

## Chapter 10 - exercise 2

- Assume we assign a group of vertices to a processor and send the edge/weight information for those vertices.

find a vertex  $u$  such that

$$d[u] = \min\{d[v] | v \text{ in } V-VT\}$$

- Assume each processor knows if its vertex is in  $V-VT$

- Using the code from Chp 10 Exercise 1, write code so each process now computes the min.

- You will need to add a weight to each edge.

- You will need a way to flag if an edge is in  $V-VT$

- You will need to assign the initial  $d[v]$  values.

- You will need a way to combine the results to determine the final  $u$ .

### Graded Rubric

\_\_\_\_ (1 Points) Able to flag  $V-VT$

\_\_\_\_ (1 Points) Able to set initial  $d[v]$  values

\_\_\_\_ (2 Points) Able to send all data to each processor

\_\_\_\_ (1 Points) Added a weight to each edge

\_\_\_\_ (1 Points) Able to compute local  $d[u]$

\_\_\_\_ (2 Points) Able to combine local  $d[u]$  to determine actual value for  $u$

\_\_\_\_ (1 Points) Test function that ensures code is working

Answer:

```
/*  
so from the exercise 1  
I need to add weight to each edge  
a way to flag vertex if edge is in V-VT  
able to assign initial value to d[u]  
a way to combine the the results something like send and  
recieve as well not bcasting
```

```
just an idea implement serial version for 24 to know if its  
correct or not initially  
then you can pump it up to larger scale
```

```
hint hint should be node 4
```

```
*/  
#include  
<mpi.h>  
// Include MPI library
```

```

#include
<iostream>
// Include iostream for input/output
#include
<vector>
// Include vector for dynamic arrays
#include
<limits>
// Include limits for numeric limits

using namespace
std;
// Use the standard namespace

class Vertex
{
// Define Vertex class
public:
    int
value;
// Value of the vertex
    vector<pair<int, int> >
edges;
// Edges now store a pair of (neighbor, weight)
    bool
in_VT;
// Flag indicating if vertex is in V-VT

    Vertex(int val) : value(val), in_VT(false)
}
//
Constructor initializing value and in_VT
};

class Graph
{
// Define Graph class
public:
    vector<Vertex>
vertices;
// Vector of vertices

    Graph(int n)
{
// Constructor initializing n vertices

```

```

        for (int i = 0; i < n; ++i)
    {
// Loop to create vertices

vertices.emplace_back(i);
// Add vertex to the vector
    }

    void add_edge(int u, int v, int weight)
    {
//
Function to add an edge
        vertices[u].edges.emplace_back(v,
weight);
//
Add edge to vertex u
    }

    const Vertex& get_vertex(int i) const
    {
//
Function to get a vertex
        return
vertices[i];
// Return vertex at index i
    }

    void print_graph() const
    {
// Function to print the graph
        cout << "Adjacency List with Weights:
\n";
// Print
header
        for (const auto& vertex : vertices)
        {
// Loop
through vertices
            cout << "Vertex " << vertex.value << " (in V-VT: "
<< vertex.in_VT << "): ";
// Print vertex info
            for (const auto& edge : vertex.edges)
            {
// Loop
through edges
                cout << "(" << edge.first << ", " <<
edge.second << ") ";
// Print edge
info
            }
            cout <<

```

```

endl;
// New line
    }
}
};

int main()
{
// Main function
    MPI_Init(NULL,
NULL);
// Initialize MPI

    int world_rank,
world_size;
// Variables for rank and size
    MPI_Comm_rank(MPI_COMM_WORLD,
&world_rank);
// Get rank of the process
    MPI_Comm_size(MPI_COMM_WORLD,
&world_size);
// Get number of processes

    const int n =
8;
// Number of vertices
    Graph
g(n);
// Create graph with n vertices

    if (world_rank == 0)
{
// If master process

// Initialize graph with edges and weights
    g.add_edge(0, 1,
3);
// Add edge from 0 to 1 with weight 3
    g.add_edge(0, 2,
1);
// Add edge from 0 to 2 with weight 1
    g.add_edge(1, 4,
7);
// Add edge from 1 to 4 with weight 7

```

```

        g.add_edge(1, 5,
2);
// Add edge from 1 to 5 with weight 2
        g.add_edge(2, 6,
4);
// Add edge from 2 to 6 with weight 4
        g.add_edge(2, 7,
6);
// Add edge from 2 to 7 with weight 6

// Initialize in_VT and d[v] values
    for (int i = 0; i < n; ++i)
    {
// Loop through vertices
        g.vertices[i].in_VT = (i % 2 ==
0);
// Example: Even vertices are in V-VT
    }

// Send edge data to other processes
    for (int i = 1; i < world_size; ++i)
    {
// Loop
// through processes
        int num_edges =
g.get_vertex(i).edges.size();
// Get number of edges
        MPI_Send(&num_edges, 1, MPI_INT, i, 0,
MPI_COMM_WORLD);
// Send number
of edges
        for (const auto& edge : g.get_vertex(i).edges)
        {
// Loop through edges
            int data[2] = {edge.first,
edge.second};
// Create data array
            MPI_Send(data, 2, MPI_INT, i, 0,
MPI_COMM_WORLD);
// Send edge
data
        }
        MPI_Send(&g.vertices[i].in_VT, 1, MPI_C_BOOL, i, 0,
MPI_COMM_WORLD);
// Send in_VT flag
    }
} else

```

```

{
// If worker process
    int
num_edges;
// Variable for number of edges
    MPI_Recv(&num_edges, 1, MPI_INT, 0, 0, MPI_COMM_WORLD,
MPI_STATUS_IGNORE); // Receive number of edges

g.vertices[world_rank].edges.resize(num_edges);
// Resize edges vector
    for (int i = 0; i < num_edges; ++i)
{ // Loop
through edges
    int
data[2];
// Data array
    MPI_Recv(data, 2, MPI_INT, 0, 0, MPI_COMM_WORLD,
MPI_STATUS_IGNORE); // Receive edge data
    g.vertices[world_rank].edges[i] =
make_pair(data[0], data[1]); // Assign
edge data
}
    MPI_Recv(&g.vertices[world_rank].in_VT, 1, MPI_C_BOOL,
0, 0, MPI_COMM_WORLD, MPI_STATUS_IGNORE); // Receive in_VT flag
}

// Compute local minimum d[u]
    int local_min =
numeric_limits<int>::max();
// Initialize local minimum
    int local_u =
-1;
// Initialize local vertex

    if (g.vertices[world_rank].in_VT)
{ /
/ If vertex is in V-VT
    for (const auto& edge : g.get_vertex(world_rank).edges)
{ // Loop through edges
    if (edge.second < local_min)
{ //
If edge weight is less than local minimum
    local_min =

```

```

edge.second;
// Update local minimum
        local_u =
g.vertices[world_rank].value;
// Update local vertex
        }
    }

// Reduce to find the global minimum d[u]
    int
global_min;
// Variable for global minimum
    MPI_Allreduce(&local_min, &global_min, 1, MPI_INT, MPI_MIN,
MPI_COMM_WORLD); // Reduce to find global
minimum

    if (world_rank == 0)
{
// If master process
        cout << "Global minimum d[u]: " << global_min <<
endl; // Print global
minimum
    }

MPI_Finalize();
// Finalize MPI
    return
0;
// Return success
}

```

Goal	Implementation
<b>1. Add weights to edges</b>	Weights are added using add_edge(u, v, weight). Each edge has a specific cost or distance.
<b>2. Flag edges in V-VT</b>	in_VT boolean flag determines if a vertex is in the V-VT subset.

<b>3. Assign initial <math>d[v]</math> values</b>	Each vertex's $d[v]$ is initialized to <code>numeric_limits&lt;int&gt;::max()</code> .
<b>4. Combine results for final <math>u</math></b>	Use <code>MPI_Allreduce</code> to find the global minimum $d[u]$ .