



# Performance Indices Reference Booklet

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## About Performance Indices

During materials selection, one needs to optimize the performance of the material based on the design requirements. When using the Ashby Selection methodology<sup>1</sup>, these criteria are determined via the Objectives and are used during the Ranking stage.

We can determine the performance of the material by defining a performance equation. The general form of this equation can be found [elsewhere](#). When focusing on the material properties segment of this performance equation, this can be called a material index or a performance index. These material indices help us determine how well a specific material that has passed the screening stage will perform during ranking<sup>1</sup>.

As stated in our materials selection whitepaper<sup>2</sup> and Prof. Ashby's textbooks<sup>1,3</sup>, the constraints defined during the translation step of the selection methodology set property limits. In some cases, the objectives are separate from the constraints, which leads to single material property performance indices (i.e. if the performance of a beam is measured by its stiffness, the performance equation contains only one property, the elastic modulus E). In other situations, the constraints and objectives are coupled, which leads to a group of multiple properties. Familiar examples are the specific stiffness,  $E/\rho$ , and the specific strength,  $\sigma_y/\rho$ , (where E is Young's modulus,  $\sigma_y$  is the yield strength or elastic limit, and  $\rho$  is the density), but there are many others. They are a key to the optimal selection of materials.

## In this Booklet

This booklet provides pre-derived performance indices for a variety of conditions. A breakdown of the conditions can be found in the interactive table of contents on the next page.

By separating our performance equation into the function, geometry, and material elements, we can consider the material choice independently of other design factors<sup>1</sup>. This gives the indices found in this booklet great generality, which can be incredibly beneficial during the early stages of design. To truly consider all aspects of the performance, including function and geometry, one should turn to additional steps such as simulation or prototyping to ensure an optimal overall design.

## References and Additional Texts

1. Ashby MF, "Materials Selection in Mechanical Design", 5th edition, Elsevier Butterworth-Heinemann, Oxford, UK, 2016.
2. Parnell, H, Tyler, K, "[Granta EduPack White Paper: Material Selection](#)", Ansys
3. Ashby MF, "Materials and the Environment", 2nd Edition, Elsevier Butterworth Heinemann, Oxford, UK, 2012.
4. Goedkoop, M.J., Demmers, M. and Collignon, M.X. "Eco-Indicator '95, Manual", Pré Consultants, and the Netherlands Agency for Energy and the Environment, Amersfort, Holland (1995), ISBN 90-72130-80-4.

## Booklet Contents

Use the interactive table below to access the different performance indices by type. References shown in the tables can be found under the references section.

The symbols list can be found by [clicking here](#).

	Mass	Cost	Embodied Energy	Carbon Footprint
Stiffness-limited Design	kg	\$	H <sub>m</sub>	CO <sub>2</sub>
Strength-limited Design	kg	\$	H <sub>m</sub>	CO <sub>2</sub>

Vibration-limited Design

Damage-tolerant Design

Abrasion-resistant Design

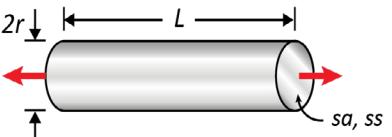
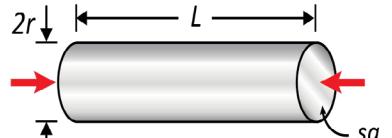
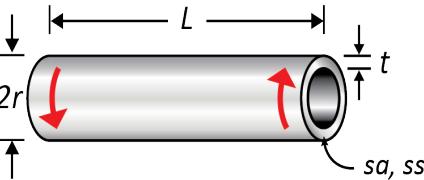
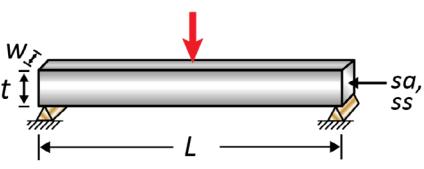
Thermo-mechanical Design

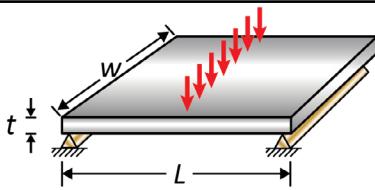
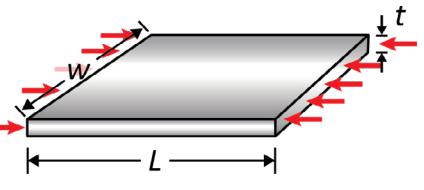
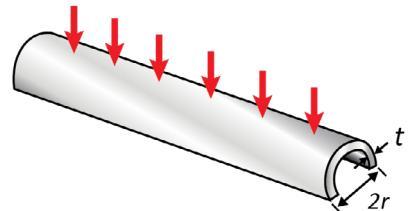
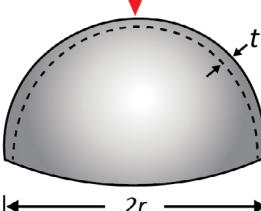
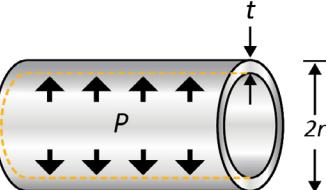
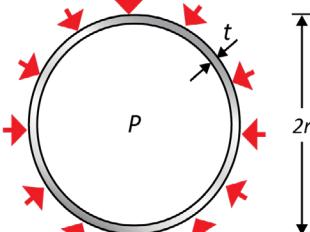
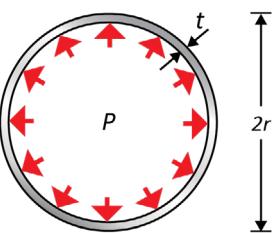
Electro-mechanical Design

Vapor barrier Design

Strength-limited design to optimize performance

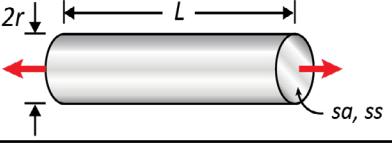
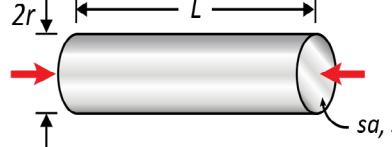
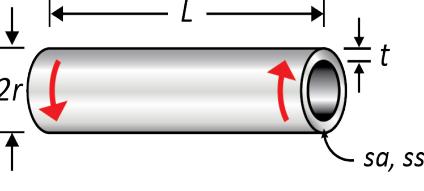
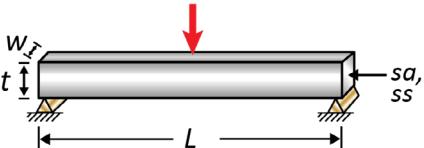
## Stiffness-limited design at minimum mass

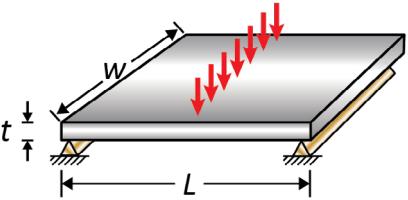
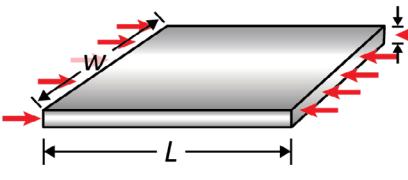
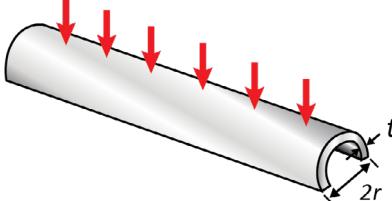
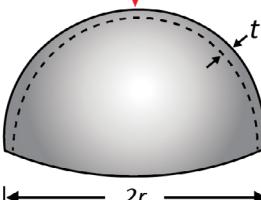
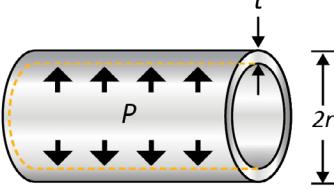
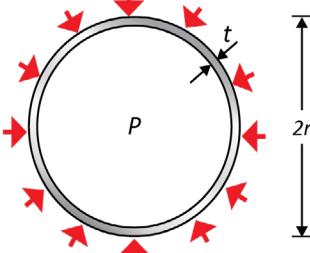
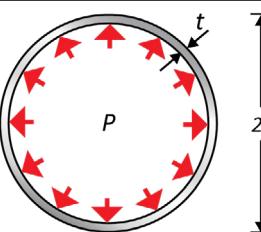
Function and Constraints*			Maximize	Minimize
Tie in Tension		Length fixed; section area free	$E/\rho$	$\rho/E$
Column in compression		Length, section shape fixed; section area free	$E/\rho$	$\rho/E$
		Length fixed; section area and section shape free	$(E\phi)/\rho$	$\rho/(E\phi)$
		Length, section shape fixed; section area free; buckling stiffness limited	$E^{1/2}/\rho$	$\rho/E^{1/2}$
Shaft in torsion		Length, section shape fixed; section area free	$G^{1/2}/\rho$	$\rho/G^{1/2}$
		Length, wall-thickness fixed; outer radius free	$G^{1/3}/\rho$	$\rho/G^{1/3}$
		Length, outer radius fixed; wall-thickness free	$G/\rho$	$\rho/G$
Beam in bending		Length, shape fixed; section area free	$E_f^{1/2}/\rho$	$\rho/E_f^{1/2}$
		Length fixed; section area and section shape free	$(\phi E_f)^{1/2}/\rho$	$\rho/(\phi E_f)^{1/2}$
		Length, thickness, section shape fixed; width free	$E_f/\rho$	$\rho/E_f$
		Length, thickness fixed; width, section shape free	$(\phi E_f)/\rho$	$\rho/(\phi E_f)$
		Length, width, section shape fixed; thickness free	$E_f^{1/3}/\rho$	$\rho/E_f^{1/3}$
		Length, width, section shape fixed; thickness free	$(\phi E_f)^{1/3}/\rho$	$\rho/(\phi E_f)^{1/3}$

Function and Constraints*			Maximize	Minimize
<b>Panel in bending</b>		Length fixed, width fixed; thickness free	$E_f^{1/3}/\rho$	$\rho/E_f^{1/3}$
<b>Panel in compression</b>		Collapse load, length and width fixed; thickness free	$E_f/\rho$	$\rho/E_f$
<b>Single-curvature shell under linear load</b>		Radius fixed; wall-thickness free	$E_f^{1/3}/\rho$	$\rho/E_f^{1/3}$
<b>Dome under central load</b>		Radius fixed; wall-thickness free	$E_f^{1/2}/\rho$	$\rho/E_f^{1/2}$
<b>Cylinder with internal pressure</b>		Radius fixed; wall-thickness free	$E/\rho$	$\rho/E$
<b>Sphere with external pressure</b>		Radius fixed; wall-thickness free; buckling stiffness limited	$E_f^{1/2}/\rho$	$\rho/E_f^{1/2}$
		Radius fixed; wall-thickness free; buoyancy limited	$E/\rho$	$\rho/E$
<b>Sphere with internal pressure</b>		Radius fixed; wall-thickness free	$E/(1-v)\rho$	$(1-v)\rho/E$

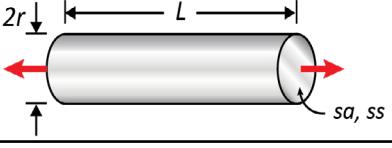
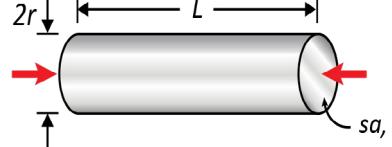
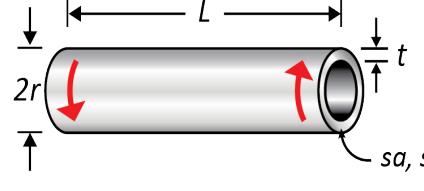
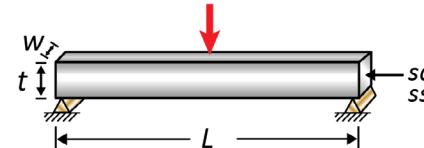
\* to minimize **volume**, replace density  $\rho$  by 1 (one). <sup>1,2,3</sup>

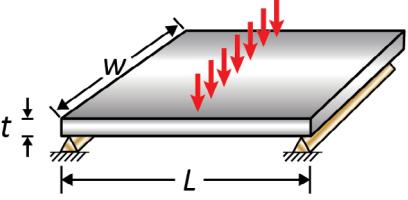
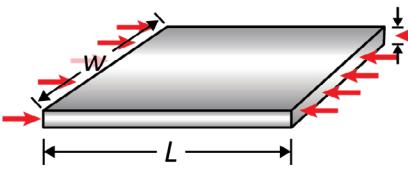
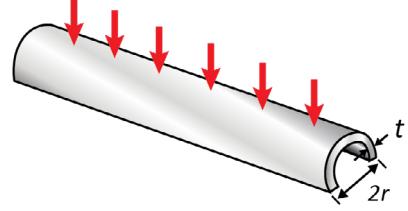
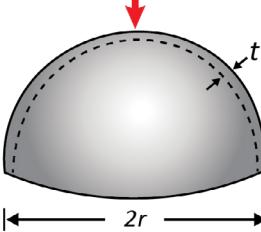
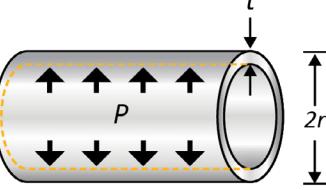
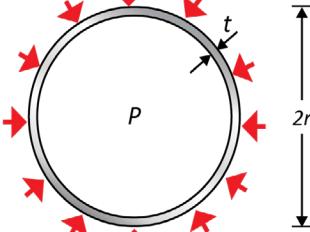
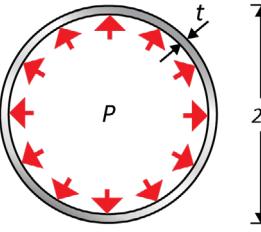
## Stiffness-limited design at minimum cost

Function and Constraints			Maximize	Minimize
<b>Tie in Tension</b>		Length fixed; section area free	$E/C_m\rho$	$C_m\rho/E$
<b>Column in compression</b>		Length, section shape fixed; section area free	$E/C_m\rho$	$C_m\rho/E$
		Length fixed; section area and section shape free	$(E\phi)/C_m\rho$	$C_m\rho/(E\phi)$
		Length, section shape fixed; section area free; buckling stiffness limited	$E^{1/2}/C_m\rho$	$C_m\rho/E^{1/2}$
<b>Shaft in torsion</b>		Length, section shape fixed; section area free	$G^{1/2}/C_m\rho$	$C_m\rho/G^{1/2}$
		Length, wall-thickness fixed; outer radius free	$G^{1/3}/C_m\rho$	$C_m\rho/G^{1/3}$
		Length, outer radius fixed; wall-thickness free	$G/C_m\rho$	$C_m\rho/G$
<b>Beam in bending</b>		Length, shape fixed; section area free	$E_f^{1/2}/C_m\rho$	$C_m\rho/E_f^{1/2}$
		Length fixed; section area and section shape free	$(\phi E_f)^{1/2}/C_m\rho$	$C_m\rho/(\phi E_f)^{1/2}$
		Length, thickness, section shape fixed; width free	$E_f/C_m\rho$	$C_m\rho/E_f$
		Length, thickness fixed; width, section shape free	$(\phi E_f)/C_m\rho$	$C_m\rho/(\phi E_f)$
		Length, width, section shape fixed; thickness free	$E_f^{1/3}/C_m\rho$	$C_m\rho/E_f^{1/3}$
		Length, width, section shape fixed; thickness free	$(\phi E_f)^{1/3}/C_m\rho$	$C_m\rho/(\phi E_f)^{1/3}$

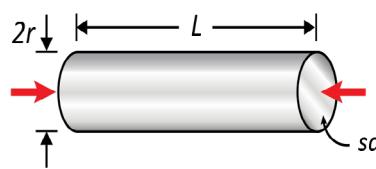
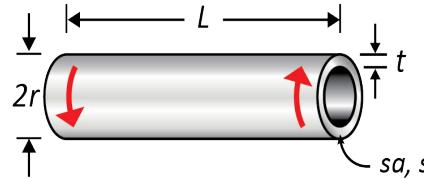
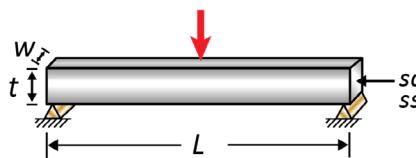
Function and Constraints			Maximize	Minimize
<b>Panel in bending</b>		Length fixed, width fixed; thickness free	$E_f^{1/3} / C_m \rho$	$C_m \rho / E_f^{1/3}$
<b>Panel in compression</b>		Collapse load, length and width fixed; thickness free	$E_f / C_m \rho$	$C_m \rho / E_f$
<b>Single-curvature shell under linear load</b>		Radius fixed; wall-thickness free	$E_f^{1/3} / C_m \rho$	$C_m \rho / E_f^{1/3}$
<b>Dome under central load</b>		Radius fixed; wall-thickness free	$E^{1/2} / C_m \rho$	$C_m \rho / E^{1/2}$
<b>Cylinder with internal pressure</b>		Radius fixed; wall-thickness free	$E / C_m \rho$	$C_m \rho / E$
<b>Sphere with external pressure</b>		Radius fixed; wall-thickness free; buckling stiffness limited	$E^{1/2} / C_m \rho$	$C_m \rho / E^{1/2}$
		Radius fixed; wall-thickness free; buoyancy limited	$E / C_m \rho$	$C_m \rho / E$
<b>Sphere with internal pressure</b>		Radius fixed; wall-thickness free	$E / (1 - \nu) C_m \rho$	$(1 - \nu) C_m \rho / E$

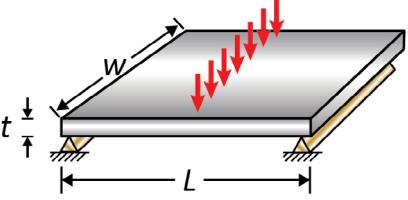
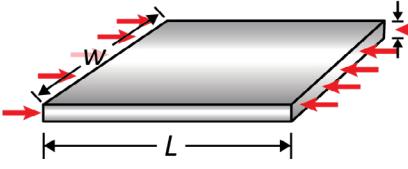
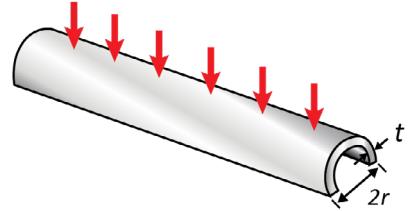
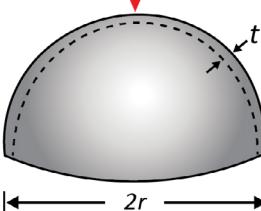
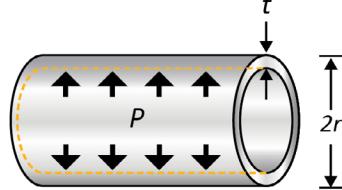
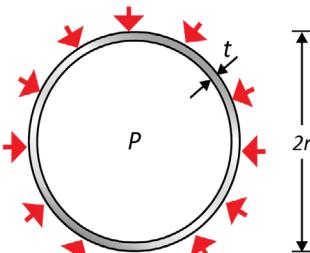
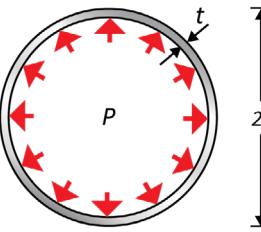
## Stiffness-limited design at minimum energy

Function and Constraints <sup>1</sup>			Maximize <sup>2</sup>	Minimize <sup>3</sup>
Tie in Tension		Length fixed; section area free	$E / H_m \rho$	$H_m \rho / E$
Column in compression		Length, section shape fixed; section area free	$E / H_m \rho$	$H_m \rho / E$
		Length fixed; section area and section shape free	$(E\phi) / H_m \rho$	$H_m \rho / (E\phi)$
		Length, section shape fixed; section area free; buckling stiffness limited	$E^{1/2} / H_m \rho$	$H_m \rho / E^{1/2}$
Shaft in torsion		Length, section shape fixed; section area free	$G^{1/2} / H_m \rho$	$H_m \rho / G^{1/2}$
		Length, wall-thickness fixed; outer radius free	$G^{1/3} / H_m \rho$	$H_m \rho / G^{1/3}$
		Length, outer radius fixed; wall-thickness free	$G / H_m \rho$	$H_m \rho / G$
Beam in bending		Length, shape fixed; section area free	$E_f^{1/2} / H_m \rho$	$H_m \rho / E_f^{1/2}$
		Length fixed; section area and section shape free	$(\phi E_f)^{1/2} / H_m \rho$	$H_m \rho / (\phi E_f)^{1/2}$
		Length, thickness, section shape fixed; width free	$E_f / H_m \rho$	$H_m \rho / E_f$
		Length, thickness fixed; width, section shape free	$(\phi E_f) / H_m \rho$	$H_m \rho / (\phi E_f)$
		Length, width, section shape fixed; thickness free	$E_f^{1/3} / H_m \rho$	$H_m \rho / E_f^{1/3}$
		Length, width, section shape fixed; thickness free	$(\phi E_f)^{1/3} / H_m \rho$	$H_m \rho / (\phi E_f)^{1/3}$

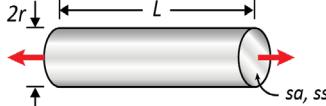
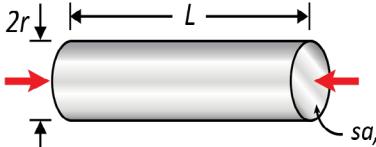
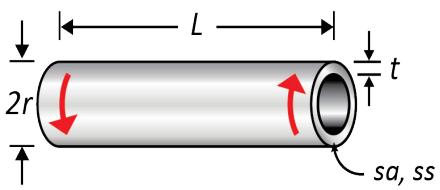
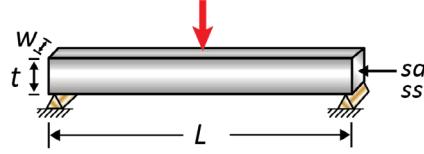
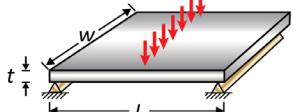
Function and Constraints			Maximize	Minimize
<b>Panel in bending</b>		Length fixed, width fixed; thickness free	$E_f^{1/3}/H_m\rho$	$H_m\rho/E_f^{1/3}$
<b>Panel in compression</b>		Collapse load, length and width fixed; thickness free	$E_f/H_m\rho$	$H_m\rho/E_f$
<b>Single-curvature shell under linear load</b>		Radius fixed; wall-thickness free	$E_f^{1/3}/H_m\rho$	$H_m\rho/E_f^{1/3}$
<b>Dome under central load</b>		Radius fixed; wall-thickness free	$E_f^{1/2}/H_m\rho$	$H_m\rho/E_f^{1/2}$
<b>Cylinder with internal pressure</b>		Radius fixed; wall-thickness free	$E/H_m\rho$	$H_m\rho/E$
<b>Sphere with external pressure</b>		Radius fixed; wall-thickness free; buckling stiffness limited	$E^{1/2}/H_m\rho$	$H_m\rho/E^{1/2}$
		Radius fixed; wall-thickness free; buoyancy limited	$E/H_m\rho$	$H_m\rho/E$
<b>Sphere with internal pressure</b>		Radius fixed; wall-thickness free	$E/(1-\nu)H_m\rho$	$(1-\nu)H_m\rho/E$

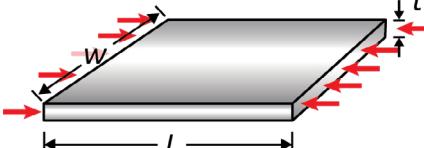
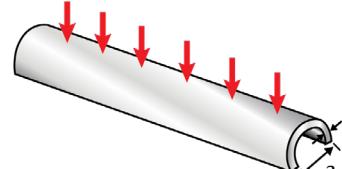
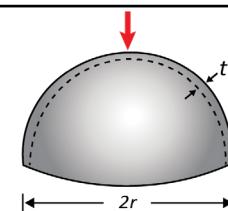
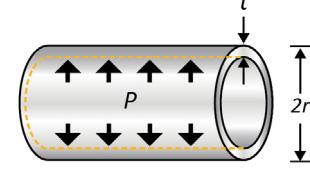
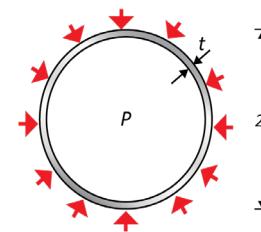
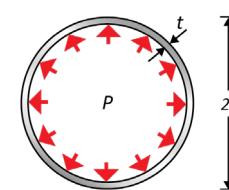
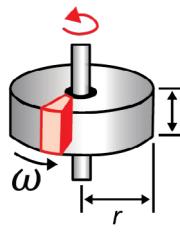
## Stiffness-limited design at minimum environmental impact

Function and Constraints			Maximize	Minimize
<b>Tie in Tension</b>		Length fixed; section area free	$E/CO_2\rho$	$CO_2\rho/E$
<b>Column in compression</b>		Length, section shape fixed; section area free	$E/CO_2\rho$	$CO_2\rho/E$
		Length fixed; section area and section shape free	$(E\phi)/CO_2\rho$	$CO_2\rho/(E\phi)$
		Length, section shape fixed; section area free; buckling stiffness limited	$E^{1/2}/CO_2\rho$	$CO_2\rho/E^{1/2}$
<b>Shaft in torsion</b>		Length, section shape fixed; section area free	$G^{1/2}/CO_2\rho$	$CO_2\rho/G^{1/2}$
		Length, wall-thickness fixed; outer radius free	$G^{1/3}/CO_2\rho$	$CO_2\rho/G^{1/3}$
		Length, outer radius fixed; wall-thickness free	$G/CO_2\rho$	$CO_2\rho/G$
<b>Beam in bending</b>		Length, shape fixed; section area free	$E_f^{1/2}/CO_2\rho$	$CO_2\rho/E_f^{1/2}$
		Length fixed; section area and section shape free	$(\phi E_f)^{1/2}/CO_2\rho$	$CO_2\rho/(\phi E_f)^{1/2}$
		Length, thickness, section shape fixed; width free	$E_f/CO_2\rho$	$CO_2\rho/E_f$
		Length, thickness fixed; width, section shape free	$(\phi E_f)/CO_2\rho$	$CO_2\rho/(\phi E_f)$
		Length, width, section shape fixed; thickness free	$E_f^{1/3}/CO_2\rho$	$CO_2\rho/E_f^{1/3}$
		Length, width, section shape fixed; thickness free	$(\phi E_f)^{1/3}/CO_2\rho$	$CO_2\rho/(\phi E_f)^{1/3}$

Function and Constraints			Maximize	Minimize
<b>Panel in bending</b>		Length fixed, width fixed; thickness free	$E_f^{1/3}/CO_2\rho$	$CO_2\rho/E_f^{1/3}$
<b>Panel in compression</b>		Collapse load, length and width fixed; thickness free	$E_f/CO_2\rho$	$CO_2\rho/E_f$
<b>Single-curvature shell under linear load</b>		Radius fixed; wall-thickness free	$E_f^{1/3}/CO_2\rho$	$CO_2\rho/E_f^{1/3}$
<b>Dome under central load</b>		Radius fixed; wall-thickness free	$E_f^{1/2}/CO_2\rho$	$CO_2\rho/E_f^{1/2}$
<b>Cylinder with internal pressure</b>		Radius fixed; wall-thickness free	$E/CO_2\rho$	$CO_2\rho/E$
<b>Sphere with external pressure</b>		Radius fixed; wall-thickness free; buckling stiffness limited	$E^{1/2}/CO_2\rho$	$CO_2\rho/E^{1/2}$
		Radius fixed; wall-thickness free; buoyancy limited	$E/CO_2\rho$	$CO_2\rho/E$
<b>Sphere with internal pressure</b>		Radius fixed; wall-thickness free	$E/(1-v)CO_2\rho$	$(1-v)CO_2\rho/E$

## Strength-limited design at minimum mass

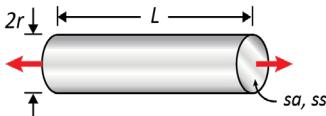
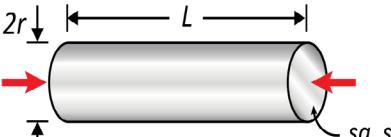
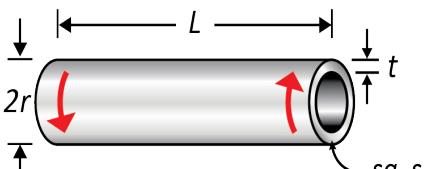
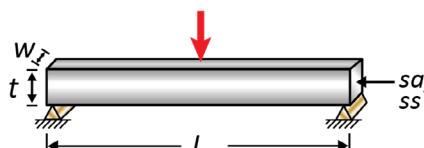
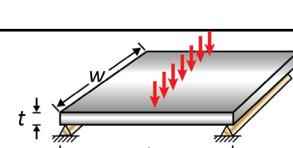
Function and Constraints*†			Maximize	Minimize
Tie in Tension		Length fixed; section area free	$\sigma_y/\rho$	$\rho/\sigma_y$
Column in compression		Length, section shape fixed; section area free	$\sigma_c/\rho$	$\rho/\sigma_c$
		Length fixed; section area and section shape free	$(\phi^{1/2}\sigma_y)/\rho$	$\rho/(\phi^{1/2}\sigma_y)$
		Length, section shape fixed; section area free; buckling stiffness limited	$(\phi^{1/2}\sigma_y)^{2/3}/\rho$	$\rho/(\phi^{1/2}\sigma_y)^{2/3}$
Shaft in torsion		Length, section shape fixed; section area free	$\sigma_y^{2/3}/\rho$	$\rho/\sigma_y^{2/3}$
		Length, wall-thickness fixed; outer radius free	$\sigma_y^{1/2}/\rho$	$\rho/\sigma_y^{1/2}$
		Length, outer radius fixed; wall-thickness free	$\sigma_y/\rho$	$\rho/\sigma_y$
Beam in bending		Length, shape fixed; section area free	$\sigma_y^{2/3}/\rho$	$\rho/\sigma_y^{2/3}$
		Length fixed; section area and section shape free	$(\phi^{1/2}\sigma_f^{2/3})/\rho$	$\rho/(\phi^{1/2}\sigma_f^{2/3})$
		Length, thickness, section shape fixed; width free	$\sigma_f/\rho$	$\rho/\sigma_f$
		Length, thickness fixed; width, section shape free	$(\phi^{1/2}\sigma_f)/\rho$	$\rho/(\phi^{1/2}\sigma_f)$
		Length, width, section shape fixed; thickness free	$\sigma_f^{1/2}/\rho$	$\rho/\sigma_f^{1/2}$
		Length, width, section shape fixed; thickness free	$(\phi\sigma_f)^{1/2}/\rho$	$\rho/(\phi\sigma_f)^{1/2}$
Panel in bending		Length fixed, width fixed; thickness free	$\sigma_f^{1/2}/\rho$	$\rho/\sigma_f^{1/2}$

Function and Constraints*†			Maximize	Minimize
Panel in compression		Length, width fixed; thickness free Length, width, thickness free; buckling strength fixed	$\sigma_c^{1/2}/\rho$	$\rho/\sigma_c^{1/2}$
			$\sigma_y^{1/2}/\rho$	$\rho/\sigma_y^{1/2}$
Single-curvature shell under linear load		Radius fixed; wall-thickness free	$\sigma_f^{1/3}/\rho$	$\rho/\sigma_f^{1/3}$
Dome under central load		Radius fixed; wall-thickness free	$\sigma_f^{1/2}/\rho$	$\rho/\sigma_f^{1/2}$
Cylinder with internal pressure		Radius fixed; wall-thickness free	$\sigma_y/\rho$	$\rho/\sigma_y$
Sphere with external pressure		Radius fixed; wall-thickness free; buckling stiffness limited	$\sigma_c/\rho$	$\rho/\sigma_c$
		Radius fixed; wall-thickness free; buoyancy limited	$\sigma_y^{2/3}/\rho$	$\rho/\sigma_y^{2/3}$
Sphere with internal pressure		Radius fixed; wall-thickness free	$\sigma_y/\rho$	$\rho/\sigma_y$
Flywheel/rotating disk		Radius fixed; thickness free; angular velocity limited	$\rho$	$1/\rho$
		Thickness fixed; angular velocity, radius free	$\sigma_y/\rho$	$\rho/\sigma_y$

\* to minimize **volume**, replace density  $\rho$  by 1 (one). <sup>1,2,3</sup>

† For design for infinite fatigue life, replace  $\sigma_y$  by the fatigue strength (endurance limit)  $\sigma_E$ .

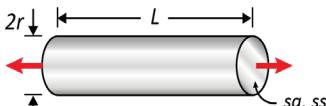
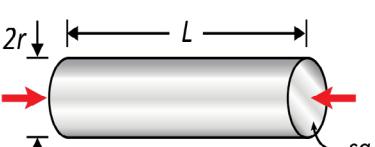
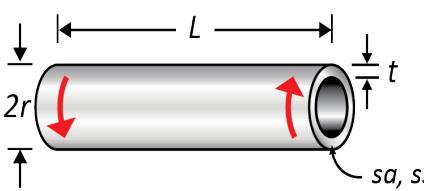
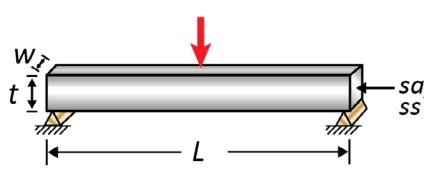
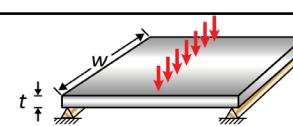
## Strength-limited design at minimum cost

Function and Constraints†			Maximize	Minimize
Tie in Tension		Length fixed; section area free	$\sigma_y/C_m\rho$	$C_m\rho/\sigma_y$
Column in compression		Length, section shape fixed; section area free	$\sigma_c/C_m\rho$	$C_m\rho/\sigma_c$
		Length fixed; section area and section shape free	$(\phi^{1/2}\sigma_y)/C_m\rho$	$C_m\rho/(\phi^{1/2}\sigma_y)$
		Length, section shape fixed; section area free; buckling stiffness limited	$(\phi^{1/2}\sigma_y)^{2/3}/C_m\rho$	$C_m\rho/(\phi^{1/2}\sigma_y)^{2/3}$
Shaft in torsion		Length, section shape fixed; section area free	$\sigma_y^{2/3}/C_m\rho$	$C_m\rho/\sigma_y^{2/3}$
		Length, wall-thickness fixed; outer radius free	$\sigma_y^{1/2}/C_m\rho$	$C_m\rho/\sigma_y^{1/2}$
		Length, outer radius fixed; wall-thickness free	$\sigma_y/C_m\rho$	$C_m\rho/\sigma_y$
Beam in bending		Length, shape fixed; section area free	$\sigma_f^{2/3}/C_m\rho$	$C_m\rho/\sigma_f^{2/3}$
		Length fixed; section area and section shape free	$(\phi^{1/2}\sigma_f^{2/3})/C_m\rho$	$C_m\rho/(\phi^{1/2}\sigma_f^{2/3})$
		Length, thickness, section shape fixed; width free	$\sigma_f/C_m\rho$	$C_m\rho/\sigma_f$
		Length, thickness fixed; width, section shape free	$(\phi^{1/2}\sigma_f)/C_m\rho$	$C_m\rho/(\phi^{1/2}\sigma_f)$
		Length, width, section shape fixed; thickness free	$\sigma_f^{1/2}/C_m\rho$	$C_m\rho/\sigma_f^{1/2}$
		Length, width, section shape fixed; thickness free	$(\phi\sigma_f)^{1/2}/C_m\rho$	$C_m\rho/(\phi\sigma_f)^{1/2}$
Panel in bending		Length fixed, width fixed; thickness free	$\sigma_f^{1/2}/C_m\rho$	$C_m\rho/\sigma_f^{1/2}$

Function and Constraints†			Maximize	Minimize
<b>Panel in compression</b>		Length, width fixed; thickness free	$\sigma_c^{1/2}/C_m\rho$	$C_m\rho/\sigma_c^{1/2}$
		Length, width, thickness free; buckling strength fixed	$\sigma_y^{1/2}/C_m\rho$	$C_m\rho/\sigma_y^{1/2}$
<b>Single-curvature shell under linear load</b>		Radius fixed; wall-thickness free	$\sigma_f^{1/3}/C_m\rho$	$C_m\rho/\sigma_f^{1/3}$
<b>Dome under central load</b>		Radius fixed; wall-thickness free	$\sigma_f^{1/2}/C_m\rho$	$C_m\rho/\sigma_f^{1/2}$
<b>Cylinder with internal pressure</b>		Radius fixed; wall-thickness free	$\sigma_y/C_m\rho$	$C_m\rho/\sigma_y$
<b>Sphere with external pressure</b>		Radius fixed; wall-thickness free; buckling stiffness limited	$\sigma_c/C_m\rho$	$\rho/C_m\sigma_c$
		Radius fixed; wall-thickness free; buoyancy limited	$\sigma_y^{2/3}/C_m\rho$	$C_m\rho/\sigma_y^{2/3}$
<b>Sphere with internal pressure</b>		Radius fixed; wall-thickness free	$\sigma_y/C_m\rho$	$C_m\rho/\sigma_y$
<b>Flywheel/rotating disk</b>		Radius fixed; thickness free; angular velocity limited	$C_m\rho$	$1/C_m\rho$
		Thickness fixed; angular velocity, radius free	$\sigma_y/C_m\rho$	$C_m\rho/\sigma_y$

† For design for infinite fatigue life, replace  $\sigma_y$  by the fatigue strength (endurance limit)  $\sigma_E$ .

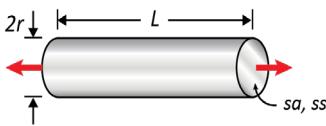
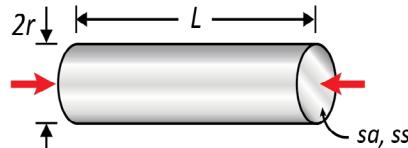
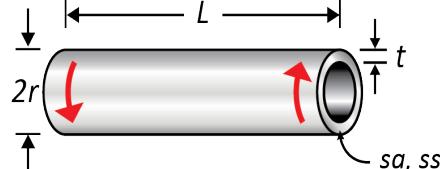
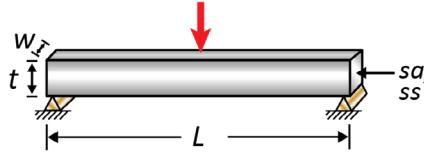
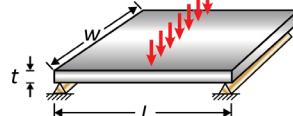
# Strength-limited design at minimum energy

Function and Constraints†			Maximize	Minimize
Tie in Tension		Length fixed; section area free	$\sigma_y/H_m\rho$	$H_m\rho/\sigma_y$
Column in compression		Length, section shape fixed; section area free	$\sigma_c/H_m\rho$	$H_m\rho/\sigma_c$
		Length fixed; section area and section shape free	$(\phi^{1/2}\sigma_y)/H_m\rho$	$H_m\rho/(\phi^{1/2}\sigma_y)$
		Length, section shape fixed; section area free; buckling stiffness limited	$(\phi^{1/2}\sigma_y)^{2/3}/H_m\rho$	$H_m\rho/(\phi^{1/2}\sigma_y)^{2/3}$
Shaft in torsion		Length, section shape fixed; section area free	$\sigma_y^{2/3}/H_m\rho$	$H_m\rho/\sigma_y^{2/3}$
		Length, wall-thickness fixed; outer radius free	$\sigma_y^{1/2}/H_m\rho$	$H_m\rho/\sigma_y^{1/2}$
		Length, outer radius fixed; wall-thickness free	$\sigma_y/H_m\rho$	$H_m\rho/\sigma_y$
Beam in bending		Length, shape fixed; section area free	$\sigma_f^{2/3}/H_m\rho$	$H_m\rho/\sigma_f^{2/3}$
		Length fixed; section area and section shape free	$(\phi^{1/2}\sigma_f^{2/3})/H_m\rho$	$H_m\rho/(\phi^{1/2}\sigma_f^{2/3})$
		Length, thickness, section shape fixed; width free	$\sigma_f/H_m\rho$	$H_m\rho/\sigma_f$
		Length, thickness fixed; width, section shape free	$(\phi^{1/2}\sigma_f)/H_m\rho$	$H_m\rho/(\phi^{1/2}\sigma_f)$
		Length, width, section shape fixed; thickness free	$\sigma_f^{1/2}/H_m\rho$	$H_m\rho/\sigma_f^{1/2}$
		Length, width, section shape fixed; thickness free	$(\phi\sigma_f)^{1/2}/H_m\rho$	$H_m\rho/(\phi\sigma_f)^{1/2}$
Panel in bending		Length fixed, width fixed; thickness free	$\sigma_f^{1/2}/H_m\rho$	$H_m\rho/\sigma_f^{1/2}$

Function and Constraints†			Maximize	Minimize
<b>Panel in compression</b>		Length, width fixed; thickness free  Length, width, thickness free; buckling strength fixed	$\sigma_c^{1/2}/H_m\rho$	$H_m\rho/\sigma_c^{1/2}$
			$\sigma_y^{1/2}/H_m\rho$	$H_m\rho/\sigma_y^{1/2}$
<b>Single-curvature shell under linear load</b>		Radius fixed; wall-thickness free	$\sigma_f^{1/3}/H_m\rho$	$H_m\rho/\sigma_f^{1/3}$
<b>Dome under central load</b>		Radius fixed; wall-thickness free	$\sigma_f^{1/2}/H_m\rho$	$H_m\rho/\sigma_f^{1/2}$
<b>Cylinder with internal pressure</b>		Radius fixed; wall-thickness free	$\sigma_y/H_m\rho$	$H_m\rho/\sigma_y$
<b>Sphere with external pressure</b>		Radius fixed; wall-thickness free; buckling stiffness limited	$\sigma_c/H_m\rho$	$\rho/H_m\sigma_c$
		Radius fixed; wall-thickness free; buoyancy limited	$\sigma_y^{2/3}/H_m\rho$	$H_m\rho/\sigma_y^{2/3}$
<b>Sphere with internal pressure</b>		Radius fixed; wall-thickness free	$\sigma_y/H_m\rho$	$H_m\rho/\sigma_y$
<b>Flywheel/rotating disk</b>		Radius fixed; thickness free; angular velocity limited	$H_m\rho$	$1/H_m\rho$
		Thickness fixed; angular velocity, radius free	$\sigma_y/H_m\rho$	$H_m\rho/\sigma_y$

† For design for infinite fatigue life, replace  $\sigma_y$  by the fatigue strength (endurance limit)  $\sigma_E$ .

## Strength-limited design at minimum environmental impact

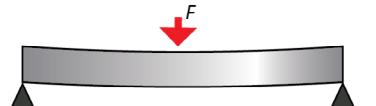
Function and Constraints†			Maximize	Minimize
Tie in Tension		Length fixed; section area free	$\sigma_y/CO_2\rho$	$CO_2\rho/\sigma_y$
Column in compression		Length, section shape fixed; section area free	$\sigma_c/CO_2\rho$	$CO_2\rho/\sigma_c$
		Length fixed; section area and section shape free	$(\phi^{1/2}\sigma_y)/CO_2\rho$	$CO_2\rho/(\phi^{1/2}\sigma_y)$
		Length, section shape fixed; section area free; buckling stiffness limited	$(\phi^{1/2}\sigma_y)^{2/3}/CO_2\rho$	$CO_2\rho/(\phi^{1/2}\sigma_y)^{2/3}$
Shaft in torsion		Length, section shape fixed; section area free	$\sigma_y^{2/3}/CO_2\rho$	$CO_2\rho/\sigma_y^{2/3}$
		Length, wall-thickness fixed; outer radius free	$\sigma_y^{1/2}/CO_2\rho$	$CO_2\rho/\sigma_y^{1/2}$
		Length, outer radius fixed; wall-thickness free	$\sigma_y/CO_2\rho$	$CO_2\rho/\sigma_y$
Beam in bending		Length, shape fixed; section area free	$\sigma_f^{2/3}/CO_2\rho$	$CO_2\rho/\sigma_f^{2/3}$
		Length fixed; section area and section shape free	$(\phi^{1/2}\sigma_f^{2/3})/CO_2\rho$	$CO_2\rho/(\phi^{1/2}\sigma_f^{2/3})$
		Length, thickness, section shape fixed; width free	$\sigma_f/CO_2\rho$	$CO_2\rho/\sigma_f$
		Length, thickness fixed; width, section shape free	$(\phi^{1/2}\sigma_f)/CO_2\rho$	$CO_2\rho/(\phi^{1/2}\sigma_f)$
		Length, width, section shape fixed; thickness free	$\sigma_f^{1/2}/CO_2\rho$	$CO_2\rho/\sigma_f^{1/2}$
		Length, width, section shape fixed; thickness free	$(\phi\sigma_f)^{1/2}/CO_2\rho$	$CO_2\rho/(\phi\sigma_f)^{1/2}$
Panel in bending		Length fixed, width fixed; thickness free	$\sigma_f^{1/2}/CO_2\rho$	$CO_2\rho/\sigma_f^{1/2}$

Function and Constraints†			Maximize	Minimize
<b>Panel in compression</b>		Length, width fixed; thickness free  Length, width, thickness free; buckling strength fixed	$\sigma_c^{1/2}/CO_2\rho$	$CO_2\rho/\sigma_c^{1/2}$
			$\sigma_y^{1/2}/CO_2\rho$	$CO_2\rho/\sigma_y^{1/2}$
<b>Single-curvature shell under linear load</b>		Radius fixed; wall-thickness free	$\sigma_f^{1/3}/CO_2\rho$	$CO_2\rho/\sigma_f^{1/3}$
<b>Dome under central load</b>		Radius fixed; wall-thickness free	$\sigma_f^{1/2}/CO_2\rho$	$CO_2\rho/\sigma_f^{1/2}$
<b>Cylinder with internal pressure</b>		Radius fixed; wall-thickness free	$\sigma_y/CO_2\rho$	$CO_2\rho/\sigma_y$
<b>Sphere with external pressure</b>		Radius fixed; wall-thickness free; buckling stiffness limited	$\sigma_c/CO_2\rho$	$CO_2\rho/\sigma_c$
		Radius fixed; wall-thickness free; buoyancy limited	$\sigma_f^{2/3}/CO_2\rho$	$CO_2\rho/\sigma_f^{2/3}$
<b>Sphere with internal pressure</b>		Radius fixed; wall-thickness free	$\sigma_y/CO_2\rho$	$CO_2\rho/\sigma_y$
<b>Flywheel/rotating disk</b>		Radius fixed; thickness free; angular velocity limited	$CO_2\rho$	$1/CO_2\rho$
		Thickness fixed; angular velocity, radius free	$\sigma_y/CO_2\rho$	$CO_2\rho/\sigma_y$

† For design for infinite fatigue life, replace  $\sigma_y$  by the fatigue strength (endurance limit)  $\sigma_E$ .

## Strength-limited design for maximum performance springs, hinges, etc.

Function and Constraints <sup>x</sup>			Maximize	Minimize
<b>Diaphragm with pressure difference</b>		Maximum deflection under specified pressure or force	$\sigma_y^{3/2}/E$	$E/\sigma_y^{3/2}$
<b>Knife edge/ pivot</b>		Minimum contact area, maximum bearing load	$\sigma_y^3/E^2$ and $H$	$E^2/\sigma_y^3$ and $1/H$
<b>Static seal</b>		Maximum conformability; limit on contact pressure	$\sigma_y/E$ and $1/E$	$E/\sigma_y$ and $E$
<b>Elastic hinge with small deformation</b>		Optimize flexibility; thickness fixed; length, width free	$\sigma_y/E_f$	$E_f/\sigma_y$
<b>Elastic hinge with large deformation</b>		Optimize flexibility; thickness fixed; length, width free	$\sigma_y^3/E_f^2$	$E_f^2/\sigma_y^3$
<b>Elastic hinge with axial load</b>		Optimize flexibility; thickness fixed; length, width free	$\sigma_y^2/E_f$	$E_f/\sigma_y^2$

Function and Constraints <sup>†,γ</sup>			Maximize	Minimize
<b>Spring</b>	(a)  A horizontal beam is fixed at both ends. A downward force $F$ is applied at the center, causing the beam to bend downwards.	Optimize volume; maximum stored elastic energy per unit	$\sigma_y^2/E$	$E/\sigma_y^2$
	(b)  A coiled spring is shown with a red arrow indicating tension. (c)  A coiled spring is shown with a red arrow indicating clockwise rotation. (d)  A horizontal beam is fixed at one end and has a circular cross-section. A clockwise torque is applied at the free end, causing the beam to twist.	Optimize mass; all dimensions free; maximum stored elastic energy per unit mass	$\sigma_y^2/E\rho$	$E\rho/\sigma_y^2$

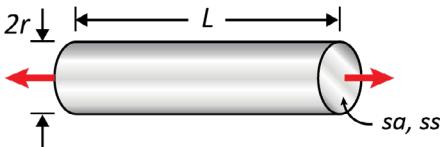
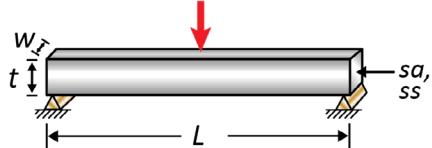
<sup>†</sup> For design for infinite fatigue life, replace  $\sigma_y$  by the fatigue strength (endurance limit)  $\sigma_E$ .

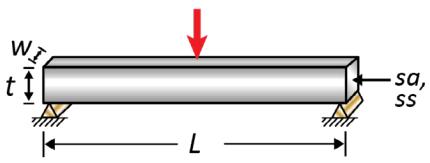
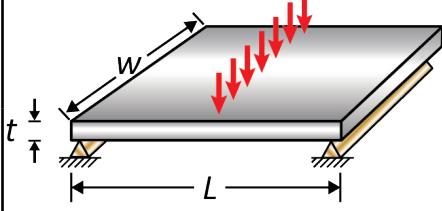
<sup>γ</sup> To minimize cost, use the above criteria for minimum weight, replacing density  $\rho$  by  $C_m \rho$ , where  $C_m$  is the material cost per unit mass

To minimize embodied energy or CO<sub>2</sub> footprint, use the above criteria for minimum mass, replacing  $\rho$  by  $H_m \rho$  or CO<sub>2</sub>ρ, where H<sub>m</sub> is the embodied energy content per unit mass and CO<sub>2</sub> is the CO<sub>2</sub> footprint per unit mass

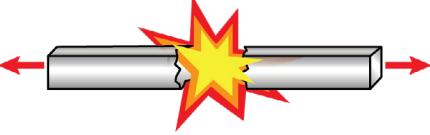
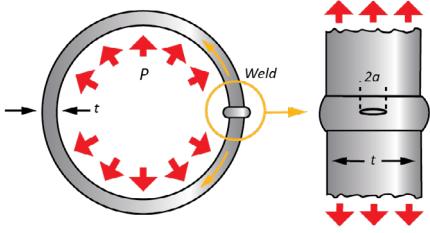
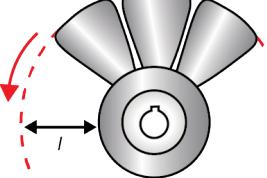
References<sup>1,2,3</sup>

## Vibration-limited design

Function and Constraints		Maximize	Minimize
Tie in Tension		Optimize for resonant frequency; length fixed; section area and section shape free	$E/\rho$
		Optimize for vibration amplitude; length fixed; section area and section shape free	$\eta E/\rho$
Beam in bending		Optimize for resonant frequency; length, section shape fixed; section area free	$E_f^{1/2}/\rho$
		Optimize for resonant frequency; length fixed; section area, section shape free	$(\phi E_f)^{1/2}/\rho$
		Optimize for resonant frequency; length, thickness, section shape fixed; width free	$E_f/\rho$
		Optimize for resonant frequency; length, thickness, fixed; width, section shape free	$\phi E_f/\rho$
		Optimize for resonant frequency; length, width, section shape fixed; thickness free	$E_f^{1/3}/\rho$
		Optimize for resonant frequency; length, width fixed; thickness, section shape free	$(\phi E_f)^{1/3}/\rho$

Function and Constraints		Maximize	Minimize
<b>Beam in bending</b>		Optimize for vibration amplitude; length, section shape fixed; section area free	$\eta E_f^{1/2} / \rho$ $\rho / \eta E_f^{1/2}$
		Optimize for vibration amplitude; length fixed; section area, section shape free	$\eta(\phi E_f)^{1/2} / \rho$ $\rho / \eta(\phi E_f)^{1/2}$
		Optimize for vibration amplitude; length, thickness, section shape fixed; width free	$\eta E_f / \rho$ $\rho / \eta E_f$
		Optimize for vibration amplitude; length, thickness fixed; width, section shape free	$\eta \phi E_f / \rho$ $\rho / \eta \phi E_f$
		Optimize for vibration amplitude; length, width, section shape fixed; thickness free	$\eta E_f^{1/3} / \rho$ $\rho / \eta E_f^{1/3}$
		Optimize for vibration amplitude; length, width fixed; thickness, section shape free	$\eta(\phi E_f)^{1/3} / \rho$ $\rho / \eta(\phi E_f)^{1/3}$
<b>Panel in bending</b>		Optimize for resonant frequency; length, width fixed; thickness free	$\eta E_f / \rho$ $\rho / \eta E_f$
		Optimize for vibration amplitude; length, width fixed; thickness free	$\eta E_f^{1/3} / \rho$ $\rho / \eta E_f^{1/3}$

## Damage-tolerant design

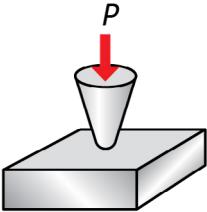
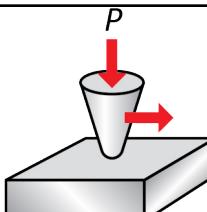
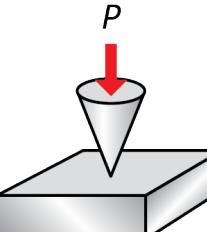
Function and Constraints* <sup>y</sup>		Maximize	Minimize
Damage tolerance (for ties, columns, shafts, beams, panels, springs, etc.)		Maximize flaw tolerance and strength; load limited design	$K_{1c}/\rho$ and $\sigma_y/\rho$
		Maximize flaw tolerance and strength; displacement limited design	$K_{1c}/E\rho$ and $\sigma_y/\rho$
		Maximize flaw tolerance and strength; energy limited design	$K_{1c}^2/E$ and $\sigma_y/\rho$
Pressure Vessel		Yield-before-break limited	$K_{1c}/\sigma_y$
		Leak-before-break limited	$K_{1c}^2/\sigma_y$
Rotating Blade		Resistance to fast fracture; blade length, defect size fixed	$K_{1c}/\rho$
		Resistance to centrifugal loading; blade length, defect size fixed	$\sigma_y/\rho$

\* to minimize **volume**, replace density  $\rho$  by 1 (one). <sup>1,2,3</sup>

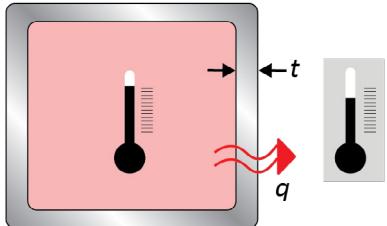
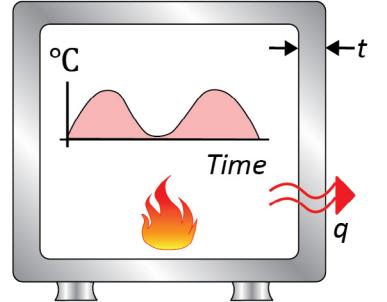
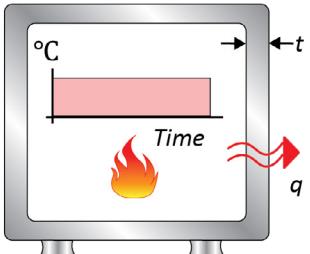
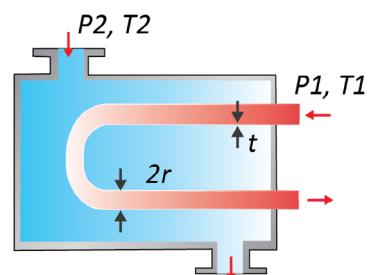
<sup>y</sup> To minimize cost, use the above criteria for minimum weight, replacing density  $\rho$  by  $C_m \rho$ , where  $C_m$  is the material cost per unit mass

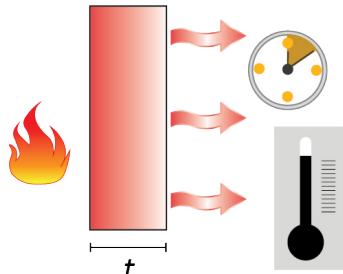
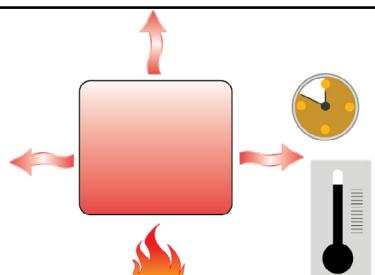
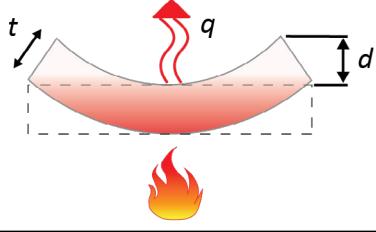
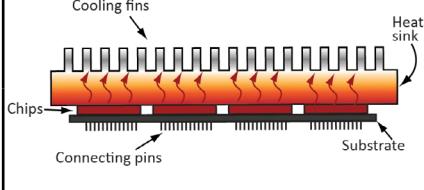
To minimize embodied energy or CO<sub>2</sub> footprint, use the above criteria for minimum mass, replacing  $\rho$  by  $H_m \rho$  or CO<sub>2</sub>  $\rho$ , where H<sub>m</sub> is the embodied energy content per unit mass and CO<sub>2</sub> is the CO<sub>2</sub> footprint per unit mass

## Abrasion resistant design

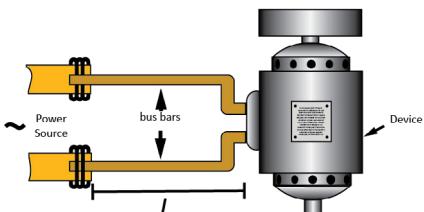
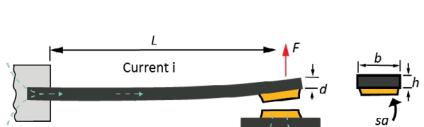
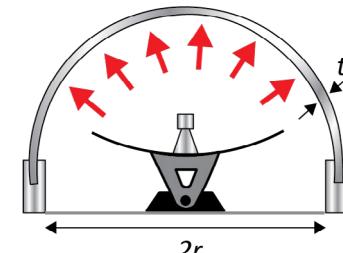
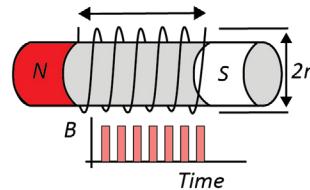
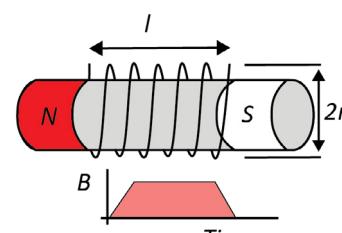
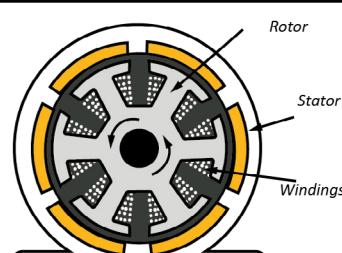
Function and Constraints			Maximize	Minimize
<b>Blunt contact, static load</b>		Optimizing resistance to yielding	$H^3/E^2$	$E^2/H^3$
		Optimizing resistance to cracking	$K_{1c}^2(1-v^2)/E$	$E/K_{1c}^2(1-v^2)$
<b>Blunt contact, sliding load</b>		Optimizing resistance to yielding	$H^3/E^2$	$E^2/H^3$
		Optimizing resistance to cracking	$K_{1c}^3/E^2(1-2v)^3$	$E^2(1-2v)^3/K_{1c}^3$
<b>Sharp contact, static load</b>		Optimizing resistance to yielding	$H$	$1/H$
		Optimizing resistance to cracking	$K_{1c}^4/H^3$	$H^3/K_{1c}^4$

# Thermal and Thermo-mechanical design

Function and Constraints			Maximize	Minimize
<b>Thermal insulation, transitional</b>		Optimize thermal stability; temperature difference, time fixed; thickness free	$1/a = \rho C_p / \lambda$	$a = \lambda / \rho C_p$
<b>Thermal insulation, cyclic heating</b>		Optimize energy consumption per cycle; temperature rise, cycle time fixed; wall thickness free	$(\sqrt{a})/\lambda = (\lambda\rho C_p)^{-1/2}$	$\lambda/(\sqrt{a}) = (\lambda\rho C_p)^{1/2}$
		Optimize mass; temperature rise, cycle time, wall thickness fixed	$(\sqrt{a})/\lambda = ((\rho C_p)/\lambda)^{1/2}$	$\lambda/(\sqrt{a}) = (\lambda/(\rho C_p))^{1/2}$
<b>Thermal insulation, steady state</b>		Optimize mass; minimum heat flux at steady state; thickness specified	$\rho/\lambda$	$\lambda/\rho$
<b>Heat exchanger tubes</b>		Maximum heat flux per unit area; no failure under $\Delta p$	$\lambda\sigma_y$	$1/\lambda\sigma_y$
		Optimize mass; maximum heat flux per unit mass; pressure and temperature difference, tube radius fixed; wall thickness free	$\sigma_y^2 \lambda / \rho$	$\rho / \sigma_y^2 \lambda$

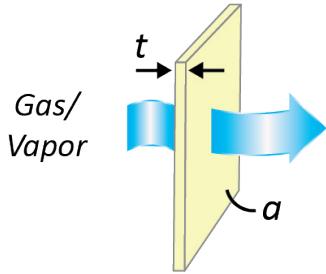
Function and Constraints			Maximize	Minimize
<b>Short-term thermal energy storage</b>		Optimize energy stored for given temperature rise and time $\lambda/(\sqrt{a}) = (\lambda\rho C_p)^{1/2}$ Maximize energy stored for given temperature rise and time $1/(\rho\sqrt{a}) = (C_p/\lambda\rho)^{1/2}$	$\lambda/(\sqrt{a}) = (\lambda\rho C_p)^{1/2}$	$(\sqrt{a})/\lambda = (\lambda\rho C_p)^{-1/2}$
			$1/(\rho\sqrt{a}) = (C_p/\lambda\rho)^{1/2}$	$\rho\sqrt{a} = (\lambda\rho/C_p)^{1/2}$
<b>Long-term thermal energy storage</b>		Maximum energy stored / unit material cost (storage heaters)	$C_p/C_m$	$C_m/C_p$
<b>Thermal stability</b>		Minimize thermal distortion for given heat flux	$\lambda/\alpha$	$\alpha/\lambda$
<b>Thermal shock resistance</b>		Maximum change in surface temperature; no failure	$\sigma_y/E\alpha$	$E\alpha/\sigma_y$
<b>Heat Sinks</b>		Maximum heat flux per unit volume; expansion limited	$\lambda/\Delta\alpha$	$\Delta\alpha/\lambda$
		Maximum heat flux per unit mass; expansion limited	$\lambda/\rho\Delta\alpha$	$\rho\Delta\alpha/\lambda$

# Electro-mechanical design

Function and Constraints			Maximize	Minimize
<b>Bus-bars</b>	 <p>Minimum life-cost; high current conductor</p>		$1/\rho_e \rho C_m$	$\rho_e \rho C_m$
<b>Relay arms</b>	 <p>Minimum response time; no fatigue failure</p>		$\sigma_e/E \rho_e$	$E \rho_e/\sigma_e$
			$\sigma_e^2/E \rho_e$	$E \rho_e/\sigma_e^2$
<b>Radome</b>	 <p>Optimize electromagnetic absorption; pressure difference, radius fixed; thickness free</p>		$\sigma_y/\varepsilon_t \tan[\delta]$	$\varepsilon_t \tan[\delta]/\sigma_y$
<b>Electro-magnet windings, short pulse length</b>	 <p>Maximum short-pulse field; no mechanical failure</p>		$\sigma_y$	$1/\sigma_y$
<b>Electro-magnet windings, long pulse length</b>	 <p>Maximize field and pulse-length, limit on temperature rise</p>		$C_p \rho / \rho_e$	$\rho_e / C_p \rho$
<b>High speed motor windings</b>	 <p>Maximum rotational speed; no fatigue failure</p>		$\sigma_e/\rho_e$	$\rho_e/\sigma_e$
			$1/\rho_e$	$\rho_e$

# Vapor Barrier Design

Vapor barrier design at minimum mass

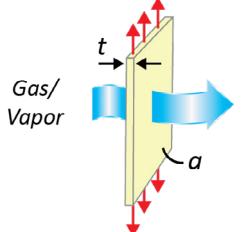
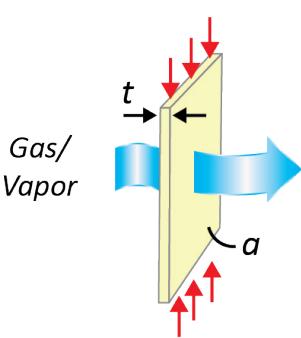
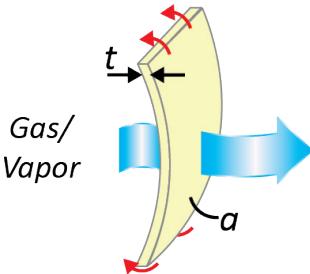
Function and Constraints			Maximize <sup>*,y</sup>	Minimize <sup>*,y</sup>
<b>GAS/VAPOR BARRIER</b> (not subject to significant loads)	 <i>Gas/ Vapor</i>	Permeability resistance (O <sub>2</sub> ), area fixed, thickness free	$1/(P_{O_2}\rho)$	$P_{O_2}\rho$
		Permeability resistance (H <sub>2</sub> O vapor), area fixed, thickness free	$1/(VTR * \rho)$	$VTR * \rho$

\* to minimize **volume**, replace density  $\rho$  by 1 (one). <sup>1,2,3</sup>

<sup>y</sup> To minimize cost, use the above criteria for minimum weight, replacing density  $\rho$  by  $C_m\rho$ , where  $C_m$  is the material cost per unit mass

To minimize embodied energy or CO<sub>2</sub> footprint, use the above criteria for minimum mass, replacing  $\rho$  by  $H_m\rho$  or CO<sub>2</sub> $\rho$ , where H<sub>m</sub> is the embodied energy content per unit mass and CO<sub>2</sub> is the CO<sub>2</sub> footprint per unit mass

## Vapor barrier design at minimum permeability ( $O_2$ )

Function and Constraints			Maximize <sup>+</sup>	Minimize <sup>+</sup>
<b>GAS/VAPOR BARRIER</b> (loaded in tension)	 Gas/Vapor	Stiffness limited, area fixed, thickness free	$E/P_{O_2}$	$P_{O_2}/E$
		Strength limited, area fixed, thickness free	$\sigma_y/P_{O_2}$	$P_{O_2}/\sigma_y$
<b>GAS/VAPOR BARRIER</b> (loaded in compression)	 Gas/Vapor	Stiffness limited, area fixed, thickness free	$E/P_{O_2}$	$P_{O_2}/E$
		Strength limited, area fixed, thickness free	$\sigma_c/P_{O_2}$	$P_{O_2}/\sigma_c$
		Buckling stiffness limited, area fixed, thickness free	$E^{1/3}/P_{O_2}$	$P_{O_2}/E^{1/3}$
		Buckling strength limited, area fixed, thickness free	$(\sigma_y^{1/2})/P_{O_2}$	$P_{O_2}/(\sigma_y^{1/2})$
<b>GAS/VAPOR BARRIER</b> (loaded in bending)	 Gas/Vapor	Stiffness limited, area fixed, thickness free	$E^{1/3}/P_{O_2}$	$P_{O_2}/E^{1/3}$
		Strength limited, area fixed, thickness free	$(\sigma_y^{1/2})/P_{O_2}$	$P_{O_2}/(\sigma_y^{1/2})$
		Elastic flexibility limited, area fixed, thickness free	$\sigma_y/(P_{O_2} * E)$	$(P_{O_2} * E)/\sigma_y$

<sup>+</sup> To minimize permeability ( $H_2O$  vapor), use the above criteria for minimum permeability ( $O_2$ ), replacing Oxygen permeability  $P_{O_2}$  by VTR, where VTR is the water vapor transmission rate

## Symbols used in performance indices for materials

Category	Property	Symbol	Units (Metric)	Units (US Customary)
General	Density	$\rho$	kg/m <sup>3</sup>	lb/in <sup>3</sup>
	Price	$C_m$	currency/kg	currency/lb.
	Shape Factor	$\phi$	dimensionless	dimensionless
Mechanical	Young's modulus	$E$	GPa	10 <sup>6</sup> psi
	Shear modulus	$G$	GPa	10 <sup>6</sup> psi
	Bulk modulus	$K$	GPa	10 <sup>6</sup> psi
	Flexural modulus	$E_f$	GPa	10 <sup>6</sup> psi
	Poisson's ratio	$\nu$	dimensionless	dimensionless
	Failure strength (Yield, fracture)	$\sigma_y$	MPa	ksi
	Fatigue strength	$\sigma_e$	MPa	ksi
	Compression strength	$\sigma_c$	MPa	ksi
	Flexural strength (modulus of rupture)	$\sigma_f$	MPa	ksi
	Hardness	$H$	Vickers	Vickers
	Fracture toughness	$K_{Ic}$	MPa.m <sup>1/2</sup>	ksi.in <sup>1/2</sup>
	Loss coefficient (damping capacity)	$\eta$	dimensionless	dimensionless
Thermal	Thermal conductivity	$\lambda$	W/m.K	BTU.ft/h.ft <sup>2</sup>
	Thermal diffusivity	$a$	m <sup>2</sup> /s	ft <sup>2</sup> /s
	Specific heat	$C_p$	J/kg.K	BTU/lb.F
	Thermal expansion coefficient	$\alpha$	K <sup>-1</sup>	°F <sup>-1</sup>
	Difference in thermal conductivity	$\Delta\alpha$	K <sup>-1</sup>	°F <sup>-1</sup>

Category	Property	Symbol	Units (Metric)	Units (US Customary)
Electrical	Electrical resistivity	$\rho_e$	$\mu\Omega \cdot \text{cm}$	$\mu\Omega \cdot \text{cm}$
	Dielectric constant (relative permittivity)	$\epsilon_r$	<i>dimensionless</i>	<i>dimensionless</i>
	Dissipation factor (dielectric loss tangent)	$\tan\delta$	<i>dimensionless</i>	<i>dimensionless</i>
Eco-properties	Energy required per unit mass to produce material (embodied energy)	$H_m$	MJ/kg	kcal/lb
	CO <sub>2</sub> footprint (CO <sub>2</sub> mass produced per unit mass of material produced)	CO <sub>2</sub>	kg/kg	lb/lb
Diffusion	Oxygen permeability	$P_{O_2}$	cm <sup>3</sup> .mm/(m <sup>2</sup> .day.atm)	cm <sup>3</sup> .mm/(m <sup>2</sup> .day.atm)
	Water vapor transmission rate	VTR	g.mm/(m <sup>2</sup> .day)	g.mm/(m <sup>2</sup> .day)

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