

Email training, N12  
December 8-14, 2019

**Problem 12.1.** Find the minimal possible value of the expression

$$|a - 1| + |b - 2| + |c - 3| + |3a + 2b + c|.$$

**Problem 12.2.** Let  $s$  is the number of divisors of positive integer  $n$ . Evaluate the product of divisors of  $n$  in terms of  $s$  and  $n$ .

**Problem 12.3.** Find the smallest integer  $n$  such that  $2019!$  is not divisible by  $n^n$ .

**Problem 12.4.** Find the maximal possible value of the expression

$$|\dots||x_1 - x_2| - x_3| - x_4| - \dots - x_{1990}|,$$

where  $x_1, x_2, \dots, x_{1990}$  is the permutation of numbers  $1, 2, 3, \dots, 1990$ .

**Problem 12.5.** The numbers 12, 1, 10, 6, 8, 3 (in written order) are written on the vertices of regular hexagon. On each step one allowed to choose any side of the hexagon and either increase by 1 values written on the vertices of the side, either decrease both of them by 1. Is it possible to get the following configurations?

- a) 14, 6, 13, 4, 5, 2;
- b) 6, 17, 14, 3, 15, 3.

**Problem 12.6.** Let there are  $n$  regions on the plane, part of them are red, and the rest are blue. At each step one allowed to choose a region  $X$ , such that most of it's region have different from  $X$  color and paint region  $X$  by opposite color. Prove, that this process can't be processed infinitely long time.

Solution submission deadline December 14, 2019