

COE-C2004 - Materials Science and Engineering

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Ductile Fracture

Definition of Damage

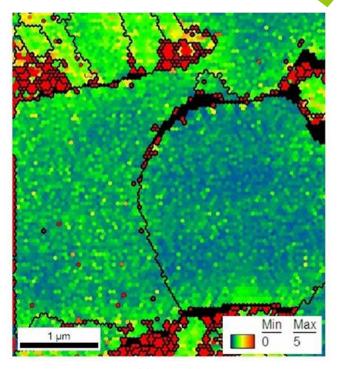


Fracture of pressure vessel

Fracture: Separation of a body into two or more pieces in response to a load.

Damage: microstructure develops an irreversible degradation on a given length scale.

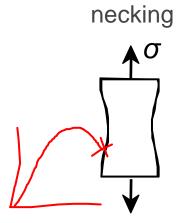
e.g. void formation



Microvoids



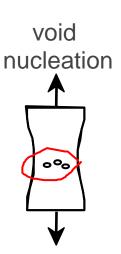
Stages of Moderately Ductile Failure



Electron micrographs of fracture surfaces (steel)

Acorn

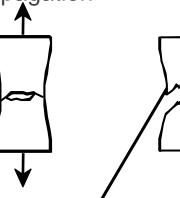
particles serve as void nucleation sites.



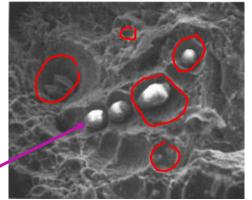




crack propagation



fracture



From V.J. Colangelo and F.A. Heiser, *Analysis of Metallurgical Failures* (2nd ed.), Fig. 11.28, p. 294, John Wiley and Sons, Inc., 1987. (Orig. source: P. Thornton, *J. Mater. Sci.*, Vol. 6, 1971, pp. 347-56.)

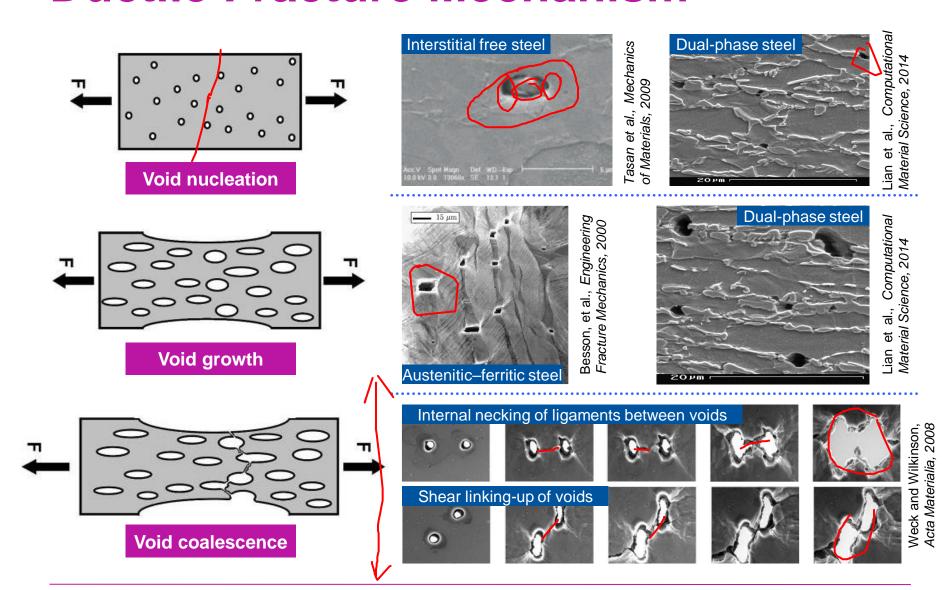


Fracture surface of tire cord wire loaded in tension. Courtesy of F. Roehrig, CC Technologies, Dublin, OH. Used with permission.

cup and cone fracture surface



Ductile Fracture Mechanism



Void coalescence

Secondary pores

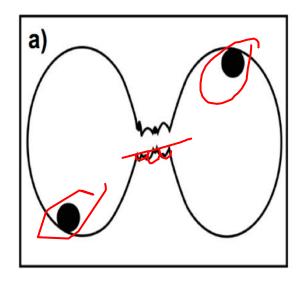
Formation of a second pore population in between bigger primary pores, mostly at hard particles of small size

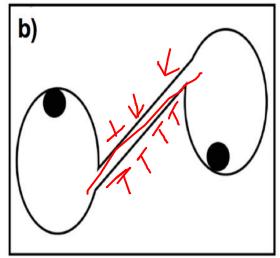
Shear bands

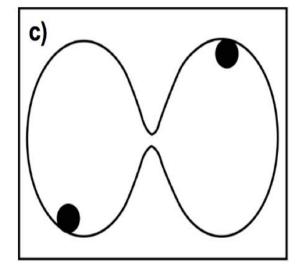
Formation of shear bands in between to primary pores due to strain localization

Coagulation

Coalescence of two primary pores which are close by



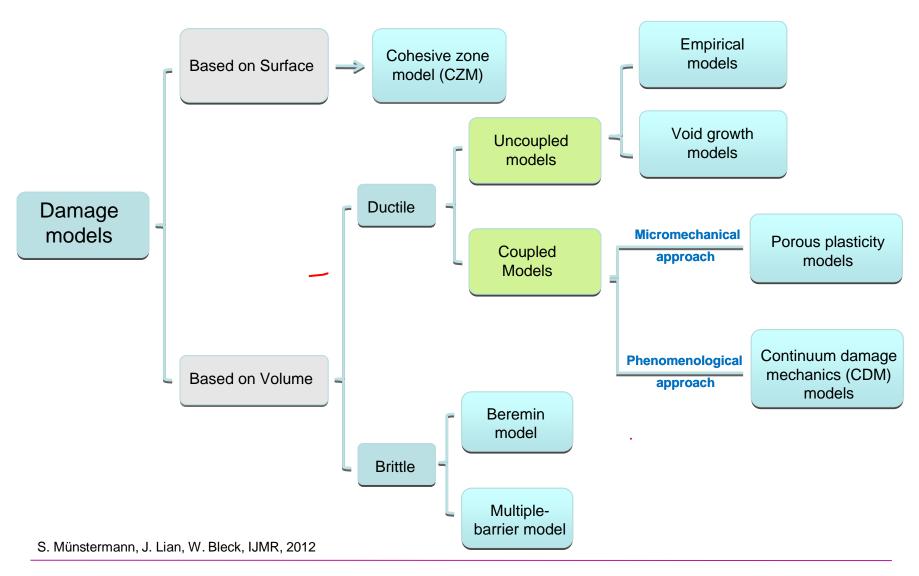




Ductile Fracture Modeling

(Seminar)

Quantify Ductile Fracture – Damage Mechanics





Damage measurement for Copper

Lemaitre, Nuclear Engineering and Design, 1984

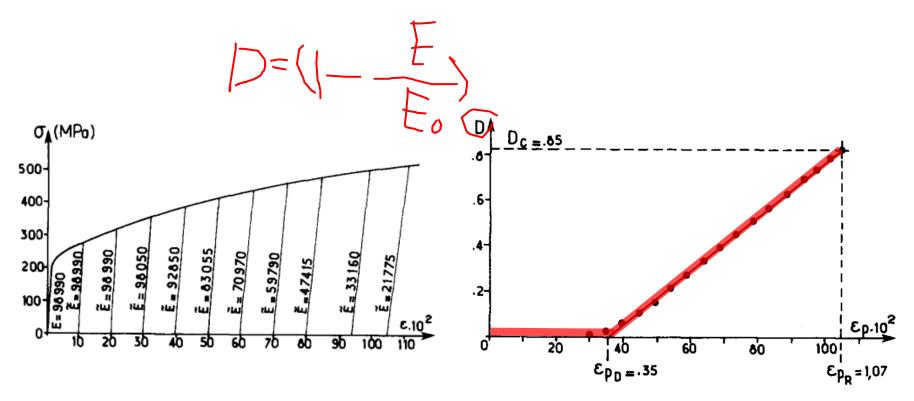
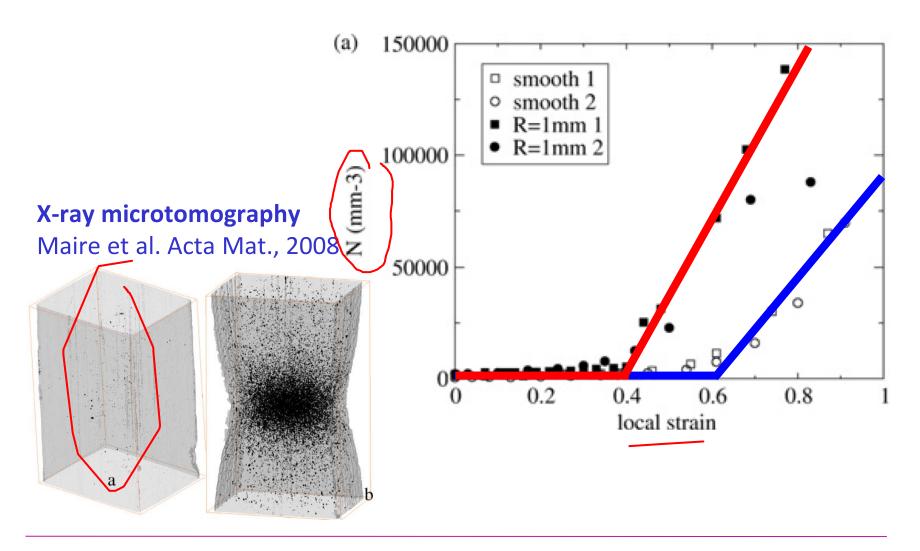


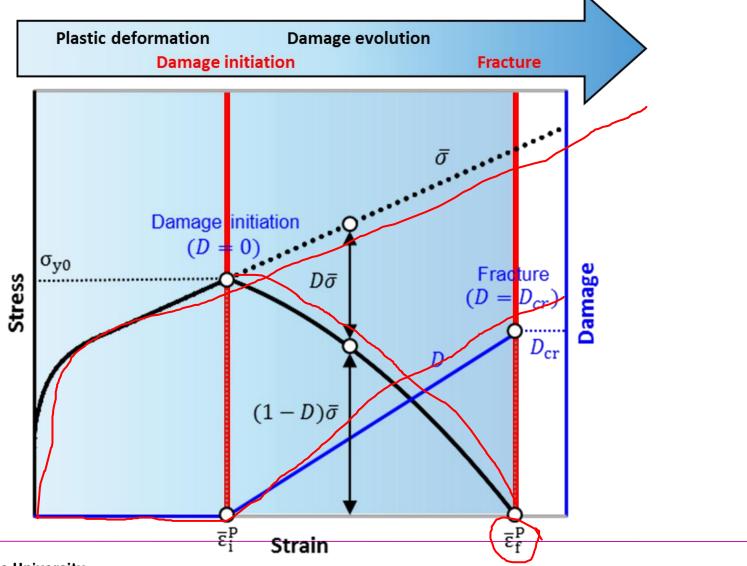
Fig. 2. Ductile plastic damage of copper 99.9%.

Damage measurement in DP600

Landron et al., Scripta Mat., 2010

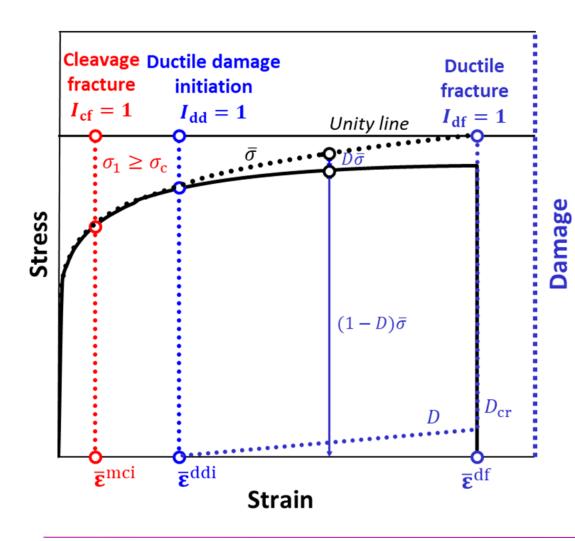


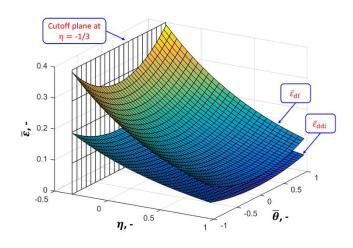
A hybrid damage mechanics model Lian et al., Int. J. Damage Mech., 2013 & 2015





Extension of the model





- Non-proportional loadings
 Wu, Lian, et al., FFEMS, 2017
- Cleavage fracture
 He, Lian et al., EFM, 2017
- Non-local formulation
 Aravas, Lian et al., IJSS, 2019
- Dynamic loading

Liu, Lian et al., IJMS, 2020

Constitutive equations



Elastoplastic deformation

Elastoplastic strain split:

$$\dot{\boldsymbol{\varepsilon}} = \dot{\boldsymbol{\varepsilon}}^{e} + \dot{\boldsymbol{\varepsilon}}^{p}$$

Elastic law:

$$\sigma = (1 - D)\mathbf{C}: \mathbf{\varepsilon}^{\mathrm{e}}$$

Yield criterion:

$$\Phi = \overline{\sigma} - (1 - D) \cdot \sigma_{v} \left(\overline{\varepsilon}^{p}, \dot{\overline{\varepsilon}}^{p} \right) \cdot f(T) \cdot f(\overline{\theta}) \leq 0$$

$$\sigma_{\mathbf{y}}\!\left(\overline{\boldsymbol{\varepsilon}}^{\mathbf{p}},\dot{\overline{\boldsymbol{\varepsilon}}}\right) = \sigma_{\mathbf{y}}\!\left(\overline{\boldsymbol{\varepsilon}}^{\mathbf{p}}\right) \cdot \left(1 + c_{1}^{\dot{\overline{\boldsymbol{\varepsilon}}}} \cdot \ln \frac{\dot{\overline{\boldsymbol{\varepsilon}}}^{p}}{\dot{\overline{\boldsymbol{\varepsilon}}}_{0}}\right) + c_{2}^{\dot{\overline{\boldsymbol{\varepsilon}}}} \cdot \overline{\sigma}_{0}\left(\dot{\overline{\boldsymbol{\varepsilon}}}^{p} - 1\right)$$

$$f(T) = c_1^T \cdot \exp(c_2^T \cdot T) + c_3^T$$

$$f(\overline{\theta}) = \left[c_{\theta}^{s} + (c_{\theta}^{ax} - c_{\theta}^{s}) \cdot \left(\omega - \frac{\omega^{m+1}}{m+1}\right)\right]$$

$$\omega = \frac{\sqrt{3}}{2 - \sqrt{3}} \left[\sec\left(\frac{\overline{\theta}\pi}{6}\right) - 1 \right]$$

- Flow rule: $\dot{\mathbf{\epsilon}}^{p} = \dot{\gamma} \frac{\partial \Phi}{\partial \sigma}$

Cleavage fracture initiation

Cleavage fracture initiation:

$$(\cdot)_{\text{avg}} = \frac{1}{\bar{\varepsilon}^{p}} \int_{0}^{\bar{\varepsilon}^{p}} (\cdot) (\bar{\varepsilon}^{p}) d\bar{\varepsilon}^{p}$$

$$\bar{\varepsilon}^{\mathrm{mci}} \big(\eta_{\mathrm{avg}}, \bar{\theta}_{\mathrm{avg}} \big) = f \big(\eta_{\mathrm{avg}}, \bar{\theta}_{\mathrm{avg}} \big)$$

$$f(\eta_{\text{avg}}, \bar{\theta}_{\text{avg}}) = [C_1 e^{-C_2 \eta} - C_3 e^{-C_4 \eta}] \bar{\theta}^2 + C_3 e^{-C_4 \eta}$$

Cleavage fracture initiation indicator:

$$I_{\rm cf} = \int_0^{\bar{\varepsilon}^{\rm p}} \frac{\mathrm{d}\bar{\varepsilon}^{\rm p}}{\bar{\varepsilon}^{\rm mci}(\eta_{\rm avg}, \bar{\theta}_{\rm avg})}$$

Ductile damage initiation

Ductile damage initiation:

$$\bar{\varepsilon}^{\text{ddi}}(\eta_{\text{avg}}, \bar{\theta}_{\text{avg}}) = \begin{cases} +\infty & \text{for } \eta \leq \eta_{\text{c}} \\ g(\eta_{\text{avg}}, \bar{\theta}_{\text{avg}}) & \text{for } \eta > \eta_{\text{c}} \end{cases}$$

$$g(\eta_{\text{avg}}, \bar{\theta}_{\text{avg}}) = [D_1 e^{-D_2 \eta} - D_3 e^{-D_4 \eta}] \bar{\theta}^2 + D_3 e^{-D_4 \eta}$$

Ductile damage initiation indicator:

$$I_{\rm dd} = \int_0^{\bar{\varepsilon}^{\rm p}} \frac{\mathrm{d}\bar{\varepsilon}^{\rm p}}{\bar{\varepsilon}^{\rm ddi}(\eta_{\rm avg}, \bar{\theta}_{\rm avg})}$$

Characteristic strain @ ddi for non-proportional loading:

$$\bar{\varepsilon}_{c}^{\mathrm{ddi}} = \bar{\varepsilon}^{\mathrm{p}}(I_{\mathrm{dd}} = 1)$$

Ductile fracture

Critical ductile damage accumulation function:

$$D_{\rm cr}(\eta_{\rm avg}, \bar{\theta}_{\rm avg}) = \begin{cases} +\infty & \text{for } \eta \leq \eta_{\rm c} \\ h(\eta_{\rm avg}, \bar{\theta}_{\rm avg}) & \text{for } \eta > \eta_{\rm c} \end{cases}$$

$$h(\eta_{\text{avg}}, \bar{\theta}_{\text{avg}}) = [E_1 e^{-E_2 \eta} - E_3 e^{-E_4 \eta}] \bar{\theta}^2 + E_3 e^{-E_4 \eta}$$

Ductile damage propagation rule:

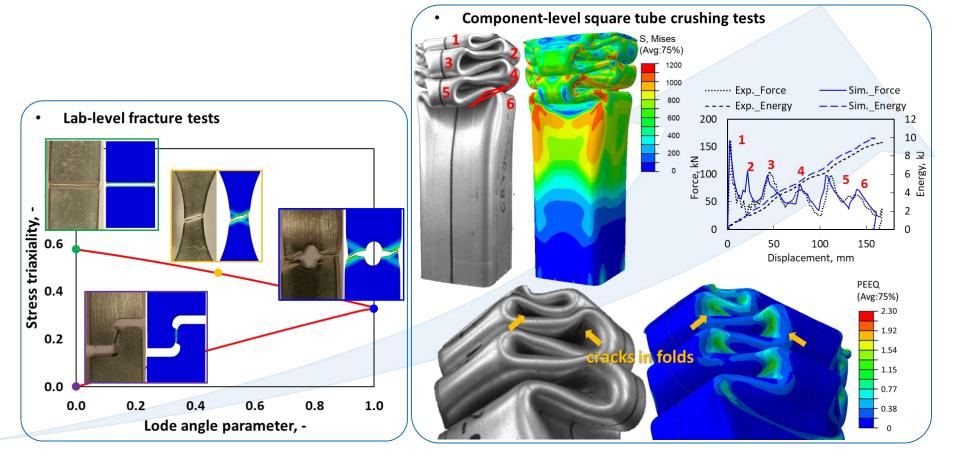
$$P_{\rm dd} = \int_{\bar{\varepsilon}_{\rm c}^{\rm ddi}}^{\bar{\varepsilon}^{\rm p}} \frac{\sigma_{\rm yi}/G_{\rm f}}{D_{\rm cr}(\eta_{\rm avg}, \bar{\theta}_{\rm avg})} \, \mathrm{d}\bar{\varepsilon}^{\rm p}$$

Ductile & cleavage interaction

Cleavage and ductile damage:

$$D = \begin{cases} 0 & \text{for } I_{\text{cf}} < 1 \land I_{\text{dd}} < 1 \\ 0 & \text{for } I_{\text{cf}} \ge 1 \land \sigma_1 < \sigma_c \land I_{\text{dd}} < 1 \\ 1 & \text{for } I_{\text{cf}} \ge 1 \land \sigma_1 \ge \sigma_c \land I_{\text{dd}} < 1 \\ P_{\text{dd}} & \text{for } I_{\text{dd}} \ge 1 \land P_{\text{dd}} < 1 \\ 1 & \text{for } I_{\text{dd}} \ge 1 \land P_{\text{dd}} \ge 1 \end{cases}$$

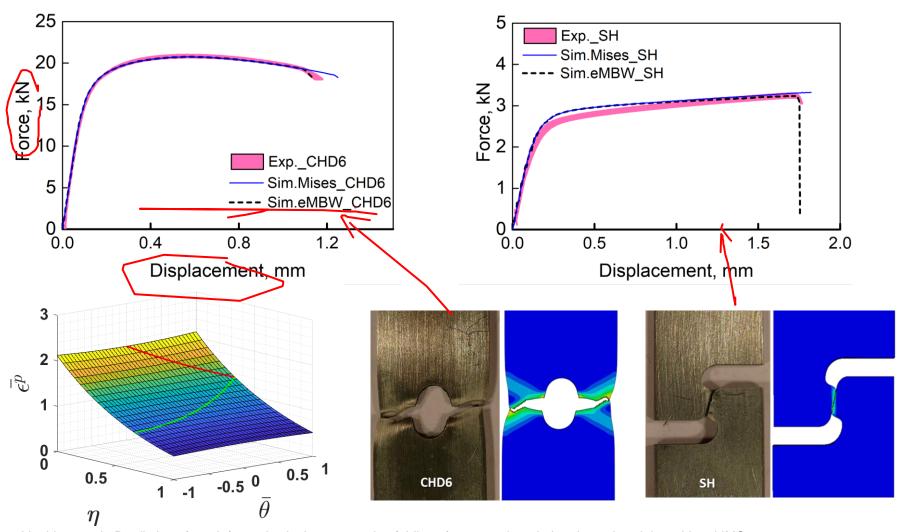
Case study: crashworthiness prediction



Liu, Lian, et al., Prediction of crack formation in the progressive folding of square tubes during dynamic axial crushing, IJMS, 2020

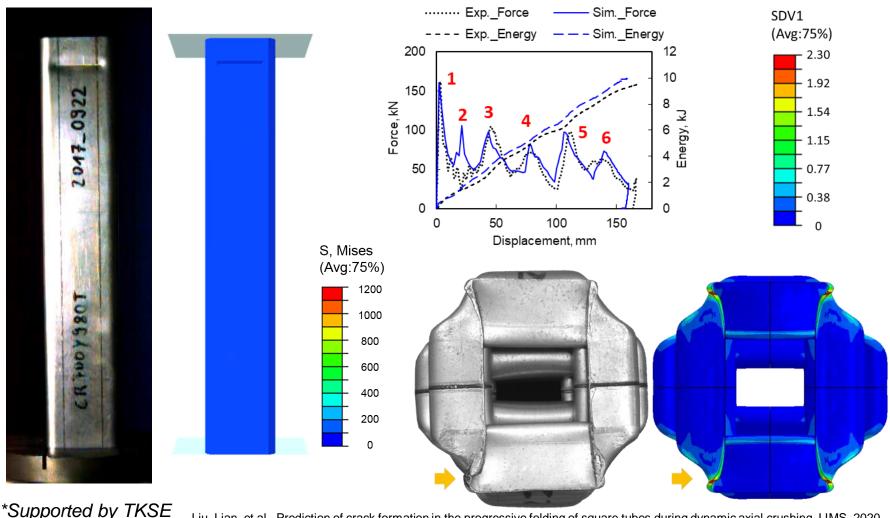


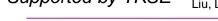
Fracture parameters calibration



Liu, Lian, et al., Prediction of crack formation in the progressive folding of square tubes during dynamic axial crushing, IJMS, 2020

Model application – prediction of crack formation during tube crushing

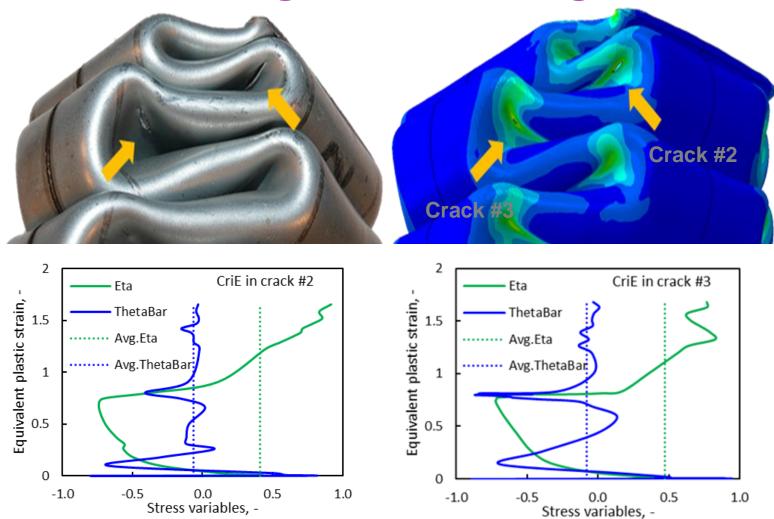




Liu, Lian, et al., Prediction of crack formation in the progressive folding of square tubes during dynamic axial crushing, IJMS, 2020



Model application – prediction of crack formation during tube crushing



Liu, Lian, et al., Prediction of crack formation in the progressive folding of square tubes during dynamic axial crushing, IJMS, 2020



- Elastoplastic strain split: $\dot{\mathbf{\epsilon}} = \dot{\mathbf{\epsilon}}^e + \dot{\mathbf{\epsilon}}^p$
- Elastic law: $\sigma = (1 D)C$: ε^e
- Yield criterion: $\Phi = \left(\frac{\sigma_V}{\sigma_V}\right)^2 + 2 \cdot q_1 \cdot f^* \cdot \cosh\left(\frac{3}{2} \cdot q_2 \cdot \frac{\sigma_H}{\sigma_V}\right) \left(1 + q_3 \cdot f^{*2}\right) = 0$
- Flow rule: $\dot{\boldsymbol{\varepsilon}}^{\mathrm{p}} = \dot{\gamma} \frac{\partial \Phi}{\partial \boldsymbol{\sigma}}$
- Damage evolution: $\dot{f} \neq \dot{f}_{GROWTH} + \dot{f}_{NUCLEATION}$ $f(t_0) = f_0$
- Loading/unloading condition :

$$\dot{\gamma} \ge 0$$
; $\Phi \le 0$; $\dot{\gamma}\Phi = 0$



Modified von Mises yield potential:

$$\Phi_{GTN} = \left(\frac{\sigma_{v}}{\sigma_{y}}\right)^{2} + 2 \cdot \underbrace{q_{1}} \cdot f^{*} \cosh\left(\frac{3}{2} \cdot \underbrace{q_{2}} \cdot \frac{\sigma_{H}}{\sigma_{y}}\right) - \left(1 + \underbrace{q_{3}} \cdot f^{*2}\right) = 0$$

Notation

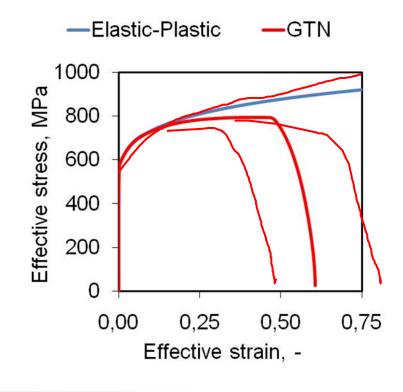
q₁, q₂, q₃: parameter for description of yield locus curve

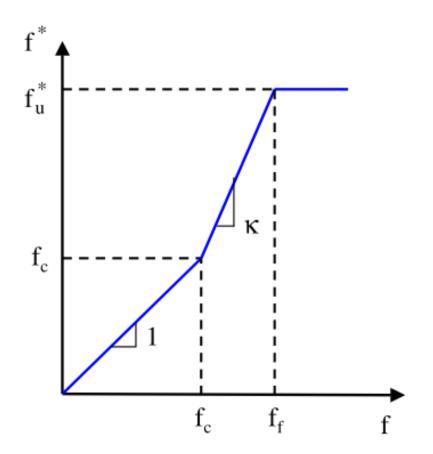
f*: from the calculated void volume f modified void volume f*

 σ_H : hydrostatic stress

 σ_{V} : von Mises effective stress

 σ_{v} : flow stress of matrix material





$$f^*(f) = \begin{cases} f; & f \leq f_c \\ f_c + \kappa(f - f_c); & f > f_c \end{cases}$$

f _c	Critical void volume fraction
K	Factor of accelerated void growth

$$\dot{f} = \dot{f}_{GROWTH} + \dot{f}_{NUCLEATION} \quad \text{with} \quad f(t_0) = f_0$$

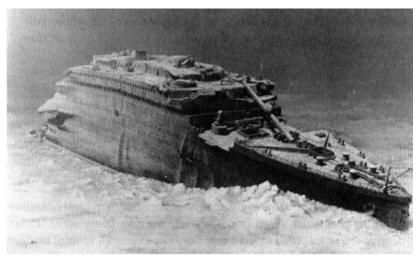
$$\dot{f}_{GROWTH} = (1 - f) \cdot \dot{\varepsilon}_{kk}^{pl} \qquad \dot{f}_{NUCLEATION} = \frac{f_N}{S_N \cdot \sqrt{2\pi}} \cdot \exp\left[-\frac{1}{2} \left(\frac{\bar{\varepsilon}^{pl} - \varepsilon_N}{S_N}\right)^2\right] \cdot \dot{\bar{\varepsilon}}^{pl}$$

Material dependent GTN-parameters		
f_0	Initial void volume fraction	
f _N	Volume fraction of secondary voids	
ϵ_{N}	Characteristic plastic strain of secondary void nucleation	
S _N	Standard deviation of ε _N	
q_1, q_2, q_3	Model parameter by Tvergaard and Needleman	
f _c	Critical void volume fraction	
K	Factor of accelerated void growth	

Brittle to Ductile Transition

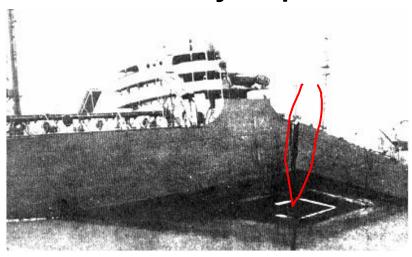
Brittle Fracture of Ductile Materials

Pre-WWII: The Titanic



Reprinted w/ permission from R.W. Hertzberg, "Deformation and Fracture Mechanics of Engineering Materials", (4th ed.) Fig. 7.1(a), p. 262, John Wiley and Sons, Inc., 1996. (Orig. source: Dr. Robert D. Ballard, *The Discovery of the Titanic.*)

WWII: Liberty ships



Reprinted w/ permission from R.W. Hertzberg, "Deformation and Fracture Mechanics of Engineering Materials", (4th ed.) Fig. 7.1(b), p. 262, John Wiley and Sons, Inc., 1996. (Orig. source: Earl R. Parker, "Behavior of Engineering Structures", Nat. Acad. Sci., Nat. Res. Council, John Wiley and Sons, Inc., NY, 1957.)

 Ships failed in a brittle manner though constructed of steel that, from tension tests, is normally ductile

Testing Ductile Materials for Brittle Failure

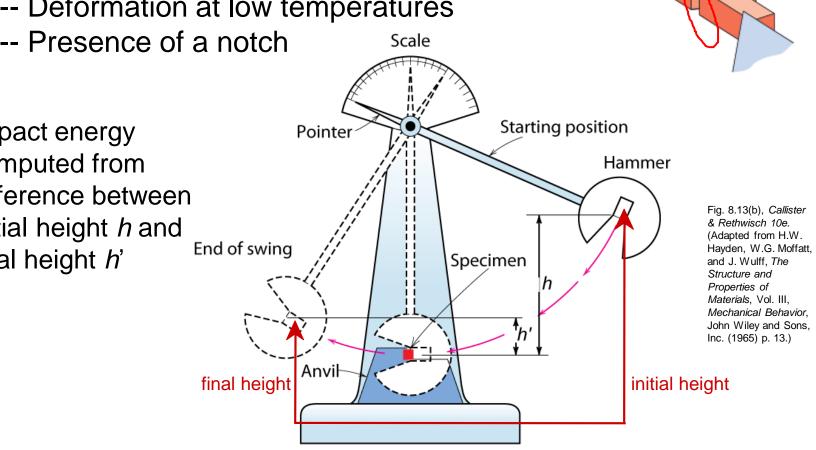
Impact Test

Test conditions promoting brittle fracture:

-- High strain rate

-- Deformation at low temperatures

Impact energy computed from difference between initial height h and final height h'



Charpy)



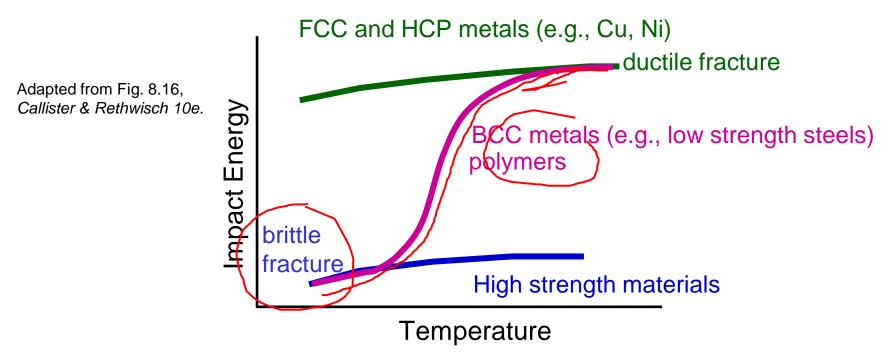
Testing Ductile Materials for Brittle Failure



https://youtu.be/tpGhqQvftAo

Influence of T on Impact Energy

- When impact tests conducted as function of temperature three kinds of behavior observed for metals
- Some BCC metals exhibit <u>Ductile-to-Brittle Transition</u> Temperature (DBTT)



Metals having DBTT should only be used at temperatures where ductile.



Fatigue

Fatigue loading and testing



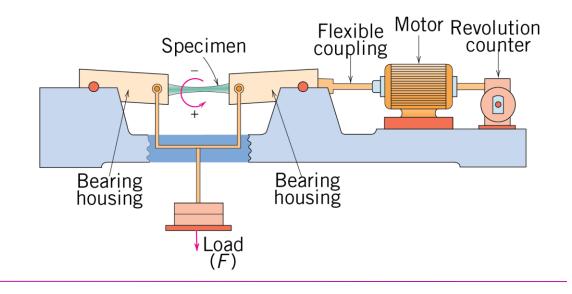
https://youtu.be/LhUclxBUV E

Fatigue Failure

- Fatigue = failure under lengthy period of repeated stress or strain cycling
- Stress varies with time.
 - -- key parameters are S, (m, m) and cycling frequency
- Key points: Fatigue... ←
 - --can cause part failure, even though applied stress $\sigma_{\text{max}} < \sigma_y$.
 - --responsible for ~ 90% of mechanical engineering failures.

Schematic diagram of an apparatus for performing rotatingbending fatigue tests

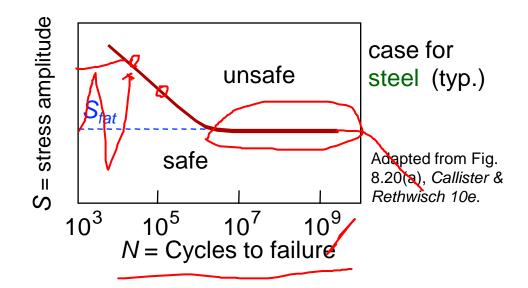
Adapted from Fig. 8.19(a), Callister & Rethwisch 10e.

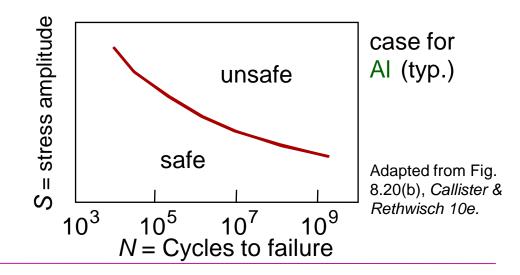




Fatigue Types

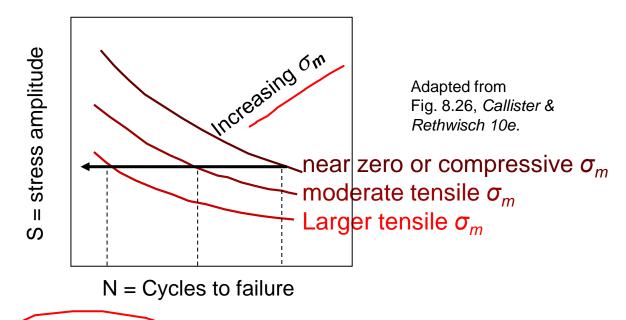
- Fatigue data plotted as stress amplitude S vs. log of number N of cycles to failure.
- Two types of fatigue behavior observed
 - Fatigue limit, S_{fat} : no fatigue if $S < S_{fat}$
 - For some materials, there is no fatigue limit!
 - Fatigue Life N_f = total number of stress cycles to cause fatigue failure at specified stress amplitude





Improving Fatigue Life

- Three general techniques to improve fatigue life
 - 1. Reducing magnitude of mean stress
 - Surface treatments
 - 3. Design changes



Decreasing mean stress increases fatigue life

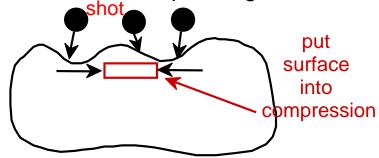


Improving Fatigue Life

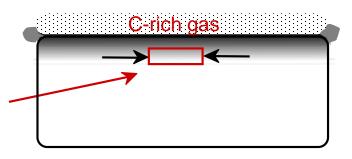
- Three general techniques to improve fatigue life
 - 1. Reducing magnitude of mean stress
 - Surface treatments
 - 3. Design changes

Imposing compressive surface stresses increases surface hardness – suppresses surface cracks from growing

--Method 1: shot peening



surface compressive stress due to plastic deformation of outer surface layer --Method 2: carburizing

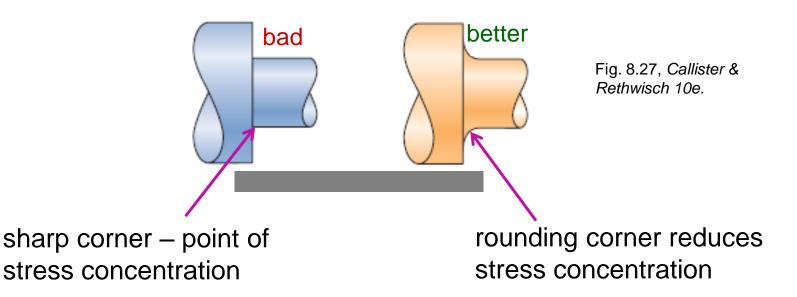


surface compressive stress due to carbon atoms diffusing into outer surface layer

Improving Fatigue Life

- Three general techniques to improve fatigue life
 - 1. Reducing magnitude of mean stress
 - Surface treatments
 - 3. Design changes

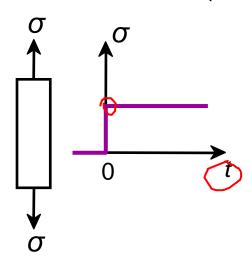
Remove stress concentrators



Creep

Creep

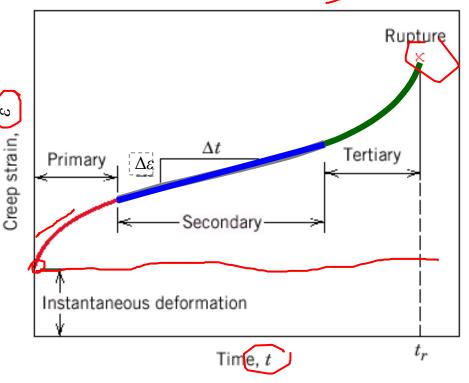
Measure deformation (strain) vs. time at constant stress



Stages of Creep

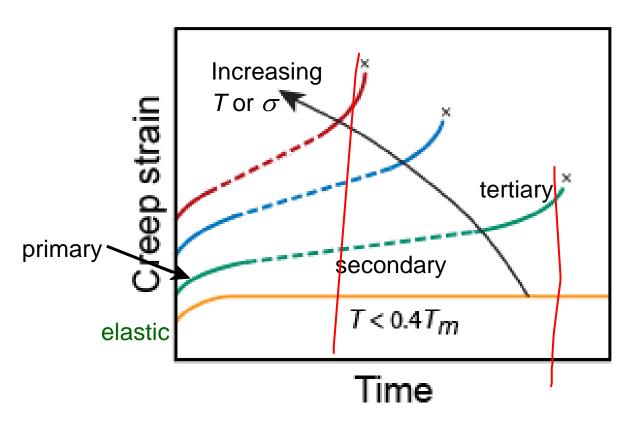
- Primary Creep: slope (creep rate) decreases with time.
- Secondary Creep: steady-state i.e., constant slope $(\Delta \varepsilon / \Delta t)$.
- Tertiary Creep: slope (creep rate)
 increases with time, i.e. acceleration of rate.

Occurs at elevated temperature for most metals, $T > 0.4 T_m$ (in K)



Adapted from Fig. 8.30, Callister & Rethwisch 10e.

Creep: Temperature Dependence



Figs. 8.31, Callister & Rethwisch 10e.

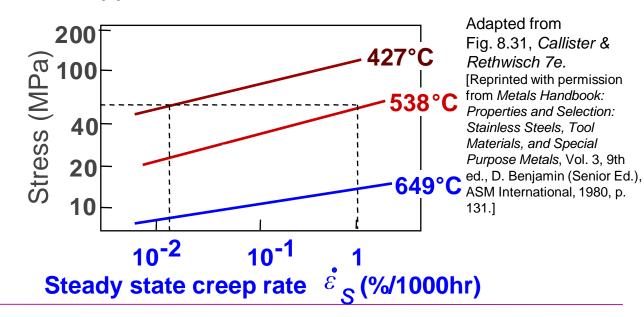
- Steady-state creep rate $(\dot{\varepsilon}_s)$ increases with increasing T and σ
- Rupture lifetime (t_r) decreases with increasing T and σ

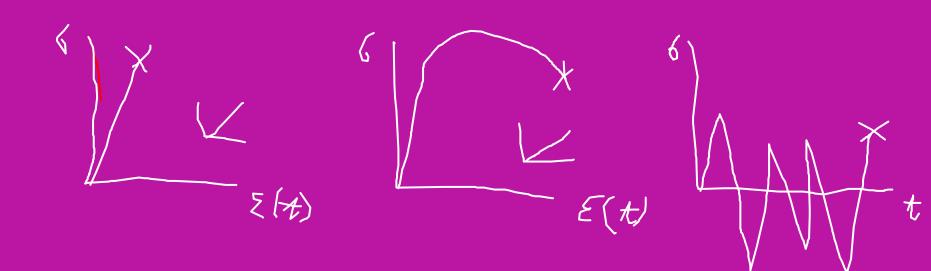
Steady-State Creep Rate

- $\dot{\mathcal{E}}$ constant for constant T, σ
 - --s strain hardening is balanced by recovery
 - -- dependence of steady-state creep rate on T, σ

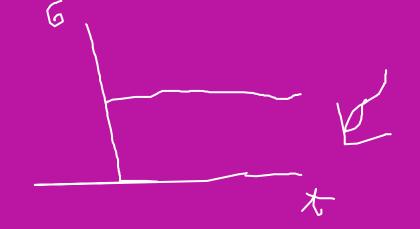
stress exponent (material parameter) $\dot{\varepsilon}_s = K_2 \sigma^n \exp\left(-\frac{Q_c}{RT}\right) \quad \text{activation energy for creep}$ material const. applied stress

Steady-state
 creep rate
 increases
 with increasing
 T, σ





Corrosion



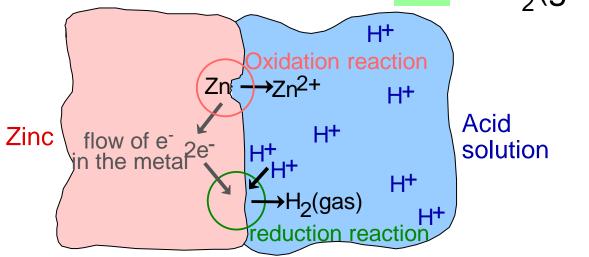
Electrochemical Corrosion

Ex: consider the corrosion of zinc in an acid solution

Two reactions are necessary:

-- oxidation reaction:
$$Zn \rightarrow Zn^{2+} + 2e^{-}$$

-- reduction reaction: $2H^+ + 2e^- \rightarrow H_2(gas)$



Other reduction reactions in solutions with dissolved oxygen:

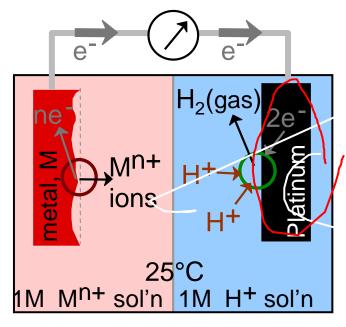
$$O_2 + 4H^+ + 4e^- \rightarrow 2H_2O$$

$$O_2 + 2H_2O + 4e^- \rightarrow 4(OH)^-$$

Standard Hydrogen Electrode

Two outcomes:

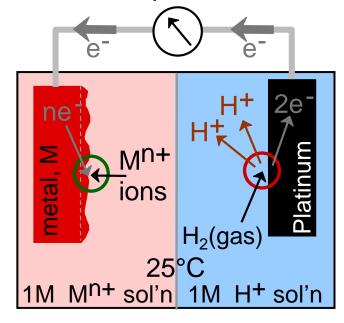




-- Metal is the anode (-)

 $V_{\text{metal}}^{\text{o}} < 0$ (relative to Pt)

-- Electrodeposition



-- Metal is the cathode (+)

$$V_{\text{metal}}^{\text{o}} > 0$$
 (relative to Pt)

Standard Electrode Potential

Standard EMF Series

 Electromotive force (EMF) series metal metal +1.420 V Au +0.340Cu more cathodic Pb - 0.126

Sn - 0.136

Ni - 0.250 Co - 0.277

- 0.403 Cd

- 0.440 Fe

Cr - 0.744

- 0.763

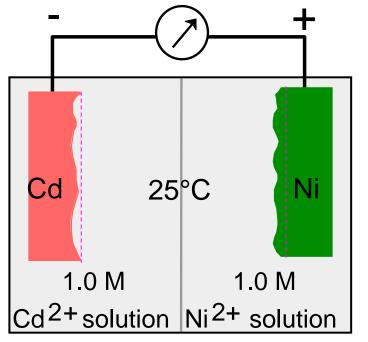
- 1.662

Mg - 2.363

- 2.714 Na

K - 2.924 Metal with smaller corrodes.

Ex: Cd-Ni cell

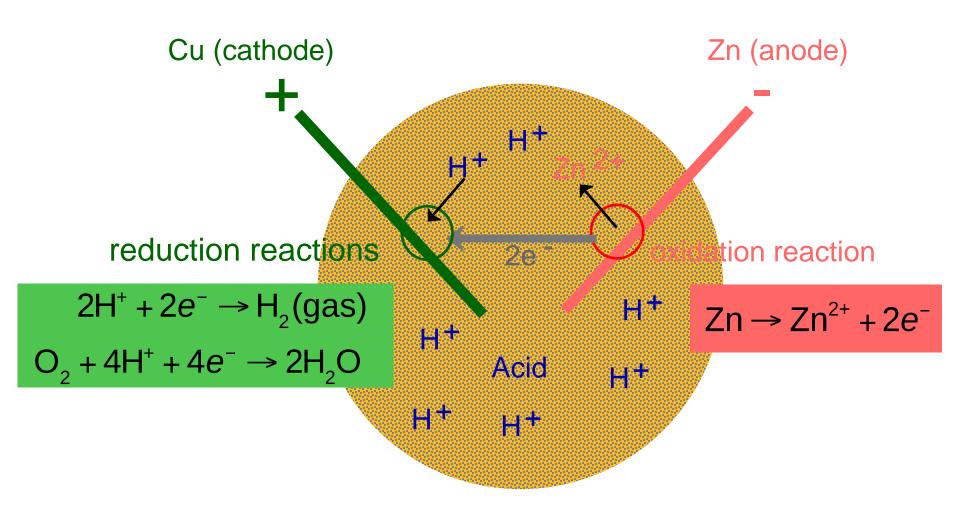


Data based on Table 17.1. Fig. 17.2, Callister & Rethwisch 10e. Callister 10e.

more anodic

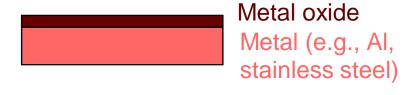
0.153V

Corrosion In A Grapefruit



Corrosion Prevention (I)

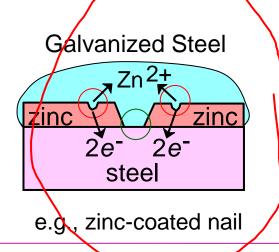
- Materials Selection
 - -- Use metals that are relatively unreactive in the corrosion environment -- e.g., Ni in basic solutions
 - -- Use metals that passivate
 - These metals form a thin, adhering oxide layer that slows corrosion.



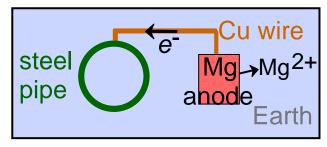
- Lower the temperature (reduces rates of oxidation and reduction)
- Apply physical barriers -- e.g., films and coatings

Corrosion Prevention (II)

- Add inhibitors (substances added to solution that decrease its reactivity)
 - -- Slow oxidation/reduction reactions by removing reactants (e.g., remove O₂ gas by reacting it w/an inhibitor).
 - -- Slow oxidation reaction by attaching species to the surface.
- Cathodic (or sacrificial) protection
 - -- Attach a more anodic material to the one to be protected.



Using a sacrificial anode



e.g., Mg Anode



Summary

- Ductile fracture behavior
 - Ductile fracture is different from damage
 - The mechanism of ductile fracture is void nucleation, growth, and coalescence.
- Damage mechanics models are developed to quantify and predict ductile fracture.
- Ductile materials may experience brittle fracture e.g. low temps. Ductile to brittle transition is measured by Charpy impact tests.
- Fatigue failure at cyclic and repeated loading.
- Creep failure at elevated temperatures and constant stress.
- Corrosion metallic corrosion involves electrochemical reactions.

Mid-term Review

Course Grade

- 10 points for participation
 - 0.5 points x 12 lectures/seminars
 - > 0.5 points x 6 exercises
 - > 1 point for **forum** activities
- 40 points quality of tasks
 - > (5-7) points x 6 weekly assignments
- 50 points on exam
- 10 points on extra activities
 - > 5 points on a computational task (details given on MyCourses)
 - 5 points on an essay task (details given on MyCourses)

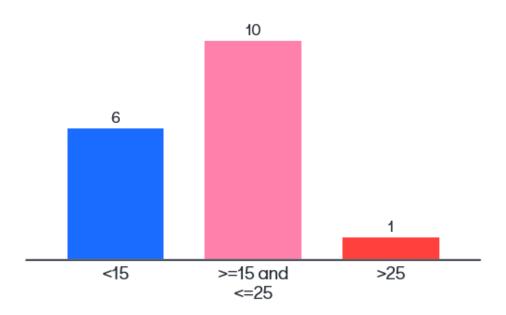
Total	Grade
≥90	5
≥80	4
≥70	3
≥60	2
≥50	1
<50	0

Course feedback

Go to www.menti.com and use the code 9345 3415

How many hours did you spend on the studying and working on assignmens?

Mentimeter







Course feedback

Go to www.menti.com and use the code 9345 3415

How do you feel like the course? Use three adjectives to describe.

Mentimeter

```
very time consuming
useful confusing
packed interesting
work time consuming
requires self-research
work time consuming
requires self-research
```







Announcements

Reading: Textbook Ch. 8, 17

Assignment: Open; DL: 18:00 Sunday

Q&A time: Tuesday 16:30

Exercise: **Thursday 10:15 – 12:00**

Preparation of your computational environment is needed before the exercise sessions.

Software preparation

Input data download: 'E3flowcurve.txt' on MyCourses

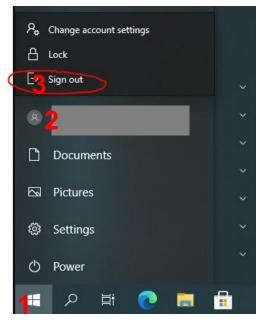
Abaqus: free student version (https://edu.3ds.com/en/software/abaqus-student-edition)

Aalto VDI system: **mfavdi.aalto.fi**, or VMware Horizon Client **vdi.aalto.fi**, for more information, please refer to Remote access to Windows classroom computers.

IMPORTANT! Please remember to do 'Sign Out' after the session (NOT Disconnect). Click your username in Start and click 'Sign Out'.

Basic Rule: Please use DOT as the decimal separator, **NO COMMA!**Contribution from Mr Binh Nguyen: For those who use win 10, go to control panel > region > additional settings > choose dot . as decimal separator.

The Abaqus student version has been installed in the VDI windows 10 3D, but it would be too slow if too many people are using VDI at the same time. You can also install the software on your own computer. Make sure that you have downloaded the data file 'E3flowcurve.txt' from MyCourses.



Abaqus student version installation



The Abaqus Student Edition is available free of charge to students, educators, and researchers for personal and educational use. The Abaqus SE is available on Windows platform only and supports structural models up to 1000 nodes. The full documentation collection in HTML format makes this the perfect Abaqus learning tool both on campus or on the move.

Now you can have your own personal finite element analysis tool to use on or away from campus. Abaqus Student Edition is ideal for those using Abaqus as part of their coursework as well as for anyone wishing to become more proficient with Abaqus.All Students, Researchers, and Educators with a 3DEXPERIENCE ID associated with an academic institution are eligible for immediate download and access to tutorials and courseware... free of charge!



Abaqus student version installation



(https://edu.3ds.com/en/software/abagus-student-edition)



ABAQUS Install instructions

PDF 1.26 MB

Abaqus 2020 Student Edition Installation Instructions & known issues



Tutorial Series

ABAQUS Tutorials

To get started. ABAOUS Tutorials are available here



Install Abaqus according to the 'Install instructions', if you have questions, contact Abaqus service or Aalto IT.



Learning Ressources

Tutorials and learning resources for Abaqus and other SIMULIA products are available at the

> SIMULIA Learning Community

Contact Abaqus for download problem

Download Issues

For download issues only (no other support for Abaqus), please contact us here

System requirements

ABAQUS Student Edition is not available on 32bits configurations

Note: The Microsoft Visual C++ 2010 SP1 Redistributable Package (x64) is required for successful execution of the Abaqus Student Editions.

- ▶ Abaqus Student Edition 2020 (latest release): This version installs this package automatically and no additional steps are required.
- ► Abaqus Student Edition 2019: This release does <u>not</u> install this package automatically, and the user must download and install the Microsoft Visual C++ 2010 SP1 Redistributable Package (x64) using this link:

https://www.microsoft.com/en-us/download/details.aspx?id=13523. Failure to install this package will produce the following fatal runtime error with

Questions?