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AI1103-Assignment-4

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Download all python codes from

https://github.com/Sravanth-k27/AI1103/tree/main/ Assignment-4/codes

Download latex-tikz codes from

https://github.com/Sravanth-k27/AI1103/tree/main/Assignment-4/Assignment-4.tex

QUESTION GATE 2021 (EC) Q.27 (EC ENGG SECTION):

A box contains following three coins.

- I. A coin with head on one face and tail on other face.
- II. A coin with heads on both the faces.
- III. A coin with tails on both the faces.

A coin is picked randomly from the box and tossed .Out of the two remaining coins in the box ,one coin is then picked randomly and tossed.If the first toss results in a head,Then the probability of getting head in second toss is :

(A)
$$\frac{2}{5}$$

(C)
$$\frac{1}{2}$$

(B)
$$\frac{1}{3}$$

(D)
$$\frac{2}{3}$$

Solution Gate 2021 (EC) Q.27 (EC engg section): Let $X \in \{1,2\}$ be a random variable.

Let $Y \in \{1, 2, 3\}$ be a random variable.

Let $Z \in \{0, 1\}$ be a random variable.

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Event	Definition
X = 1	Represents trail 1
X = 2	Represents trail 2
<i>Y</i> = 1	selecting coin 1 for a trail
Y=2	selecting coin 2 for a trail
Y=3	selecting coin 3 for a trail
Z = 0	getting tail on a trail
Z = 1	getting head on a trail
X = 1, Z = 1 Y = 1	getting head on first trail by tossing coin 1
X = 1, Z = 1 Y = 2	getting head on first trail by tossing coin2
X = 1, Z = 1 Y = 3	getting head on first trail by tossing coin3
X = 1, Z = 1	getting head on first trail
X = 1, X = 2, Z = 1	getting head on both first and second trails

TABLE 4: TABLE-1.

Now we need to find Pr(X = 2, Z = 1 | X = 1, Z = 1) = a (let)

From conditional probability we have

$$a = \frac{\Pr(X = 1, X = 2, Z = 1)}{\Pr(X = 1, Z = 1)}$$
(0.0.1)

$$\Pr(X = 1, Z = 1) = \sum_{i=1}^{3} \Pr(X = 1, Z = 1 | Y = i) \times \Pr(Y = i) \quad (0.0.2)$$

Probability	Value
$\Pr\left(Y=1\right)$	$\frac{1}{3}$
$\Pr\left(Y=2\right)$	$\frac{1}{3}$
$\Pr\left(Y=3\right)$	$\frac{1}{3}$
Pr(X = 1, Z = 1 Y = 1)	$\frac{1}{2}$
Pr(X = 1, Z = 1 Y = 2)	1
Pr(X = 1, Z = 1 Y = 3)	0
$\Pr\left(X=1,Z=1\right)$	$= \frac{1}{3} \times \frac{1}{2} + \frac{1}{3} \times 1 + \frac{1}{3} \times 0$
	$=\frac{1}{2}$
Pr(X = 1, X = 2, Z = 1)	$= \frac{1}{3} \times \frac{1}{2} \times \frac{1}{2} + \frac{1}{3} \times \frac{1}{2} \times \frac{1}{2} + \frac{1}{3} \times 0$
	$=\frac{1}{6}$

TABLE 4: Table-2.

from 4

$$\Pr(X = 2, Z = 1 | X = 2, Z = 1) = \frac{\frac{1}{6}}{\frac{1}{2}}$$
 (0.0.3)

$$Pr(X = 2, Z = 1 | X = 2, Z = 1) = \frac{1}{3}$$
 (0.0.4)

Hence the required probability is $\frac{1}{3}$

: Option B is correct