

## Task 3: The effect of shape

**Instructions:** Check the following questions and exercises. Read chapters 9 and 10 in the 4<sup>th</sup> edition of the course textbook about the selection of material and shape.

**Criterion:** A good report on this task demonstrates a good understanding of:

- the meaning of shape factors, and consequently how to calculate them
- theoretical and practical considerations of how different shapes allow the use of materials efficiently
- how shape factors can be used to take the effect of shape into account in materials selection

**Task 3.1.1:** Calculate the shape factor for bending stiffness for Glass-reinforced plastic (GRP) bar, when the profile of the bar is:

- solid square profile, width, and height 100 mm.
- solid rectangle profile, width 500 mm, height 100 mm.
- hollow square profile, outer width and height 100 mm, wall thickness 10 mm.
- hollow round pipe, outer diameter 500 mm, wall thickness 10 mm.
- a spar of the wind turbine blade, whose cross-section is either an I-beam with a width of 500 mm, height of 100 mm, flange thickness of 10 mm, and web thickness of 20 mm, or a box girder with a width of 500 mm, height 100 mm, wall thickness 10 mm

**Note:** Including the calculation procedure in your report is beneficial. In case you make mathematical mistakes at the end, there are still points for the correct solution steps.

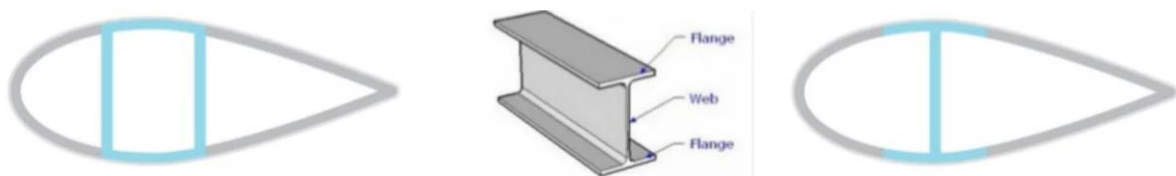


Figure 1 spar with a hollow rectangular and I-beam cross-section

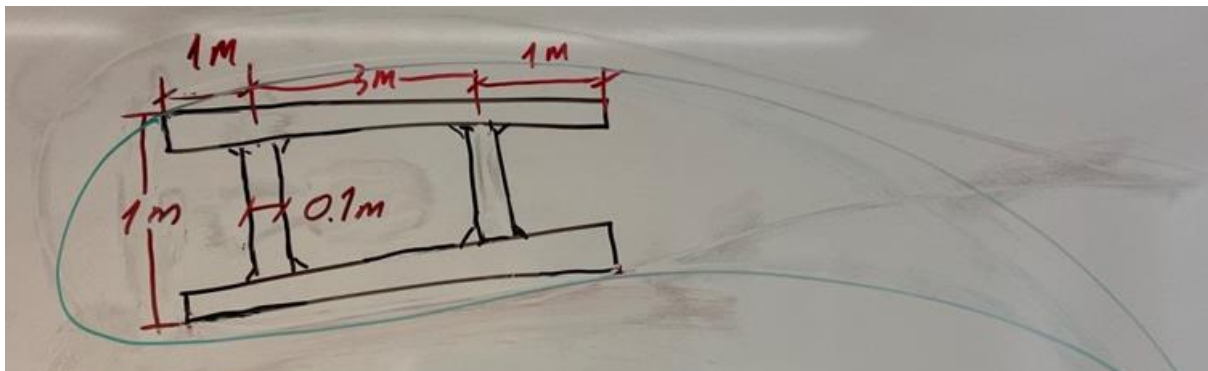


Figure 2 A box girder spar with dimensions



**Task 3.1.2:** First, **apply all 5 profiles** to the “level 2” bending stiffness map for the **GRP bar**. Then, **select 2 profiles with 2 different materials** (e.g., Carbon-fiber-reinforced polymers (CFRP) and 6061 T6 aluminum), and **add** these **4** records to the GRP bending stiffness map. **Compare** the overall **9** records among these **3** materials, and **discuss** your observations regarding the locus of these points on the selection chart, preferably with figures and tables.

**Hint:** Find the properties of each material, apply the calculated factors, and use the “Add records” tool (*Tools – Add records*) to construct the map.

**Task 3.2.1:** **Calculate** the theoretical maximum shape factor for a low alloy steel, aluminum, CFRP, and wood, according to equation 9.15a from the textbook (4<sup>th</sup> edition):  $(\varphi_B^e)_{max} \approx 2.3 \left( \frac{E}{\sigma_f} \right)^{0.5}$ .

**Compare** your results to the empirical maximum shape factors found in Table 9.4 of the textbook (4<sup>th</sup> edition) reproduced below. **Discuss** the extent to which theoretical and empirical results agree or differ.

Material	$(\varphi_B^e)_{max}$
Steel	65
6061 aluminum	44
CFRP	39
Polymer	12
Wood	5
Elastomers	<6

**Task 3.2.2:** Which of these materials, structural steel, aluminum, wood, or CFRP, would be the best choice for a bending beam? The beam must have a stiffness  $S = EI_{max} > 10^7 \text{ Nm}^2$  and the beam has to be as light as possible. Use the following shape factors in your solution: steel (I-beam) 15, aluminum (I-beam) 10, CFRP (tube) 10, and wood (beam) 2. Resolve the problem using the 4-field method, and present your answers together with the decision-making process with text and figures.

**Hint:** You do not need to draw the 4-field map by yourself, you can use the one from the book.

Material: E- $\rho$

Stiffness coefficient: E-I

Performance: A- $\rho$

Shape factor: A-I

