MEC-E8001 Finite Element Analysis; Mathematica

"Structure is a collection of elements connected by nodes. Geometry, displacement, temperature etc. of the structure are defined by the nodal values of coordinates, translation, rotation, temperature etc. of which some are known and some unknown."

STRUCTURE

$prb = \{ele, fun\}$ where
$ele = \{prt_1, prt_2,\}$ elements
$fun = \{val_1, val_2,\}$ nodes
Element
$prt = \{typ, pro, geo\}$ where
$typ = BAR \mid TORSION \mid BEAM \mid RIGID \mid \mid$ model
$pro = \{p_1, p_2, \dots, p_n\}$ properties
$geo = Point[\{n_1\}] Line[\{n_1, n_2\}] Polygon[\{n_1, n_2, n_3\}] $ geometry
Nodes
$val = \{crd, trn, rot\} \{crd, trn, rot, tmp\}$ where
$crd = \{X, Y, Z\}$ structural coordinates
$trn = \{u_X, u_Y, u_Z\}$ translation components
$rot = \{\theta_X, \theta_Y, \theta_Z\}$ rotation components
tmp = 9temperature

DISPLACEMENT ANALYSIS

Constraint
$\{ \text{JOINT}, \{ \} \{ \{ \underline{u}_X, \underline{u}_Y, \underline{u}_Z \} \}, \text{Point}[\{n_1\}] \} \qquad \qquad \text{displacement constraint}$
${JOINT, {}, Line[{n_1, n_2}]}$ displacement constraint
$\{RIGID, \{\} \{\{\underline{u}_X, \underline{u}_Y, \underline{u}_Z\}, \{\underline{\theta}_X, \underline{\theta}_Y, \underline{\theta}_Z\}\}, Point[\{n_1\}]\} \dots displacement/rotation constraint$
${RIGID,\{\},Line[\{n_1,n_2\}]\}}$ rigid constraint
$\{SLIDER, \{n_X, n_Y, n_Z\}, Point[\{n_1\}]\}$ slider constraint
Force
$\{ FORCE, \{F_X, F_Y, F_Z\}, Point[\{n_1\}] \} \dots point force$
$\{ FORCE, \{F_X, F_Y, F_Z, M_X, M_Y, M_Z\}, Point[\{n_l\}] \} \qquad point load$
$\{FORCE, \{f_X, f_Y, f_Z\}, Line[\{n_1, n_2\}]\} \\ \\ distributed \ force$
$\{FORCE, \{f_X, f_Y, f_Z\}, Polygon[\{n_1, n_2, n_3\}]\} $
Beam model
$\{BAR, \{\{E\}, \{A\}, \{f_X, f_Y, f_Z\}\}\}, Line[\{n_1, n_2\}]\}$ bar mode
$\{ \text{TORSION}, \{ \{G\}, \{J\}, \{m_X, m_Y, m_Z\} \}, \text{Line}[\{n_1, n_2\}] \} \qquad \text{torsion mode}$
{BEAM,{ $\{E,G\},\{A,I_{yy},I_{zz}\},\{f_X,f_Y,f_Z\}\}$,Line[$\{n_1,n_2\}$]}beam
$\{BEAM, \{\{E,G\}, \{A,I_{yy},I_{zz}, \{j_X,j_Y,j_Z\}\}, \{f_X,f_Y,f_Z\}\}, Line[\{n_1,n_2\}]\} \dots beam$
Plate model
$\{ \text{PLANE}, \{ \{ E, v \}, \{ t \}, \{ f_X, f_Y, f_Z \} \}, \\ \text{Polygon}[\{ n_1, n_2, n_3 \}] \} \\ \dots \\ \text{thin slab mode}$
$\{ PLANE, \{ \{ E, v \}, \{ t \}, \{ f_X, f_Y, f_Z \} \}, Polygon[\{ n_1, n_2, n_3, n_4 \}] \} thin slab mode$
$\{ PLATE, \{ \{ E, \nu \}, \{ t \}, \{ f_X, f_Y, f_Z \} \}, Polygon[\{ n_1, n_2, n_3 \}] \} \ bending mode$
$\{SHELL, \{\{E, v\}, \{t\}, \{f_X, f_Y, f_Z\}\}, Polygon[\{n_1, n_2, n_3\}]\}plate$
Solid model
$\{SOLID, \{\{E, v\}, \{f_X, f_Y, f_Z\}\}\}, Tetrahedron[\{n_1, n_2, n_3, n_4\}]\}$ solid
$\{ SOLID, \{ \{E, v\}, \{f_X, f_Y, f_Z\} \}, Hexahedron[\{n_1, n_2, n_3, n_4, n_5, n_6, n_7, n_8\}] \} \ solid$
$\{SOLID, \{\{E,v\}, \{f_X, f_Y, f_Z, m_X, m_Y, m_Z, \}\}, Tetrahedron[\{n_1, n_2, n_3, n_4\}]\} \dots solid \}$
OPERATIONS
prb = REFINE[prb] refine structure representation
Out = FORMATTED[prb]display problem definition

 $\label{eq:out_state} Out = STANDARDFORM[\textit{prb}] display virtual work expression \\ sol = SOLVE[\{DISP\}, \textit{prb}] \mid SOLVE[\textit{prb}] solve the unknowns$

VIBRATION ANALYSIS

Constraint
${\rm JOINT}, {\} \{\{\underline{u}_X, \underline{u}_Y, \underline{u}_Z\}\}, Point[\{n_1\}]\}}$ displacement constraint
${JOINT, {}, Line[{n_1, n_2}]}$ displacement constraint
$\{RIGID, \{\} \{\{\underline{u}_X, \underline{u}_Y, \underline{u}_Z\}, \{\underline{\theta}_X, \underline{\theta}_Y, \underline{\theta}_Z\}\}, Point[\{n_1\}]\} \dots displacement/rotation constraint$
${RIGID,\{\},Line[\{n_1,n_2\}]\}}$ rigid constraint
$\{SLIDER, \{n_X, n_Y, n_Z\}, Point[\{n_1\}]\} \dots $ slider constraint
Force
$\{FORCE, \{F_X, F_Y, F_Z\}, Point[\{n_1\}]\} \dots point \ force$
$\{ FORCE, \{F_X, F_Y, F_Z, M_X, M_Y, M_Z\}, Point[\{n_1\}] \} \qquad point load$
$\{ \text{FORCE}, \{f_X, f_Y, f_Z\}, \text{Line}[\{n_1, n_2\}] \} \dots \dots \dots \dots \text{distributed force}$
$\{FORCE, \{f_X, f_Y, f_Z\}, Polygon[\{n_1, n_2, n_3\}]\} \dots $
$\{FORCE, \{\{m\}\}, Point[\{n_1\}]\}$ inertia effect
$\{FORCE, \{\{m, J\}\}, Point[\{n_1\}]\}$ inertia effect
$\{ FORCE, \{ \{m, J\}, \{ \{i_X, i_Y, i_Z\}, \{ j_X, j_Y, j_Z\} \} \} \}, Point[\{n_1\}] \} \qquad \dots \dots$
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Beam model
Beam model $\{\text{BAR}, \{\{E, \rho\}, \{A\}, \{f_X, f_Y, f_Z\}\}, \text{Line}[\{n_1, n_2\}]\} \dots bar \text{ mode}$
$\{ BAR, \{ \{E, \rho\}, \{A\}, \{f_X, f_Y, f_Z\} \}, Line[\{n_1, n_2\}] \} \ \\ bar \ mode$
$ \{ \text{BAR}, \{ \{ E, \rho \}, \{ A \}, \{ f_X, f_Y, f_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \\ = \{ \text{TORSION}, \{ \{ G, \rho \}, \{ J \}, \{ m_X, m_Y, m_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \\ = \{ \text{TORSION}, \{ m_X, m_Y, m_Z \} \} \\ = \{ \text{Line}[\{ n_1, n_2 \}] \} \\ = \{ \text{Line}[\{ n_1$
$ \{ \text{BAR}, \{ \{ E, \rho \}, \{ A \}, \{ f_X, f_Y, f_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \\ \qquad \qquad \qquad \text{bar mode} $ $ \{ \text{TORSION}, \{ \{ G, \rho \}, \{ J \}, \{ m_X, m_Y, m_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \\ \qquad \qquad \qquad \text{torsion mode} $ $ \{ \text{BEAM}, \{ \{ E, G, \rho \}, \{ A, I_{yy}, I_{zz} \}, \{ f_X, f_Y, f_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \\ \qquad \qquad \qquad \text{beam} $
$ \{ \text{BAR}, \{ \{ E, \rho \}, \{ A \}, \{ f_X, f_Y, f_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \qquad \qquad \text{bar mode} $ $ \{ \text{TORSION}, \{ \{ G, \rho \}, \{ J \}, \{ m_X, m_Y, m_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \qquad \qquad \text{torsion mode} $ $ \{ \text{BEAM}, \{ \{ E, G, \rho \}, \{ A, I_{yy}, I_{zz} \}, \{ f_X, f_Y, f_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \qquad \qquad \text{beam} $ $ \{ \text{BEAM}, \{ \{ E, G, \rho \}, \{ A, I_{yy}, I_{zz}, \{ j_X, j_Y, j_Z \} \}, \{ f_X, f_Y, f_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \qquad \qquad \text{beam} $
$ \{ \text{BAR}, \{ \{ E, \rho \}, \{ A \}, \{ f_X, f_Y, f_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \ \text{bar mode} $ $ \{ \text{TORSION}, \{ \{ G, \rho \}, \{ J \}, \{ m_X, m_Y, m_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \ \text{torsion mode} $ $ \{ \text{BEAM}, \{ \{ E, G, \rho \}, \{ A, I_{yy}, I_{zz} \}, \{ f_X, f_Y, f_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \ \text{beam} $ $ \{ \text{BEAM}, \{ \{ E, G, \rho \}, \{ A, I_{yy}, I_{zz}, \{ j_X, j_Y, j_Z \} \}, \{ f_X, f_Y, f_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \ \text{beam} $ $ \text{\textbf{Plate model} } $
$ \{ \text{BAR}, \{ \{ E, \rho \}, \{ A \}, \{ f_X, f_Y, f_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \qquad \qquad \text{bar mode} $ $ \{ \text{TORSION}, \{ \{ G, \rho \}, \{ J \}, \{ m_X, m_Y, m_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \qquad \qquad \text{torsion mode} $ $ \{ \text{BEAM}, \{ \{ E, G, \rho \}, \{ A, I_{yy}, I_{zz} \}, \{ f_X, f_Y, f_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \qquad \qquad \text{beam} $ $ \{ \text{BEAM}, \{ \{ E, G, \rho \}, \{ A, I_{yy}, I_{zz}, \{ j_X, j_Y, j_Z \} \}, \{ f_X, f_Y, f_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \qquad \qquad \text{beam} $ $ \mathbf{Plate \ model} $ $ \{ \text{PLANE}, \{ \{ E, \nu, \rho \}, \{ t \}, \{ f_X, f_Y, f_Z \} \}, \text{Polygon}[\{ n_1, n_2, n_3 \}] \} \qquad \qquad \text{thin slab mode} $
$ \{ \text{BAR}, \{ \{ E, \rho \}, \{ A \}, \{ f_X, f_Y, f_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \qquad \qquad \text{bar mode} $ $ \{ \text{TORSION}, \{ \{ G, \rho \}, \{ J \}, \{ m_X, m_Y, m_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \qquad \qquad \text{torsion mode} $ $ \{ \text{BEAM}, \{ \{ E, G, \rho \}, \{ A, I_{yy}, I_{zz} \}, \{ f_X, f_Y, f_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \qquad \qquad \text{beam} $ $ \{ \text{BEAM}, \{ \{ E, G, \rho \}, \{ A, I_{yy}, I_{zz}, \{ j_X, j_Y, j_Z \} \}, \{ f_X, f_Y, f_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \qquad \qquad \text{beam} $ $ \mathbf{Plate \ model} $ $ \{ \text{PLANE}, \{ \{ E, v, \rho \}, \{ t \}, \{ f_X, f_Y, f_Z \} \}, \text{Polygon}[\{ n_1, n_2, n_3, n_4 \}] \} \qquad \qquad \text{thin slab mode} $ $ \{ \text{PLANE}, \{ \{ E, v, \rho \}, \{ t \}, \{ f_X, f_Y, f_Z \} \}, \text{Polygon}[\{ n_1, n_2, n_3, n_4 \}] \} \qquad \qquad \text{thin slab mode} $
$ \{ \text{BAR}, \{ \{ E, \rho \}, \{ A \}, \{ f_X, f_Y, f_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \qquad \qquad \text{bar mode} $ $ \{ \text{TORSION}, \{ \{ G, \rho \}, \{ J \}, \{ m_X, m_Y, m_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \qquad \qquad \text{torsion mode} $ $ \{ \text{BEAM}, \{ \{ E, G, \rho \}, \{ A, I_{yy}, I_{zz} \}, \{ f_X, f_Y, f_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \qquad \qquad \text{beam} $ $ \{ \text{BEAM}, \{ \{ E, G, \rho \}, \{ A, I_{yy}, I_{zz}, \{ j_X, j_Y, j_Z \} \}, \{ f_X, f_Y, f_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \qquad \qquad \text{beam} $ $ \{ \text{Plate model} \} $ $ \{ \text{PLANE}, \{ \{ E, v, \rho \}, \{ t \}, \{ f_X, f_Y, f_Z \} \}, \text{Polygon}[\{ n_1, n_2, n_3 \}] \} \qquad \qquad \text{thin slab mode} $ $ \{ \text{PLANE}, \{ \{ E, v, \rho \}, \{ t \}, \{ f_X, f_Y, f_Z \} \}, \text{Polygon}[\{ n_1, n_2, n_3 \}] \} \qquad \qquad \text{bending mode} $ $ \{ \text{PLATE}, \{ \{ E, v, \rho \}, \{ t \}, \{ f_X, f_Y, f_Z \} \}, \text{Polygon}[\{ n_1, n_2, n_3 \}] \} \qquad \qquad \text{bending mode} $
$ \{ \text{BAR}, \{ \{ E, \rho \}, \{ A \}, \{ f_X, f_Y, f_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \qquad \qquad \text{bar mode} $ $ \{ \text{TORSION}, \{ \{ G, \rho \}, \{ J \}, \{ m_X, m_Y, m_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \qquad \qquad \text{torsion mode} $ $ \{ \text{BEAM}, \{ \{ E, G, \rho \}, \{ A, I_{yy}, I_{zz} \}, \{ f_X, f_Y, f_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \qquad \qquad \text{beam} $ $ \{ \text{BEAM}, \{ \{ E, G, \rho \}, \{ A, I_{yy}, I_{zz}, \{ j_X, j_Y, j_Z \} \}, \{ f_X, f_Y, f_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \qquad \qquad \text{beam} $ $ \{ \text{PLANE}, \{ \{ E, v, \rho \}, \{ t \}, \{ f_X, f_Y, f_Z \} \}, \text{Polygon}[\{ n_1, n_2, n_3 \}] \} \qquad \qquad \text{thin slab mode} $ $ \{ \text{PLANE}, \{ \{ E, v, \rho \}, \{ t \}, \{ f_X, f_Y, f_Z \} \}, \text{Polygon}[\{ n_1, n_2, n_3 \}] \} \qquad \qquad \text{bending mode} $ $ \{ \text{SHELL}, \{ \{ E, v, \rho \}, \{ t \}, \{ f_X, f_Y, f_Z \} \}, \text{Polygon}[\{ n_1, n_2, n_3 \}] \} \qquad \qquad \text{plate} $
$ \{ \text{BAR}, \{ \{ E, \rho \}, \{ A \}, \{ f_X, f_Y, f_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \qquad \qquad \text{bar mode} $ $ \{ \text{TORSION}, \{ \{ G, \rho \}, \{ J \}, \{ m_X, m_Y, m_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \qquad \qquad \text{torsion mode} $ $ \{ \text{BEAM}, \{ \{ E, G, \rho \}, \{ A, I_{yy}, I_{zz} \}, \{ f_X, f_Y, f_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \qquad \qquad \text{beam} $ $ \{ \text{BEAM}, \{ \{ E, G, \rho \}, \{ A, I_{yy}, I_{zz}, \{ j_X, j_Y, j_Z \} \}, \{ f_X, f_Y, f_Z \} \}, \text{Line}[\{ n_1, n_2 \}] \} \qquad \qquad \text{beam} $ $ \{ \text{PLANE}, \{ \{ E, v, \rho \}, \{ t \}, \{ f_X, f_Y, f_Z \} \}, \text{Polygon}[\{ n_1, n_2, n_3 \}] \} \qquad \qquad \text{thin slab mode} $ $ \{ \text{PLANE}, \{ \{ E, v, \rho \}, \{ t \}, \{ f_X, f_Y, f_Z \} \}, \text{Polygon}[\{ n_1, n_2, n_3 \}] \} \qquad \qquad \text{bending mode} $ $ \{ \text{SHELL}, \{ \{ E, v, \rho \}, \{ t \}, \{ f_X, f_Y, f_Z \} \}, \text{Polygon}[\{ n_1, n_2, n_3 \}] \} \qquad \qquad \text{plate} $ $ \text{Solid model} $

OPERATIONS

prb = REFINE[prb]	refine structure representation
Out = FORMATTED[prb]	display problem definition
Out = STANDARDFORM[{VIBR}, prb]	display virtual work expression
$sol = SOLVE[\{VIBR\}, prb]$	solve the eigenfrequencies and modes
sol = SOLVE[{VIBR,ini}, prb] solve the	e unknowns (does not work with DAEs)

STABILITY ANALYSIS

Constraint $\{JOINT, \{\} | \{\{u_X, u_Y, u_Z\}\}\}, Point[\{n_1\}]\} \dots displacement constraint$ $\{\text{JOINT}, \{\}, \text{Line}[\{n_1, n_2\}]\}$displacement constraint $\{RIGID, \{\} | \{\{\underline{u}_X, \underline{u}_Y, \underline{u}_Z\}, \{\underline{\theta}_X, \underline{\theta}_Y, \underline{\theta}_Z\}\}\}, Point[\{n_1\}]\} \dots displacement/rotation constraint$ $\{RIGID, \{\}, Line[\{n_1, n_2\}]\}$rigid constraint $\{SLIDER, \{n_X, n_Y, n_Z\}, Point[\{n_1\}]\}$ slider constraint **Force** $\{FORCE, \{F_X, F_Y, F_Z\}, Point[\{n_1\}]\}$point force $\{FORCE, \{F_X, F_Y, F_Z, M_X, M_Y, M_Z\}, Point[\{n_1\}]\}$point load $\{FORCE, \{f_X, f_Y, f_Z\}, Line[\{n_1, n_2\}]\}$distributed force $\{FORCE, \{f_X, f_Y, f_Z\}, Polygon[\{n_1, n_2, n_3\}]\}$distributed force Beam model $\{BAR, \{\{E\}, \{A\}, \{f_X, f_Y, f_Z\}\}\}, Line[\{n_1, n_2\}]\}$bar mode $\{TORSION, \{\{G\}, \{J\}, \{\{m_X, m_Y, m_Z\}\}\}\}, Line[\{n_1, n_2\}]\}$ torsion mode {BENDING, $\{E\}, \{I_v, I_z\}, \{f_X, f_Y, f_Z\}\}$, Line $[\{n_1, n_2\}]$ }.....bending mode {BEAM, $\{E,G\}, \{A,I_{yy},I_{zz}\}, \{f_X,f_Y,f_Z\}\}$, Line $[\{n_1,n_2\}]\}$beam {BEAM,{E,G},{ A,I_{yy},I_{zz} ,{ i_X,i_Y,i_Z }},{ f_X,f_Y,f_Z }},Line[n_1,n_2]}....beam Plate model $\{PLANE, \{\{E,v\}, \{t\}, \{f_X, f_Y, f_Z\}\}\}, Polygon[\{n_1, n_2, n_3\}]\} \dots$ thin slab mode $\{PLANE, \{\{E,v\}, \{t\}, \{f_X, f_Y, f_Z\}\}\}, Polygon[\{n_1, n_2, n_3, n_4\}]\} \dots$ thin slab mode $\{PLATE, \{\{E, v\}, \{t\}, \{f_X, f_Y, f_Z\}\}\}, Polygon[\{n_1, n_2, n_3\}]\} \dots$ bending mode $\{SHELL, \{\{E, v\}, \{t\}, \{f_X, f_Y, f_Z\}\}\}, Polygon[\{n_1, n_2, n_3\}]\}$plate Solid model $\{SOLID, \{\{E,v\}, \{f_X, f_Y, f_Z\}\}\}, Tetrahedron[\{n_1, n_2, n_3, n_4\}]\}$solid $\{SOLID, \{\{E,v\}, \{f_X, f_Y, f_Z\}\}\}, Hexahedron[\{n_1, n_2, n_3, n_4, n_5, n_6, n_7, n_8\}]\} \dots solid$ $\{SOLID, \{\{E,v\}, \{f_X, f_Y, f_Z, m_X, m_Y, m_Z, \}\}, Tetrahedron[\{n_1, n_2, n_3, n_4\}]\} \dots solid$ **OPERATIONS** prb = REFINE[prb] refine structure representation

Out = $FORMATTED[prb]$	display problem definition
Out = STANDARDFORM[{STA	AB}, prb]display virtual work expression
$sol = SOLVE[\{STAB, p\}, prb]$	find the critical values of p and the modes

NONLINEAR ANALYSIS

Constraint
$\{ JOINT, \{ \} \{ \{ \underline{u}_X, \underline{u}_Y, \underline{u}_Z \} \}, Point[\{n_1\}] \} \qquad \qquad displacement constraint$
${JOINT, {}, Line[{n_1, n_2}]}$
$\{\text{RIGID}, \{\} \{\{\underline{u}_X, \underline{u}_Y, \underline{u}_Z\}, \{\underline{\theta}_X, \underline{\theta}_Y, \underline{\theta}_Z\}\}, \text{Point}[\{n_1\}]\} \dots \text{displacement/rotation constraint}$
${RIGID,\{\},Line[\{n_1,n_2\}]\}}$ rigid constraint
$\{SLIDER, \{n_X, n_Y, n_Z\}, Point[\{n_1\}]\}$ slider constraint
Force
$\{FORCE, \{F_X, F_Y, F_Z\}, Point[\{n_1\}]\} \dots point \ force$
$\{ FORCE, \{F_X, F_Y, F_Z, M_X, M_Y, M_Z\}, Point[\{n_1\}] \} \qquad point load$
$\{FORCE, \{f_X, f_Y, f_Z\}, Line[\{n_1, n_2\}]\} \dots \\ distributed force$
$\{FORCE, \{f_X, f_Y, f_Z\}, Polygon[\{n_1, n_2, n_3\}]\} \\ \dots \\ distributed force$
Beam model
$\{ BAR, \{ \{E\}, \{A\}, \{f_X, f_Y, f_Z\} \}, Line[\{n_1, n_2\}] \} \ \\ bar \ mode$
Plate model
$\{ PLANE, \{ \{ E, v \}, \{ t \}, \{ f_X, f_Y, f_Z \} \}, Polygon[\{ n_1, n_2, n_3 \}] \} thin slab mode$
$\{PLANE, \{\{E,v\}, \{t\}, \{f_X, f_Y, f_Z\}\}, Polygon[\{n_1, n_2, n_3, n_4\}]\} \dots $ thin slab mode
Solid model
$\{ \text{SOLID}, \{ \{E, v\}, \{f_X, f_Y, f_Z\} \}, \text{Tetrahedron}[\{n_1, n_2, n_3, n_4\}] \} \dots \dots (\text{nonlinear}) \text{ solid}$
$\{ \text{SOLID}, \{ \{E, v\}, \{f_X, f_Y, f_Z\} \}, \text{Hexahedron} [\{n_1, n_2, n_3, n_4, n_5, n_6, n_7, n_8\}] \} \ \dots (\text{nonlinear}) \ \text{solid}$
$\{ \text{SOLID}, \{ \{E, v\}, \{f_X, f_Y, f_Z, m_X, m_Y, m_Z, \} \}, \text{Tetrahedron}[\{n_1, n_2, n_3, n_4\}] \} \ \dots (\text{nonlinear}) \ \text{solid}$
OPERATIONS
prb = REFINE[prb] refine structure representation
$Out = FORMATTED[{NONL}, prb]$ display problem definition
$Out = STANDARDFORM[\{NONL\}, prb] display virtual work expression$
$sol = SOLVE[{NONL}, prb]$ find the likely numerical solution
$sol = SOLVE[{NONL,ALL}, prb]$ find all solutions

THERMO-MECHANICAL ANALYSIS

Constraint $\{\text{JOINT}, \{\} | \{\{u_X, u_Y, u_Z\}\}, \text{Point}[\{n_1\}]\} \dots displacement constraint}$ $\{\text{JOINT}, \{\}, \text{Line}[\{n_1, n_2\}]\}$displacement constraint $\{RIGID, \{\} | \{\{\underline{u}_X, \underline{u}_Y, \underline{u}_Z\}, \{\underline{\theta}_X, \underline{\theta}_Y, \underline{\theta}_Z\}\}, Point[\{n_1\}]\} \dots displacement/rotation constraint$ $\{RIGID, \{\}, Line[\{n_1, n_2\}]\}$rigid constraint $\{SLIDER, \{n_X, n_Y, n_Z\}, Point[\{n_1\}]\}$ slider constraint **Force** $\{FORCE, \{F_X, F_Y, F_Z\}, Point[\{n_1\}]\}$ point force $\{\mathsf{FORCE}, \{F_X, F_Y, F_Z, M_X, M_Y, M_Z\}, \mathsf{Point}[\{n_1\}]\} \ \dots \dots \mathsf{point} \ \mathsf{load}$ $\{FORCE, \{f_X, f_Y, f_Z\}, Line[\{n_1, n_2\}]\}$distributed force $\{FORCE, \{f_X, f_Y, f_Z\}, Polygon[\{n_1, n_2, n_3\}]\}$distributed force Beam model $\{BAR, \{\{E, \alpha, k\}, \{A\}, \{\{f_X, f_Y, f_Z\}, \{s, \mathcal{G}_0\}\}\}\}, Line[\{n_1, n_2\}]\}$bar mode Plate model $\{ \text{PLANE}, \{ \{ E, v, \alpha, k \}, \{ t \}, \{ \{ f_X, f_Y, f_Z \}, \{ s, \mathcal{G}_0 \} \} \}, \\ \text{Polygon}[\{ n_1, n_2, n_3 \}] \} \ \dots \dots \text{ thin slab mode}$ $\{PLANE, \{\{E, v, \alpha, k\}, \{t\}, \{\{f_X, f_Y, f_Z\}, s, \mathcal{S}_0\}\}, Polygon[\{n_1, n_2, n_3, n_4\}]\} \dots$ thin slab mode Solid model $\{SOLID, \{\{E, v, \alpha, k\}, \{\{f_X, f_Y, f_Z\}, \{s, \mathcal{G}_0\}\}\}\}, Tetrahedron[\{n_1, n_2, n_3, n_4\}]\} \dots solid$ **Functions** *prb* = REFINE[*prb*] refine structure representation

 $sol = SOLVE[\{TMEC\}, prb]$ solve the unknowns