SD - Aug 30

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Question: Draw 50 random sample of size 25 each from the following distributions:

- (i) Rectangular(0, 1)
- (ii) Nomal(0, 1)

##

(iii) Cauchy(0, 1)

Compute the statistics below for each sample:

```
(i) \bar{X}_n, (ii) X_{(1)}, (iii) X_{(n)}, (iv) Med(X) set.seed(30) library(ggplot2)
```

The Rectangular (0, 1) distribution:

Drawing 50 random samples:

```
samp1 <- replicate(50, runif(25, 0, 1))
samp1

## [,1] [,2] [,3] [,4] [,5] [,6]
## [1,] 0.09878282 0.2973978 0.13645145 0.395779653 0.19794849 0.4357022
## [2,] 0.48823179 0.4763574 0.16730515 0.984985246 0.80378294 0.3857202
## [3,] 0.36403673 0.2563579 0.29659443 0.882247154 0.54903277 0.3594613</pre>
```

[5,] 0.30096439 0.4693751 0.07762887 0.094879959 0.26773305 0.3251900 ## [6,] 0.14763513 0.6058477 0.88565553 0.159730863 0.13038539 0.8013029 ## [7,] 0.89857491 0.2333836 0.10698215 0.484631268 0.04328997 0.4495942 ## [8,] 0.22355651 0.4921895 0.07899135 0.878909588 0.83419952 0.1789526 ## [9,] 0.96596330 0.6071742 0.59170621 0.795814868 0.76295112 0.4197278 ## [10,] 0.14106704 0.2998100 0.85000749 0.315599537 0.64596295 0.6556245 ## [11,] 0.06535501 0.6686493 0.04224549 0.098180273 0.17995765 0.5759580 ## [12,] 0.39725471 0.0793686 0.09535451 0.047571812 0.48125640 0.6384687 ## [13,] 0.54399676 0.4103161 0.73067664 0.047516478 0.99531705 0.6138759 ## [14,] 0.87963113 0.0333278 0.56602656 0.871602137 0.86108949 0.9513179

[4,] 0.42061913 0.8106153 0.41316954 0.001670874 0.61189834 0.9425587

[15,] 0.22338939 0.2747117 0.76634877 0.621060567 0.30446102 0.5853048 ## [16,] 0.92094417 0.4371046 0.60961343 0.375395771 0.53469872 0.8675296 ## [17,] 0.25146172 0.6206256 0.48317353 0.134578747 0.19314806 0.7498351

[18,] 0.83046382 0.7747034 0.19993850 0.569797243 0.29127136 0.2294632 ## [19,] 0.60815737 0.4851259 0.58550682 0.654165118 0.65070246 0.3818295

[20,] 0.43135087 0.1808502 0.98846726 0.265818339 0.83008782 0.9778312 ## [21,] 0.15308963 0.6901507 0.96161447 0.995261409 0.83498573 0.5440337

```
## [22,] 0.58556296 0.7881247 0.03811624 0.050551693 0.58363913 0.4897843
## [23,] 0.03442537 0.2748119 0.58720106 0.075601726 0.65512150 0.1465837
  [24,] 0.32988994 0.9319606 0.62571272 0.250955993 0.26920039 0.4660419
   [25,] 0.25213389 0.1649692 0.70245644 0.010477407 0.63617399 0.5842838
                [,7]
                           [,8]
                                     [,9]
                                               [,10]
                                                          [,11]
                                                                      [,12]
##
    [1,] 0.692021806 0.84496502 0.6955628 0.07277298 0.77010700 0.72370103
    [2,] 0.289385920 0.23255791 0.3091034 0.02951835 0.08064415 0.10842686
    [3,] 0.234163941 0.14725974 0.1232451 0.01136248 0.18508206 0.49358280
    [4,] 0.051134567 0.67383079 0.8774552 0.91084470 0.96645063 0.21281199
    [5,] 0.865500215 0.14374284 0.7491301 0.61299291 0.57374567 0.43444714
    [6,] 0.151273756 0.71376553 0.7261369 0.10962091 0.70326575 0.01971062
    [7,] 0.263506581 0.95611736 0.2918561 0.32805381 0.11934085 0.10817603
   [8,] 0.930298233 0.41224375 0.4913098 0.65776352 0.02140614 0.36677609
   [9,] 0.421836107 0.92724681 0.3679289 0.35030832 0.34383348 0.99949264
## [10,] 0.004004411 0.31942295 0.7907357 0.19155336 0.73368451 0.42280594
## [11,] 0.802764247 0.83955466 0.5458015 0.22329389 0.40620436 0.63797663
## [12,] 0.954157097 0.71657280 0.8297549 0.85201816 0.12287562 0.24056558
## [13,] 0.285644288 0.17463708 0.2139297 0.74431942 0.45159445 0.75656125
## [14,] 0.469624718 0.09796882 0.3717849 0.91153499 0.74424168 0.93345296
## [15,] 0.439502541 0.46960682 0.6879379 0.05955640 0.13985608 0.88441077
## [16,] 0.674009262 0.60308014 0.9173555 0.30808086 0.63671048 0.06786013
## [17,] 0.333993289 0.80900927 0.5959598 0.33668941 0.93603420 0.53997199
## [18,] 0.957794233 0.53989606 0.3071337 0.02486925 0.76923553 0.11263237
## [19.] 0.986746531 0.12306094 0.5473485 0.89081715 0.84278787 0.18192331
## [20,] 0.702242127 0.60624939 0.2788492 0.95537335 0.21856648 0.04165444
## [21,] 0.020996978 0.24412915 0.4526890 0.19972966 0.96089413 0.88588319
## [22,] 0.815329046 0.58391438 0.7055959 0.69792332 0.94799822 0.10294309
## [23,] 0.143222455 0.23347346 0.5713688 0.92172704 0.88258693 0.55297433
## [24,] 0.900612770 0.08322308 0.5329214 0.03141096 0.37373876 0.15940196
  [25,] 0.942039193 0.80947109 0.2543833 0.37381262 0.14121825 0.43712100
##
              [,13]
                         [,14]
                                     [,15]
                                               [,16]
                                                          [,17]
##
    [1,] 0.22195921 0.89030099 0.338600985 0.6003906 0.42129555 0.11452322
    [2,] 0.97325657 0.72381253 0.095665211 0.6636447 0.45788055 0.27914954
    [3,] 0.44972098 0.18551558 0.250598309 0.5275241 0.65635253 0.13794890
    [4,] 0.66591407 0.13518944 0.554320173 0.2462430 0.96121626 0.17156126
   [5,] 0.17032431 0.48510523 0.858856739 0.3540606 0.86768899 0.65297969
    [6,] 0.71050789 0.04642570 0.599453649 0.0089029 0.87150560 0.80949441
   [7,] 0.28366301 0.05119415 0.548733333 0.1986179 0.39775045 0.72911179
    [8,] 0.16717404 0.51860728 0.156667443 0.9445149 0.91226587 0.02552564
   [9,] 0.61915059 0.31575681 0.432355981 0.5139751 0.89539333 0.82580260
## [10,] 0.13782779 0.16599924 0.318859533 0.9031082 0.32043654 0.24367859
## [11,] 0.05340944 0.47176338 0.950332988 0.6193075 0.07277936 0.13310983
## [12,] 0.97126520 0.01004325 0.001377158 0.6089844 0.17562269 0.80563828
## [13,] 0.04657108 0.44922264 0.037994377 0.9953839 0.68999758 0.91149100
## [14,] 0.33409237 0.18140094 0.970445728 0.3002348 0.94983026 0.41402115
## [15,] 0.65585573 0.03216818 0.117516203 0.1968216 0.63117686 0.59905752
## [16,] 0.46988378 0.59196233 0.015774151 0.4382741 0.19976297 0.91048721
## [17,] 0.02002500 0.55678626 0.920887904 0.7544148 0.13331506 0.09205075
## [18,] 0.71082238 0.35426583 0.994959084 0.3924943 0.52927172 0.39939335
## [19,] 0.19646000 0.36367295 0.719795119 0.1198882 0.52597929 0.09722963
## [20,] 0.53028791 0.02836102 0.312087854 0.7391164 0.96324012 0.98444160
## [21,] 0.86917857 0.14234072 0.898161637 0.3599746 0.76389148 0.40298082
## [22,] 0.23633955 0.37938796 0.618978276 0.1011689 0.51267767 0.97093580
## [23,] 0.44016330 0.29270269 0.135893565 0.4632031 0.54496063 0.50766174
```

```
## [24,] 0.56039413 0.05981305 0.293934692 0.4353388 0.81168334 0.91197132
   [25,] 0.77081281 0.99328463 0.072332910 0.2781692 0.82940078 0.19875491
##
                          [,20]
                                     [,21]
                                                 [,22]
    [1,] 0.29408054 0.311778182 0.23371977 0.140295117 0.002523081 0.442409225
##
##
    [2,] 0.24779042 0.144438945 0.41466086 0.357329789 0.703200192 0.448565430
    [3,] 0.78361957 0.950417558 0.89589626 0.601600691 0.168903483 0.555024537
##
    [4,] 0.92274413 0.780230260 0.42267745 0.992589954 0.036175763 0.335922234
    [5,] 0.29308329 0.731204654 0.22681910 0.688944571 0.932342545 0.769074283
    [6,] 0.18580017 0.040930673 0.70568604 0.213524386 0.529006831 0.478981720
    [7,] 0.39609163 0.056601550 0.75330500 0.977344373 0.716931635 0.561561592
    [8,] 0.19697373 0.148751318 0.13692213 0.951613500 0.290582908 0.477952700
   [9,] 0.94510859 0.442900970 0.60829967 0.024130482 0.853192323 0.535023910
## [10,] 0.05911431 0.768673621 0.41823938 0.085238743 0.491982570 0.814692287
## [11,] 0.22635133 0.792308825 0.39692283 0.585878141 0.317625932 0.091447619
## [12,] 0.55308646 0.109910481 0.64089145 0.880217842 0.512529559 0.815768319
## [13,] 0.57417748 0.727027005 0.18886555 0.005918184 0.700121480 0.774776843
## [14,] 0.10634544 0.849044108 0.76316497 0.390972439 0.398606442 0.301657159
## [15,] 0.29071622 0.964650379 0.19210122 0.702037414 0.141272729 0.483891945
## [16,] 0.74470414 0.180267791 0.83241123 0.237828817 0.115988636 0.252828720
## [17,] 0.31383967 0.565645968 0.11289691 0.527150075 0.587711293 0.919860395
## [18,] 0.96211532 0.686360021 0.01816265 0.382302124 0.317692986 0.425786042
## [19,] 0.21449216 0.544901679 0.34645791 0.571707363 0.042413462 0.842307801
## [20,] 0.56870566 0.239301624 0.76381245 0.240712078 0.441417954 0.780012067
## [21,] 0.51155953 0.529253500 0.04211637 0.114867788 0.349124721 0.800752893
## [22,] 0.33380417 0.007755061 0.01741369 0.464718077 0.251548364 0.948441539
  [23,] 0.98507899 0.243613814 0.07992041 0.483778921 0.609875458 0.169576000
  [24,] 0.81644494 0.390909684 0.36839629 0.688967616 0.891015803 0.034971510
   [25,] 0.34163974 0.100562136 0.62828754 0.827096262 0.996273146 0.001138356
##
              [,25]
                         [,26]
                                   [,27]
                                               [,28]
                                                          [,29]
    [1,] 0.22430510 0.70182615 0.6979170 0.638379752 0.54828852 0.988755857
    [2,] 0.44744544 0.86114730 0.3284509 0.833529117 0.81388016 0.011906762
##
    [3,] 0.57617682 0.80742664 0.2745280 0.845036386 0.12036259 0.186018289
    [4,] 0.78300349 0.03154611 0.7525333 0.981749326 0.98171036 0.003329883
    [5,] 0.92151400 0.54481680 0.6555585 0.684297744 0.57208251 0.374704920
    [6,] 0.02426103 0.48269100 0.5447201 0.801647214 0.73225618 0.182790284
   [7,] 0.48751974 0.20725718 0.5862766 0.731230332 0.31078984 0.270007835
    [8,] 0.47458255 0.71247625 0.2193005 0.110689448 0.96643583 0.743639232
   [9,] 0.95704982 0.53259469 0.2878961 0.894142610 0.16926626 0.651583354
## [10,] 0.58130966 0.07441521 0.7739067 0.277469387 0.09906288 0.679616107
## [11,] 0.27247687 0.91260408 0.8339184 0.267030181 0.43025874 0.836636999
## [12,] 0.14140404 0.55520098 0.5276322 0.861100549 0.10505288 0.375852058
## [13,] 0.72323325 0.02822487 0.4577087 0.544924249 0.08177472 0.689197883
## [14,] 0.86445043 0.81668628 0.8155624 0.387598166 0.55956367 0.969238055
## [15,] 0.55643007 0.12342621 0.3644800 0.231062325 0.59123819 0.815624179
## [16,] 0.26824204 0.73860036 0.1336865 0.271626313 0.34662501 0.961664900
## [17,] 0.19043913 0.84522428 0.1404868 0.316376099 0.73696628 0.938272316
## [18,] 0.74483573 0.55794817 0.3544226 0.974022008 0.84062658 0.444735781
## [19,] 0.54885578 0.36757361 0.6474187 0.941739990 0.06340573 0.463708312
## [20,] 0.65793842 0.13289883 0.8918689 0.005325485 0.43370922 0.109877445
## [21,] 0.14981974 0.17056128 0.9750785 0.866459585 0.04302924 0.401949235
## [22,] 0.78313099 0.76525246 0.1480687 0.431438042 0.79133036 0.613156848
## [23,] 0.64331024 0.86148586 0.8419956 0.470394799 0.56643381 0.195325563
## [24,] 0.21386901 0.13610607 0.6225040 0.153448379 0.71203103 0.504338674
## [25,] 0.93299062 0.47515572 0.4694915 0.536352560 0.13112496 0.642743037
```

```
[,32]
                                    [,33]
                                                 [,34]
                                                            [,35]
    [1,] 0.9516199 0.21441015 0.000650994 0.9159515155 0.89357406 0.418307451
##
    [2,] 0.3137542 0.76512301 0.344416323 0.6830185989 0.09098538 0.681078823
    [3,] 0.7532431 0.08654085 0.667466387 0.0528826369 0.08584761 0.049999142
    [4,] 0.5786835 0.22193493 0.211487222 0.7311529121 0.27067759 0.004346256
    [5,] 0.4977007 0.16800178 0.972796772 0.9305858128 0.04906291 0.848449549
##
    [6,] 0.9787163 0.79842413 0.699442412 0.5731677625 0.85749543 0.010320184
    [7,] 0.4002913 0.64605565 0.998254652 0.0903098816 0.46003577 0.261627201
    [8,] 0.1933602 0.21780751 0.006467780 0.5877454171 0.39897562 0.687559162
    [9,] 0.8294406 0.94811648 0.201937143 0.9194327882 0.78421562 0.537168685
  [10,] 0.9930752 0.20606211 0.510632197 0.7227278876 0.01568811 0.089830031
  [11,] 0.7200510 0.09044462 0.521428020 0.1945894591 0.06889243 0.091815122
  [12,] 0.5552021 0.02807093 0.698261563 0.8521334073 0.55135509 0.811797715
## [13,] 0.4460849 0.24630528 0.754551927 0.9686448707 0.76548353 0.233904565
## [14,] 0.8791966 0.94880020 0.947019577 0.6875784164 0.71842509 0.154771921
## [15,] 0.9496184 0.26150966 0.772988017 0.7568100218 0.59175775 0.841242276
## [16,] 0.7731587 0.56890443 0.950224898 0.0001352641 0.74641201 0.854456792
## [17,] 0.2240990 0.89575364 0.669055003 0.1087737761 0.96692832 0.533747477
## [18,] 0.3820063 0.96716475 0.205376261 0.5330054769 0.34674714 0.407434175
## [19,] 0.2042817 0.69115355 0.316888799 0.0238596904 0.19502703 0.422317875
## [20,] 0.1632326 0.14340754 0.259843213 0.4513600988 0.76710708 0.905097357
## [21,] 0.6279583 0.29597732 0.031769275 0.9043137820 0.03288380 0.731062069
## [22,] 0.8919962 0.89410296 0.273115210 0.7024052353 0.95928931 0.366684634
## [23,] 0.9276193 0.35409248 0.314627938 0.6427455551 0.33402801 0.443111462
   [24,] 0.5756935 0.09009547 0.274502333 0.3925404469 0.12906298 0.880401264
   [25,] 0.4968500 0.24315592 0.065947107 0.6504013503 0.99035152 0.868453018
##
              [,37]
                          [,38]
                                     [,39]
                                               [,40]
                                                          [,41]
    [1,] 0.94456209 0.357606173 0.30381990 0.3190106 0.81343641 0.25290196
    [2,] 0.26923494 0.294294079 0.47307796 0.1397403 0.57330458 0.69508540
    [3,] 0.35221977 0.391752410 0.58198443 0.4799231 0.85680220 0.45345906
    [4,] 0.51695056 0.633910292 0.54094185 0.2063539 0.37977533 0.17298793
    [5,] 0.53033226 0.529288011 0.43666576 0.1004529 0.13425752 0.10880252
    [6,] 0.62308381 0.319243054 0.68151551 0.3773391 0.31465596 0.13681436
    [7,] 0.00952775 0.787027872 0.19743712 0.8305240 0.71633688 0.62316956
    [8,] 0.03151089 0.722309563 0.02418926 0.6372843 0.04714883 0.14910642
   [9,] 0.55208796 0.836486696 0.94702925 0.1477464 0.39016005 0.94402299
## [10,] 0.71795120 0.911931055 0.85398087 0.1846938 0.81628961 0.31453155
## [11,] 0.16092177 0.002249812 0.45753939 0.2403049 0.62492932 0.15342701
## [12,] 0.81221268 0.879739488 0.11625999 0.6364739 0.16397134 0.25829341
## [13,] 0.98903296 0.692129708 0.78236240 0.3219120 0.96407202 0.08059727
## [14,] 0.86048363 0.567899579 0.96196811 0.4582701 0.38950933 0.71035187
## [15,] 0.02897580 0.082477422 0.14547020 0.6614586 0.33545601 0.18480475
## [16,] 0.70479089 0.667754014 0.51643788 0.5278304 0.45116759 0.49334658
## [17,] 0.54617169 0.999843023 0.43393624 0.9304231 0.99127839 0.47359772
## [18,] 0.96482702 0.493124211 0.28566912 0.7189614 0.23037063 0.85798235
## [19,] 0.83813145 0.138362033 0.32217127 0.3707934 0.20523008 0.31036662
## [20,] 0.13596448 0.836900318 0.48355956 0.5889265 0.16386444 0.94457944
## [21,] 0.38287509 0.689958882 0.85589249 0.5432043 0.31629181 0.30586078
## [22,] 0.37739719 0.483939623 0.73230579 0.4837839 0.82640682 0.01157267
## [23,] 0.38621286 0.371952861 0.95499755 0.4865244 0.04108188 0.60116121
## [24,] 0.01418721 0.416868865 0.23180395 0.8258671 0.32288796 0.95079146
## [25,] 0.15373332 0.179966519 0.31804636 0.4255709 0.10153656 0.29202308
##
              [,43]
                         [,44]
                                    [,45]
                                               [,46]
                                                          [,47]
                                                                     [,48]
   [1,] 0.84259881 0.77676651 0.80864264 0.14974247 0.99136840 0.6877329
```

```
[2,] 0.11282887 0.82665878 0.17495515 0.67421270 0.23317506 0.1892408
   [3,] 0.67534040 0.56396821 0.84426747 0.96350861 0.92269940 0.7173697
   [4,] 0.19390484 0.68897016 0.13653873 0.75435498 0.30713896 0.7708146
  [5,] 0.78674603 0.81639548 0.72885648 0.53037414 0.75036572 0.6967160
   [6,] 0.97826477 0.06281172 0.26524376 0.37593875 0.21299405 0.6508152
  [7,] 0.75975398 0.31052858 0.98620106 0.48192488 0.64945459 0.5967672
  [8,] 0.40866943 0.42988873 0.14545790 0.20824573 0.30522818 0.9122680
## [9,] 0.02994009 0.84626286 0.70929675 0.42232568 0.04310857 0.2802713
## [10,] 0.42448971 0.65388395 0.61507502 0.85383652 0.36367181 0.2247707
## [11,] 0.73219554 0.84137500 0.28778724 0.86110210 0.34533710 0.6387120
## [12,] 0.31132588 0.23509840 0.22264660 0.20618495 0.19560035 0.4332023
## [13,] 0.08532719 0.96326992 0.67356443 0.19701098 0.58796162 0.2421155
## [14,] 0.19410138 0.45079829 0.64305452 0.98431348 0.95616945 0.1849660
## [15,] 0.64143895 0.16224306 0.53861996 0.90852686 0.34974103 0.1987029
## [16,] 0.18616073 0.75110790 0.09449500 0.47639161 0.92553835 0.3127301
## [17,] 0.58519453 0.85281524 0.48490277 0.92940966 0.78186062 0.6238281
## [18,] 0.41447300 0.80608902 0.70018179 0.48544934 0.36532833 0.9250960
## [19,] 0.76968759 0.12220329 0.08590316 0.17501270 0.87824003 0.4532865
## [20,] 0.26411429 0.92890716 0.95192979 0.68265351 0.47362448 0.2413260
## [21,] 0.25394757 0.71199183 0.49395141 0.12673660 0.60939709 0.4258400
## [22,] 0.96352172 0.55606255 0.02282222 0.10761578 0.28592079 0.6944911
## [23,] 0.99478139 0.30131675 0.29904184 0.76791182 0.85678857 0.2644468
## [24,] 0.10955078 0.20229025 0.43074029 0.80705671 0.09455955 0.5524170
## [25.] 0.70151346 0.77247716 0.27593128 0.02297501 0.49470240 0.8805130
##
              [,49]
                        [,50]
   [1,] 0.82368279 0.4891343
   [2,] 0.11526344 0.3967687
   [3,] 0.34703619 0.3592841
  [4,] 0.94203395 0.6786118
  [5,] 0.10902410 0.1724208
##
   [6,] 0.52979553 0.2016020
   [7,] 0.86588062 0.7798039
  [8,] 0.52784045 0.0808286
  [9,] 0.97380013 0.9816547
## [10,] 0.53559211 0.5157456
## [11,] 0.28904488 0.9695043
## [12,] 0.33791675 0.9699722
## [13,] 0.43426482 0.9364704
## [14,] 0.64901260 0.2526310
## [15,] 0.08593573 0.1946434
## [16,] 0.93985540 0.5025675
## [17,] 0.59301489 0.9077823
## [18,] 0.39422985 0.9312351
## [19,] 0.27869431 0.7905641
## [20,] 0.11871959 0.1460613
## [21,] 0.94689232 0.1944843
## [22,] 0.70295368 0.9814702
## [23,] 0.91430335 0.4452738
## [24,] 0.86905086 0.9042947
## [25,] 0.11407775 0.6335137
```

Calculating mean for the above sample:

```
samp1_mean <- replicate(50, mean(runif(25, 0, 1)))
samp1_mean

## [1] 0.4242015 0.5200406 0.5017782 0.4902966 0.4670296 0.4265392 0.4972424
## [8] 0.4946778 0.4290083 0.4922050 0.5490255 0.4485942 0.5079615 0.4451926
## [15] 0.5362271 0.4315300 0.4957183 0.5023440 0.5014595 0.6067149 0.4994223
## [22] 0.5466601 0.4139500 0.5060135 0.3668918 0.5173425 0.3997405 0.4508578
## [29] 0.5770198 0.5876233 0.5483592 0.4182377 0.3710242 0.5436938 0.4641644
## [36] 0.3946543 0.4436471 0.5508089 0.4460531 0.4519154 0.4985648 0.5323046
## [43] 0.4250067 0.5620196 0.4952670 0.4649322 0.4512556 0.5805571 0.4962565
## [50] 0.5399272</pre>
```

Calculating minimum for each of the above samples:

```
samp1_min <- replicate(50, min(runif(25, 0, 1)))
samp1_min

## [1] 0.003689917 0.105844652 0.072148430 0.024065241 0.006919096 0.040734239
## [7] 0.055408920 0.014543394 0.036304511 0.011940632 0.070607972 0.073674982
## [13] 0.067236380 0.002631008 0.055728340 0.001808006 0.043558556 0.003462068
## [19] 0.037358899 0.133136444 0.168777044 0.003483265 0.044110296 0.039450905
## [25] 0.029509597 0.047041128 0.010190208 0.001805829 0.005312536 0.030717315
## [31] 0.014488494 0.022903054 0.014523079 0.038127724 0.025270938 0.003029816
## [37] 0.023421920 0.014239904 0.004028954 0.037418598 0.046825035 0.009141473
## [43] 0.040813657 0.012714515 0.023348854 0.038002664 0.003324724 0.077604079
## [49] 0.012343351 0.023700084</pre>
```

Calculating maximum for each of the above samples:

```
samp1_max <- replicate(50, max(runif(25, 0, 1)))
samp1_max

## [1] 0.9940864 0.9443692 0.8671208 0.9943593 0.9223705 0.9102514 0.9696273
## [8] 0.9991450 0.9655174 0.9117923 0.9848463 0.9993197 0.9829833 0.9431326
## [15] 0.9750815 0.8474711 0.9703309 0.9667354 0.9810141 0.9681867 0.9699511
## [22] 0.9575549 0.9668233 0.9266872 0.9774207 0.9165798 0.9658592 0.9925993
## [29] 0.9810713 0.9589875 0.9497282 0.9887019 0.9907580 0.9096894 0.9796691
## [36] 0.9894741 0.8920092 0.9732112 0.9358926 0.9943915 0.9808538 0.9848268
## [43] 0.9407670 0.9486007 0.9984547 0.9165140 0.9546213 0.9799196 0.9704686
## [50] 0.9357774</pre>
```

Calculating median for each of the above samples:

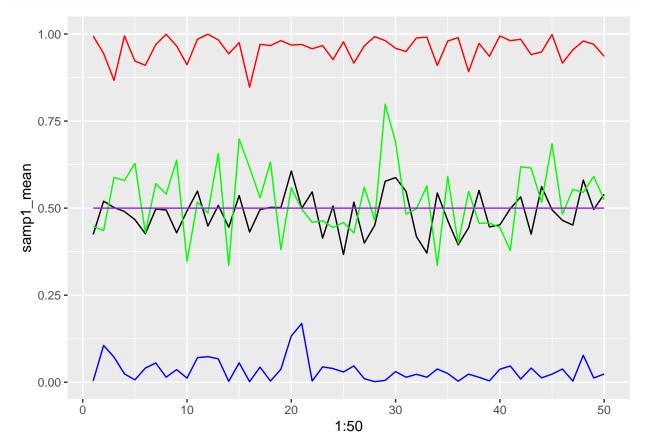
```
samp1_mid <- replicate(50, median(runif(25, 0, 1)))
samp1_mid

## [1] 0.4484540 0.4352211 0.5881784 0.5792439 0.6284931 0.4295968 0.5702661
## [8] 0.5403792 0.6374086 0.3474937 0.5174726 0.4857749 0.6564957 0.3351414
## [15] 0.6986765 0.6162572 0.5298832 0.6324712 0.3813259 0.5585472 0.4973086
## [22] 0.4592361 0.4638133 0.4441378 0.4589612 0.4288996 0.5608110 0.4651315
## [29] 0.7980895 0.6894594 0.4827991 0.4983421 0.5640077 0.3356282 0.5910946
## [36] 0.3987274 0.5478936 0.4564261 0.4574427 0.4445859 0.3781859 0.6184745</pre>
```

```
## [43] 0.6151763 0.5167851 0.6848569 0.4828917 0.5539644 0.5453286 0.5909060 ## [50] 0.5240244
```

Plotting these 4 statistics:

```
ggplot(NULL,aes(1:50))+geom_line(aes(y =samp1_mean), color = "black") +
    geom_line(aes(y =samp1_max), color = "red") +
    geom_line(aes(y = samp1_mid), color = "green") +
    geom_line(aes(y = samp1_min), color = "blue") + geom_line(aes(y = 0.5), color = "purple")
```



%-----

The Normal (0, 1) distribution:

Drawing 50 random samples:

```
samp2 <- replicate(50, rnorm(25, 0, 1))</pre>
samp2
##
                 [,1]
                             [,2]
                                          [,3]
                                                       [,4]
                                                                    [,5]
                                                                                [,6]
##
    [1,] -0.157165079 -1.05107125 -4.48321385
                                                0.367008206
                                                             0.27378755
                                                                         0.22717701
   [2,] -1.101688171 -0.42562741 -0.05270364 -0.009165949
                                                             1.02152550 -0.09413663
##
##
    [3,] -0.796675750  0.62006701  1.18202246 -0.430416421 -0.16747753  0.50769704
##
    [4,] 0.005729214
                       0.08649163 -0.49535475
                                               0.009559083 -0.25965106 -1.02770936
##
    [5,] 1.376738235
                       1.85458597 -0.56988105 0.636848558 -1.57240490 -1.82485320
##
    [6,] 1.347774499
                      2.15215047 2.54242481 0.452841768 1.05451156 -1.05592298
    [7,] -0.537242032   0.98882483 -0.46645347   0.654150543 -1.62954796 -1.43104756
##
```

```
[8,] 0.684765805 -0.11401333 -0.42314493 1.340323129 0.21935186 1.22877743
  [9,] -1.823733193 -0.40379221 0.91764748 0.643678049 -0.97800570 0.12540878
## [10,] 0.692806439 -0.55505717 0.94614267 -0.086571639 -0.38638812 0.94165077
## [11,] 0.561837377 -0.72774615 -0.35322599 1.070840308 -0.08564649
                                                             0.43402847
## [12,] -0.337906180 -0.07586157 0.84397878 0.112304365 -0.17847459 -1.54317676
## [13,] 1.004786214 -0.81827161 0.36627932 -0.235210287 -0.73232325 0.74788115
## [14,] 0.869192263 0.49660246 0.88050247 0.920772564 0.14829670 0.58646824
## [15,] -1.372505083 -0.02333126  0.51097999  0.564791988  1.15655161  0.02606438
## [17,] -1.190051907 -0.35448765 -0.09666309 -0.725721476 0.18873835 1.29588972
## [18,] 0.976318261 -0.43218582 -0.91581804 0.753963708 -0.30721715 -0.39371165
## [20,] 0.100241594 -0.71082659 0.43563352 -0.635893859 0.12690591 0.61002905
## [21,] 1.648602023 -0.37283663 -0.76684423 1.122940188 -0.52842147 0.95872691
## [23,] 0.491703335 0.08247336 0.43284267 -1.649549210 -0.94544107 -0.09984537
   \begin{bmatrix} 24, \end{bmatrix} \quad 0.228507373 \quad -1.00395144 \quad -0.14968890 \quad -0.710369327 \quad -0.41484014 \quad -1.81401793 
  [25,] 0.686162988 -0.74020953 -0.79436979 0.262624189 0.78574580 -0.26646770
##
                        [,8]
                                 [,9]
                                           [,10]
                                                                [,12]
              [,7]
                                                     [,11]
##
   [1,] -0.50091945 2.00047392 -1.0368885 0.76238548 0.88177552 0.31308940
##
   [2,] 1.89180053 1.20563890 0.9405297 -0.86570585 0.24777592 1.20548998
   [3,] -0.30507606 -0.79411707 0.5443181 1.09796231 -3.29524849 -1.39777916
   [4,] -0.48281825 1.14786560 -0.8424091 -0.08038888 0.30229541 -0.01900567
##
   [5,] 0.46807824 -0.48732190 1.9766817 -0.37878770 -0.42260567 0.26675584
   [6,] -0.29817682  0.57376256  0.7911632 -1.40287548  0.17644428  1.78324284
   [7,] -0.40414192 0.19337581 0.5030862 -0.11216004 -0.57712057 1.14767567
   [8,] 0.11179456 1.20959510 0.4863586 -0.24276021 1.89174439 -1.49928446
   [9,] 2.74436797 -0.14538024 -0.9258424 0.76421607 0.01184916 1.33129624
## [11,] 1.98039137 0.56011679 0.6399530 0.16853412 1.38896292 -0.99045551
## [12,] 0.59942363 0.32594843 1.1865812 -0.44555047 0.88815424 0.21973436
## [13,] 0.91448859 0.57768626 1.3443289 0.10237772 -0.16606704 -0.16090884
## [14,] -0.19462063 -1.06767045 0.2145542 -0.10960851 0.64500650 -0.98614445
## [16,] -0.67576743 0.75817073 1.0507171 -0.15209490 0.09088487 0.22810448
## [17,] -0.85926540 -0.50844169 1.5467545 -0.78616659 -0.25523471 0.16170447
## [18,] 0.33197562 0.40995623 -0.8236284 -1.55889369 0.44529163 0.19216928
## [19,] 0.18279626 -1.40652044 1.2742950 0.76643305 -0.40433212 1.31184711
## [21,] 0.02689055 0.33477930 0.9314568 0.01528244 -1.30672407 -0.10164148
## [23,] -0.06539965 1.54485564 0.9873141 0.43704696 0.43567971 0.88397362
  [24,] -0.15311099 -0.03081351 1.1010061 1.93019165 -0.64200259 -0.12736770
  [25,] -0.59437693 -0.90108485 1.3436009 1.10193146 1.56082437 0.86876540
             [,13]
                        [,14]
                                 [,15]
                                            [,16]
                                                      [,17]
   [1,] -1.29499203 3.401045394 -0.8366054 0.91340057 0.04259349 -0.66892604
##
##
   [2,] 0.12726555 0.211068157 0.1175786 0.73957287 -0.18918845 0.33754348
   [3,] 0.88218278 2.448753519 -1.1959169 -1.37542714 -0.72767870 -2.01235375
   [4,] 0.07088568 -0.212925631 0.1237483 -1.52852731 0.93502185 0.24950686
   [5,] 1.53607022 1.620825087 1.7830813 -0.41620448 -0.09043330 -0.38002852
##
    \hbox{ \tt [6,] -0.90554287 } \hbox{ \tt 1.068058994 -0.2377112 -1.41330722 -0.62851290 -0.19477465} 
##
   [7,] -0.75522895 -0.918623271 -1.4541535 -0.43544352 0.05112854 -1.04745978
   [8,] 0.17199158 -0.068926758 -1.4566576 -0.69593187 0.82960249 -0.25738733
   [9,] -1.33723116  0.218269702 -1.8300269  0.54084011 -0.69503379 -0.43943926
```

```
## [11,] -1.01635563 -0.237390979 -0.2510309 -1.08878410 -0.21996804 0.76231067
## [12,] 1.37279322 0.773281150 -0.6859658 0.85140335 0.67363297 0.15724058
## [14,] -1.15433824 -0.231360990 2.3376603 -0.14560675 -0.59875668 0.58966348
## [15,] 0.91118057 0.953583683 1.0991234 0.83991683 -0.37139332 -0.32143136
## [16,] 0.18613766 2.297839509 -0.2549753 -0.88655022 -0.69992097 0.50988201
## [17,] -0.98417690 0.633109945 0.2346176 0.80819016 1.27657965 -0.08604882
## [18,] 0.18451891 -0.741049976 -0.4942565 0.42029928 1.56145054 -0.03159373
## [19,] 0.20395627 -0.320962274 0.4246028 -1.41697455 0.47955237 0.69035746
## [21,] -0.04102047 -0.540082331 -1.4395131 -0.05748058 -0.02951012 -0.69539674
## [22,] 1.18489332 0.429577219 -0.1783301 0.17054938 -0.50202491 -0.52476754
## [23,] -0.27290098 -0.848775163 -0.6537093 0.91716519 0.26931890 0.50743546
## [24,] 0.87890718 1.475605879 0.7887432 0.15745554 0.89560159 0.03620666
## [25,] -0.73354165 -1.418272045 0.4795460 -1.63933914 -1.22319487 0.57727225
##
            [,19]
                      [,20]
                                 [,21]
                                           [,22]
                                                     [,23]
##
   [1,] -0.89294580 -0.80698734 -1.27031363 1.19079530 0.65280507 0.27868660
   [3,] 2.71557128 -0.26796724 -0.31670063 0.01351031 -0.48121764 0.48187435
##
    \begin{bmatrix} 4, \end{bmatrix} - 0.26521740 \quad 0.12557275 \quad -0.89577142 \quad -0.77045930 \quad -2.68021791 \quad 0.16703469 
   [5,] -0.55539049 -1.19401969 -0.93480955 -0.86886193 0.26326563 2.21045395
   [6,] 0.50725511 -0.80276100 -1.10005709 -0.11170818 0.24065102 -0.23305870
##
   [7,] 1.12040799 2.02475428 1.06550829 -1.26890246 0.59630533 -2.21352733
##
   [8,] 0.80074820 0.68550333 -0.84296931 0.09278781 -0.46256664 0.21392165
   [9,] -0.04512243 -1.32841586  0.14610929 -0.31903461 -0.28330741 -1.41482783
## [11,] -1.17768010 -1.12375069 0.12156692 -0.27660394 -0.12205934 0.09472429
## [14,] 1.31851902 -0.37286688 -1.00086120 0.85701087 0.57065687 -0.22474008
## [16,] 0.71430818 -1.47496964 0.44521810 -1.49857876 -1.04836907 1.58773201
## [17,] 0.31168959 -0.78812103 0.37895709 -0.58385367 0.94372808 0.90101003
## [18,] 0.73671082 0.32382943 0.43587251 1.42590717 -1.04199451 -0.22591140
## [19,] -1.44913772  0.70559267 -0.42637992 -0.58929273  2.22396280  0.08486415
## [20,] -2.13717832 1.12138849 -1.47177867 -1.92822720 1.25856062 -1.00446749
## [21,] 1.31269051 -2.08538157 -0.19707160 -0.49284075 -0.25979938 0.47559472
## [22,] 0.17000283 1.29043416 0.94417782 -0.82526793 0.30117242 -0.78520987
## [23,] 0.14177822 -1.08968841 1.22869269 -1.63039881 0.58176396 -0.54801594
  [24,] 0.24354081 0.06613051 1.20963319 -1.81022362 -0.51979081 -0.93333610
  [25,] 1.68579559 -0.07246143 -0.05429993 1.18673736 -0.19262280 0.42693046
##
           [,25]
                    [,26]
                                [,27]
                                          [,28]
                                                     [,29]
                                                              [,30]
   [1,] -0.2083785 -0.1781990 0.066528073 -0.81325997 -2.057694145 0.5127033
##
   [2,] 1.1193905 -0.5423456 -1.002493862 1.46751133 -0.877201805 -0.4713157
   [3,] 1.0469607 -0.9862883 0.042015380 0.16482832 0.311772528 -0.7443993
##
   [4,] -1.1201164 -0.8527057 -0.421793491 -0.84870143 -0.537405212 -0.4889800
   [5,] -0.4867866  0.9409770 -1.150199950  0.69856321 -0.430077247 -0.2845931
   [6,] -0.3663055 -0.8483458 -0.259061348 0.22953469 0.816138506 -0.5204499
   [7,] 1.1714034 -1.2078539 -1.433673433 -3.21955847 -1.047160263 0.5184304
   [8,] 1.5629233 -0.2672346 0.007730724 0.05034718 0.272863540 0.9539263
  [9,] -0.5033041 -0.8947188 -0.215982135 -0.73170665 0.003160043 0.3563087
## [10,] 1.9204751 0.6355432 -1.695620721 -0.05294474 -0.240805941 -1.1601005
## [11,] 0.8097028 -1.3099218 0.934852347 -0.29655164 1.669347672 -0.2106277
```

```
## [12,] -0.9462463 -1.2100277 0.337907565 0.67860472 0.847441549 0.6403305
## [14,] 2.6627882 0.4782981 0.754552839 -0.23360443 1.444564731 0.6258638
## [15,] -1.0099017 -1.4090139 -0.795103655 0.50420188 -1.375829683 -1.4627315
## [16,] -0.4196535 -0.6085244 -0.254161079 1.24378381 0.410811811 2.1925332
## [17,] 0.1296194 -0.2067844 -0.513200876 0.80621545 0.416607339 -0.2216212
## [18,] -2.2051943 -0.6530495 0.638384603 0.60493716 0.569814184 -1.3665115
## [19,] 0.6875386 -1.5371696 -0.158006871 1.65438757 0.851680768 -0.9417173
## [20,] 1.0936103 -0.9815714 -0.153781761 -0.28923553 0.412281897 0.6657738
## [21,] -0.7949704 -1.1356096 -0.529258313 0.06662475 0.436717615 0.5392061
## [22,] 1.2989360 0.8540797 1.947677300 -0.20533001 -0.811939571 -1.1700903
## [23,] 0.6133207 0.6997419 0.494571918 0.45902253 0.296009022 -1.2714092
  [24,] -0.8846486   0.8131396 -0.534218604 -1.66390422 -0.573679448 -1.5948186
  [25,] 0.4024096 0.1766598 -2.589492470 -0.11859761 -1.417237114 0.5227795
##
             [,31]
                         [,32]
                                    [,33]
                                               [,34]
                                                         [,35]
##
   [1,] 0.28462823 1.435955538 -1.28576769 1.04495522 -1.8162750 1.207849892
   [2,] 0.30579710 -1.063894481 -2.05940779 -0.27896844 2.1910621 0.904622911
##
   [3,] 0.67194317 -0.741716853 -0.06052267 -1.28927385 1.2939766 -1.212112937
   [4,] 0.52834306 -0.179882749 -2.29180767 -0.08313792 -1.1013977 -0.322546760
   [5,] 0.44087491 -1.083106214 0.52788664 0.10357541 0.5997957 -0.949463152
##
    \hbox{ \tt [6,] -0.38341087 } \quad \hbox{ \tt 0.583981378 -0.96884869 -1.45908676 -0.3340396 -0.719004954 } 
   [7,] 0.07407137 -1.981997565 2.17406100 0.45241601 -1.3086230 0.578367685
   [8,] 0.37665919 0.455285161 -0.03097747 1.08135941 0.3214944 0.994826715
##
   [9,] 1.30094940 0.194050016 -0.53630346 2.79477709 -0.5847118 -1.286178021
## [10,] 0.23013162 0.907278392 0.72103267 0.18054752 -1.8696083 0.358016400
## [11,] 0.03575538 1.125250753 -0.18013589 -0.25272770 -1.1579139 -0.778819696
## [12,] 1.06136188 1.532900024 -1.34599568 -0.38030586 0.6138782 0.373555137
## [13,] 0.86095443 0.373065675 1.59713215 -1.24548369 -0.5610597 1.084411311
## [14,] 0.61575158 -0.007452553 -0.74933871 0.77265430 -0.4522569 -0.917529659
## [15,] 1.65748210 -0.197061159 1.43501988 -0.43274437 -0.6597148 -0.603445185
## [16,] -1.44557036 -0.140489448 1.08654598 1.06387133 1.0390014 0.689937602
## [17,] 1.63205693 1.399397055 1.37739227 -0.99462504 -0.9834481 0.004389165
## [18,] -0.58512505 -0.192847922 -0.48980599 -0.39546012 0.9503031 1.345420045
## [19,] -0.71922535 -0.544758434 0.08400927 -0.11226980 -1.4179447 1.925116650
## [21,] 0.34551735 0.264846538 -0.16640310 0.20602707 -1.5299815 -1.365558216
## [23,] 1.47195055 1.611441628 -0.14443948 -1.53279046 0.2009428 0.100540479
## [24,] -1.33440343 -0.089180847 0.18503231 1.31319067 -0.1345385 -0.213192963
  [25,] -0.93364612 -0.183311103 0.32399336 -1.59326422 -1.5645663 -0.749991494
            [,37]
                       [,38]
                                   [,39]
                                              [,40]
                                                         [,41]
##
   [1,] 0.2195779 0.51049499 0.205422751 1.39254621 0.81622334 -0.65631872
   [2,] 0.2480374 0.44193604 0.925096645 0.16353777 -0.57103417 1.04748631
   [3,] 1.4953637 0.26347861 1.421693192 1.39031224 1.47796027 0.05319752
   [4,] -1.0427956 1.34379504 -0.577589146 -0.39098452 1.53417534 -1.74652612
   [5,] -0.5153262 -0.67550745 1.080017083 -0.25531940 -0.44127923 0.37631733
   [6,] -1.1481512  0.53308666  1.079989579  -0.38960173  -0.87122271  -1.96000951
   [7,] 0.6740339 -0.47161844 -1.764995625 0.93607833 0.81048486 -0.47941408
   [8,] -1.2128392  0.75656264  0.109248450 -0.52882551  0.71187071 -0.65877755
   [9,] -1.6052609  0.83244674 -0.362484038 -0.81343559  0.39726341 -2.12138002
## [10,] 0.3371754 -0.79296781 -0.124297905 0.36412907 -0.85641586 -0.68498503
## [11,] 0.4315097 0.89443045 -0.254579011 0.27171822 -0.49435269 1.54983426
## [13,] 1.2364650 0.17923547 0.647668211 -1.06230960 0.19691697 -0.74564406
```

```
## [14,] 1.0651155 -1.05149606 0.991606962 -0.09718064 0.96358345 0.97432206
## [15,] 0.3807213 1.78004873 -1.577717068 -2.13293855 -2.38286786 -1.21827666
## [16,] -0.2163689 -0.36941244 -0.005526195 -0.12050984 1.56576319 -0.78155167
## [18,] 0.7850767 1.58766928 0.675728105 0.67954701 0.95776486 0.14875257
## [19,] -0.3273333 1.29164985 -1.104514081 0.46993138 0.07904168 -1.05047338
## [20,] -1.9201315 -1.90985831 0.924590302 0.56342911 -0.34942111 0.75016575
## [21,] 0.1243218 -0.36180203 -0.844546234 1.06096018 0.76051007 0.92051070
## [22,] 1.3434945 -1.05536148 0.453114040 2.19822870 0.35896073 -0.40338218
## [23,] -1.9181619 -1.37954292 0.809493473 0.03559199 0.98226164 0.32291756
## [24,] 0.1057962 -0.06165629 -0.858666173 0.96232123 0.63139284 -1.12006118
[,43]
                        [,44]
                                  [,45]
                                              [,46]
                                                         [,47]
                                                                    [,48]
   [1,] 0.52356247 -0.77146750 0.24130833 -0.460865476 -1.05470330 1.34464847
##
   [2,] -1.07496750 -0.16550267 -1.70680799 -1.686397797 -0.70465675 0.79315853
   [3,] 0.86495280 -0.54056082 -0.04426055 0.951267444 0.73933299 -2.15592947
   [4,] 0.40000393 1.31158742 0.46487715 0.977164071 -1.33083922 -0.82542968
   [5,] 1.02223148 -0.48246962 -0.41475583 0.225168777 0.44604941 0.03965802
   [6,] -1.76567986 -0.45685706 0.08320470 -0.564156311 -1.19037562 -0.64899000
   [7,] 0.79513032 -0.49882773 0.14615313 -0.960489479 -0.79549349 -0.59742274
##
   [8,] 0.78817728 -0.49104937 0.22704160 0.292439128 -0.60801437 -1.12960984
  [9,] 0.66106549 -0.04625656 -0.35167908 -0.771799943 0.33354844 -0.75401744
## [10,] -0.94955941 0.20193720 -0.82346213 2.383161485 0.06065837 -0.01043044
## [11,] 0.05263522 0.51681304 0.48692598 -2.034443836 -0.32134571 -0.96943371
## [12,] 0.08676866 -0.08364944 -0.73422198 -1.111517023 0.61667645 -0.80402602
## [13,] 0.83932398 0.22708583 0.12352309 0.864711519 -0.57828854 0.35284106
## [14,] -0.88173222 -0.99274562 0.77225387 1.032021681 0.89122290 -0.69372094
## [15,] 0.92648091 0.26978051 -0.24068413 0.829850424 -0.01583543 0.07213318
## [16,] 1.32252168 -1.53642727 0.22374330 -1.581255569 0.76739075 1.24060688
## [17,] 0.11621358 -0.97195527 0.14949326 0.145065912 1.51041438 -1.42428326
## [18,] 0.47725232 0.38706293 0.02449655 -1.423858054 -0.02992355 0.22378470
## [19,] -0.55007761 -0.25936654 -0.07838071 0.787869818 -0.51753652 0.11855724
## [20,] 0.75929533 0.04226360 -0.16396029 -2.719127808 1.28750879
## [22,] -0.87940355 -0.46839461 1.30954508 1.033051326 -0.46077809
                                                              1.62040257
## [23,] 0.53192467 -1.98022712 0.62810472 -3.278798916 1.02854737 -0.48263756
## [24,] -1.22018765 -0.73843847 0.43470324 -0.100831167 1.77208848 0.70625346
## [25,] 0.34739667 0.21072159 -1.19534562 0.008836008 0.65580827 0.95207048
##
             [,49]
                         [,50]
##
   [1,] -0.28624343 0.576588559
   [2,] 2.19381984 0.221767303
   [3,] -1.22577257 -0.009135614
##
   [4,] 0.34909993 1.011930381
##
   [5,] 1.10827090 2.454683522
   [6,] -0.47761208  0.848281770
   [7,] 0.83761056 0.672980487
##
   [8,] -0.94610383 1.775315654
  [9,] 1.70822669 0.788218099
## [10,] -0.86677004 -1.739010818
## [11,] -0.20737582 1.778082721
## [12,] -1.31393527 0.328437002
## [13,] -0.95998707 0.548371587
## [14,] 0.06882298 0.262119354
## [15,] 0.21489998 -0.675561478
```

```
## [16,] 1.29908423 0.352065641

## [17,] -0.37656275 0.419643576

## [18,] 0.37345634 0.266613832

## [19,] 0.62252143 1.044461269

## [20,] -0.72918440 0.509800124

## [21,] 1.72759612 1.389826575

## [22,] 0.29561129 -0.350170390

## [23,] 0.93560363 0.163302711

## [24,] 0.67469318 0.020300760

## [25,] -1.70142942 -2.003212586
```

Calculating mean for the above sample:

```
samp2 mean <- replicate(50, mean(rnorm(25, 0, 1)))</pre>
samp2_mean
  [1] -0.215361182  0.286070885 -0.137913158 -0.078460761  0.461717133
##
  [6] -0.030122600 0.008544982 0.211976856 0.586361301 -0.298348810
## [11] -0.022755942  0.510428849  0.206004331 -0.107430113 -0.001617816
## [16]
     0.355162709 -0.046321362 -0.133155771
                              0.087762727 -0.173604281
## [21]
     ## [36] -0.212884050 -0.103540125 -0.115424716 0.087910225 -0.017087571
     0.123906927 -0.081894760 -0.297265483 0.404775262 -0.438967023
## [41]
```

Calculating minimum for each of the above samples:

```
samp2_min <- replicate(50, min(rnorm(25, 0, 1)))
samp2_min

## [1] -0.8799941 -1.9312839 -1.0877639 -1.1388401 -2.0192164 -2.8346501
## [7] -1.4832714 -2.1353210 -2.7374942 -1.4571395 -1.9133943 -1.2183526
## [13] -1.5173347 -1.6131079 -2.4188486 -1.1774608 -1.4782943 -1.8272874
## [19] -1.5909965 -2.2088316 -2.1615354 -1.1480573 -1.3366186 -1.7729477
## [25] -1.7575891 -2.0302766 -1.3592238 -1.9394025 -1.6613809 -2.1885141
## [31] -1.9748600 -2.1798477 -2.3549865 -2.4293668 -1.6013633 -1.7621738
## [37] -1.6634193 -1.2559628 -1.6401215 -2.0677227 -2.4340628 -1.2596262
## [43] -2.2802102 -2.6060920 -2.2845763 -1.3930710 -1.8398801 -1.8113108
## [49] -2.3052418 -1.0993483</pre>
```

Calculating maximum for each of the above samples:

```
samp2_max <- replicate(50, max(rnorm(25, 0, 1)))
samp2_max

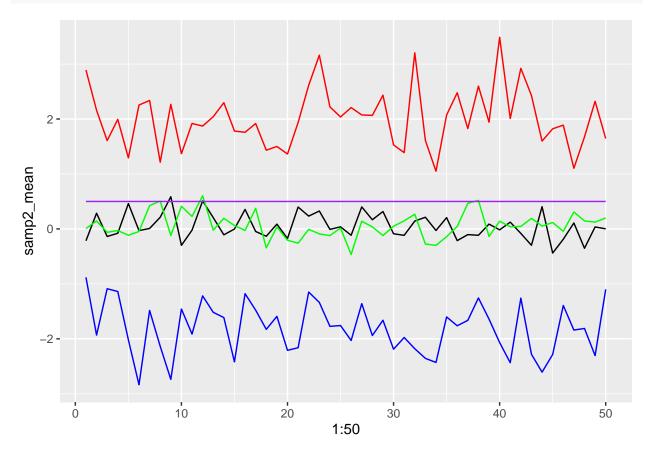
## [1] 2.892517 2.158661 1.606470 1.994791 1.292425 2.254764 2.338164 1.214242
## [9] 2.266771 1.369280 1.918971 1.871587 2.042418 2.297186 1.781088 1.758692
## [17] 1.917733 1.432253 1.501084 1.362703 1.936739 2.614130 3.162368 2.220821
## [25] 2.037150 2.208530 2.074212 2.065867 2.434250 1.528484 1.388842 3.205089
## [33] 1.608914 1.051026 2.072090 2.478604 1.826188 2.598734 1.943017 3.486931
## [41] 2.009507 2.922449 2.427460 1.598070 1.821917 1.888597 1.103632 1.674961
## [49] 2.322979 1.645287</pre>
```

Calculating median for each of the above samples:

```
samp2_mid <- replicate(50, median(rnorm(25, 0, 1)))</pre>
samp2_mid
##
       [1]
   [6] -0.046171703  0.425221608  0.506256002 -0.120126752
##
                                                       0.412475615
       0.227496514 \quad 0.603824493 \quad -0.022304803 \quad 0.193070990
                                                       0.063284553
  [16] -0.028057850  0.375012940 -0.344062054  0.035239774 -0.204843466
  [21] -0.258763724 -0.007440941 -0.090492415 -0.121156559
                                                       0.016684706
  [26] -0.464372346
                   0.049008796
                   0.267857895 -0.274300197 -0.299242222 -0.140089651
  [31]
       0.147100797
  [36]
       0.045160089
                   0.466536365 \quad 0.520014011 \quad -0.136812423
##
                                                       0.140683983
  [41]
       0.039623202
                   0.045645150 0.192343548
                                           0.052545199
                                                       0.116314653
  [46] -0.042857603
                   0.308209900 0.145810083 0.123720124
                                                       0.200051673
```

Plotting these 4 statistics:

```
ggplot(NULL,aes(1:50))+geom_line(aes(y =samp2_mean), color = "black") +
    geom_line(aes(y =samp2_max), color = "red") +
    geom_line(aes(y = samp2_mid), color = "green") +
    geom_line(aes(y = samp2_min), color = "blue") + geom_line(aes(y = 0.5), color = "purple")
```



The Cauchy (0, 1) distribution:

Drawing 50 random samples:

```
samp3 \leftarrow replicate(50, reauchy(25, 0, 1))
samp3
                                                                                  [,6]
##
                              [,2]
                                           [,3]
                                                         [,4]
                                                                      [,5]
                   [,1]
##
    [1,]
           0.278761326 -0.3847469
                                    1.75576144
                                                 0.287490176 -0.38705626
                                                                            -0.3277274
##
    [2,]
          -4.276741027 -0.1556373
                                    0.45147699
                                                 1.403018521 -3.01962209
                                                                             3.4059936
##
    [3,]
           1.041007403
                         0.2737653
                                    0.20004815
                                                 0.093152976 -1.41161064
                                                                             5.9830163
##
    [4,]
          -0.809799537
                         3.1919829
                                    0.46780191 -1.066420918
                                                              0.14597361
                                                                             0.2620174
##
    [5,]
          -0.474532070 -0.7339769 -0.38749506 -1.316490734 -4.96954818
                                                                            -0.3774137
    [6,]
##
           6.059216931
                         7.7458984 -3.29537951
                                                 1.159306557
                                                               5.23632301
                                                                            -1.3978367
##
    [7,]
           0.522545154
                         1.2339418 -5.48728871 -0.057161480 -0.97080454
                                                                             3.4374525
##
    [8,]
          -0.099017488
                         0.4705693
                                    5.40357582
                                                 0.193166036
                                                               5.32121584
                                                                             2.0004521
##
    [9,]
          -0.004720126 -0.1820592 -3.81483258
                                                 1.104764154
                                                               0.11823453
                                                                            -3.9512509
   [10,]
          -0.602123827
                         0.2413327
                                    0.60524312 -0.081266294 -0.36349666
                                                                            -1.4937217
##
                                    5.46221838 -0.126499779 -2.53411565
##
   [11,]
          -0.939452626
                         2.5218418
                                                                            -2.5120058
   [12,]
          -0.343035450
                         3.9157016
                                    1.23041804
                                                 2.189036542 -0.83563364
                                                                            -0.4051656
##
  [13,] -15.296345684 -0.2218550
                                    1.04687151
                                                 2.570020476
                                                               1.13921767
                                                                             1.3480029
   [14,]
          20.051485495
                         0.1152689 -4.58199607
                                                 1.658136370 -1.08543520
                                                                             3.2379347
##
   [15,]
           0.125471028 -2.9943105
                                    0.27812210
                                                 0.292183270 -5.37015113
                                                                            -0.4723875
   [16,]
           0.331953112 -2.6683787 -0.14737307 -0.324013830
                                                               1.66116555
                                                                             3.6842996
   [17,]
           3.602964032 -8.0054685
                                    0.08019741
                                                 0.882632516
                                                               0.30728126
                                                                            -1.0088965
##
          -1.794416442 -1.5058916 -7.90365462
##
   [18,]
                                                 1.634811531 -0.07118328
                                                                             1.1015947
##
  [19,]
           1.704346736 2.3680521
                                   9.98709822 -1.951195831 -0.10415668
                                                                             0.5482349
## [20,]
          -1.938402472 -1.9491743 -0.27496470
                                                 0.792093497
                                                               0.14246347
                                                                            -0.8848706
## [21,]
           0.097926441 -2.6456579
                                    0.04684382
                                                 0.006109949 -7.01949192
                                                                             0.8119719
## [22,]
           2.363750578
                         0.7042117
                                    2.16560563
                                                 4.794960650 -0.71166002 -24.7694095
   [23,]
                         0.5179760 -0.31989025 -0.423693670 0.27795946
##
          -0.933242865
                                                                            -1.0685263
##
   [24,]
          -7.392941435
                         0.5160146
                                    2.14130154 -0.262928741 -0.31551247
                                                                             0.3781279
##
   [25,]
           0.030938961
                        -0.7799148 -0.65885953 -0.083570756
                                                               1.31988947
                                                                             3.9086698
                                             [,9]
                                [,8]
##
                   [,7]
                                                          [,10]
                                                                       [,11]
                                       0.13612166
##
    [1,]
           -1.20795669
                         0.16279647
                                                   -1.06552886 -1.18143712
##
    [2,]
           -7.80153650 -2.40480810
                                      -0.34840094
                                                   -5.83848499 10.50589869
    [3,]
##
            0.42461275
                         0.96014649
                                      -0.45894458
                                                    0.01109498 -1.79644172
##
    [4,]
          -11.95091743
                         0.81976867
                                       0.10632429
                                                    1.89764437 -0.31315046
##
    [5,]
           -0.18827640
                         1.90545379
                                      -0.64207466
                                                   -0.08702104
                                                                 0.58751799
##
    [6,]
          -27.05177258
                         0.27005840
                                      -0.54665885
                                                   -0.42555773 -0.90721939
           -1.54611701 -1.16293192
                                      -0.35856791
##
    [7,]
                                                    0.55361665 -0.09324211
    [8,]
##
           -2.62854200 -0.45393103
                                       6.91768447
                                                    0.54567627
                                                                 2.52450560
##
    [9,]
           -0.60070484
                         1.85631136
                                      -0.23895967
                                                    2.53444459 -1.02165209
## [10,]
            0.15602528
                         4.28206727
                                       1.16940801
                                                   -0.09324582
                                                                 1.19714668
##
  [11,]
            0.84751306
                         1.18251989
                                      -4.04247807
                                                    0.27846756
                                                                 0.86950239
  [12,]
         -296.16818121 -0.88266618
                                                   -1.79949563
                                                                 3.47379740
##
                                       5.10882140
  [13,]
            0.62575386 -0.21523271
                                      -1.31497417
                                                   -7.69905192
                                                                 0.97923248
##
   [14,]
           -0.36168599
                         0.13124512
                                       0.64782586
                                                    0.26168543 -0.20389774
## [15,]
            1.09276490 -0.06132453
                                       0.06102988
                                                   -0.22195334
                                                                 1.07807744
## [16,]
          -15.91385886
                         1.27849215
                                      -0.38197653
                                                  -16.51889749
                                                                 3.19262019
## [17,]
            0.03760635
                         0.28002104
                                      -0.70596627
                                                    0.73792507 -0.79053424
## [18,]
            1.04515572
                         4.86504936
                                      -1.31450566
                                                    5.49619629 -0.54042734
  [19,]
##
           -0.77995904
                         0.52245526 -24.98297820
                                                    0.24609001 12.13206960
  [20,]
           -0.19683914 -3.74255683
                                      12.34852050
                                                    0.84611168 -0.58211678
  [21,]
            0.23811821 10.65703097
                                      -0.35229293
                                                    1.67808216 0.75734287
##
```

```
## [22,]
           -1.18485743 -0.36782719
                                     -1.39062518
                                                  -0.43840197 1.79755143
  [23,]
##
           -0.62636114 -0.63847724
                                      0.02290524
                                                  -0.74476021
                                                               0.02759001
  [24,]
                                                    1.42823836 -0.52721591
           -0.91309030 -0.97690005
                                     -0.21205869
   [25,]
           -0.27419058 0.35616442
                                      4.50787627
                                                    0.29190940 1.08308411
##
##
                 [,12]
                             [,13]
                                         [,14]
                                                       [,15]
                                                                     [,16]
##
          -0.05615688
                       -1.9897186 21.36381805
                                                  0.41573995
                                                              -0.08340240
    [1,]
##
    [2,]
          -0.79591791
                       -0.6840475 -1.00940974
                                                 -1.92743158
                                                              -3.24376529
                                                              -2.48570265
##
    [3,]
           0.35410312
                         0.2176623 0.06684169
                                                  0.05126856
##
    [4,]
          -1.28817526 -46.6817620 0.31889187
                                                  1.97508207
                                                               0.06659890
##
    [5,]
           0.28212524
                         1.0342245 -3.75070932
                                                -0.91033997
                                                               4.84515781
    [6,]
          -0.49492615
                         0.1564969 -0.49812963
                                                 14.86997064
                                                               0.38275385
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##
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    [9,]
##
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## [10,]
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##
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                                                 -0.73189837
  [14,]
##
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                                                              -0.19632156
## [15,]
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## [16,]
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                                                              -1.10893297
## [17,]
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## [18,]
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## [19.]
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## [20,]
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                                                               3.41022359
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##
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                                                               1.16533401
##
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                                                               2.05818783
##
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                                                              -1.05867152
##
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                                                               1.16277516
##
                 [,17]
                              [,18]
                                            [,19]
                                                          [,20]
                                                                         [,21]
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##
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##
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## [20,] 0.012327282 -13.43994828
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## [21,] 0.173880282
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## [22,] -0.496188500
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                                                                  -7.05219895
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## [24,] -0.346224054
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                                                 1.135598238
                                                               -3.18246741
##
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                           [,23]
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                                                                [,26]
##
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##
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##
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##
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                            [,28]
                                        [,29]
                                                    [,30]
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##
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##
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##
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##
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##
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##
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##
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## [14.]
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## [17,]
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## [21,]
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## [22,]
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## [24,]
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```

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##
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##
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##
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##
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##
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```

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##
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                                               2.72306663 -3.50972342
    [7,]
                                   1.0878948
##
           1.06410073 -1.3800848
                                               0.23935010 2.16800914
    [8.]
                                  -0.3071689
         -0.05630305 0.5821719
                                              -2.05606982 -0.94286574
   [9,]
##
           0.74739494 -3.9096814
                                  -0.6570428
                                               6.92869698 -0.09464746
## [10.]
         -0.79553577 0.8719903
                                  -0.4776656
                                              -0.47957535 -0.71486335
## [11,]
         -1.18904018 -0.2378484
                                 -1.1216568
                                               1.09582342 2.46333144
## [12,] -21.63753853
                      0.3842553
                                  0.3819082
                                               3.94907998 0.21202540
                                 -0.7556294
## [13,] -12.99713379
                      0.4153756
                                              -0.23613903 -8.71656303
## [14,]
           1.11165489
                      1.4985960
                                  0.1153394
                                              -0.16402725 -0.50441451
## [15,]
           5.34038772 0.3405517
                                 -0.5538997
                                               8.68575316 -0.28440396
## [16,]
                                 -2.7647630
                                               1.27306916 7.13848861
           0.38043863 0.4613996
## [17,]
           3.64404445 -0.5188132
                                   0.5059657
                                              -2.10332511 -1.19030604
## [18,]
         -0.83018979 -1.0247575 -10.4431722
                                               2.52568902 0.04975206
## [19,]
         -0.37536622 3.5100832
                                 -1.0058101
                                              -0.29151599 -1.49809577
## [20,]
         -1.76610986
                      0.6351492
                                  0.1300558
                                              -0.60260083 -7.27211111
## [21,]
          0.29625309 0.9568594
                                   0.1639851
                                               4.90580473 0.43415645
## [22,]
           1.11329562 13.9226252
                                   3.2003010
                                              -0.02096475 0.26926946
## [23,]
           0.78931159 0.5213105
                                   1.1396507
                                               0.02090706 1.84163992
## [24,]
          -0.54458484 -0.4312384 15.9918871
                                             11.84627496 -0.88417335
  [25.]
          -0.07362209 -0.4755580 -0.2973035
##
                                             -0.05264331 -1.13896972
##
                 [,48]
                             [,49]
                                         [,50]
    [1,]
           6.967136485 -1.5703199 0.26451102
    [2,]
          -0.002637138 132.0469016 1.43552368
##
##
    [3,]
         -2.410661616
                         0.5869404 -3.15597602
##
   [4,]
                         0.3224476 2.70904958
          2.324330159
   [5,]
         -1.466381386
                        -6.0767862 0.48579315
##
    [6,]
          -0.085043162
                         0.4141890 -3.06083018
##
    [7,]
         -0.229645779
                         0.6480610 -2.90649706
   [8,]
##
         -2.457168734
                         1.2016668
                                   1.10298931
   [9,]
                         0.2752185
##
           0.945771605
                                   0.08010101
## [10,]
          7.334595812
                         7.3020329
                                    3.40797060
## [11,]
          1.532952769
                         1.1145167
                                   0.42101816
## [12,]
         -0.879990383
                        -0.2838799
                                   0.53531811
## [13,]
          -0.592237140
                         4.6226423 -0.45890778
## [14,]
           2.940847220
                         0.6489980 0.13098320
## [15,]
                        -1.1202903 -0.36766142
         -0.095474114
## [16,] -18.186112044
                        15.2337040
                                   0.14637586
## [17,]
                         1.1098213
         -0.510726769
                                   1.38293079
## [18.]
           0.878522601
                         1.0029844 0.10969917
## [19,]
         -1.102226977 -20.1549967 -0.15726647
## [20,]
           0.671338544
                       -0.5279281 1.32290734
## [21,]
                        -1.3163921 -3.21158253
           4.493129174
## [22,]
         -6.790805424
                        -0.6964072 0.18499751
## [23,]
           0.738427989
                        -0.2578525 -0.11079481
## [24,]
         -1.901202626
                         0.1459617 -0.07707384
## [25,]
         -0.804429413
                         0.8135950 -0.01748014
```

Calculating mean for the above sample:

```
samp3 mean <- replicate(50, mean(rcauchy(25, 0, 1)))</pre>
samp3 mean
         10.60540111
                        0.17580826
                                    45.08518278
                                                   0.30970705
                                                                0.11871822
##
    [1]
##
    [6]
          0.31109963
                       0.81890460 -12.98426015 -13.73533581
                                                               -1.59564998
## [11]
          0.04048490
                       0.74043617
                                   -0.02504744
                                                 -0.43948835
                                                               -1.63800729
## [16]
         -0.14480717
                        3.93396266
                                   -0.75220236
                                                   0.58832701
                                                                1.66100518
## [21]
         -0.35303556
                        2.70703831
                                    -1.28620514
                                                 -1.79988243
                                                                0.21496578
## [26]
          0.30781538
                      -2.28844608
                                     2.31675213
                                                 -1.62631271
                                                                0.57537983
## [31]
          1.34317360
                        2.82182540
                                    -0.88997205
                                                 -2.26039442
                                                                0.13875088
## [36]
         26.61599258
                       5.45532443
                                    -0.05782822
                                                   0.15416727
                                                                0.51599983
## [41]
          0.71134724 -11.52216813
                                     1.38221668
                                                   1.01610078
                                                               -1.89567282
## [46]
          1.25935158
                      -1.91795764
                                   -0.24734063 13.31732796
                                                                0.42127376
```

Calculating minimum for each of the above samples:

```
samp3_min <- replicate(50, min(rcauchy(25, 0, 1)))</pre>
samp3_min
         -10.892500
##
    [1]
                      -9.874914
                                  -22.760627
                                                -7.567045
                                                           -58.599954
                                                                        -3.984514
                                   -7.646513
##
    [7]
         -14.060826
                     -28.381999
                                              -20.594932
                                                           -42.169496
                                                                       -21.185816
## [13]
         -24.178804
                     -38.951214
                                   -7.735813
                                              -14.665276 -297.075108
                                                                       -29.528985
## [19]
         -23.579924
                      -5.920546
                                  -12.902788
                                                -4.632523 -17.380445
                                                                       -21.845295
## [25]
         -12.338575
                       -6.846647
                                  -25.183095
                                                -5.964571
                                                           -13.403662
                                                                        -6.300439
## [31]
          -5.294006
                       -5.237055 -159.125313
                                              -62.770444
                                                            -4.181435
                                                                        -4.855082
## [37]
         -11.754150 -180.377968
                                  -11.420862
                                                -7.421176
                                                            -9.637843
                                                                        -6.416297
## [43]
         -17.114307
                       -3.462034
                                  -19.348138
                                                -6.618833
                                                            -3.139000
                                                                        -4.261080
## [49]
          -8.457381
                     -31.071273
```

Calculating maximum for each of the above samples:

```
samp3_max <- replicate(50, max(rcauchy(25, 0, 1)))</pre>
samp3_max
         10.410015 191.786222 10.289752
##
    [1]
                                           15.355463
                                                       35.431619
                                                                   6.151836
##
   [7]
          9.835686
                     5.046289
                                 2.740874
                                            7.509404
                                                        6.091772 518.744907
## [13]
          8.788717
                     3.438673 35.262464 137.270370
                                                       18.007531
                                                                   5.172403
## [19] 117.154595 17.787057
                                 3.580094
                                           15.893513
                                                        7.126428
                                                                   8.874548
## [25]
          1.644631
                     2.861025
                                16.264516
                                           42.255806 174.259291
                                                                  11.323687
## [31]
         11.085073
                    17.228088
                                22.898692
                                           18.208739
                                                       19.917855
                                                                   4.005289
## [37]
         25.658333
                     7.424817
                                11.137992
                                           15.390476
                                                        4.276890
                                                                   9.299606
## [43]
                                12.097685
                                           11.070314 17.459538 189.267719
         12.381957
                    26.334448
## [49]
         58.689126
                     4.918791
```

Calculating median for each of the above samples:

0.127764825

[11]

```
samp3_mid <- replicate(50, median(rcauchy(25, 0, 1)))
samp3_mid

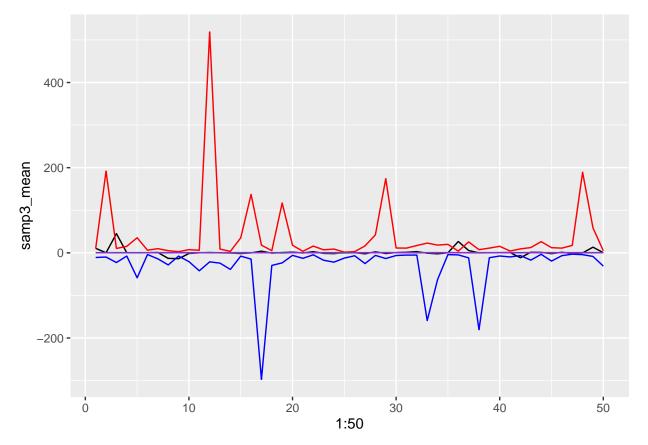
## [1] -0.132687642  0.260170128 -0.257878289 -0.075394656 -0.235539447</pre>
```

0.036887459 -0.243005163 0.189176401 -0.280433247

 $0.263661813 \ -0.226708396 \ -0.024084979 \ -0.224875980 \ -0.306193953$

Plotting these 4 statistics:

```
ggplot(NULL,aes(1:50))+geom_line(aes(y =samp3_mean), color = "black") +
    geom_line(aes(y =samp3_max), color = "red") +
    geom_line(aes(y = samp3_mid), color = "green") +
    geom_line(aes(y = samp3_min), color = "blue") + geom_line(aes(y = 0.5), color = "purple")
```



```
#A = matrix(replicate(50, rnorm(25, 0, 1)))

#A1 = apply(A, 2, mean)

#A2 = apply(A, 2, median)

#A3 = apply(A, 2, min)

#A4 = apply(A, 2, max)

#matplot(1:50, cbind(A1, A2, A3, A4), type = "l", col = 1:4, x = "sample number", y = "Statistics")

#alt+ctrl+i for a R block
```