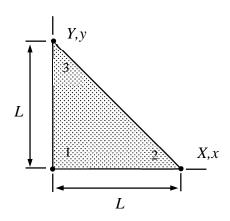
Assignment 2

Consider the temperature distribution in the structure shown which is composed of one triangle element. Assuming that the thermal conductivity k and thickness t of the element are constants, derive the element contribution $\delta P^{\rm int}$. Temperature at nodes 1 and 2 is known to be \mathcal{G}° and the unknown nodal temperature is \mathcal{G}_3 .



Solution template

In stationary thermo-elasticity, the variational densities of the thin slab mode of the plate model

$$\delta p_{\Omega}^{\text{int}} = - \begin{cases} \frac{\partial \delta \theta}{\partial x} & \text{otherwise} \\ \frac{\partial \delta \theta}{\partial y} & \text{otherwise} \end{cases}^{\text{T}} kt \begin{cases} \frac{\partial \theta}{\partial x} & \text{otherwise} \\ \frac{\partial \theta}{\partial y} & \text{otherwise} \end{cases}, \ \delta p_{\Omega}^{\text{ext}} = \delta \theta s$$

represent the energy balance. Linear shape functions of the temperature approximation can be deduced from the figure

Approximation to $\mathcal{G}(x, y)$ and its variation $\mathcal{S}\mathcal{G}(x, y)$ (notice that the variation of a given quantity vanishes)

$$\mathcal{G} = \underline{\hspace{1cm}}, \quad \frac{\partial \mathcal{G}}{\partial x} = \underline{\hspace{1cm}}, \quad \frac{\partial \mathcal{G}}{\partial y} = \underline{\hspace{1cm}},$$

$$\delta \theta = \underline{\hspace{1cm}}, \ \frac{\partial \delta \theta}{\partial x} = \underline{\hspace{1cm}}, \ \frac{\partial \delta \theta}{\partial y} = \underline{\hspace{1cm}}.$$

When the approximation is substituted there, the variational density simplifies to

$$\delta p_{\rm O}^{\rm int} =$$

Integration over the element gives

$$\delta P^{\rm int} = \int_{\Omega} \delta p_{\Omega}^{\rm int} dA = \underline{\qquad}.$$