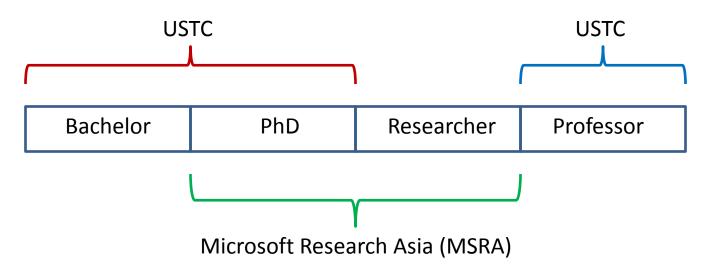
# Python与深度学习基础之神经网络(Neural Network)

Zhiwei Xiong (熊志伟)

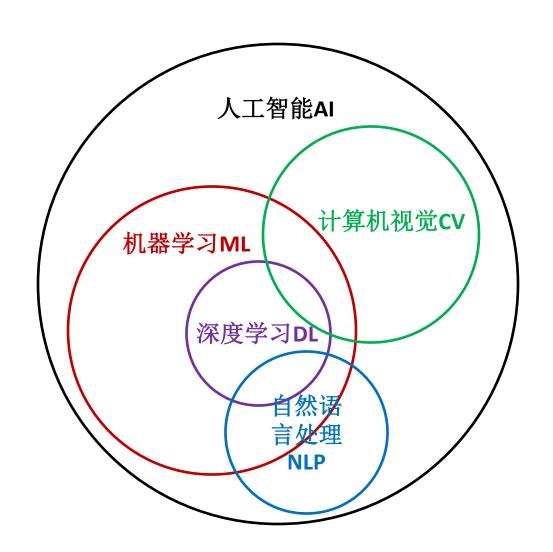
http://staff.ustc.edu.cn/~zwxiong/

## Self Introduction



- USTC from 2002
- MSRA from 2006
- Back to USTC 2016
- Research: computer vision & image processing

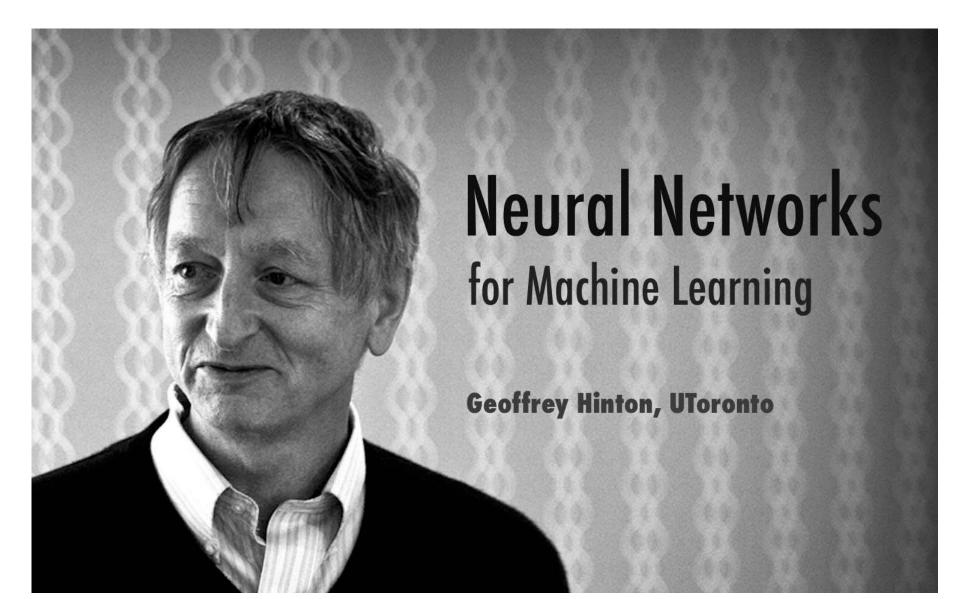
# What is deep learning?



## What is neural network?

- 机器学习方法
  - 决策树 Decision Tree
  - 线性分类器Linear Classification
  - 支持向量机Support Vector Machine
  - -神经网络Neural Network
    - 深度神经网络Deep Neural Network

# Father of Deep Learning



# **Turing Award 2019**

**Geoffrey Hinton** 

#### Yann LeCun

Yoshua Bengio

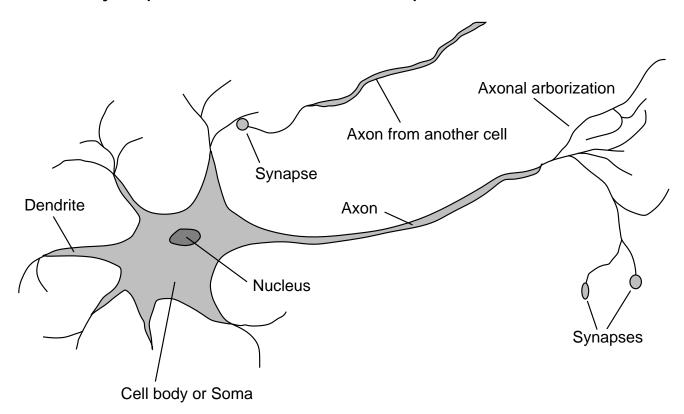




- 反向传播
- 玻尔兹曼机
- 改进了卷积神经网络
- 卷积神经网络CNN
- 反向传播雏形
- 拓展了神经网络的视野
- 序列的概率模型
- 高维词汇嵌入和注意机制
- 生成对抗网络GAN

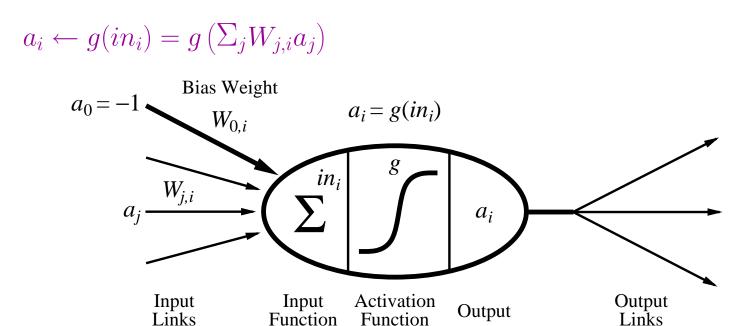
#### **Brains**

 $10^{11}$  neurons of >20 types,  $10^{14}$  synapses, 1ms–10ms cycle time Signals are noisy "spike trains" of electrical potential



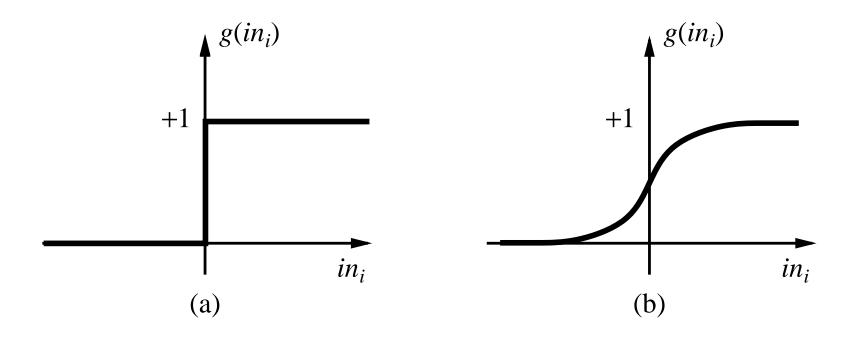
#### McCulloch-Pitts "unit"

Output is a "squashed" linear function of the inputs:



A gross oversimplification of real neurons, but its purpose is to develop understanding of what networks of simple units can do

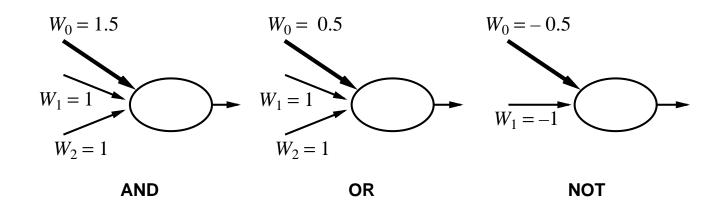
#### **Activation functions**



- (a) is a step function or threshold function
- (b) is a sigmoid function  $1/(1+e^{-x})$

Changing the bias weight  $W_{0,i}$  moves the threshold location

#### Implementing logical functions



McCulloch and Pitts: every Boolean function can be implemented

#### Network structures

#### Feed-forward networks:

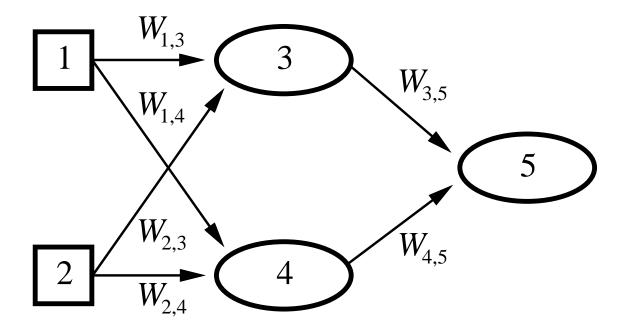
- single-layer perceptrons
- multi-layer perceptrons

Feed-forward networks implement functions, have no internal state

#### Recurrent networks:

- Hopfield networks have symmetric weights  $(W_{i,j} = W_{j,i})$  g(x) = sign(x),  $a_i = \pm 1$ ; holographic associative memory
- Boltzmann machines use stochastic activation functions,  $\approx$  MCMC in Bayes nets
- recurrent neural nets have directed cycles with delays
  - $\Rightarrow$  have internal state (like flip-flops), can oscillate etc.

#### Feed-forward example

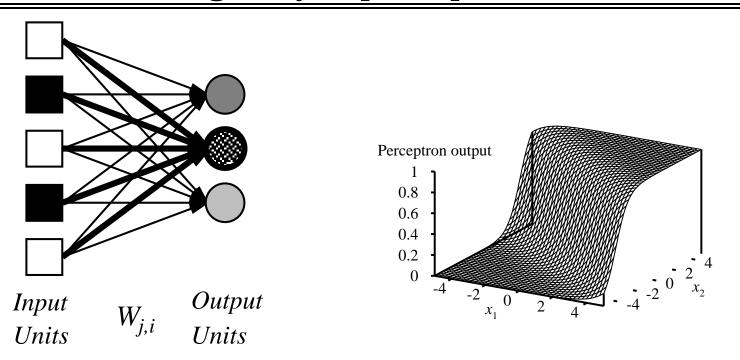


Feed-forward network = a parameterized family of nonlinear functions:

$$a_5 = g(W_{3,5} \cdot a_3 + W_{4,5} \cdot a_4)$$
  
=  $g(W_{3,5} \cdot g(W_{1,3} \cdot a_1 + W_{2,3} \cdot a_2) + W_{4,5} \cdot g(W_{1,4} \cdot a_1 + W_{2,4} \cdot a_2))$ 

Adjusting weights changes the function: do learning this way!

### Single-layer perceptrons



Output units all operate separately—no shared weights

Adjusting weights moves the location, orientation, and steepness of cliff

#### Expressiveness of perceptrons

Consider a perceptron with g = step function (Rosenblatt, 1957, 1960)

Can represent AND, OR, NOT, majority, etc., but not XOR

Represents a linear separator in input space:

Minsky & Papert (1969) pricked the neural network balloon

#### Perceptron learning

Learn by adjusting weights to reduce error on training set

The squared error for an example with input x and true output y is

$$E = \frac{1}{2}Err^2 \equiv \frac{1}{2}(y - h_{\mathbf{W}}(\mathbf{x}))^2 ,$$

Perform optimization search by gradient descent:

$$\frac{\partial E}{\partial W_j} = Err \times \frac{\partial Err}{\partial W_j} = Err \times \frac{\partial}{\partial W_j} \left( y - g(\sum_{j=0}^n W_j x_j) \right)$$
$$= -Err \times g'(in) \times x_j$$

Simple weight update rule:

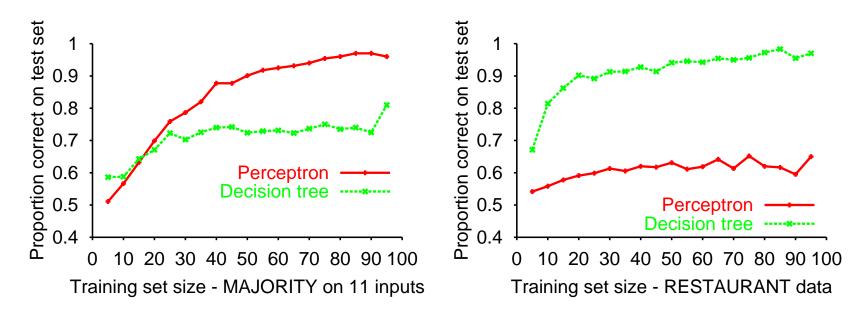
$$W_j \leftarrow W_j + \alpha \times Err \times g'(in) \times x_j$$

E.g., +ve error  $\Rightarrow$  increase network output

 $\Rightarrow$  increase weights on +ve inputs, decrease on -ve inputs

#### Perceptron learning contd.

Perceptron learning rule converges to a consistent function for any linearly separable data set

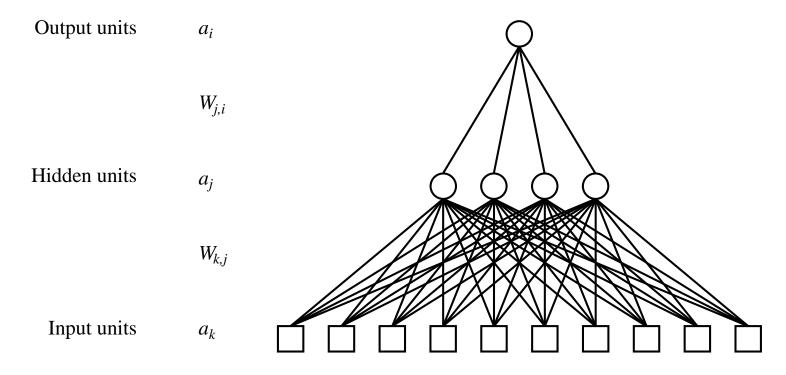


Perceptron learns majority function easily, DTL is hopeless

DTL learns restaurant function easily, perceptron cannot represent it

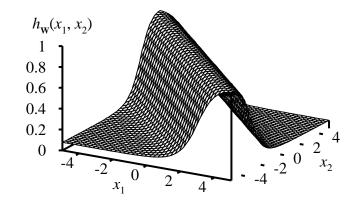
### Multilayer perceptrons

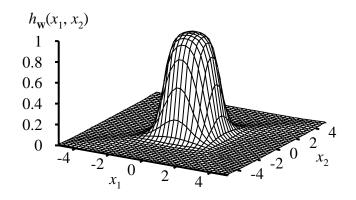
Layers are usually fully connected; numbers of hidden units typically chosen by hand



#### Expressiveness of MLPs

All continuous functions w/2 layers, all functions w/3 layers





Combine two opposite-facing threshold functions to make a ridge

Combine two perpendicular ridges to make a bump

Add bumps of various sizes and locations to fit any surface

Proof requires exponentially many hidden units (cf DTL proof)

#### Back-propagation learning

Output layer: same as for single-layer perceptron,

$$W_{j,i} \leftarrow W_{j,i} + \alpha \times a_j \times \Delta_i$$

where 
$$\Delta_i = Err_i \times g'(in_i)$$

Hidden layer: back-propagate the error from the output layer:

$$\Delta_j = g'(in_j) \sum_i W_{j,i} \Delta_i .$$

Update rule for weights in hidden layer:

$$W_{k,j} \leftarrow W_{k,j} + \alpha \times a_k \times \Delta_j$$
.

(Most neuroscientists deny that back-propagation occurs in the brain)

#### Back-propagation derivation

The squared error on a single example is defined as

$$E = \frac{1}{2} \sum_{i} (y_i - a_i)^2 ,$$

where the sum is over the nodes in the output layer.

$$\frac{\partial E}{\partial W_{j,i}} = -(y_i - a_i) \frac{\partial a_i}{\partial W_{j,i}} = -(y_i - a_i) \frac{\partial g(in_i)}{\partial W_{j,i}} 
= -(y_i - a_i) g'(in_i) \frac{\partial in_i}{\partial W_{j,i}} = -(y_i - a_i) g'(in_i) \frac{\partial}{\partial W_{j,i}} \left(\sum_j W_{j,i} a_j\right) 
= -(y_i - a_i) g'(in_i) a_j = -a_j \Delta_i$$

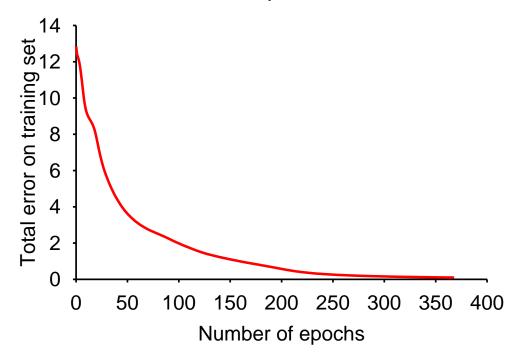
#### Back-propagation derivation contd.

$$\frac{\partial E}{\partial W_{k,j}} = -\sum_{i} (y_i - a_i) \frac{\partial a_i}{\partial W_{k,j}} = -\sum_{i} (y_i - a_i) \frac{\partial g(in_i)}{\partial W_{k,j}} 
= -\sum_{i} (y_i - a_i) g'(in_i) \frac{\partial in_i}{\partial W_{k,j}} = -\sum_{i} \Delta_i \frac{\partial}{\partial W_{k,j}} \left( \sum_{j} W_{j,i} a_j \right) 
= -\sum_{i} \Delta_i W_{j,i} \frac{\partial a_j}{\partial W_{k,j}} = -\sum_{i} \Delta_i W_{j,i} \frac{\partial g(in_j)}{\partial W_{k,j}} 
= -\sum_{i} \Delta_i W_{j,i} g'(in_j) \frac{\partial in_j}{\partial W_{k,j}} 
= -\sum_{i} \Delta_i W_{j,i} g'(in_j) \frac{\partial}{\partial W_{k,j}} \left( \sum_{k} W_{k,j} a_k \right) 
= -\sum_{i} \Delta_i W_{j,i} g'(in_j) a_k = -a_k \Delta_j$$

#### Back-propagation learning contd.

At each epoch, sum gradient updates for all examples and apply

Training curve for 100 restaurant examples: finds exact fit



Typical problems: slow convergence, local minima

#### Back-propagation learning contd.

Learning curve for MLP with 4 hidden units:



MLPs are quite good for complex pattern recognition tasks, but resulting hypotheses cannot be understood easily

#### Summary

Most brains have lots of neurons; each neuron  $\approx$  linear–threshold unit (?)

Perceptrons (one-layer networks) insufficiently expressive

Multi-layer networks are sufficiently expressive; can be trained by gradient descent, i.e., error back-propagation

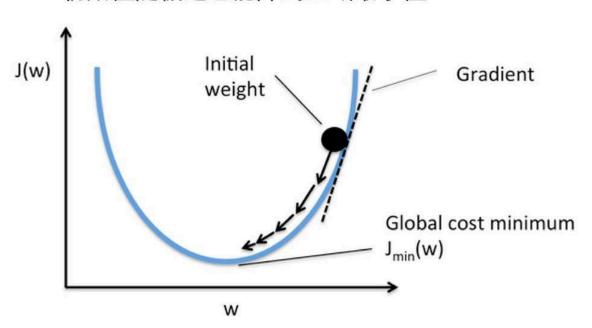
Many applications: speech, driving, handwriting, fraud detection, etc.

Engineering, cognitive modelling, and neural system modelling subfields have largely diverged

## **Gradient Descent**

線性關係

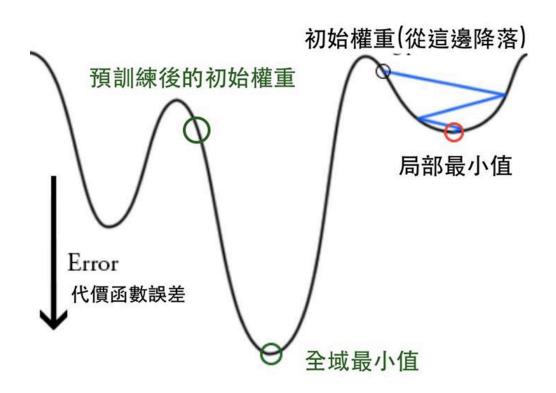
代價函數為凸函數 初始值隨機選也能降到全域最小值



# Vanishing Gradient

#### 非線性關係

代價函數為非凸函數 初始值隨機選容易降到局部最小值



# Reducing the Dimensionality of Data with Neural Networks

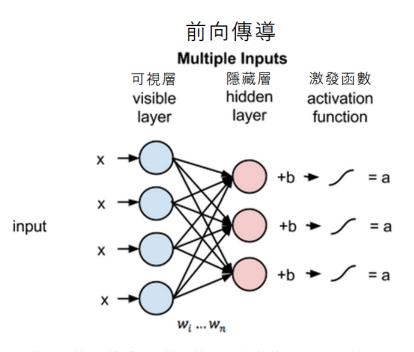
G. E. Hinton\* and R. R. Salakhutdinov

High-dimensional data can be converted to low-dimensional codes by training a multilayer neural network with a small central layer to reconstruct high-dimensional input vectors. Gradient descent can be used for fine-tuning the weights in such "autoencoder" networks, but this works well only if the initial weights are close to a good solution. We describe an effective way of initializing the weights that allows deep autoencoder networks to learn low-dimensional codes that work much better than principal components analysis as a tool to reduce the dimensionality of data.

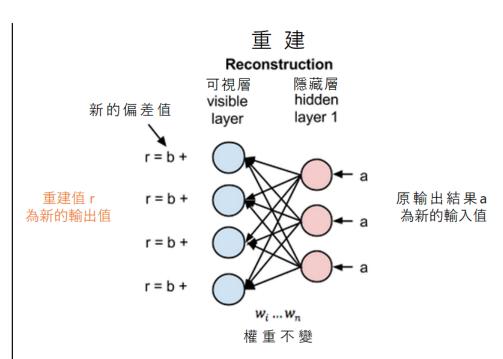
imensionality reduction facilitates the classification, visualization, communication, and storage of high-dimensional data. A simple and widely used method is principal components analysis (PCA), which

finds the directions of greatest variance in the data set and represents each data point by its coordinates along each of these directions. We describe a nonlinear generalization of PCA that uses an adaptive, multilayer "encoder" network

## Restricted Boltzmann Machines

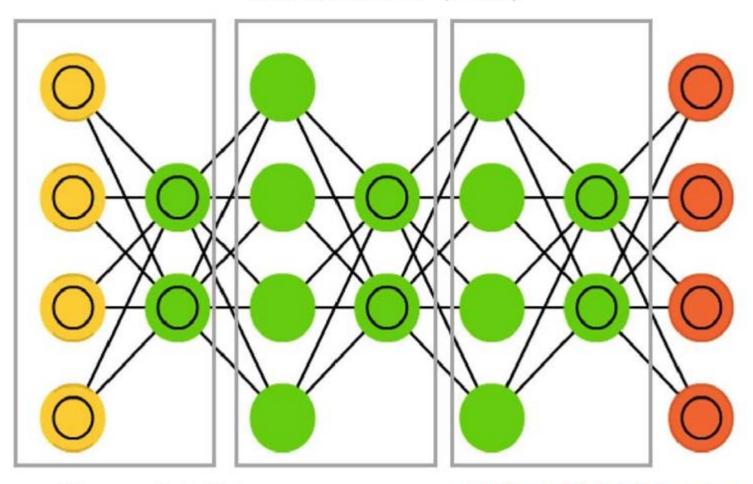


激發函數 f((權重 w \* 輸入值 x) + 偏差值 b) = 輸出結果 a



# Deep Belief Network

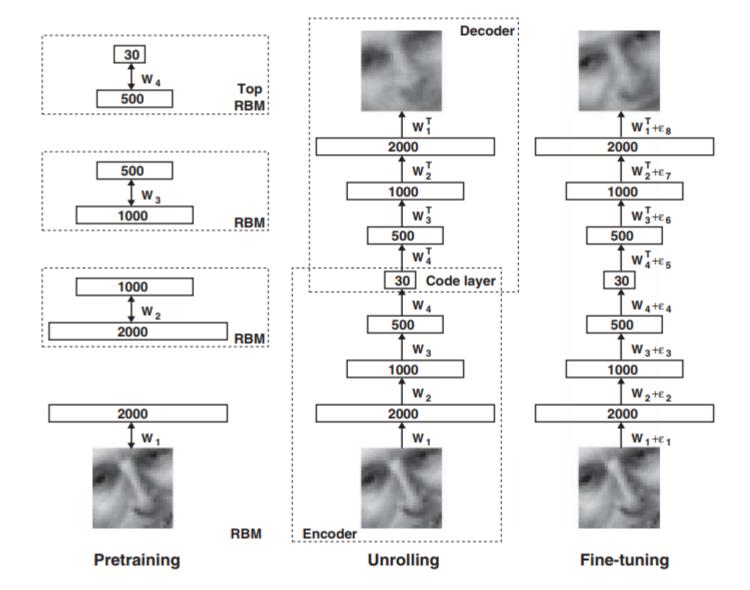
深度信念網路 (DBN)



將 RBM 堆疊起來 (Stacked RBM)

最後一層放分類器 (Classifier)

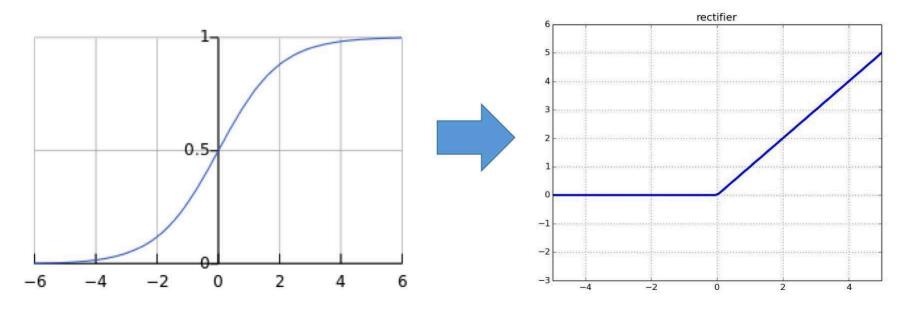
## Autoencoder Network



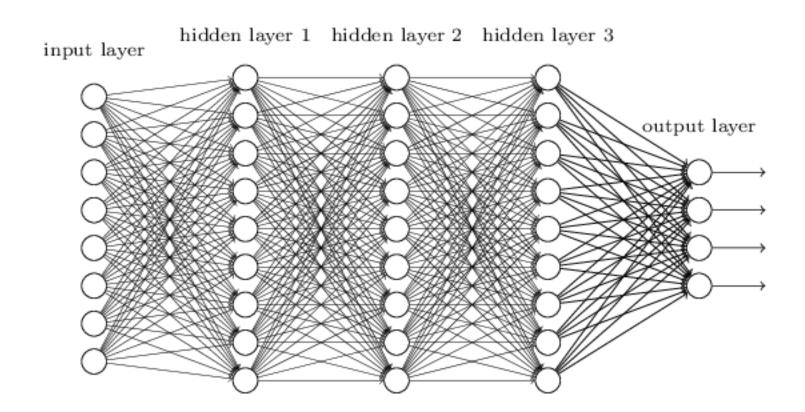
## A Better Solution: MLP + ReLU

#### 激發函數的調整更好解決梯度消失問題

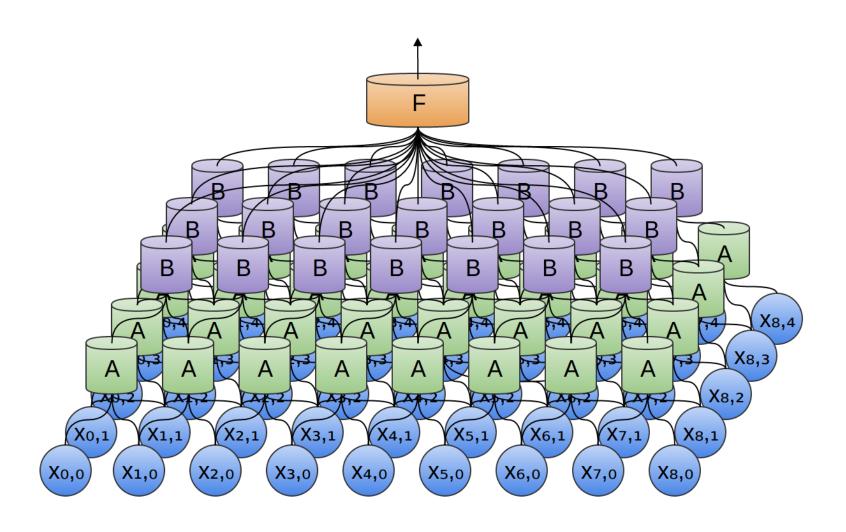
ReLU函數近年來有取代傳統sigmoid函數神經元的趨勢。



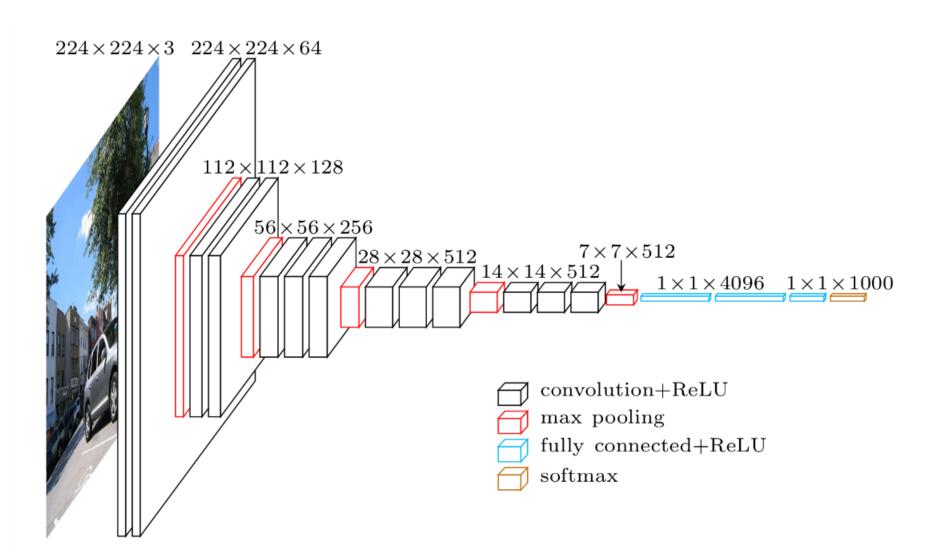
# Fully Connected Layers



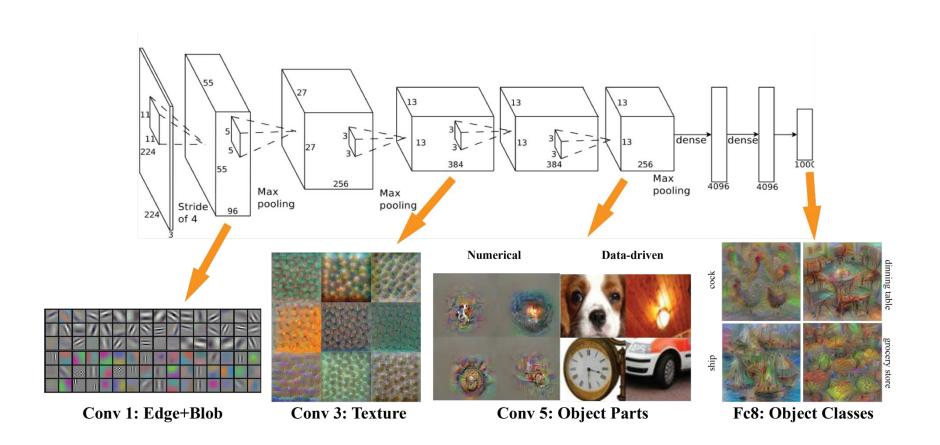
# Convolutional Layers



# A Typical Deep Network



## Visualization of CNN



# More Reading

## REVIEW

doi:10.1038/nature14539

## Deep learning

Yann LeCun<sup>1,2</sup>, Yoshua Bengio<sup>3</sup> & Geoffrey Hinton<sup>4,5</sup>

Deep learning allows computational models that are composed of multiple processing layers to learn representations of data with multiple levels of abstraction. These methods have dramatically improved the state-of-the-art in speech recognition, visual object recognition, object detection and many other domains such as drug discovery and genomics. Deep learning discovers intricate structure in large data sets by using the backpropagation algorithm to indicate how a machine should change its internal parameters that are used to compute the representation in each layer from the representation in the previous layer. Deep convolutional nets have brought about breakthroughs in processing images, video, speech and audio, whereas recurrent nets have shone light on sequential data such as text and speech.