

## EE22BTECH11029 - Komakula Sreeja

### Question 11.16.3.20

While shuffling a pack of 52 playing cards, 2 cards are dropped. Find the probability that the missing cards to be of different colours.

**Solution:** We know that the 52 playing cards contain 26 red cards and 26 black cards.

Let  $X_1$  and  $X_2$  be two random variables denoting the colour of first card and second card respectively:

$$X_i = \begin{cases} 0, & \text{red card} \\ 1, & \text{black card} \end{cases} \quad \{i = 1, 2\} \quad (1)$$

Probability of choosing the first card:

$$p_{X_1}(k) = \frac{26}{52} \quad \{k = 0, 1\} \quad (2)$$

$$= \frac{1}{2} \quad (3)$$

Probability that second card chosen is red after selecting the first card as red

$$= \frac{25}{51} \times \frac{26}{52} \div \frac{26}{52} = \frac{25}{51} \quad (4)$$

Probability that second card chosen is black after selecting the first card as red

$$= \frac{26}{51} \times \frac{26}{52} \div \frac{26}{52} = \frac{26}{51} \quad (5)$$

Probability that second card chosen is red after selecting the first card as black

$$= \frac{26}{51} \times \frac{26}{52} \div \frac{26}{52} = \frac{26}{51} \quad (6)$$

Probability that second card chosen is black after selecting the first card as black

$$= \frac{25}{51} \times \frac{26}{52} \div \frac{26}{52} = \frac{25}{51} \quad (7)$$

Probability that both cards have different colour:

$$pr(X_1 \neq X_2) = p_{X_1}(0) p(X_2 = 1|X_1 = 0) + p_{X_1}(1) p(X_2 = 0|X_1 = 1) \quad (8)$$

$$= \frac{26}{52} \times \frac{26}{51} + \frac{26}{52} \times \frac{26}{51} \quad (9)$$

$$= 2 \times \frac{26}{52} \times \frac{13}{51} \quad (10)$$

$$= \frac{26}{51} \quad (11)$$

TABLE 1: Description of random variables

Random Variable	Values	Description
$X_1$	0	First card is red
	1	First card is black
$X_2$	0	Second card is red
	1	Second card is black