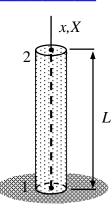
## **Assignment 2**

Assuming that node 1 of the bar shown is fixed, derive the expression of the axial displacement  $u_{X2}(t)$  at the free end for t > 0. The initial conditions at t = 0 are  $u_{X2}(0) = 0$  and  $\dot{u}_{X2}(0) = V$ .



## **Solution template**

Virtual work expression of internal and inertia forces of the bar model is given by

$$\delta W = -\begin{cases} \delta u_{x1} \\ \delta u_{x2} \end{cases}^{\mathrm{T}} \left( \frac{EA}{h} \begin{bmatrix} 1 & -1 \\ -1 & 1 \end{bmatrix} \begin{cases} u_{x1} \\ u_{x2} \end{cases} + \frac{\rho Ah}{6} \begin{bmatrix} 2 & 1 \\ 1 & 2 \end{bmatrix} \begin{Bmatrix} \ddot{u}_{x1} \\ \ddot{u}_{x2} \end{Bmatrix} \right)$$

in which A is the cross-sectional area, E is the Young's modulus, and  $\rho$  is the density of the material. In terms of the displacement components of the structural coordinate system

$$\delta W = -\left\{ \begin{array}{c|c} & \\ \end{array} \right\}^{\mathrm{T}} \left( \frac{EA}{L} \begin{bmatrix} 1 & -1 \\ -1 & 1 \end{bmatrix} \left\{ \begin{array}{c} \\ \end{array} \right\} + \frac{\rho AL}{6} \begin{bmatrix} 2 & 1 \\ 1 & 2 \end{bmatrix} \left\{ \begin{array}{c} \\ \end{array} \right\} \right).$$

$$\delta W = -\delta u_{X2}(\underline{\hspace{1cm}})$$

Initial value problem, consisting of an ordinary differential equation (implied by the virtual work expression) and initial conditions, is given by

$$\ddot{u}_{X2} + \underline{\qquad} u_{X2} = 0 \qquad t > 0,$$

$$u_{X2} = 0$$
 and  $\dot{u}_{X2} = V$   $t = 0$ .

Expression  $u_{X2}(t) = A\sin(\omega t)$ , which describes a harmonic periodic motion, satisfies all the equations with selections

$$\omega =$$
 and  $A =$  .