

Recursion in C

Recursion is a process in programming where a function calls itself to solve smaller instances of the same problem until it reaches a base case (the stopping condition). It breaks down complex problems into smaller, more manageable sub-problems.

Key Concepts:

1. ***Base Case:*** Every recursive function must have a base case to prevent infinite recursion. The base case is the condition under which the recursion stops.
2. ***Recursive Case:*** This is the part of the function where the function calls itself with modified arguments, gradually approaching the base case.

```
int nSum(int n)
{
    if (n==0) {
        return 0;
    }

    int res = n+ nsum(n-1);
    return res;
}
```

Base condition

Recursive case

How Recursion Works:

- The problem is divided into sub-problems.
- The function calls itself with updated arguments.
- Once the base case is reached, the function begins to return, and the results are combined as it "unwinds" back to the initial call.

Example 1: Factorial using Recursion

FACTORIAL OF N

$$n! = n * (n-1) * (n-2) * (n-3) * (n-4) * (n-5) \dots 1$$

Example:

$$5! = 5 * 4 * 3 * 2 * 1 = 120$$

The factorial of a non-negative integer n is the product of all positive integers less than or equal to n . It is denoted by $n!$.

Factorial of n :

- $n! = n * (n-1) * (n-2) * \dots * 1$

- Base Case: $n = 0$, $0! = 1$

C Program to Calculate Factorial Using Recursion:

```
#include <stdio.h>

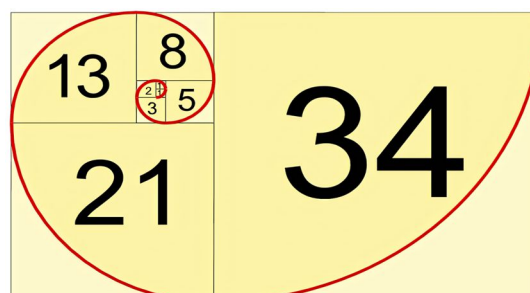
int factorial(int n) {
    if (n == 0) {
        return 1; // Base case
    } else {
        return n * factorial(n - 1); // Recursive case
    }
}

int main() {
    int num;
    printf("Enter a number: ");
    scanf("%d", &num);
    printf("Factorial of %d is %d\n", num, factorial(num));
    return 0;
}
```

Explanation:

- The factorial function calls itself with $n-1$ until n becomes 0 (the base case), after which it starts returning the computed values.

Example 2: Fibonacci Series using Recursion



The Fibonacci sequence is a series of numbers where each number is the sum of the two preceding ones. It starts with 0 and 1.

Fibonacci of n:

- $\text{Fib}(0) = 0$
- $\text{Fib}(1) = 1$
- $\text{Fib}(n) = \text{Fib}(n-1) + \text{Fib}(n-2)$ for $n > 1$

C Program to Print Fibonacci Sequence Using Recursion:

```
#include <stdio.h>

int fibonacci(int n) {
    if (n == 0) {
        return 0; // Base case
    } else if (n == 1) {
        return 1; // Base case
    } else {
        return fibonacci(n - 1) + fibonacci(n - 2); // Recursive case
    }
}

int main() {
    int n, i;

    printf("Enter the number of terms: ");
    scanf("%d", &n);

    printf("Fibonacci Series: ");
    for (i = 0; i < n; i++) {
        printf("%d ", fibonacci(i));
    }

    printf("\n");

    return 0;
}
```

Explanation:

- The fibonacci function calls itself twice: once for $n-1$ and once for $n-2$. The function continues until it reaches the base cases $n == 0$ or $n == 1$.