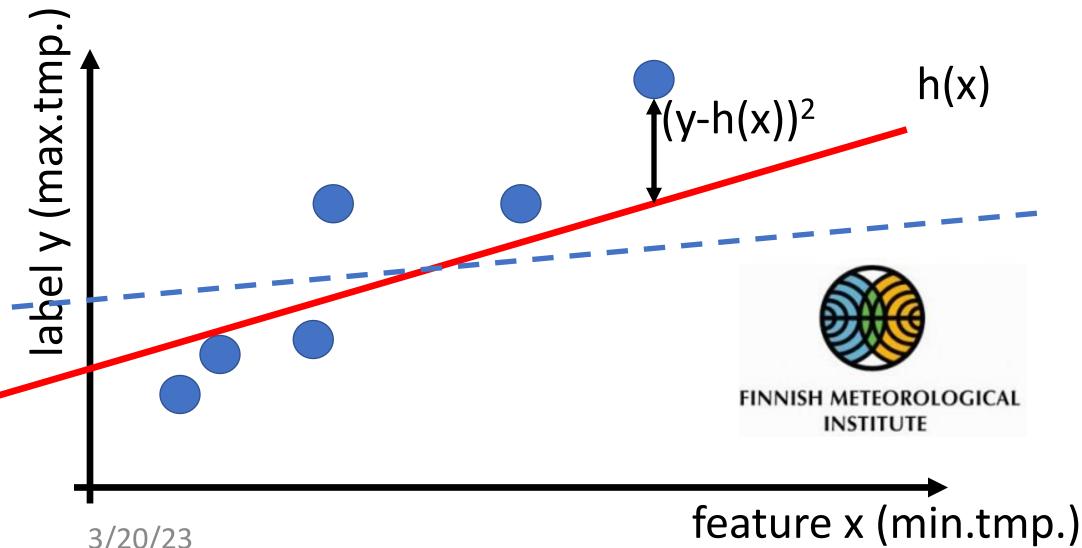
# CS-E4740 Federated Learning "Network Models"

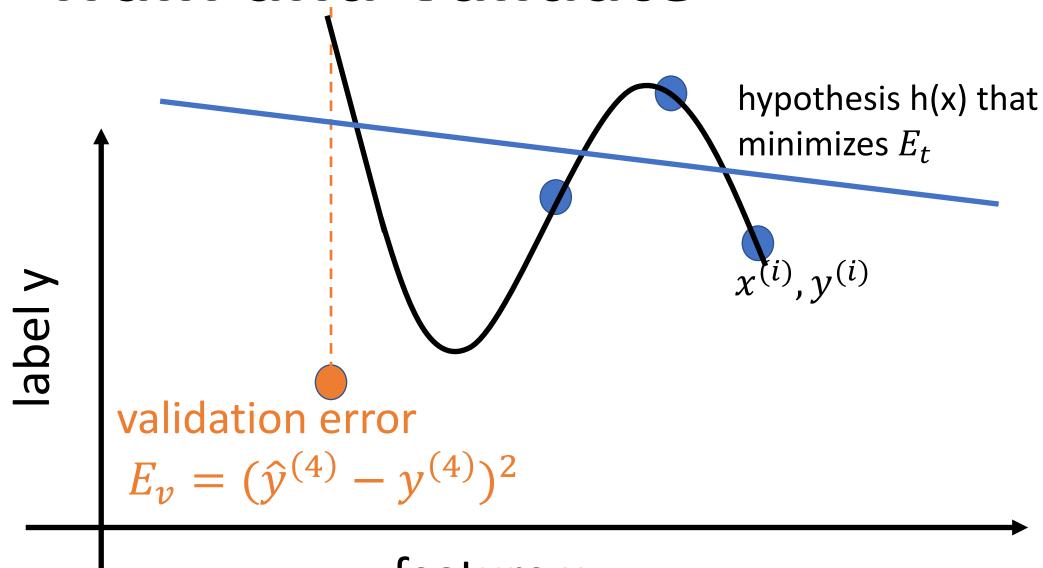
Dipl.-Ing. Dr. techn. Alexander Helmut Jung

# What are the main components of ML and how are they combined?

# Plain Old Machine Learning



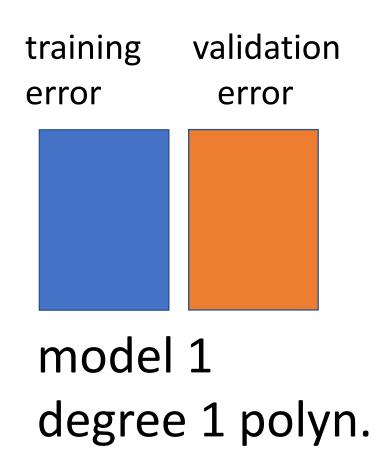
#### **Train and Validate**

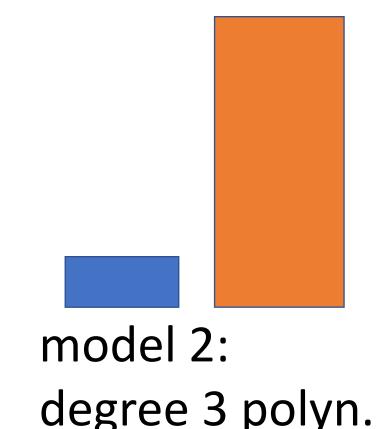


feature x

#### **Basic Idea of Model Selection**

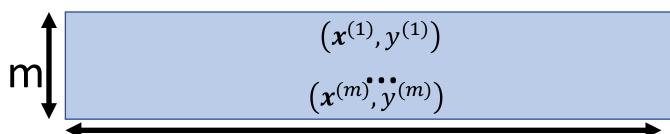
choose model with smallest validation error!





20.3.2023

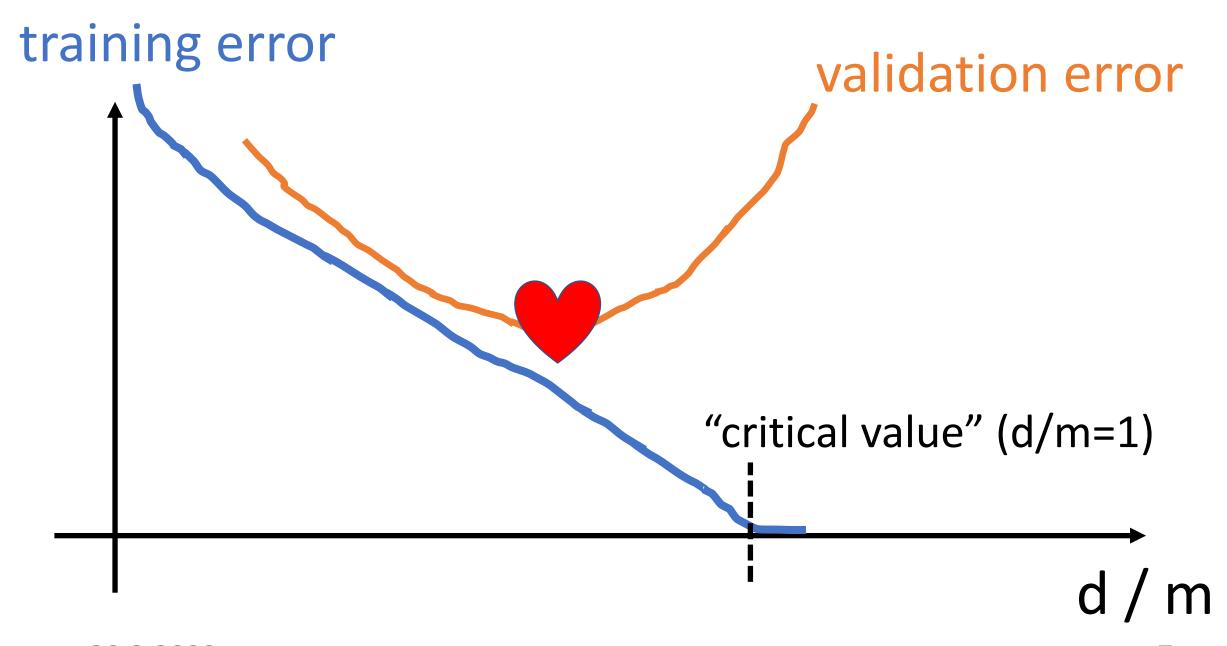
# Data and Model Size



nr. of features n crucial parameter is the ratio d/m

hypospace/model eff. dimension d

20.3.2023

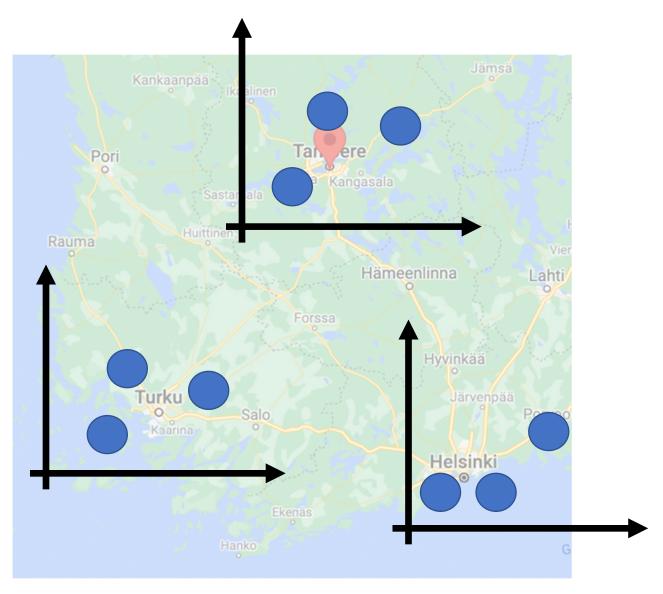


20.3.2023

# Networked Data

#### **Networked Weather Data**



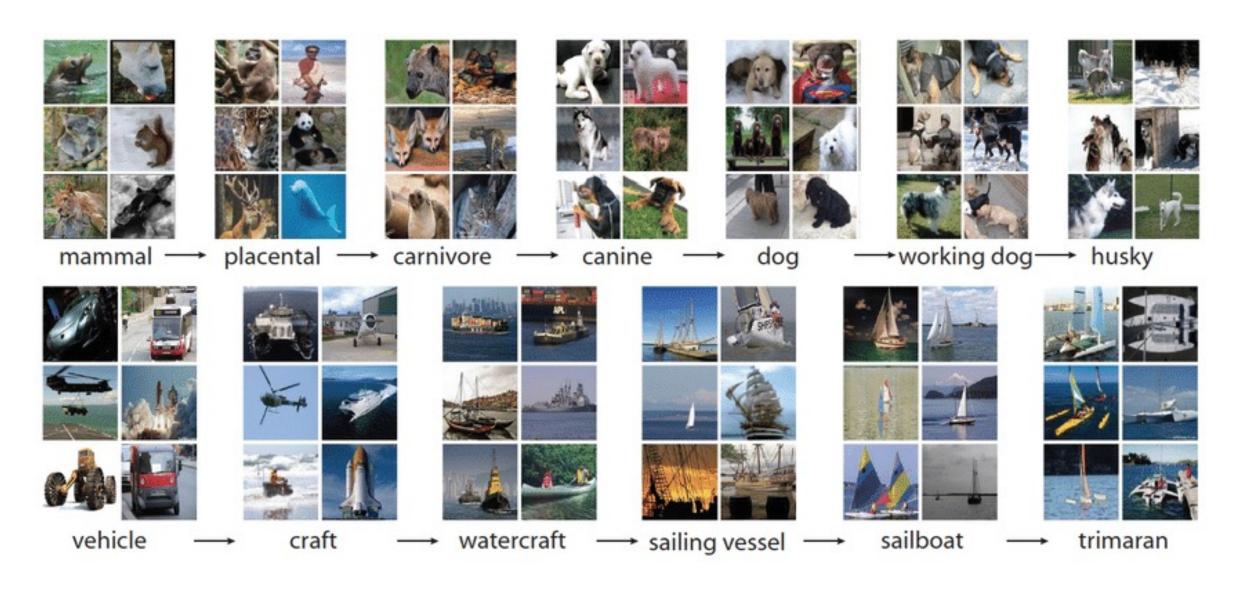


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#### **ImageNet**

"...ImageNet is an image database organized according to the WordNet hierarchy (currently only the nouns), in which each node of the hierarchy is depicted by hundreds and thousands of images..."

https://image-net.org/



Devopedia. 2021. "ImageNet." Version 16, April 7. Accessed 2023-02-11. https://devopedia.org/imagenet

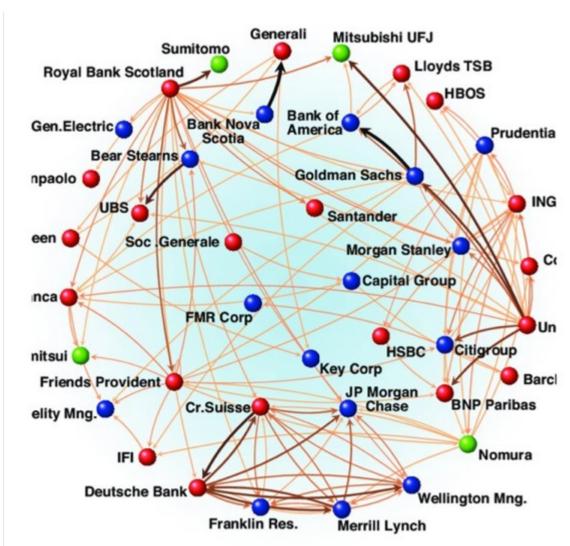
12

#### **Noble Networks**

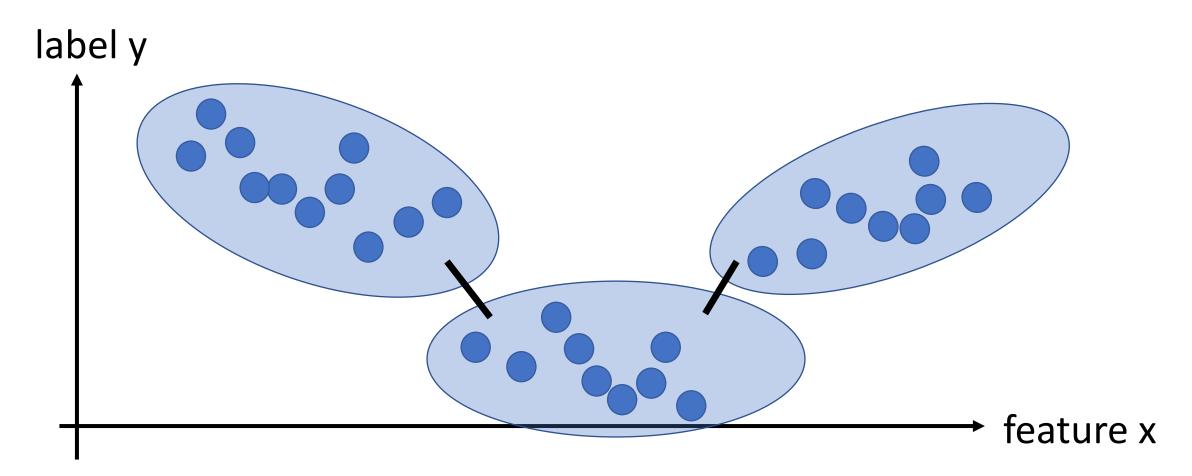


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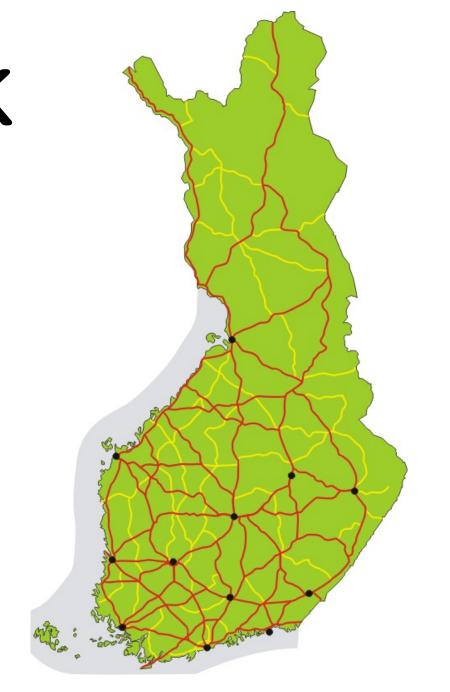
#### **Finance Networks**



#### Point Cloud Networks.

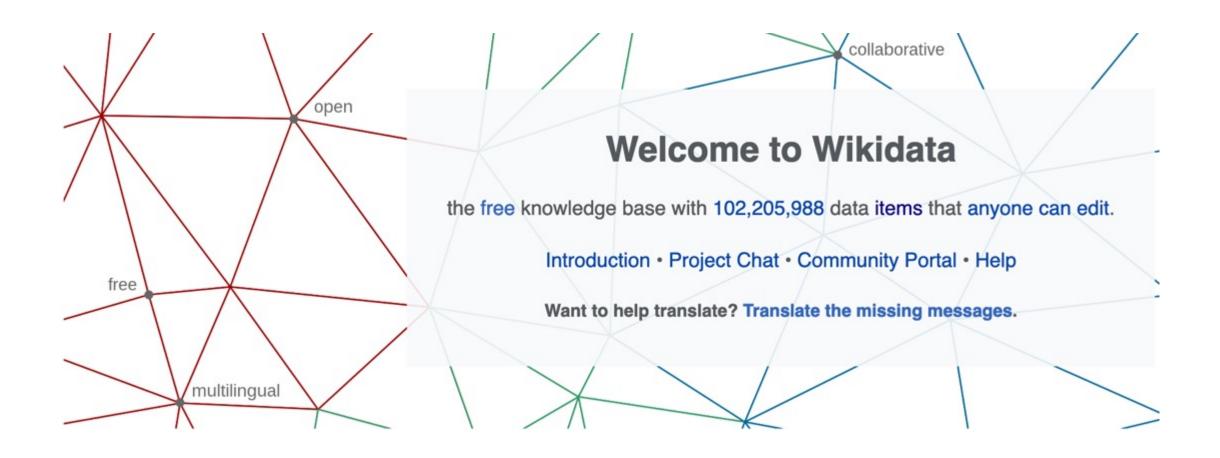


# Road Network



#### **Business Process**





https://www.wikidata.org/wiki/Wikidata:Main\_Page

#### **Empirical Graph - Nodes**

```
i=1
```

2

each node carries:



```
3
```

```
# the node attribute "X" stores
G.nodes[iter_node]["X"] = X

# the node attribute "y" stores
G.nodes[iter_node]["y"] = y
```

```
4
```

```
G_FMI = nx.Graph()
G_FMI.add_nodes_from(range(0,num_stations))
```

#### **Attach Local Datasets to Nodes**

```
for i,station in enumerate(data.station.unique())
    # first filter out rows in dataframe data wit
    # current value of station
    df = data[data.station==station]
   # store the name of the current station in th
    G_FMI.nodes[i]['name'] = station
   # store the lat and lon of the current statio
    G_FMI.nodes[i]['coord'] = np.array([df.latitu
    # store the min. daytime temp_in the node at
    G_FMI.nodes[i]['X'] = df.min_temp.to_numpy().
   # store the max. daytime temp. in the node at
    G_FMI.nodes[i]['y'] = df.max_temp.to_numpy().
```

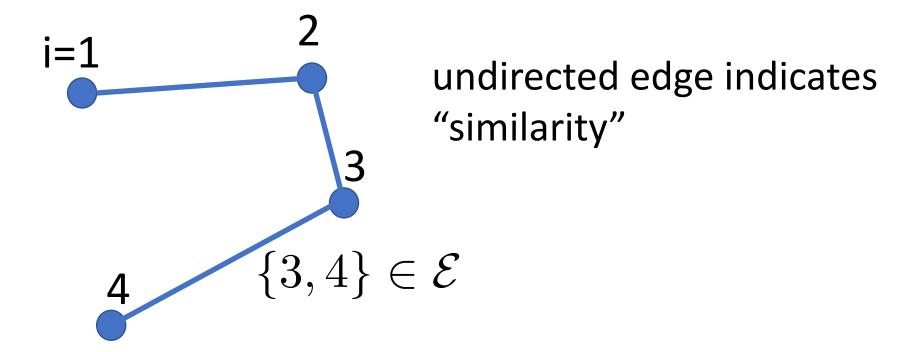
name of FMI station

latitude, longitude of FMI station

use min. daytime tmp. as feature of datapoint (=some day)

use max. daytime tmp. as labels of datapoint (= some day)

### **Empirical Graph - Edges**



edge weight  $A_{3,4}$  = level of similarity

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#### Measure Statistical Similarity

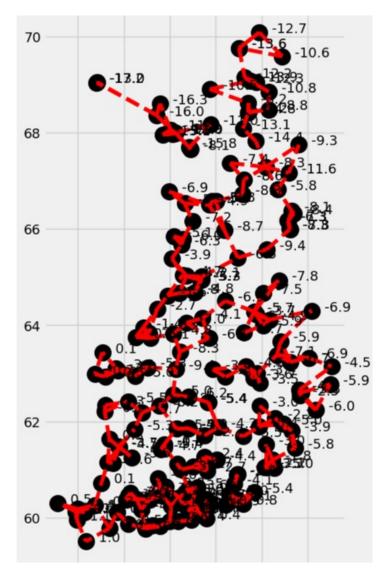
```
>>> from scipy.stats import ks_2samp
>>> import numpy as np
>>>
>>> np.random.seed(12345678)
>>> x = np.random.normal(0, 1, 1000)
>>> y = np.random.normal(0, 1, 1000)
>>> z = np.random.normal(1.1, 0.9, 1000)
>>>
>>> ks 2samp(x, y)
>>> ks_2samp(x, z)
Ks_2sampResult(statistic=0.41800000000000004, pvalue=3.7081494119242173e-77)
```

https://stackoverflow.com/questions/10884668/two-sample-kolmogorov-smirnov-test-in-python-scipy

https://en.wikipedia.org/wiki/Kolmogorov%E2%80%93Smirnov\_test

# Spatio-Temporal Similarity

connect FMI stations with its k nearest neighbours (use geodesic distance)



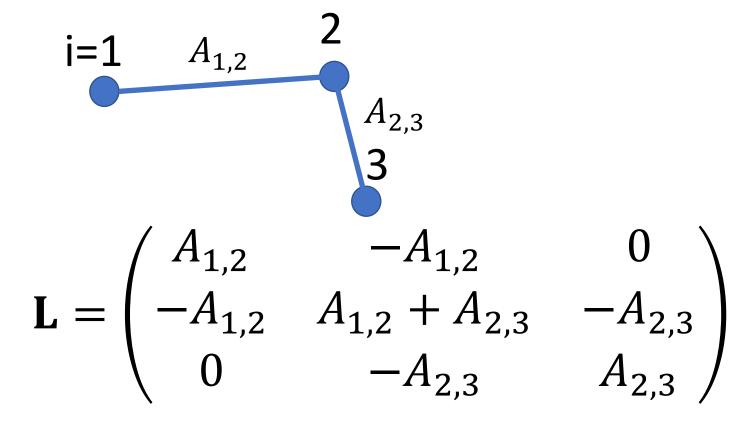
### How to choose Empirical Graph?

• empirical graph is a design choice

more edges means more comp./comm.

sufficient number of edges between similar datasets

#### Graph Laplacian Matrix

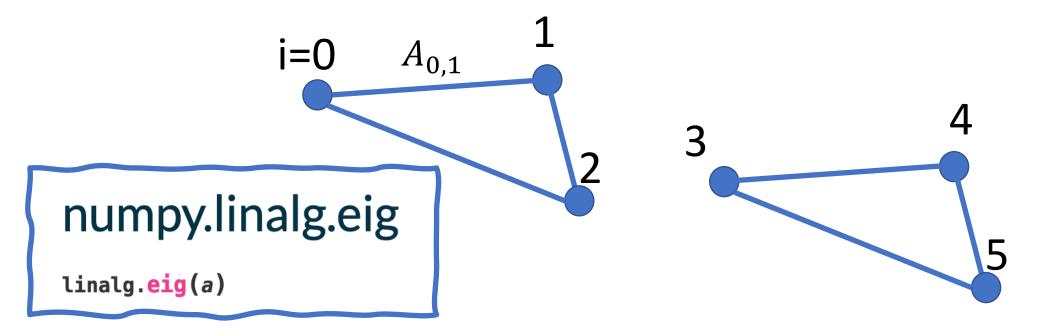


L is pos. sem.def. with eig.vals

$$\lambda_1 = 0 \le \lambda_2 \dots \le \lambda_{nr \ nodes}$$

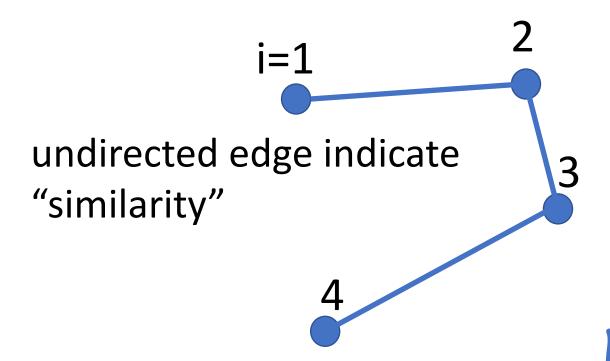
# Spectral Graph Clustering

eig.vecs of **L** corresponding to smallest pos. eig.vals  $\lambda_1 = 0 \le \lambda_2$  are piece-wise constant over clusters



# What is Component 2 of ML?

#### **Local Model for Local Data**



#### each node carries:

local dataset

```
# the node attribute "X" stores
G.nodes[iter_node]["X"] = X

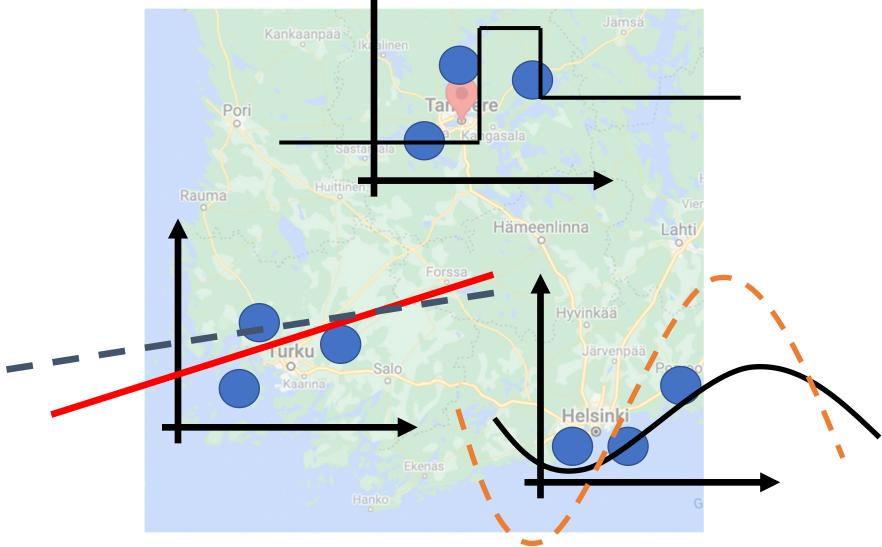
# the node attribute "y" stores
G.nodes[iter_node]["y"] = y
```

local model

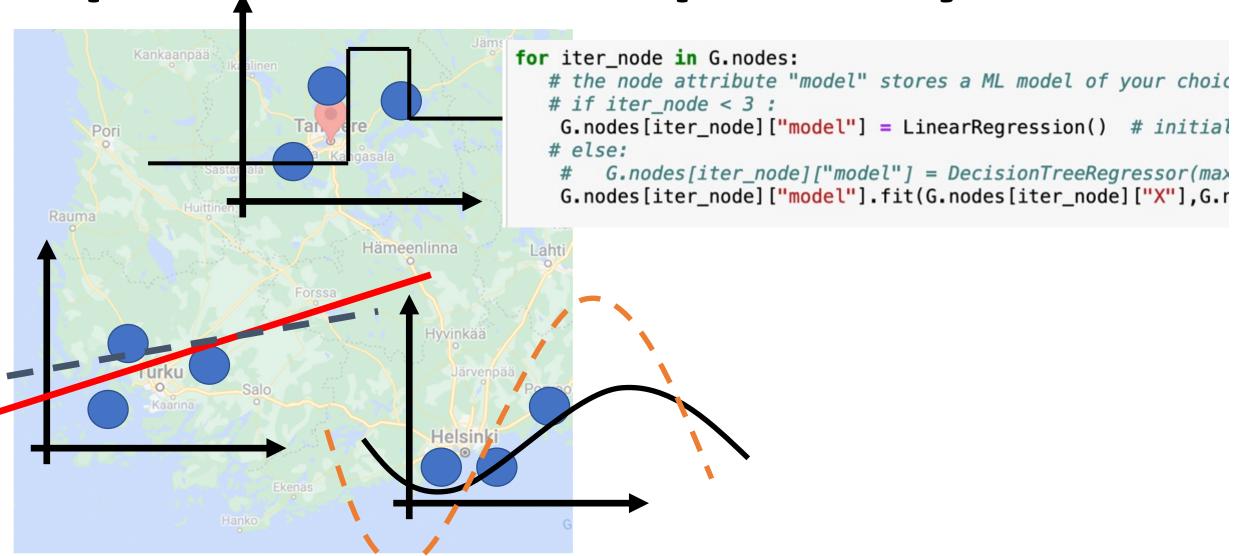
```
# the node attribute "model" stores a ML model of
G.nodes[iter_node]["model"] = LinearRegression()
G.nodes[iter_node]["model"].fit(G.nodes[iter_node]
```

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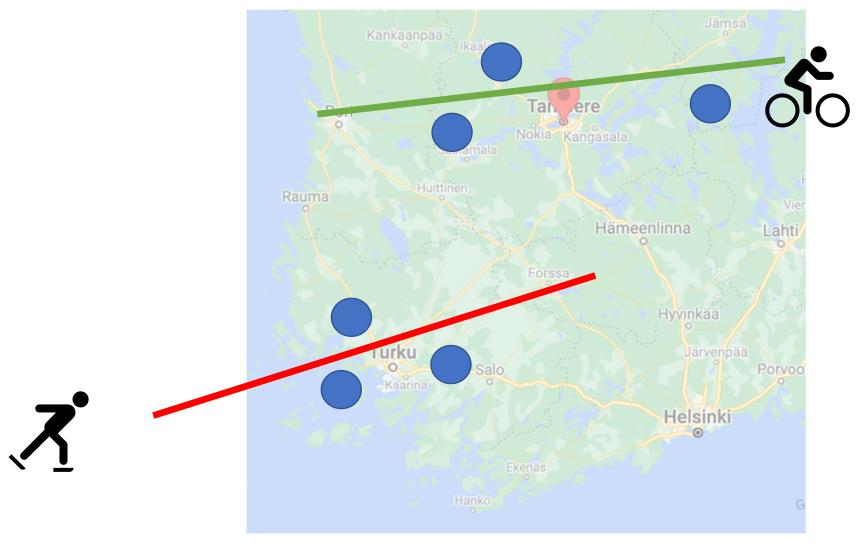
### Networked Models



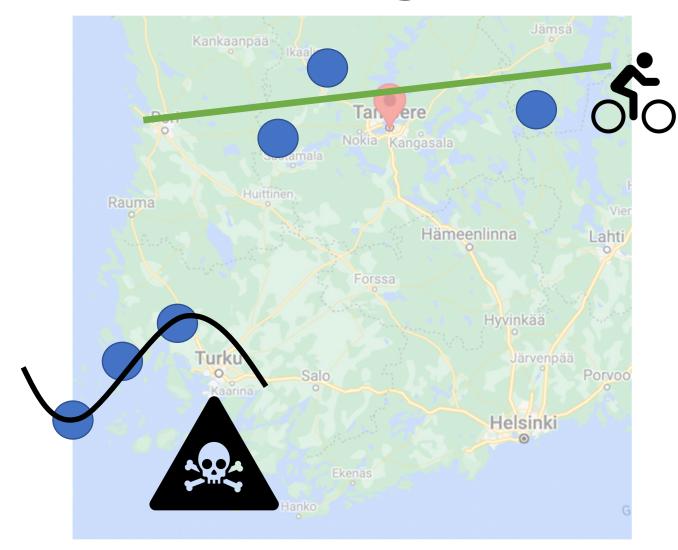
# Option 1: Train Separately



#### **Pro: Personalization**

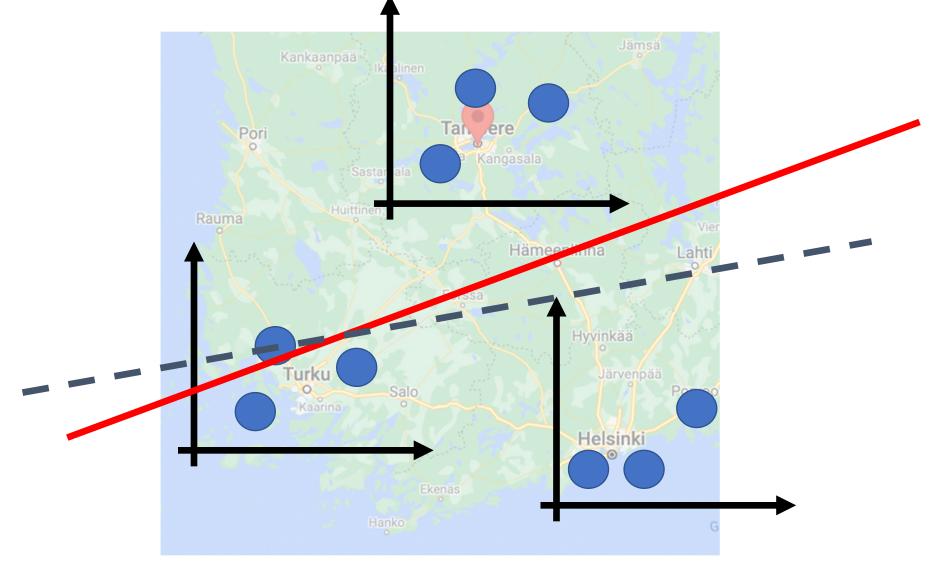


# Con: Overfitting

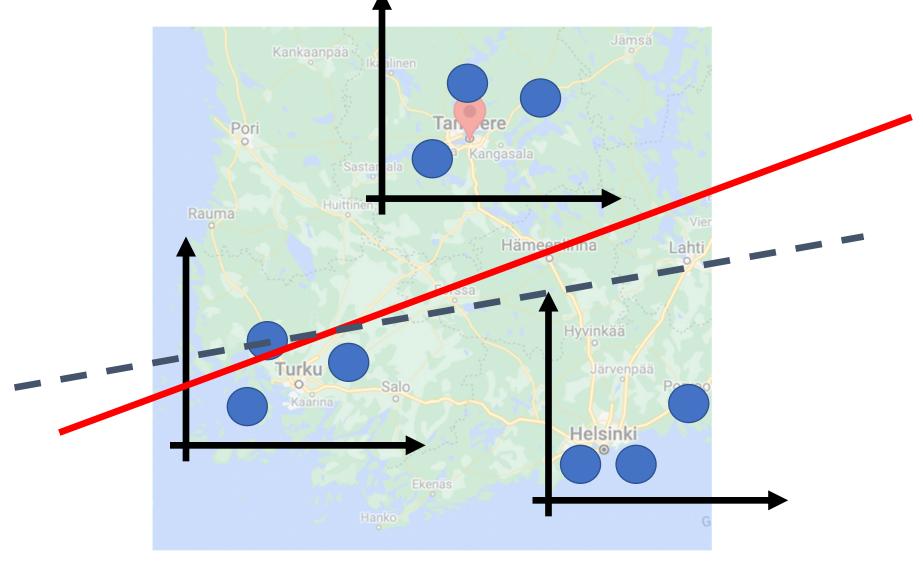


<u>Z</u>

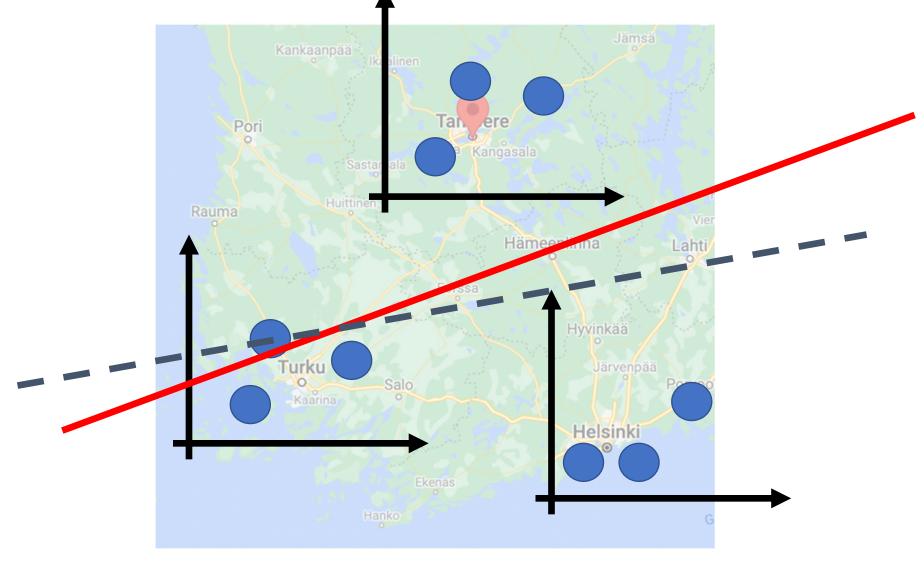
#### **Option 2: Global Model**



### Pro: No Overfitting

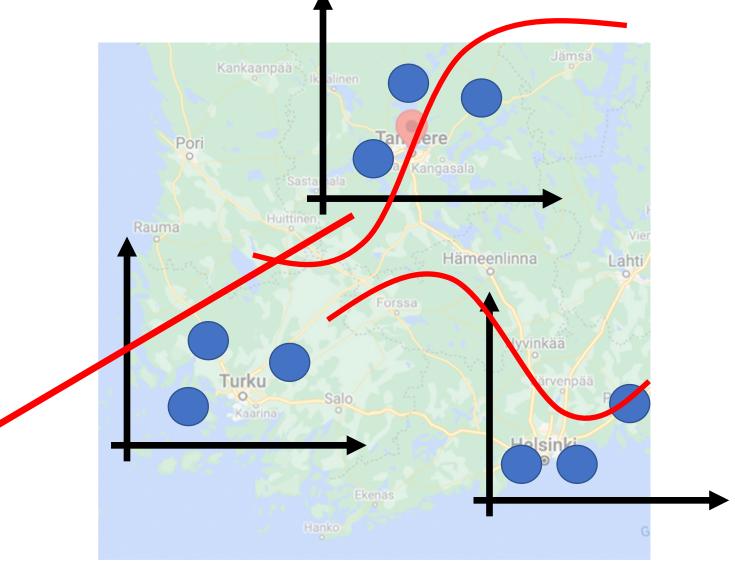


#### Con: Low Accuracy

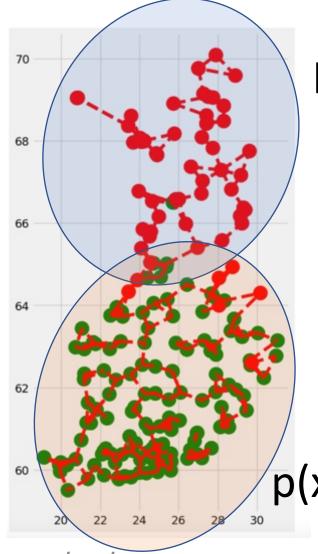


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#### Option 3: Clustered FL



# Clustering Assumption

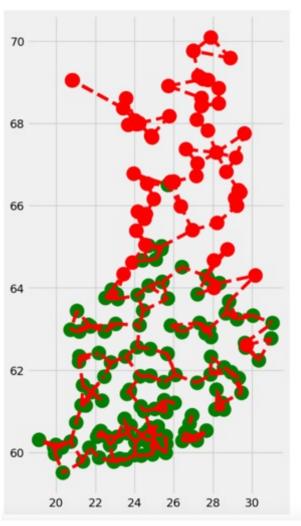


p(x,y; c=1)

local datasets in cluster "c" contain data points that can be approximated as i.i.d. with prob. dist p(x,y;c)

p(x,y; c=2)

# **Cluster-Wise Training**



pool local datasets of nodes in same cluster to train ML model

trained model is used for all nodes in same cluster

### Clustering via Regularization

cluster structure typically unknown

how to pool local datasets in same cluster?

pooling = enforce constant local model params

penalize variation of local model params

# Regularization

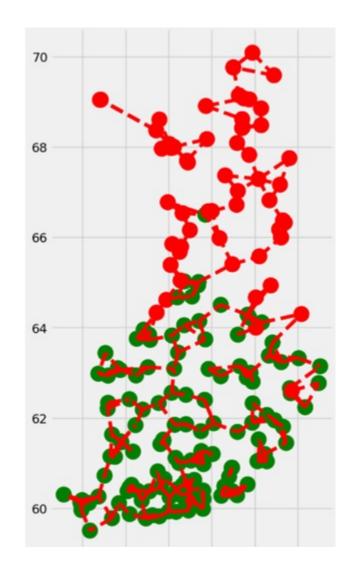
require small variation  $\mathbf{w}^{(i)} - \mathbf{w}^{(j)}$ 



#### **Total Variation Minimization**

 requiring small variation enforces piece-wise constant local model params

piece-wise constant model
 params = pooling of local data



#### Wrap-Up

• emp. graph with nodes carrying local datasets and models

undirected weighted edges represent similarities

different sources for similarity

• emp. graph is a design choice

# Any Questions?