

Consider a square of sidelength n and $(n + 1)^2$ interior points. Prove that we can choose 3 of these points so that they determine a triangle (eventually degenerated) of area at most $\frac{1}{2}$.