

SRECHARAN SSELVAM

Project: Part 1

24-677 Special Topics: Modern Control - Theory and Design Prof. D. Zhao

Due: Oct 31, 2023, 11:59 pm. Submit within the deadline.

- Your online version and its timestamp will be used for assessment.
- We will use Gradescope to grade. The link is on the panel of CANVAS. If you are confused about the tool, post your questions on Campuswire.
- Submit your_controller.py to Gradescope under P1-code and your solutions in .pdf format to P1-writeup. Insert the performance plot image in the .pdf. We will test your_controller.py and manually check all answers.
- We will make extensive use of Webots, an open-source robotics simulation software, for this project. Webots is available here for Windows, Mac, and Linux.
- For Python usage with Webots, please see the Webots page on Python. Note that you may have to reinstall libraries like numpy, matplotlib, scipy, etc. for the environment you use Webots in.
- Please familiarize yourself with Webots documentation, specifically their User Guide and their Webots for Automobiles section, if you encounter difficulties in setup or use. It will help to have a good understanding of the underlying tools that will be used in this assignment. To that end, completing at least Tutorial 1 in the user guide is highly recommended.
- If you have issues with Webots that are beyond the scope of the documentation (e.g. the software runs too slow, crashes, or has other odd behavior), please let the TAs know via Campuswire. We will do our best to help.
- We advise you to start with the assignment early. All the submissions are to be done before the respective deadlines of each assignment. For information about the late days and scale of your Final Grade, refer to the Syllabus in Canvas.

1 Introduction

This project will entail using Webots, an open-source robotics simulation software, to learn more about control methods for autonomous vehicles. Webots was chosen because of its ease of use, flexibility, and impressive rendering capability. A brief guide for Windows, Mac OS, and Linux follows. Please see the links on the previous page for a link to documentation and more information.

For Windows:

- 1. Download and install Webots R2021b.
- 2. Download and install Python natively from Python's official webpage. 3.9 is recommended, but any version from 3.7 3.9 will work.
- 3. Open a Command Prompt window (right-click and select "Run as Administrator"). On the command line, install numpy, scipy, and matplotlib with the following command: python -m pip install package-name>.
- 4. If you encounter issues installing matplotlib, please try upgrading pip and setuptools:: python -m pip install --upgrade pip python -m pip install --upgrade setuptools

For Mac:

- 1. Download and install Webots R2021b.
- 2. Download and install Python natively from Python's official webpage. 3.8 is recommended, but 3.7 will also work.
- 3. In a Terminal window, install numpy, scipy, and matplotlib with the following command:

```
pip3.x install <package-name>
where x is the version number you installed.
```

4. Check where your Python is installed with:

```
which python3.x
```

Copy the path that appears and open Webots. In the Webots menu at the top, open $Tools \rightarrow Preferences$, and paste the copied path under "Python command".

For Linux:

- 1. Download and install Webots R2021b.
- 2. In a terminal window, make sure you have numpy, scipy, and matplotlib with the following command:

```
pip install <package-name>.
```

Buggy is a time-honored CMU tradition (you can learn more about it here and here). You will be asked to create a controller that helps a vehicle to complete the same course in simulation. However, instead of controlling an actual Buggy, you'll be controlling a Tesla Model 3. It's a bit more fun and stylish (we hope)!

We will follow the steps listed below to learn more about the system and synthesize several different kinds of controllers:

- 1. Examine the provided nonlinear control model
- 2. Linearize the state space system equations [P1]
- 3. Develop a PID controller for the system [P1]
- 4. Check the controllability and stabilizability of the system [P2]
- 5. Design a full-state feedback controller using pole placement [P2]
- 6. Design an optimal controller [P3]
- 7. Implement A* algorithm [P3]
- 8. Implement an extended Kalman filter (EKF) for simultaneous localization and mapping (SLAM) [P4]

The project has been divided into 4 parts to reflect this:

- P1 (a) Linearize the state space model
 - (b) Design a PID lateral and PID longitudinal controller
- P2 (a) Check the controllability and stabilizability of the linearized system
 - (b) Design a lateral full-state feedback controller
- P3 (a) Design an lateral optimal controller
 - (b) Implement A* path planning algorithm
- P4 (a) Implement EKF SLAM to control the vehicle without default sensor input
 - (b) Race with other Buggy competitors in the class

2 Model

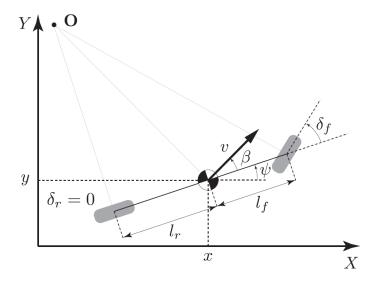


Figure 1: Bicycle model [2]

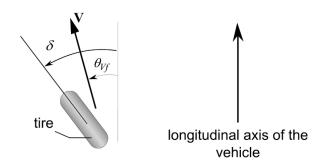


Figure 2: Tire slip-angle [2]

We will make use of a bicycle model for the vehicle, which is a popular model in the study of vehicle dynamics. Shown in Figure 1, the car is modeled as a two-wheel vehicle with two degrees of freedom, described separately in longitudinal and lateral dynamics. The model parameters are defined in Table 2.

2.1 Lateral dynamics

Ignoring road bank angle and applying Newton's second law of motion along the y-axis:

$$ma_y = F_{yf}\cos\delta_f + F_{yr}$$

where $a_y = \left(\frac{d^2y}{dt^2}\right)_{inertial}$ is the inertial acceleration of the vehicle at the center of geometry in the direction of the y axis, F_{yf} and F_{yr} are the lateral tire forces of the front and rear

wheels, respectively, and δ_f is the front wheel angle, which will be denoted as δ later. Two terms contribute to a_y : the acceleration \ddot{y} , which is due to motion along the y-axis, and the centripetal acceleration. Hence:

 $a_y = \ddot{y} + \dot{\psi}\dot{x}$

Combining the two equations, the equation for the lateral translational motion of the vehicle is obtained as:

 $\ddot{y} = -\dot{\psi}\dot{x} + \frac{1}{m}(F_{yf}\cos\delta + F_{yr})$

Moment balance about the axis yields the equation for the yaw dynamics as

$$\ddot{\psi}I_z = l_f F_{yf} - l_r F_{yr}$$

The next step is to model the lateral tire forces F_{yf} and F_{yr} . Experimental results show that the lateral tire force of a tire is proportional to the "slip-angle" for small slip-angles when vehicle's speed is large enough - i.e. when $\dot{x} \geq 0.5$ m/s. The slip angle of a tire is defined as the angle between the orientation of the tire and the orientation of the velocity vector of the vehicle. The slip angle of the front and rear wheel is

$$\alpha_f = \delta - \theta_{Vf}$$
$$\alpha_r = -\theta_{Vr}$$

where θ_{Vp} is the angle between the velocity vector and the longitudinal axis of the vehicle, for $p \in \{f, r\}$. A linear approximation of the tire forces are given by

$$F_{yf} = 2C_{\alpha} \left(\delta - \frac{\dot{y} + l_f \dot{\psi}}{\dot{x}} \right)$$
$$F_{yr} = 2C_{\alpha} \left(-\frac{\dot{y} - l_r \dot{\psi}}{\dot{x}} \right)$$

where C_{α} is called the cornering stiffness of the tires. If $\dot{x} < 0.5$ m/s, we just set F_{yf} and F_{yr} both to zeros.

2.2 Longitudinal dynamics

Similarly, a force balance along the vehicle longitudinal axis yields:

$$\ddot{x} = \dot{\psi}\dot{y} + a_x$$

$$ma_x = F - F_f$$

$$F_f = fmg$$

where F is the total tire force along the x-axis, and F_f is the force due to rolling resistance at the tires, and f is the friction coefficient.

2.3 Global coordinates

In the global frame we have:

$$\dot{X} = \dot{x}\cos\psi - \dot{y}\sin\psi$$
$$\dot{Y} = \dot{x}\sin\psi + \dot{y}\cos\psi$$

2.4 System equation

Gathering all of the equations, if $\dot{x} \ge 0.5$ m/s, we have:

$$\ddot{y} = -\dot{\psi}\dot{x} + \frac{2C_{\alpha}}{m}(\cos\delta\left(\delta - \frac{\dot{y} + l_f\dot{\psi}}{\dot{x}}\right) - \frac{\dot{y} - l_r\dot{\psi}}{\dot{x}})$$

$$\ddot{x} = \dot{\psi}\dot{y} + \frac{1}{m}(F - fmg)$$

$$\ddot{\psi} = \frac{2l_fC_{\alpha}}{I_z}\left(\delta - \frac{\dot{y} + l_f\dot{\psi}}{\dot{x}}\right) - \frac{2l_rC_{\alpha}}{I_z}\left(-\frac{\dot{y} - l_r\dot{\psi}}{\dot{x}}\right)$$

$$\dot{X} = \dot{x}\cos\psi - \dot{y}\sin\psi$$

$$\dot{Y} = \dot{x}\sin\psi + \dot{y}\cos\psi$$

otherwise, since the lateral tire forces are zeros, we only consider the longitudinal model.

2.5 Measurements

The observable states are:

$$y = \begin{bmatrix} \dot{x} \\ \dot{y} \\ \dot{\psi} \\ X \\ Y \\ \psi \end{bmatrix}$$

2.6 Physical constraints

The system satisfies the constraints that:

$$\begin{split} |\delta| &\leqslant \tfrac{\pi}{6} \ rad \\ F &\geqslant 0 \ \text{and} \ F \leqslant 15736 \ N \\ \dot{x} &\geqslant 10^{-5} \ m/s \end{split}$$

Table 1: Model parameters.

Name	Description	Unit	Value
(\dot{x},\dot{y})	Vehicle's velocity along the direction of	m/s	State
	vehicle frame		
(X,Y)	Vehicle's coordinates in the world	m	State
	frame		
$\dot{\psi},\dot{\psi}$	Body yaw angle, angular speed	rad,	State
		rad/s	
δ or δ_f	Front wheel angle	rad	Input
\overline{F}	Total input force	N	Input
\overline{m}	Vehicle mass	kg	1888.6
l_r	Length from rear tire to the center of	m	1.39
	mass		
l_f	Length from front tire to the center of	m	1.55
	mass		
C_{α}	Cornering stiffness of each tire	N	20000
I_z	Yaw intertia	kg m^2	25854
F_{pq}	Tire force, $p \in \{x, y\}, q \in \{f, r\}$	N	Depends on input force
f	Rolling resistance coefficient	N/A	0.019
delT	Simulation timestep	sec	0.032

3 Resources

3.1 Simulation

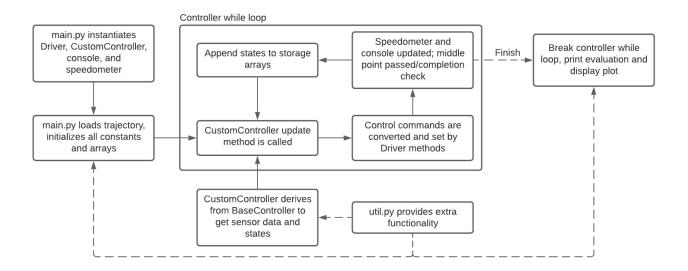


Figure 3: Simulation code flow

Several files are provided to you within the controllers/main folder. The main.py script initializes and instantiates necessary objects, and also contains the controller loop. This loop runs once each simulation timestep. main.py calls your_controller.py's update method on each loop to get new control commands (the desired steering angle, δ , and longitudinal force, F). The longitudinal force is converted to a throttle input, and then both control commands are set by Webots internal functions. The additional script util.py contains functions to help you design and execute the controller. The full codeflow is pictured in Figure 3.

Please design your controller in the your_controller.py file provided for the project part you're working on. Specifically, you should be writing code in the update method. Please do not attempt to change code in other functions or files, as we will only grade the relevant your_controller.py for the programming portion. However, you are free to add to the CustomController class's __init__ method (which is executed once when the CustomController object is instantiated).

3.2 BaseController Background

The CustomController class within each your_controller.py file derives from the Base-Controller class in the base_controller.py file. The vehicle itself is equipped with a Webots-generated GPS, gyroscope, and compass that have no noise or error. These sensors are started in the BaseController class, and are used to derive the various states of the vehicle. An explanation on the derivation of each can be found in the table below.

Table 2: State Derivation.NameExplanation(X,Y)From GPS readings (\dot{x},\dot{y}) From the derivative of GPS readings $\dot{\psi}$ From the compass readings $\dot{\psi}$ From the gyroscope readings

3.3 Trajectory Data

The trajectory is given in buggyTrace.csv. It contains the coordinates of the trajectory as (x, y). The satellite map of the track is shown in Figure 4.



Figure 4: Buggy track[3]

4 P1: Problems

Exercise 1. Model Linearization. As mentioned in class, model linearization is always the first step for non-linear control. During this assignment, you will approximate the given model with a linear model.

Since the longitudinal term \dot{x} is non-linear in the lateral dynamics, we can simplify the controller by controlling the lateral and longitudinal states separately. You are required to write the system dynamics in linear forms as $\dot{s_1} = A_1 s_1 + B_1 u$ and $\dot{s_2} = A_2 s_2 + B_2 u$ in terms of the following given input and states:

$$u = \begin{bmatrix} \delta \\ F \end{bmatrix}, s_1 = \begin{bmatrix} y \\ \dot{y} \\ \psi \\ \dot{\psi} \end{bmatrix}, s_2 = \begin{bmatrix} x \\ \dot{x} \end{bmatrix}$$

Hints:

- When linearizing lateral dynamics, you can assume longitudinal states to be constant, so they can be included in the linear model. Vice versa for the longitudinal dynamics.
- For longitudinal dynamics, if you have some terms that cannot be combined into A_2 and B_2 , you can write them as disturbances and put it as an extra term.

ANSWER:

MER:
Coniver that,
$$M = \begin{bmatrix} 8 \\ F \end{bmatrix}$$
, $S_1 = \begin{bmatrix} 9 \\ 9 \\ \psi \end{bmatrix}$, $S_2 = \begin{bmatrix} n \\ n \end{bmatrix}$

Now,
$$S_1 = \begin{pmatrix} y \\ y \end{pmatrix}$$
, the cauvalent point will be $\begin{pmatrix} y \\ y \end{pmatrix}$

$$\dot{y} = 0$$
, $\dot{y} = 0$, $8 = 0$
 $\dot{y} = \dot{y} \left[-\frac{4c_{2}}{m\dot{n}} \right] + \dot{y} \left(-\frac{4c_{2}(4r-4)}{m\dot{n}} \right) + 8 \left(\frac{2c_{2}}{m} \right)$

$$\ddot{\varphi} = \dot{g} \left(\frac{2(l_f^2 + l_f^2)C_d}{2z\dot{x}} \right) + \dot{\psi} \left(\frac{2(l_f^2 + l_f^2)C_d}{2z\dot{x}} \right)$$

$$+8\left(\frac{2lfCd}{Iz}\right)$$

Now, let fily, y, q, \vec{\pi}, \

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and
$$B_1 = \begin{bmatrix} 2C2 & 0 \\ 2C2 & 0 \\ 0 & 0 \\ 2C2 & 0 \\ 172 & 0 \end{bmatrix}$$

Now, S = A + B + B + M, and plug in m = 1886.6 kg, ly = 1.39 m, lf = 1.55 m, cd = 2000 N, IZ = 25854

$$3) S_{1} = \begin{cases} 0 & 1 & 0 & 0 \\ 0 & -\frac{20}{3} & 0 & -\frac{3.379}{3} - i \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \\ 0 & 5.28 & 0 & -\frac{6.70}{3} & 2.398 & 0 \end{cases}$$

Now for Szy

$$\dot{n} = F(\lambda_m) + \dot{\gamma}\dot{y} - fg$$

 $(n i 8 F) = (f_1) = (i y + m (F-f_m g))$

$$A_{2} = \begin{pmatrix} \frac{\partial H}{\partial x} & \frac{\partial f_{1}}{\partial \hat{x}} \\ \frac{\partial f_{2}}{\partial x} & \frac{\partial f_{3}}{\partial \hat{x}} \end{pmatrix} = \begin{pmatrix} 0 & 1 \\ 0 & 0 \end{pmatrix}$$

$$B_{2} = \begin{pmatrix} \frac{\partial f_{1}}{\partial x} & \frac{\partial f_{2}}{\partial \hat{x}} \\ \frac{\partial f_{2}}{\partial x} & \frac{\partial f_{3}}{\partial \hat{x}} \end{pmatrix} = \begin{pmatrix} 0 & 0 \\ 0 & y_{m} \end{pmatrix}$$

$$Pugging values in S_{2} = A_{2}S_{2} + B_{2}U$$

$$= \int S_{2} = \begin{pmatrix} 0 & 1 \\ 0 & 0 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} + \begin{pmatrix} 0 & 0 \\ 0 & 0.000529 \end{pmatrix} \begin{pmatrix} x \\ F \end{pmatrix}$$

$$+ \begin{pmatrix} 0 & 0 \\ y \end{pmatrix} \begin{pmatrix} y \\ -fq \end{pmatrix}$$

Exercise 2. Controller Synthesis in Simulation. The driver functions that control the car take the desired steering angle δ and a throttle input - ranging from 0 to 1 - which is derived from the desired longitudinal force F.

For this question, you have to design a PID longitudinal controller and a PID lateral controller for the vehicle. A PID is an error-based controller that requires tuning proportional, integral, and derivative gains. As a PID allows us to minimize the error between a set point and process variable without deeper knowledge of the system model, we will not need our result from Exercise 1 (though it will be useful in future project parts).

Design the two controllers in your_controller.py. You can make use of Webots' built-in code editor, or use your own.

Check the performance of your controller by running the Webots simulation. You can press the play button in the top menu to start the simulation in real-time, the fast-forward button to run the simulation as quickly as possible, and the triple fast-forward to run the simulation without rendering (any of these options is acceptable, and the faster options may be better for quick tests). If you complete the track, the scripts will generate a performance plot via matplotlib. This plot contains a visualization of the car's trajectory, and also shows the variation of states with respect to time.

Submit your_controller.py and the final completion plot as described on the title page. Your controller is **required** to achieve the following performance criteria to receive full points:

- 1. Time to complete the loop = 400 s
- 2. Maximum deviation from the reference trajectory = 10.0 m
- 3. Average deviation from the reference trajectory = 5 m

Some hints that may be useful:

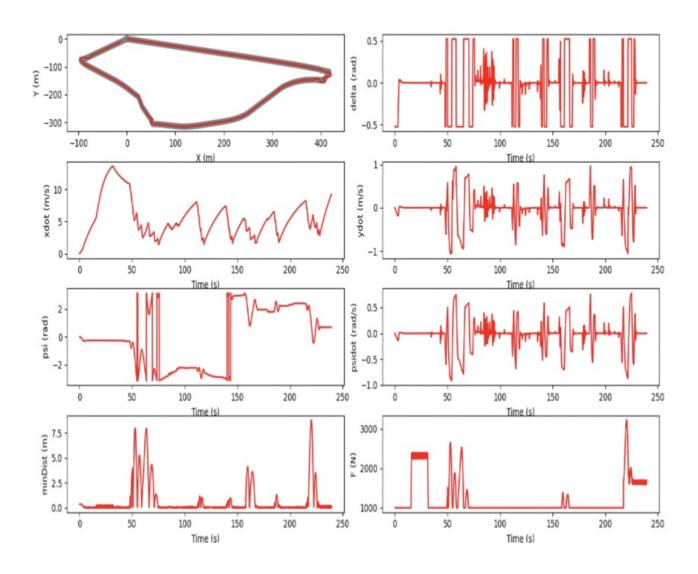
- Using a PID controller requires storing variables between method calls. Python allows this through use of the self preface (in other words, making them class member variables). Think about which variables you use in your controller that you will need to store, and be sure to add them to CustomController's __init__ method so they are initialized.
- If you are tuning your lateral controller for a point on the trajectory that is the closest to the vehicle, the controller may struggle on sudden turns. Think about how to add some mechanism that "looks ahead" of your current position before calculating a control command.
- Functions in util.py might be useful. For example, closestNode returns the absolute value of the cross-track error, which is the distance from the vehicle's center of gravity to the nearest waypoint on the trajectory. In addition, the function also returns the

index of the closest waypoint to the vehicle. Also you may need to use wrapToPi when you deal with angles.

• If your car does not perform well, it may just be that it requires tuning. You may already have some experience tuning PID controllers, but if not, viewing online resources is recommended. See this Wiki link [4] for more background in the process of manual tuning.

ANSWER:

THE PERFORMANCE PLOT IMAGE OF THE CONTROLLER:



INFO: main: Starting controller: C:\Users\srech\AppData\Local\Microsoft\WindowsApps\python3.8.exe -u main.py

Evaluating...

Score for completing the loop: 30.0/30.0 Score for average distance: 30.0/30.0 Score for maximum distance: 30.0/30.0

Your time is 239.36

Your total score is: 100.0/100.0

total steps: 239360

maxMinDist: 8.798280257295637 avgMinDist: 0.7100386692383279 INFO: 'main' controller exited successfully.

5 Reference

- 1. Rajamani Rajesh. Vehicle Dynamics and Control. Springer Science & Business Media, 2011.
- 2. Kong Jason, et al. "Kinematic and dynamic vehicle models for autonomous driving control design." Intelligent Vehicles Symposium, 2015.
- 3. cmubuggy.org, https://cmubuggy.org/reference/File:Course_hill1.png
- 4. "PID Controller Manual Tuning." *Wikipedia*, Wikimedia Foundation, August 30th, 2020. https://en.wikipedia.org/wiki/PID_controller#Manual_tuning