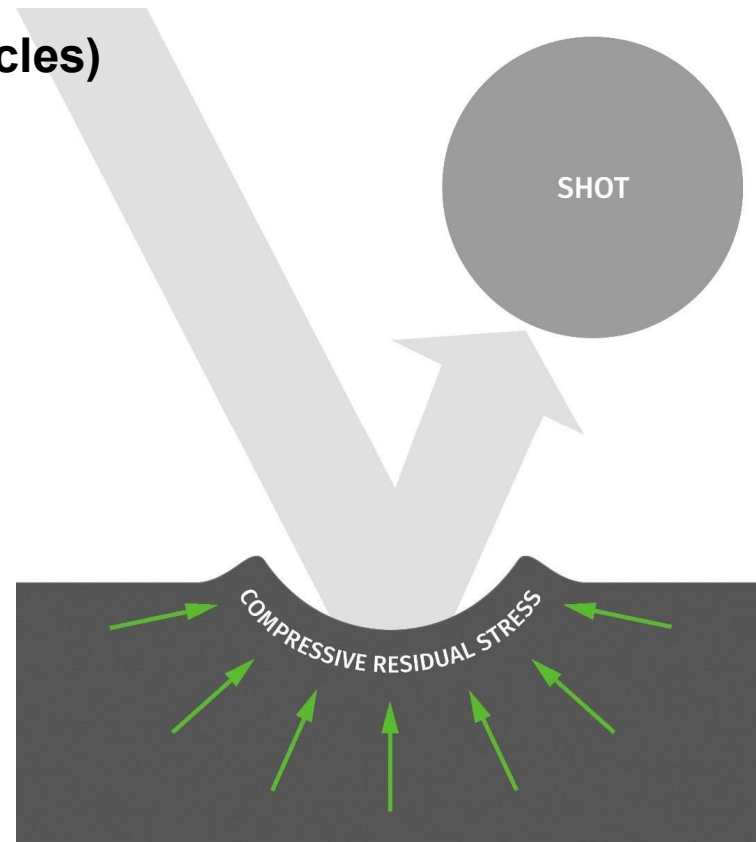
Fatigue resistance of notched shot-peened specimens is similar to that of smooth specimens

- The notch became harmless after shot-peening due to the residual compressive stresses



# Influence of residual stresses

**Shot-peening**  
**Cold working process**  
(round metallic, glass or ceramic particles)



# Methods inducing residual stresses

**Methods**, which induce residual stresses, can be divided into four main groups:

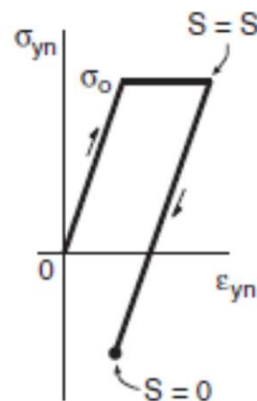
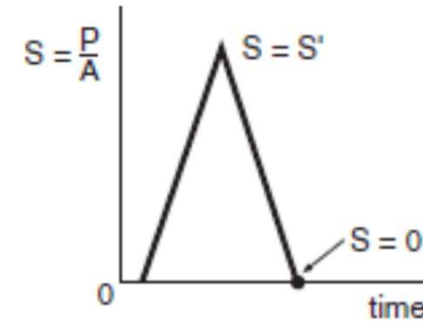
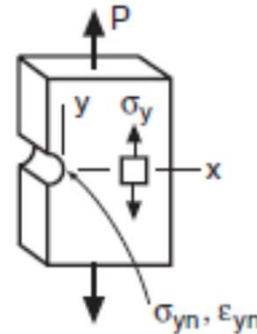
- Mechanical methods
- Thermal methods
- Plating
- Machining

# Methods inducing residual stresses

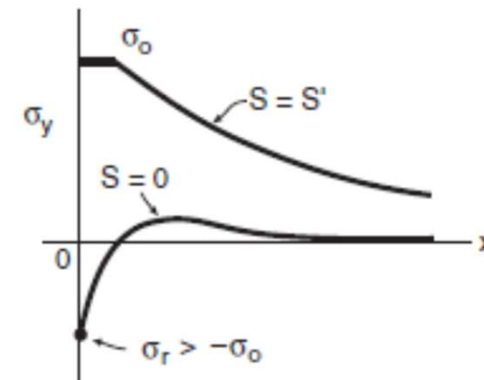
## Mechanical methods

External load produces inelastic deformation

Stress–strain behavior at the notch and residual stress distributions after loading and unloading



(a)



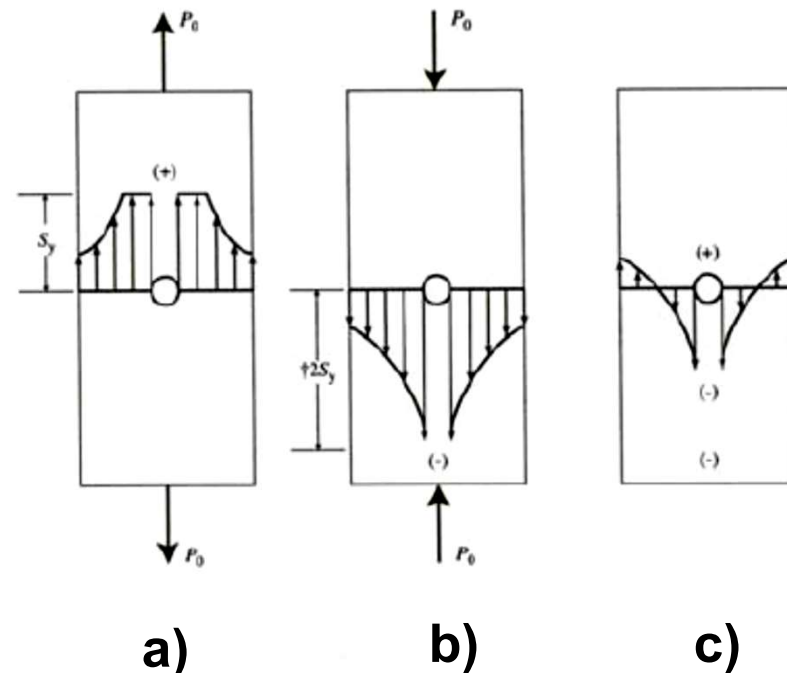
# Methods inducing residual stresses

**Stretching** (tensile overload) of the notched specimen

- Non-uniform tensile stress distribution during the inelastic loading (a)
- Elastic recover during unloading (b)
- Resultant residual stress after inelastic loading and elastic unloading (c)

Tensile overloads with notches result in residual compressive stresses at the notch

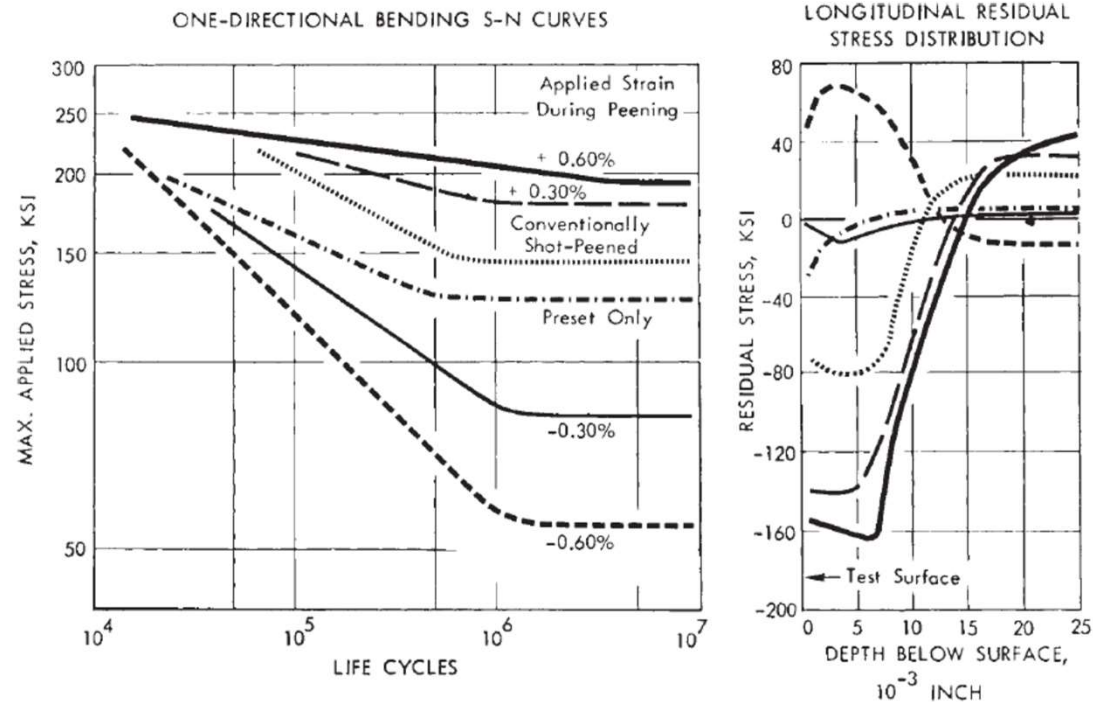
Compressive overloads with notches result in residual tensile stresses at the notch



# Methods inducing residual stresses

## Shot-peening

- Used in many parts
- The depth of the residual compressive stress ranges from about 0.025 to 0.5 mm.
- The maximum residual stress is depended on material ultimate strength

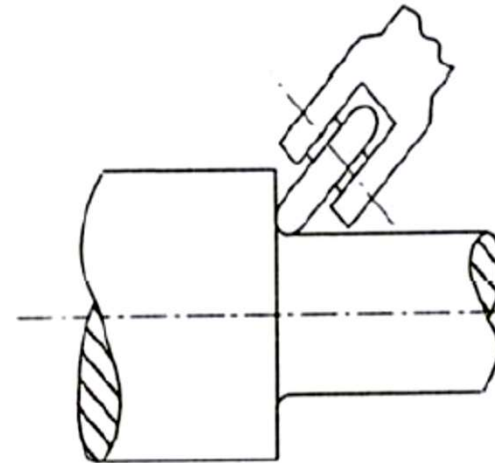


Shot peened steel leaf springs

# Methods inducing residual stresses

## Rolling

- Compressive residual stress of fillets for components such as crankshafts, axles, gear teeth, turbine blades



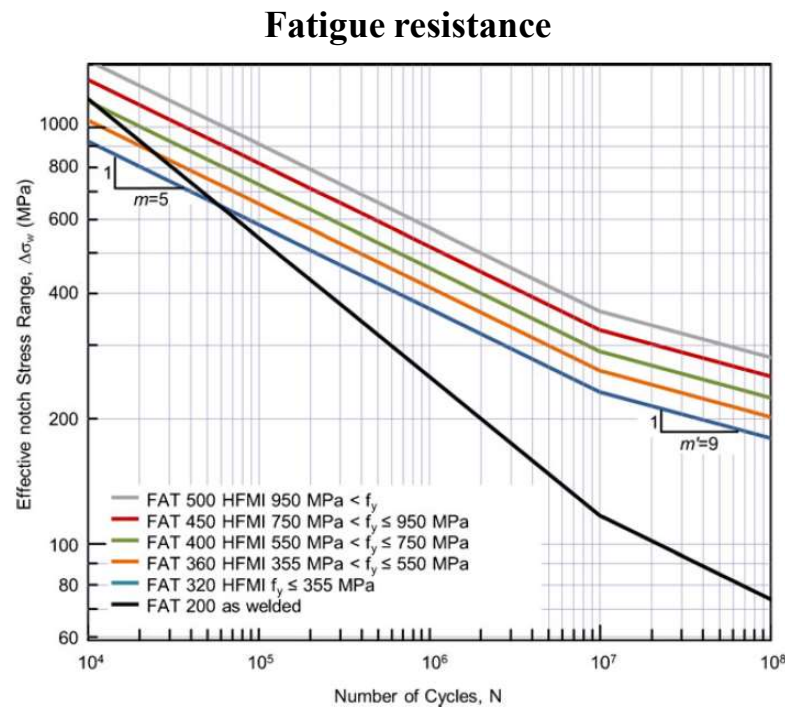
**TABLE 8.2** Fatigue Strength at  $10^5$  Cycles, 0.2 Hz, AISI 8635 Steel [6,7]

| Environment                                       | Rolled Threads<br>$S_{Nf}$ – MPa (ksi) | Cut Threads<br>$S_{Nf}$ – MPa (ksi) | % Increase<br>from Rolling |
|---|--|-------------------------------------|----------------------------|
| Air   | 510 (74)                               | 303 (44)                            | 68                         |
| 3.5% NaCl   | 414 (60)                               | 290 (42)                            | 43                         |
| H <sub>2</sub> S + CH <sub>3</sub> COOH + 5% NaCl | 317 (46)                               | <276 (40)                           | >15                        |

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# Methods inducing residual stresses

## High frequency peening of welds



(Marquis et al., 2013)

After the treatment



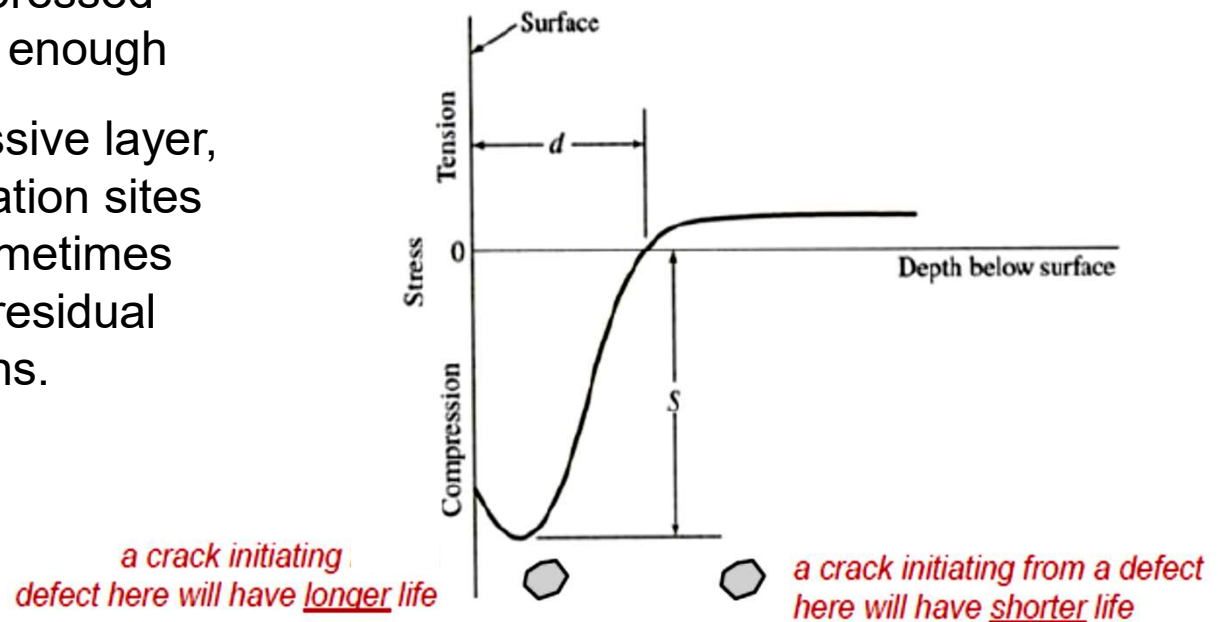
Before the treatment (As weld)



# Methods inducing residual stresses

## Mechanical methods

- Adequate depth of the compressively stressed layer is important; the compressed layer must be deep enough
- Due to the compressive layer, fatigue crack nucleation sites and growth may sometimes shift to subsurface residual tensile stress regions.

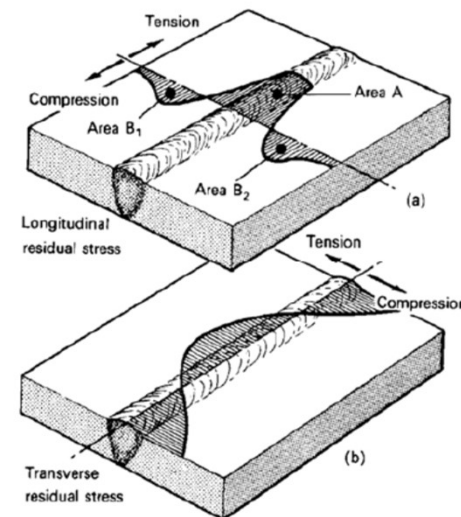




# Methods inducing residual stresses

## Thermal processes

- used in manufacturing procedures for forming parts
- includes several manufacturing processes such as casting, forging, hot-rolling, extrusion, injection molding, welding, brazing, quench and tempering, temper stress relief, flame or induction hardening, carburizing, and nitriding
- Induce a wide variety of residual stress and their effect may be beneficial or detrimental



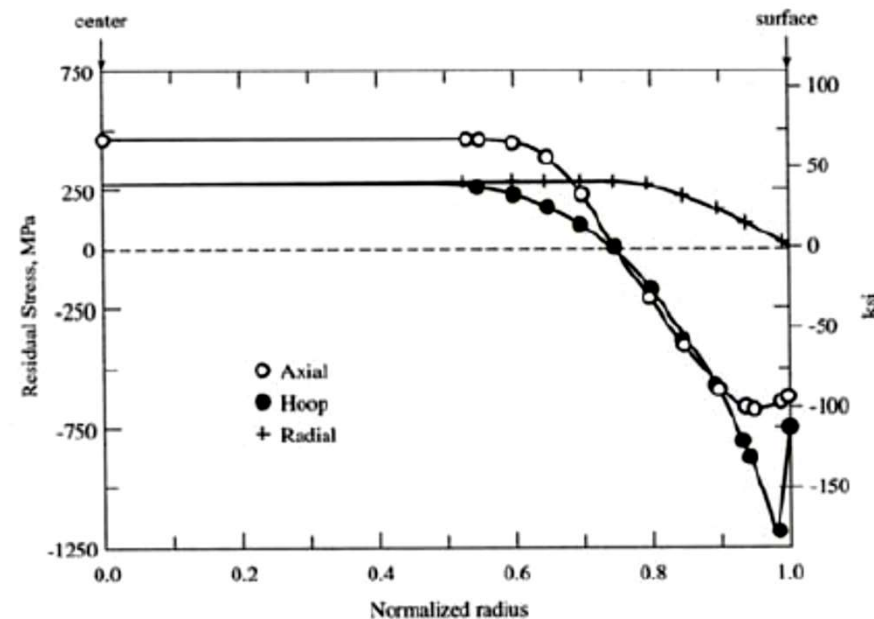
# Methods inducing residual stresses

## Induction hardening

- Surface hardening and compressive residual stress is accomplished by thermal treatment

### Example: SAE 1045 40 mm diameter steel shaft

- Residual stress distributions from surface hardening
- Induction hardened shafts with surface or subsurface failure have significantly greater fatigue resistance than non-hardened shafts



# Methods inducing residual stresses

**Plating** by electrolytic means can involve

- Soft plating materials such as zinc, tin, lead, or copper, or harder plating materials such as chromium and nickel

Plating of parts is done

- To increase corrosion resistance and for esthetic appearance
- To increase wear resistance plating (chromium)

Electroplating with chromium or nickel will

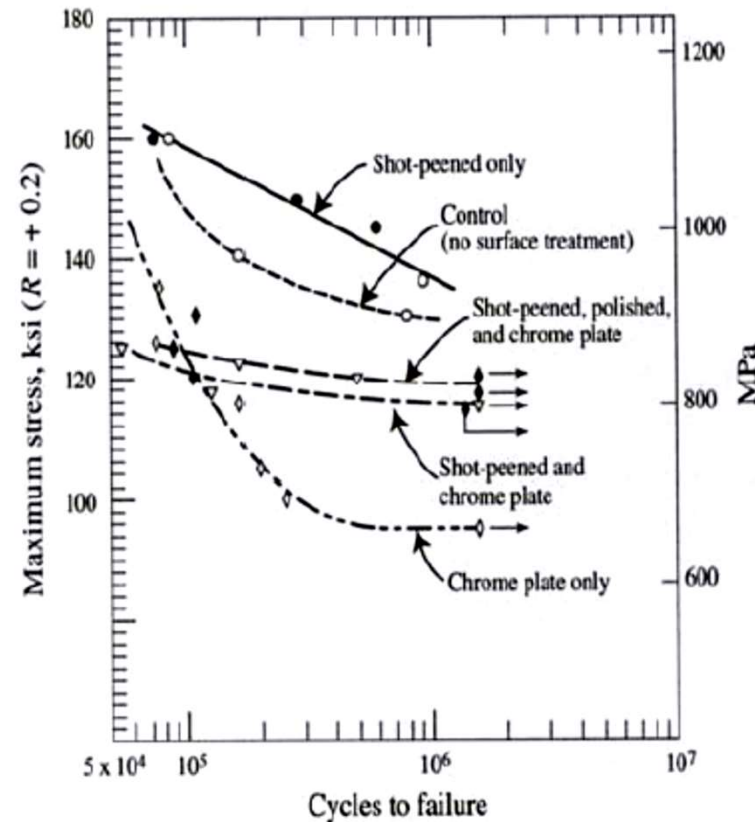
- create significant residual tensile stresses in the plating material along with microcracking
- contribute to significant reduction in fatigue resistance of chromium or nickel plated parts
- the reductions are greatest in higher strength steels at longer and intermediate lives, and depend upon the plating thickness



# Methods inducing residual stresses

## Example: Chrome plating of 4130 steel

- Detrimental fatigue aspects due to chromium plating.
- Methods that produce desirable compressive surface stresses such as shot-peening, nitriding, or surface rolling can be used to nullify much of the detrimental fatigue aspects of chromium or nickel plating.
- This has been done successfully, both before and after the electroplating.



# Methods inducing residual stresses

**Machining** operations such as turning, milling, grinding, polishing, and honing can significantly affect fatigue resistance.

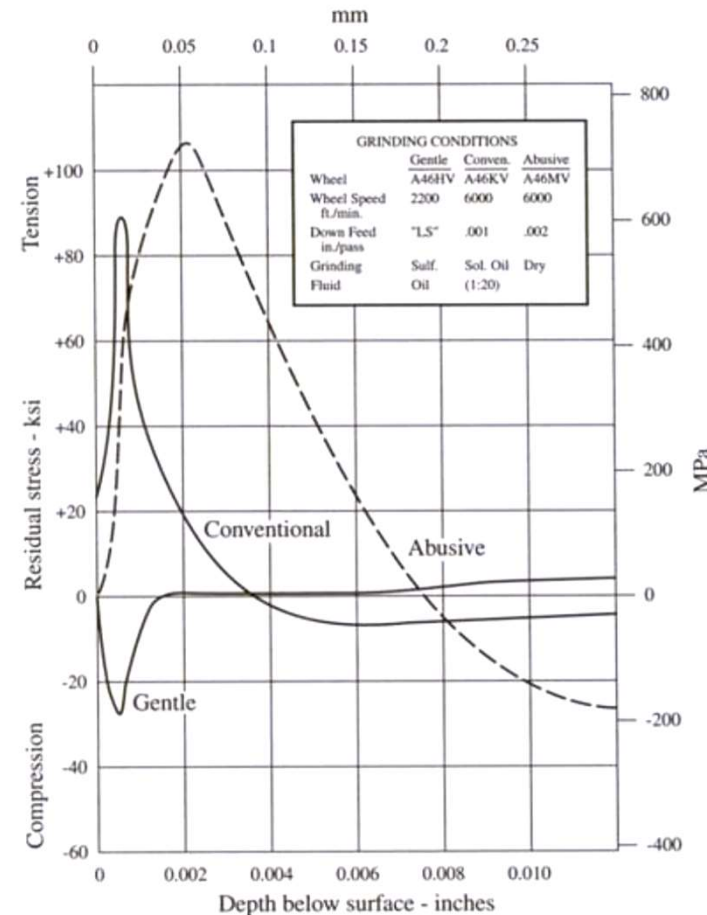
These methods all involve surface operations where fatigue cracks usually nucleate and grow.

- They can involve four major factors that affect fatigue resistance, -- surface finish -- cold working -- possible phase transformations -- residual stresses.
- All four of these factors contribute to fatigue resistance, however residual stresses may be the most dominant factor.
- The greatest effects of machining on fatigue resistance is at longer and intermediate lives.

# Methods inducing residual stresses

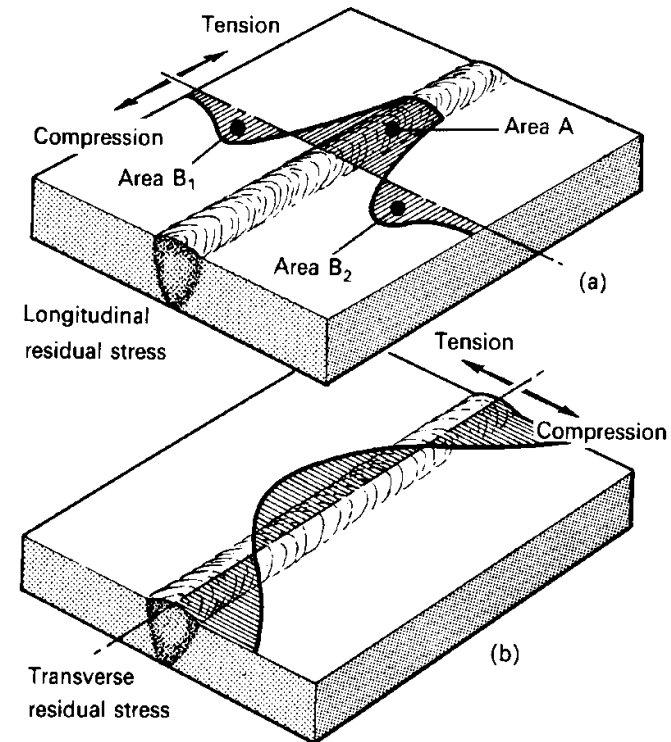
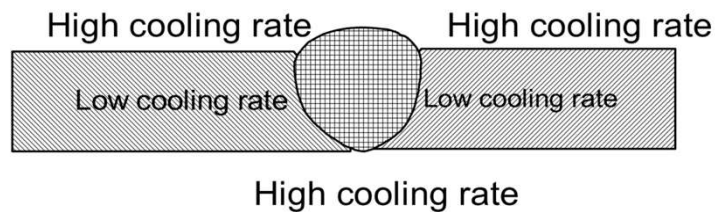
## Machining

- Residual stress depth, sign and magnitude as well as surface finish are depended on
  - cutting velocity
  - tool pressure
  - feed
  - tool geometry
  - cooling
- Grinding causes also high variety in residual stresses and fatigue strength



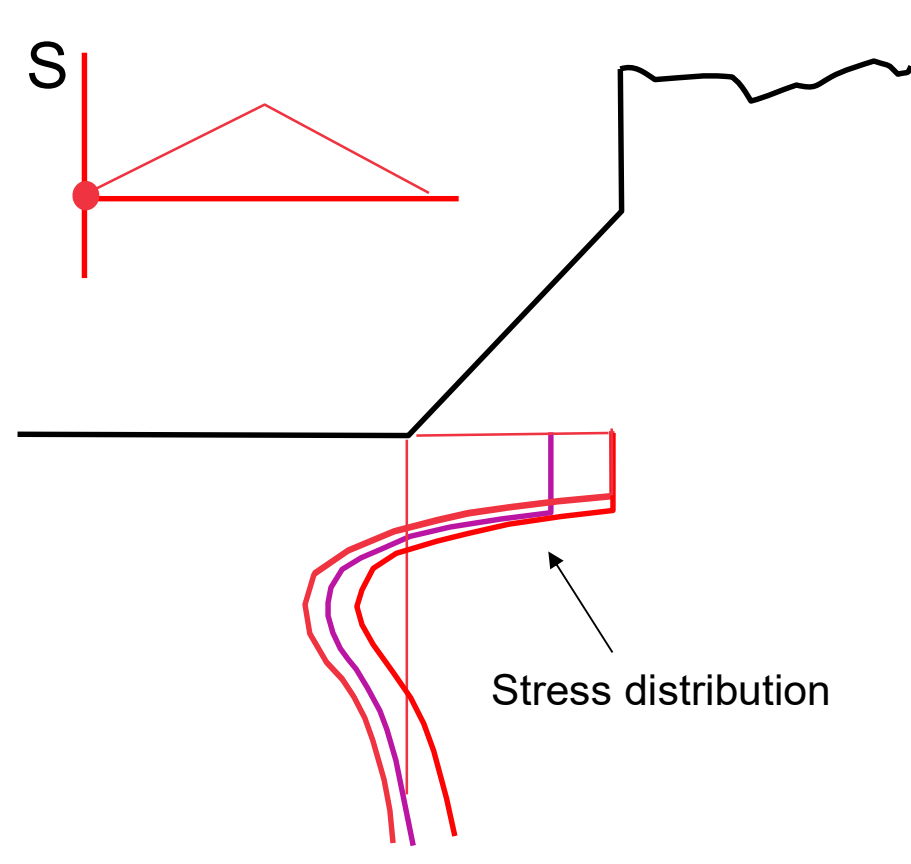
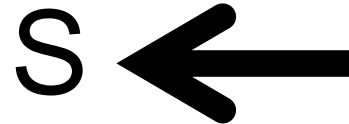
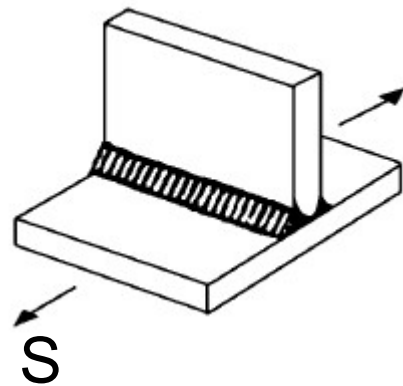
# Residual stresses in welded joint

- Due to heating and cooling process
- High variation in the welded joint in both longitudinal and transversal direction



# Residual stresses in welded joint

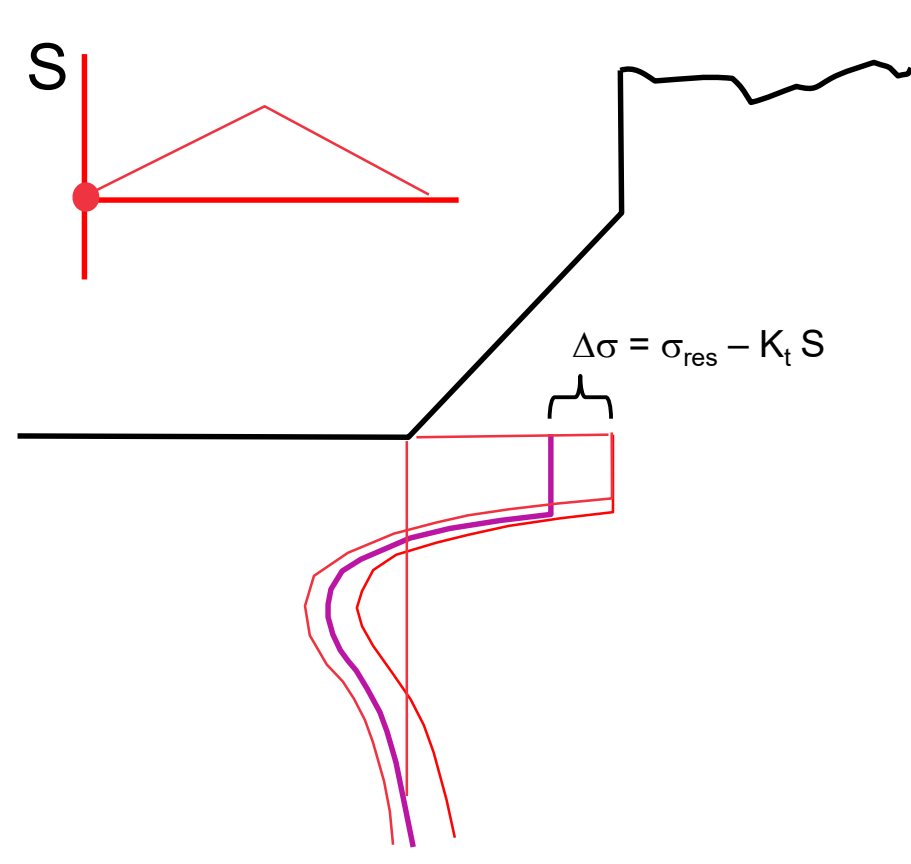
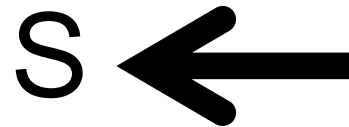
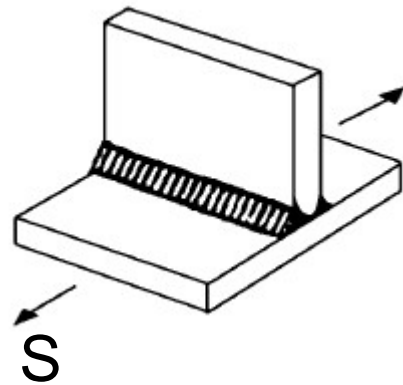
Development of notch stress  $\sigma$   
during reversal loading





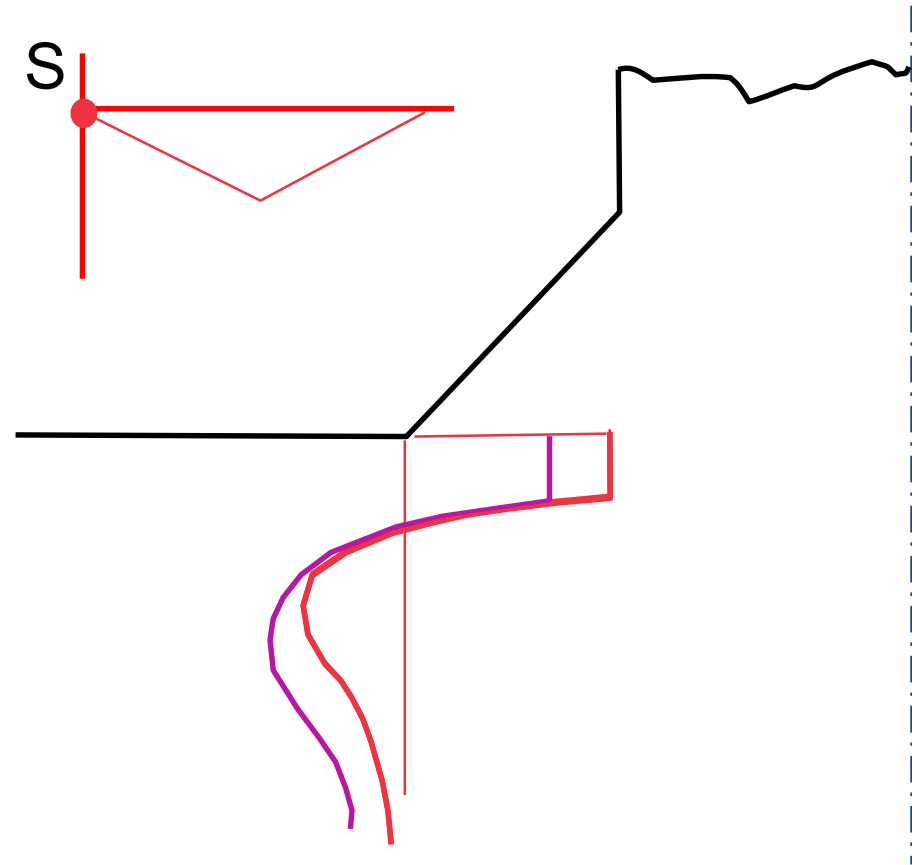
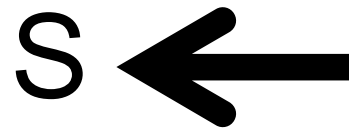
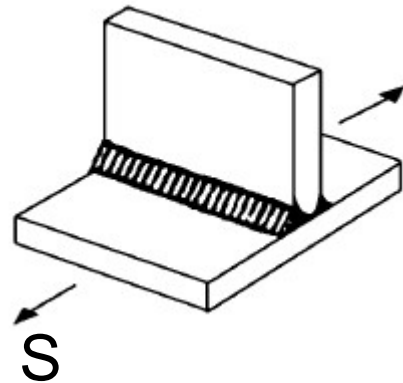
# Residual stresses in welded joint

Development of notch stress  $\sigma$   
during reversal loading



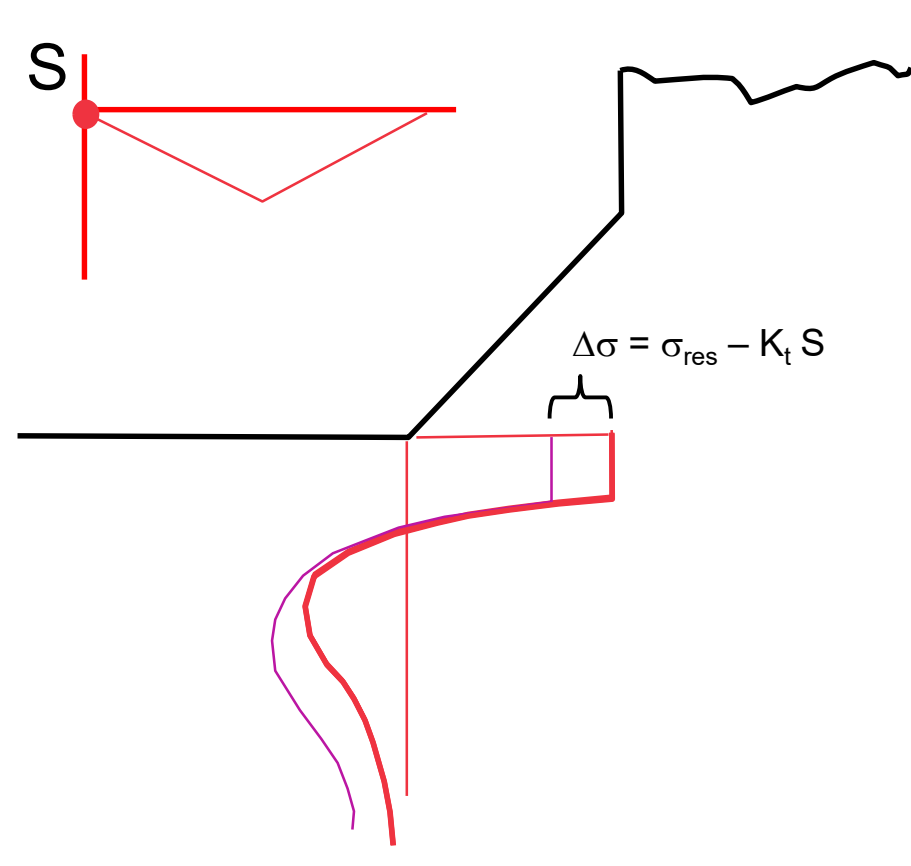
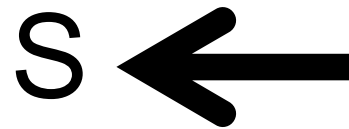
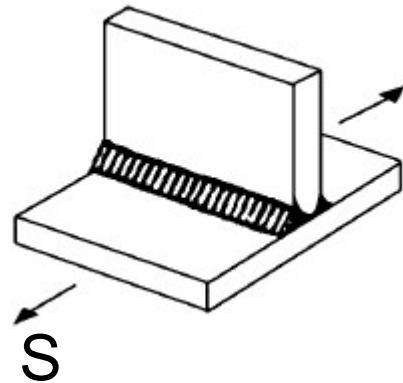
# Residual stresses in welded joint

Development of notch stress  $\sigma$   
during reversal loading



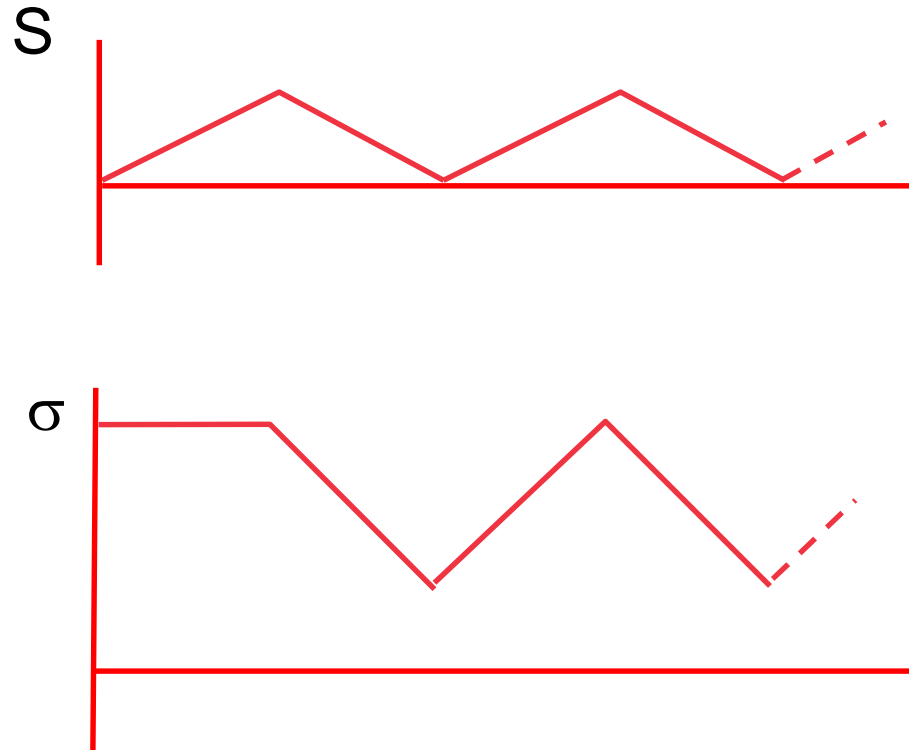
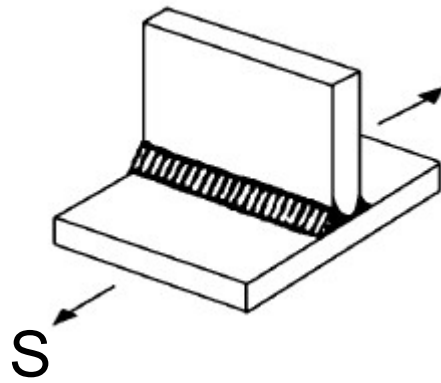
# Residual stresses in welded joint

Development of notch stress  $\sigma$   
during reversal loading



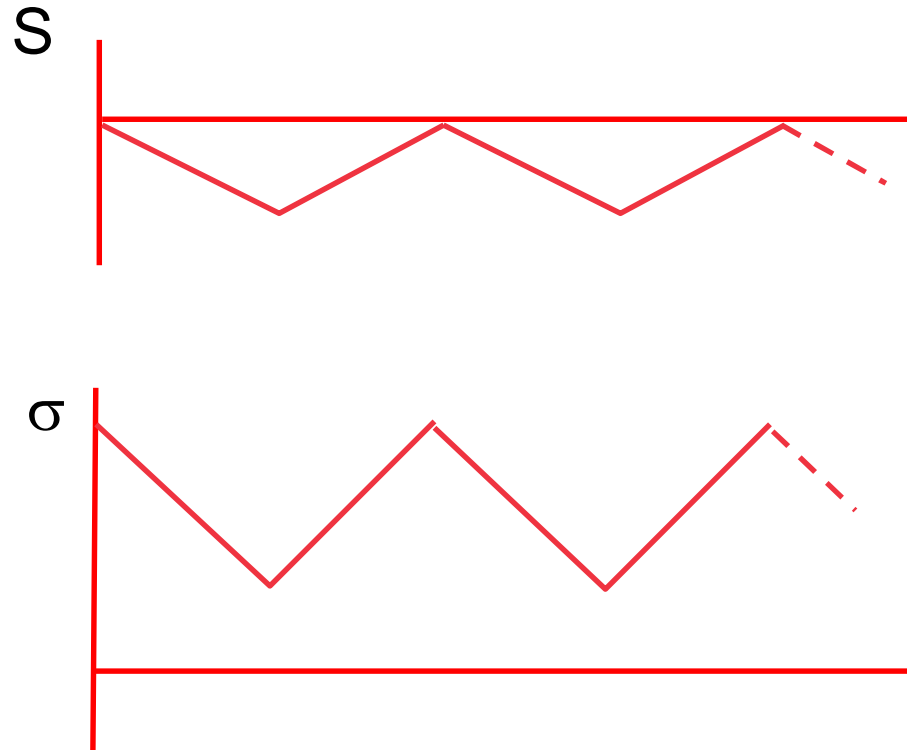
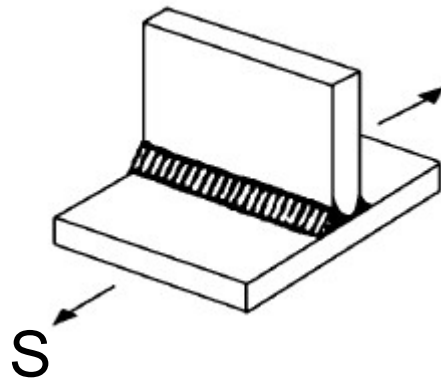
# Residual stresses in welded joint

Development of notch stress  $\sigma$   
during reversal loading

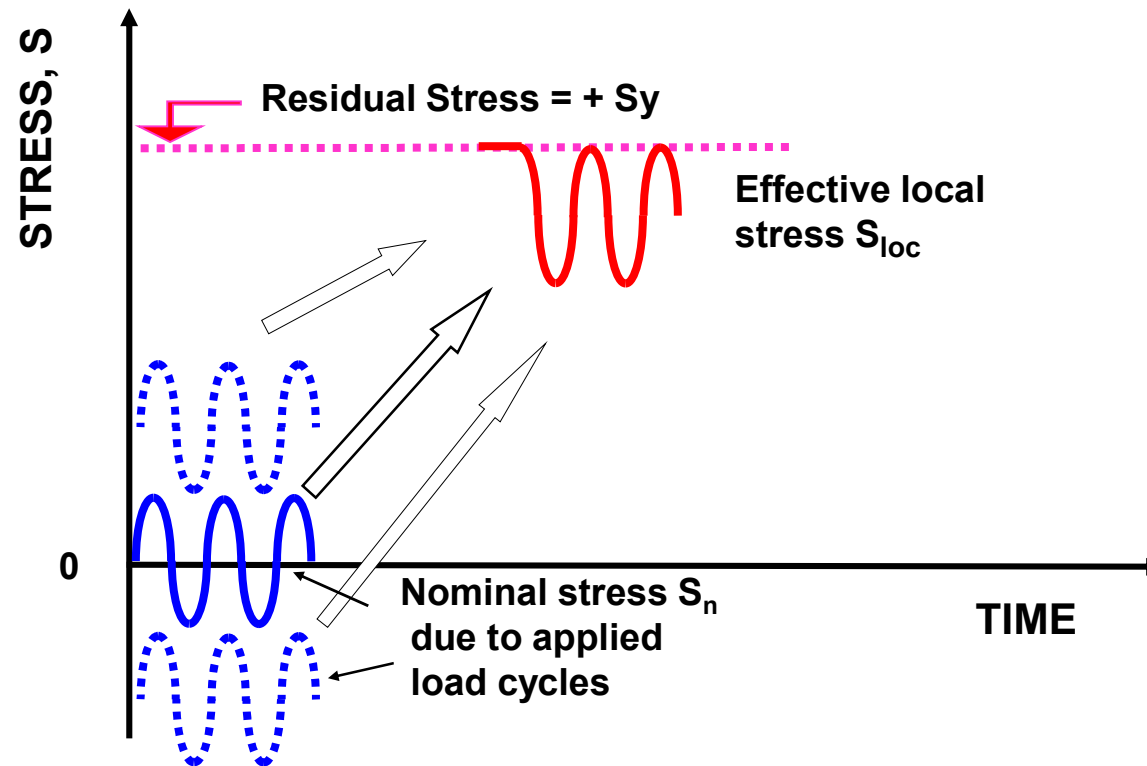


# Residual stresses in welded joint

Development of notch stress  $\sigma$   
during reversal loading



# Residual stresses in welded joint



# Residual stresses determination

Residual stresses may be determined:

- Analytically (i.e. the local strain approach )
- Computationally with finite element analysis
- Experimentally (the most common methods)

Determination of surface residual stresses can be non-destructive, while subsurface residual stress determination methods are mostly destructive.

# Residual stresses determination

The Society for Experimental Mechanics *Handbook of Measurement of Residual Stresses* describes the major experimental methods for determining residual stresses.

- hole-drilling and ring core
- layer removal
- sectioning
- X-ray diffraction
- neutron diffraction
- ultrasonic
- magnetic methods

ASTM has standard test methods for the hole-drilling method and for X-ray diffraction measurements.



# Residual stresses determination

The **hole-drilling** method involves:

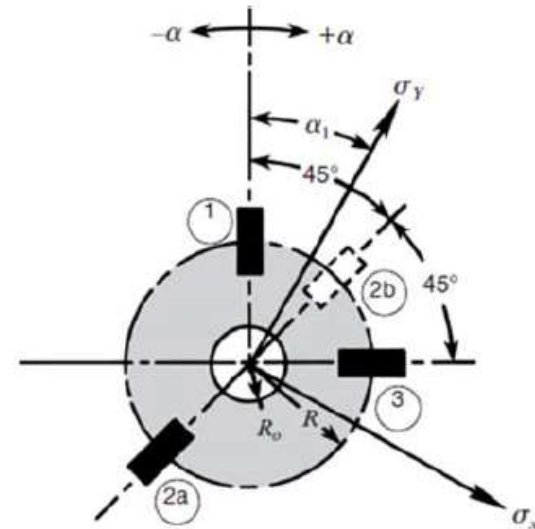
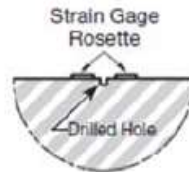
- drilling a small hole typically 1.5 to 3 mm deep through a three element radial strain gage rosette attached to the part.
- the strain gage relaxation around the hole from the drilling is then measured and converted to biaxial residual stresses in the hole vicinity.

**Sectioning** methods are used to measure subsurface residual stresses by:

- Removing a beam, ring, or prism specimen from a residual stressed part of concern..
- The surface is subjected to repetitive surface layer removal by electrochemical polishing, etching, or machining.
- The curvature changes or deflections of the specimen for each layer removal is measured and these measurements are then related to residual stress magnitudes.

# Residual stresses determination

## Hole drilling method



$$\sigma_{max} = \frac{\epsilon_1 + \epsilon_3}{4A} - \frac{1}{4B} \sqrt{(\epsilon_3 - \epsilon_1)^2 + (\epsilon_3 + \epsilon_1 - 2\epsilon_2)^2}$$

$$\sigma_{min} = \frac{\epsilon_1 + \epsilon_3}{4A} + \frac{1}{4B} \sqrt{(\epsilon_3 - \epsilon_1)^2 + (\epsilon_3 + \epsilon_1 - 2\epsilon_2)^2}$$

$$\tan 2\alpha = \frac{\epsilon_1 - 2\epsilon_2 + \epsilon_3}{\epsilon_1 - \epsilon_3}$$



# Residual stresses determination

**X-ray diffraction** can be used non-destructively to measure surface residual stresses and destructively for subsurface values.

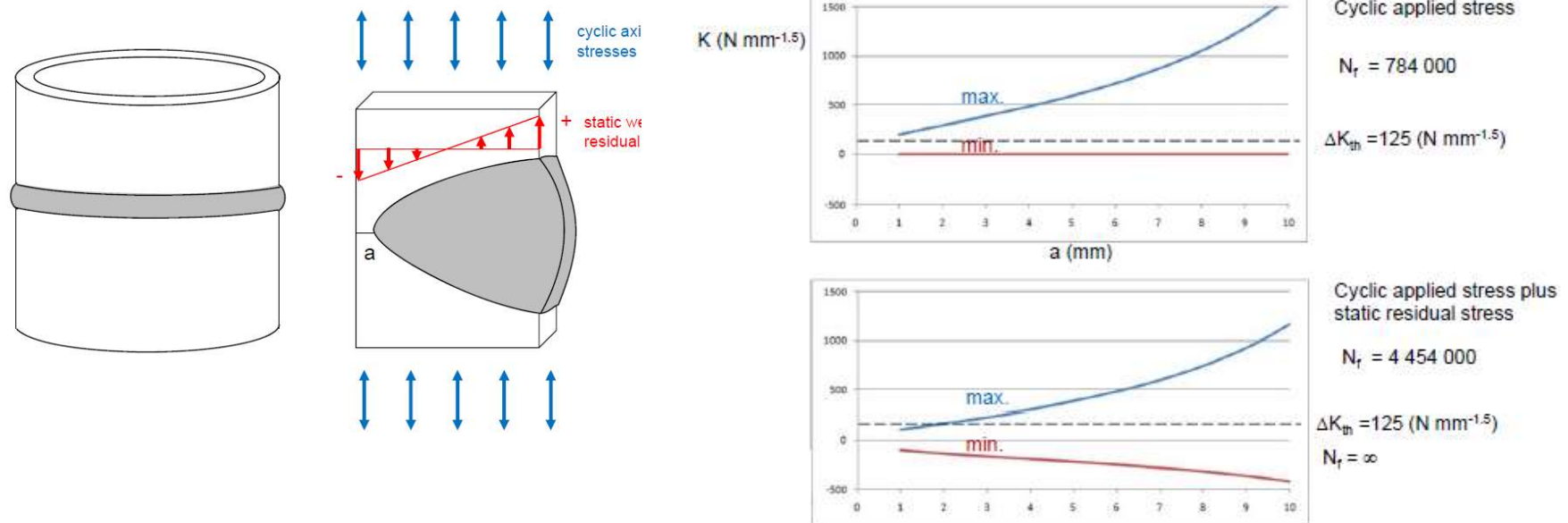
- Residual stresses cause crystal lattice distortion and a measurement of interplaner spacing of the crystal lattice indicates the residual stress magnitude.
- By electrochemical polishing away thin layers of metal, subsurface residual stresses can be measured.

Both portable and non-portable X-ray diffraction equipment are available for many diverse situations making the X-ray diffraction method very popular.

Typical precision of X-ray diffraction residual stress measurements can be as low as  $\pm 7$  MPa or up to  $\pm 35$  MPa .

# Residual stresses in fatigue analysis

## Example: One-side welded pipe connection



*Application of LEFM to study the influence of residual stress on fatigue life*

# Residual stresses in fatigue analysis

- Similitude exists between mean stress and residual stress and S-N,  $\epsilon$ -N, and  $da/dN$ - $\Delta K$  methods can be used for both mean and residual stresses.
- The residual stresses persist as long as the sum of residual stress and applied stress does not exceed the pertinent yield strength,  $S_y$  or  $S_y'$ , of the materials.
- Thus residual stresses are more beneficial (and potentially more harmful) when applied to hard metals with high yield strengths.
- In softer metals such as mild steel the residual stresses can be more easily decreased by yielding.
- Therefore mild steel is not usually shot-peened and it can be welded with fewer precautions than harder materials.



# Residual stresses in fatigue analysis

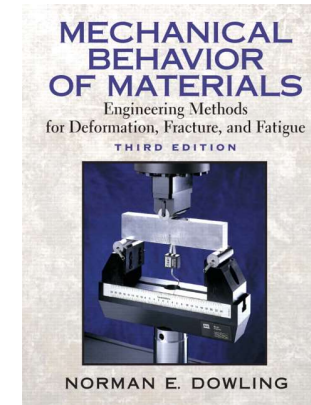
- Loading in one direction only, as in springs and most gears, will not destroy beneficial residual stresses.
- Automobile leaf springs are usually shot-peened on the tension side. In springs, as in other parts that are loaded predominantly in one direction, an overload applied early in the life introduces desirable residual compressive stresses at the proper surface.
- Springs, hoists, and pressure vessels are strengthened by proof loading with a load higher than the highest expected service load.
- Thermal stress relief can also relax residual stresses. At proper stress relief temperatures, residual stresses will relax with time in a decreasing exponential manner. Different materials will have different best stress relief temperatures and time at temperature.

# Readings – Course material

## Course book

Mechanical Behavior of Materials Engineering  
Methods for Deformation, Fracture, and Fatigue,  
Norman E. Dowling

- Section 9.6.4, 10.9.2, 13.3-13.6



## Additional papers and reports given in MyCourses webpages

- Sticchi, M., Schnubel, D., Kashaev, N., and Huber, N. Review of Residual Stress Modification Techniques for Extending the Fatigue Life of Metallic Aircraft Components. Appl. Mech. Rev. 2015, 67:010801.
- James, M.N. Residual stress influences on structural reliability, Engineering Failure Analysis, 2011, 18:1909-1920.