CSE-5311-Project

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Implement and compare the following sorting algorithm:

- Mergesort
- Heapsort
- Quicksort (Regular quick sort* and quick sort using 3 medians)
- Insertion sort
- Selection sort
- Bubble sort

Sorting Algorithms: A Sorting Algorithm is used to rearrange a given array or list elements according to a comparison operator on the elements. The comparison operator is used to decide the new order of element in the respective data structure.

A **sorting algorithm** is an algorithm that puts elements of a list in a certain order. The most frequently used orders are numerical order and lexicographical order. Efficient sorting is important for optimizing the efficiency of other algorithms (such as search and merge algorithms) that require input data to be in sorted lists

Data Structure used: For all the sorting methods, I used Arrays as the data structures.

Merge Sort: Merge Sort is a **Divide and Conquer** algorithm. It divides the input array into two halves, calls itself for the two halves, and then merges the two sorted halves. The merge() function is used for merging two halves.

Divide the unsorted list into 2 sub lists each time. Do this until each sub list has 1 element. Take adjacent pairs of two singleton lists and merge them to form a list of 2 elements. N will now convert into N/2 lists of size 2. Repeat the process till a single sorted list of obtained..

Merge Sort Algorithm Time Complexity:

Best Case: $\Omega(n(\log n))$

Average Case: $\Theta(n(\log n))$

Worst Case: O(n(logn))

```
# left-leftarray
# right - rightArray
#method to perform merge
def merge(left, right):
  ans = []
   while i < len(left) and j < len(right):
      if left[i] < right[j]:</pre>
         ans.append(left[i])
         ans.append(right[j])
   while i < len(left):
          ans.append(left[i])
   while j < len(right):
          ans.append(right[j])
   return ans
def mergeSort(mArray):
   length=len(mArray)
  if length == 1:
      return mArray
   mid = length // 2
   IP = mergeSort(mArray[0:mid])
   rP = mergeSort(mArray[mid:])
  return merge(IP, rP)
```

In this method we have used two method. mergeSort() method is used to divide the array in two halves by calling mergeSort() method recursively. merge() method is used to join the array after sorting the list.

Run time for different test cases:

WORST CASE:

```
Enter the array size: 7

Enter the Element 0: 7

Enter the Element 1: 6

Enter the Element 2: 5

Enter the Element 3: 4

Enter the Element 4: 3

Enter the Element 5: 2

Enter the Element 6: 1

Results after applying Merge sort: [1, 2, 3, 4, 5, 6, 7]

Runtime of Merge sort = 1.60000000002236447e-05

Best Case:

Enter the array size: 7

Enter the Element 0: 1

Enter the Element 1: 2

Enter the Element 2: 3
```

Results after applying Merge sort: [1, 2, 3, 4, 5, 6, 7]

Enter the Element 3:4

Enter the Element 4:5

Enter the Element 5:6

Enter the Element 6:7

Runtime of Merge sort = 5.140000000256796e-05

Average Case:

```
Enter the array size: 7

Enter the Element 0: 4

Enter the Element 1: 1

Enter the Element 2: 5

Enter the Element 3: 3

Enter the Element 4: 2

Enter the Element 5: 7
```

Enter the Element 6:6

Results after applying Merge sort: [1, 2, 3, 4, 5, 6, 7]

Runtime of Merge sort = 1.5199999999999997e-05

Heap Sort: Heap sort is a comparison based sorting technique based on Binary Heap data structure. It is similar to selection sort where we first find the minimum element and place the minimum element at the beginning. We repeat the same process for the remaining elements.

Heap Sort Time Complexity:

Best Case: $\Omega(n(\log n))$

Average Case: $\Theta(n(\log n))$

Worst Case: O(n(logn))

```
#method to heapify
def heapify(array, n, i):
    greatest= i
    left = 2 * i + 1
    right = 2 * i + 2

if left < n and array[greatest] < array[left]:
    greatest = left</pre>
```

```
if right < n and array[greatest] < array[right]:</pre>
      greatest = right
   if greatest != i:
      array[i], array[greatest] = array[greatest], array[i]
      heapify(array, n, greatest)
def heapSort(heaparr):
   length = len(heaparr)
  for i in range(length // 2 - 1, -1, -1):
      heapify(heaparr, length, i)
  for i in range(length - 1, 0, -1):
      heaparr[i], heaparr[0] = heaparr[0], heaparr[i]
      heapify(heaparr, i, 0)
  return heaparr
```

Here we implemented two methods.

One is heapify() method which is used to build a max heap using the given values. heapSort() method is used to arrange the values in a sorted order using the heapify() method.

Run time for different test cases:

Worst Case:

Enter the size of the array: 7

Enter the Element 0:7

Enter the Element 1:6

```
Enter the Element 2:5
```

Enter the Element 3:4

Enter the Element 4:3

Enter the Element 5:2

Enter the Element 6:1

Results after applying heap Sort: [1, 2, 3, 4, 5, 6, 7]

Runtime=2.0100000000411455e-05

Best case:

Enter the size of the array: 7

Enter the Element 0:1

Enter the Element 1:2

Enter the Element 2:3

Enter the Element 3:4

Enter the Element 4:5

Enter the Element 5:6

Enter the Element 6:7

Results after applying heap Sort: [1, 2, 3, 4, 5, 6, 7]

Runtime= 2.240000000644127e-05

Average Case:

Enter the size of the array: 7

Enter the Element 0:5

Enter the Element 1:1

Enter the Element 2:2

Enter the Element 3:7

Enter the Element 4:6

Enter the Element 5:3

Enter the Element 6:4

Results after applying heap Sort: [1, 2, 3, 4, 5, 6, 7]

Runtime = 2.33999999999895726e-05

Quick Sort: QuickSort is a Divide and Conquer algorithm. It picks an element as pivot and partitions the given array around the picked pivot. There are many different versions of quickSort that pick pivot in different ways.

- 1. Always pick first element as pivot.
- 2. Always pick last element as pivot (implemented below)
- 3. Pick a random element as pivot.
- 4. Pick median as pivot.

Quick Sort Time Complexity:

Best Case: $\Omega(n(\log n))$

Average Case: $\Theta(n(\log n))$

Worst Case: $O(n^2)$

```
#method to perform partition

def partition(inputArray, least, highest): #l=low , h=high
    count = (least - 1)
    pivot = inputArray[highest]

for j in range(least, highest):

    if inputArray[j] <= pivot:
        count += 1
        inputArray[count], inputArray[j] = inputArray[j], inputArray[count]

inputArray[count + 1], inputArray[highest] = inputArray[highest],
inputArray[count + 1]
    return count + 1</pre>

# Method to do Quick sort
```

```
def quickSort(array, lowest, highest):
    if len(array) == 1:
        return array
    if lowest < highest:
        pivot = partition(array, lowest, highest)

# Separately sort elements before
    # partition and after partition
    quickSort(array, lowest, pivot - 1)
    quickSort(array, pivot + 1, highest)
    return array</pre>
```

Here we used two methods.

partition() method is used to get the pivot value. quickSort() method is used to divide the array by calling quickSort recursively to sort the array and call the partition().

Run time for different test cases:

```
Enter the Element 1 of List: 2
Enter the Element 2 of List: 3
Enter the Element 3 of List: 4
Enter the Element 4 of List: 5
Enter the Element 5 of List: 6
Enter the Element 6 of List: 7
Results after performing Quick Sort: [1, 2, 3, 4, 5, 6, 7]
Quick sort Runtime= 1.609999999852344e-05
Average Case:
Enter the array size: 7
Enter the Element 0 of List: 3
Enter the Element 1 of List: 1
Enter the Element 2 of List: 6
Enter the Element 3 of List: 2
Enter the Element 4 of List: 4
Enter the Element 5 of List: 5
Enter the Element 6 of List: 7
Results after performing Quick Sort: [1, 2, 3, 4, 5, 6, 7]
```

Quick sort Runtime= 1.950000000505224e-05

Quick Sort Using Medians: The best case for quick sort is that if we could find the middle element. In this algorithm the pivot is picked as the median of the left most, centre and rightmost element in array. By selecting the median as the pivot we can, overcome the drawback in quick sort algorithm.

Here the drawback in the quick sort is ignored by selecting the pivot as median and hence the worst case in quick sort is converted to average case.

```
import time
#Method to perform Quick Sort
def quickSort_median(arr, lowest, highest):
   if lowest < highest:
      p = partition(arr, lowest, highest)
      quickSort_median(arr, lowest, p - 1)
      quickSort_median(arr, p + 1, highest)
   return arr
#A=Array name
def pivot(A, lowest, highest):
   mid = (lowest + highest) // 2
  if A[lowest] <= A[mid] <= A[highest]:</pre>
      return mid
  if A[highest] <= A[mid] <= A[lowest]:</pre>
      return mid
  if A[lowest] <= A[highest] <= A[mid]:</pre>
      return highest
  if A[mid] <= A[highest] <= A[lowest]:
      return highest
   return lowest
def partition(A, lowest, highest):
  pivotldx = pivot(A, lowest, highest)
  pivotValue = A[pivotIdx]
  A[pivotldx], A[lowest] = A[lowest], A[pivotldx]
  pointer = lowest
  for i in range(lowest, highest + 1):
      if A[i] < pivotValue:
         pointer += 1
         A[i], A[pointer] = A[pointer], A[i]
   A[lowest], A[pointer] = A[pointer], A[lowest]
  return pointer
```

Here, we used three methods.

pivot() method is get the median value from three values which we have taken that is value at index 0 , value at index (size-1)and value at middl index . quickSort_median

is used to divide the array into parts by calling the quickSort_median recursively. partition() method is used to get the pivot value.

Run time for different test cases: Worst Case: Enter the array size: 7 Enter the Element 0 of List: 7 Enter the Element 1 of List: 6 Enter the Element 2 of List: 5 Enter the Element 3 of List: 4 Enter the Element 4 of List: 3 Enter the Element 5 of List: 2 Enter the Element 6 of List: 1 Results after applying quick sort using Median: [1, 2, 3, 4, 5, 6, 7] Runtime= 1.340000000274304e-05 Best Case: Enter the array size: 7 Enter the Element 0 of List: 1 Enter the Element 1 of List: 2 Enter the Element 2 of List: 3 Enter the Element 3 of List: 4

Enter the Element 4 of List: 5

Enter the Element 5 of List: 6

Enter the Element 6 of List: 7

Results after applying quick sort using Median: [1, 2, 3, 4, 5, 6, 7]

Runtime= 1.2500000000414957e-05

Average Case:

```
Enter the array size: 7

Enter the Element 0 of List: 5

Enter the Element 1 of List: 1

Enter the Element 2 of List: 3

Enter the Element 3 of List: 2

Enter the Element 4 of List: 4

Enter the Element 5 of List: 7

Enter the Element 6 of List: 6
```

Results after applying quick sort using Median: [1, 2, 3, 4, 5, 6, 7]

Runtime= 2.059999999149077e-05

Insertion Sort: Insertion sort is a simple sorting algorithm that builds the final sorted array (or list) one item at a time. It is much less efficient on large lists than more advanced algorithms such as quicksort, heapsort, or merge sort.

The input is an unsorted array. Find the correct position of xi in the list. Move other elements to Insert xi in the correct place

Insertion Sort Time Complexity:

Best Case: $\Omega(n)$

Average Case: $\Theta(n^2)$

Worst Case: O(n^2)

```
import time

#insertion sort method

def insertionSort(iArray, n): #name of the array

for i in range(n):
    data = iArray[i]
    j = i-1
    while j >= 0 and data < arr[j]:
    iArray[j+1] = iArray[j]
    j -= 1</pre>
```

iArray[j+1] = data return iArray

Here, we used insertionSort() method to sort the values.

Run time for different test cases:

Worst Case:

Enter the array size: 7

Enter the elements 0: 7

Enter the elements 1: 6

Enter the elements 2: 5

Enter the elements 3: 4

Enter the elements 4: 3

Enter the elements 5: 2

Enter the elements 6: 1

Results after applying insertion sort: [1, 2, 3, 4, 5, 6, 7]

Runtime of insertion sort: 8.0999999873412e-06

Best Case:

Enter the array size: 7

Enter the elements 0: 1

Enter the elements 1: 2

Enter the elements 2: 3

Enter the elements 3: 4

Enter the elements 4: 5

Enter the elements 5: 6

Enter the elements 6: 7

Results after applying insertion sort: [1, 2, 3, 4, 5, 6, 7]

Runtime of insertion sort: 7.700000001165108e-06

Average Case:

Enter the array size: 7

Enter the elements 0: 5

Enter the elements 1: 1

Enter the elements 2: 2

Enter the elements 3: 7

Enter the elements 4: 6

Enter the elements 5: 3

Enter the elements 6: 4

Results after applying insertion sort: [1, 2, 3, 4, 5, 6, 7]

Runtime of insertion sort: 6.800000013057615e-06

Selection Sort: Selection sort is a simple sorting algorithm. This sorting algorithm is an in-place comparison-based algorithm in which the list is divided into two parts, the sorted part at the left end and the unsorted part at the right end. Initially, the sorted part is empty and the unsorted part is the entire list.

Initially, the sorted part is empty, and the unsorted part is the entire list. The smallest element is selected from the unsorted array and swapped with the leftmost element, and that element becomes a part of the sorted array. This process continues moving unsorted array boundary by one element to the right.

Selection Sort Time Complexity:

Best Case: $\Omega(n^2)$

Average Case: $\Theta(n^2)$

Worst Case: O(n^2)

```
import time
# selection sort method
def selectionSort(sArray, length): #sArray= name of the array
for i in range(length):
```

```
minIdx = i
I=len(sArray) #I=length of array

for j in range(i + 1, l):
    if sArray[minIdx] > sArray[j]:
        minIdx = j

# Swap
    sArray[i], sArray[minIdx] = sArray[minIdx], sArray[i]

return sArray
```

Here, we used selectionSort() method to sort the values.

Run time for different test cases:

```
Worst Case:
```

Enter the Element 0:7

Enter the Element 1:6

Enter the Element 2:5

Enter the Element 3:4

Enter the Element 4:3

Enter the Element 5:2

Enter the Element 6:1

Results after applying selection sort: [1, 2, 3, 4, 5, 6, 7]

Run time of selection sort = 9.39999999715192e-06

Best Case:

Enter the size of the array: 7

Enter the Element 0:1

Enter the Element 1:2

Enter the Element 2:3

Enter the Element 3:4

```
Enter the Element 4:5
Enter the Element 5:6
Enter the Element 6:7
Results after applying selection sort: [1, 2, 3, 4, 5, 6, 7]
Run time of selection sort = 1.299999999152578e-05
Average Case:
Enter the size of the array: 7
Enter the Element 0:4
Enter the Element 1:1
Enter the Element 2:3
Enter the Element 3:6
Enter the Element 4:7
Enter the Element 5:2
Enter the Element 6:5
Results after applying selection sort: [1, 2, 3, 4, 5, 6, 7]
Run time of selection sort = 9.9000000022917e-06
Bubble Sort: Bubble sort is a simple sorting algorithm. This sorting algorithm is
comparison-based algorithm in which each pair of adjacent elements is compared and
the elements are swapped if they are not in order.
Bubble Sort Time Complexity:
Best Case: \Omega(n)
Average Case: \Theta(n^2)
Worst Case: O(n^2)
 import time
#bubble Sort method
def bubbleSort(bArray, length):
```

```
for i in range (length):
      for j in range (length-i-1):
         if bArray[j] > bArray[j + 1]:
            bArray[j], bArray[j+1] = bArray[j+1], bArray[j]
   return bArray #return array after sorting
Run time for different test cases:
Worst Case:
Enter the size of the array: 7
Enter the Elements 0:7
Enter the Elements 1:6
Enter the Elements 2:5
Enter the Elements 3:4
Enter the Elements 4:3
Enter the Elements 5:2
Enter the Elements 6:1
Results after performing Bubble sort: [1, 2, 3, 4, 5, 6, 7]
Bubble sort Runtime= 9.89999999340992e-06
Enter the size of the array: 7
Enter the Elements 0:1
Enter the Elements 1:2
Enter the Elements 2:3
Enter the Elements 3:4
Enter the Elements 4:5
Enter the Elements 5:6
Enter the Elements 6:7
```

Results after performing Bubble sort: [1, 2, 3, 4, 5, 6, 7]

Bubble sort Runtime= 1.08999999948077e-05

```
Average Case:
```

Enter the size of the array: 7

Enter the Elements 0:5

Enter the Elements 1:1

Enter the Elements 2:3

Enter the Elements 3:2

Enter the Elements 4:4

Enter the Elements 5:7

Enter the Elements 6:6

Results after performing Bubble sort: [1, 2, 3, 4, 5, 6, 7]

Bubble sort Runtime= 8.9000000097757e-06

newmain.py: In this file we imported all the sorting methods from other files. This is the main file where we can execute all the sorting Algorithm.

main() method is used to call all the sorting algorithms

It takes the input one time and gives the sorted results and running time of all the algorithms.

Here Graph is also plotted to compare the run time of the algorithms in different cases.

```
import time

from heapSort import heapSort

from newquickSort import quickSort

from quickUsingMedian import quickSort_median

from insertionSort import insertionSort

from bubbleSort import bubbleSort

from selectionSort import selectionSort

from newmerge import mergeSort

import numpy as np

import matplotlib.pyplot as plt
```

```
def main():
  globalArr = [7
  size = int(input("Enter the size of the array: "))
  for i in range(size):
     value = int (input("Enter the Element %d of array: " % i))
     globalArr.append(value)
  print(globalArr)
  arrayForSelectionSort = globalArr.copy()
  selection_start = time.perf_counter()
  r = selectionSort(arrayForSelectionSort, size)
  selection_time = time.perf_counter() - selection_start
  print("Results after performing Selection sort:", r)
  print("Run time of Selection Sort =", selection_time)
  arrayForbubbleSort = globalArr.copy()
  bubble_start = time.perf_counter()
  r = bubbleSort(arrayForbubbleSort, size)
  bubble_time = time.perf_counter() - bubble_start
  print("Results after performing Bubble sort:", r)
  print("Runtime of Bubble sort =", bubble_time)
  arrayForMergeSort = globalArr.copy()
  merge_start = time.perf_counter()
  r = mergeSort(arrayForMergeSort)
  merge_time = time.perf_counter() - merge_start
  print("Results after performing Merge sort:", r)
  print("Runtime of Merge sort=", merge_time)
  arrayForInsertionSort = globalArr.copy()
  insertion_start = time.perf_counter()
  r = insertionSort(arrayForInsertionSort, size)
  insertion_time = time.perf_counter() - insertion_start
  print("Results after performing Insertion sort:", r)
  print("Runtime of Insertion sort=", insertion_time)
  arrayForQuickSort = globalArr.copy()
  quick_start = time.perf_counter()
  r = quickSort(arrayForQuickSort, 0, len(arrayForQuickSort) - 1)
```

```
quick_time = time.perf_counter() - quick_start
  print("Results after performing Quick sort:", r)
  print("Runtime of Quick sort=", quick_time)
  arrayForQuickSortMedian = globalArr.copy()
  quickstart_UsingMedain = time.perf_counter()
  r = quickSort_median(arrayForQuickSortMedian, 0, len(arrayForQuickSortMedian)
  quickMedian_time = time.perf_counter() - quickstart_UsingMedain
  print("Result after performing Quick sort using Median:", r)
  print("Runtime of Quick sort using Median=", quickMedian_time)
  arrayForheapSort = globalArr.copy()
  heap_start = time.perf_counter()
  r = heapSort(arrayForheapSort)
  heap_time = time.perf_counter() - heap_start
  print("Results after performing Heap sort:", r)
  print("Runtime of Heap sort=", heap_time)
  x = [bubble_time, insertion_time, selection_time, heap_time, merge_time,
quick_time, quickMedian_time]
  plt.xticks(np.arange(7), (
'guickSortUsingMedian'))
  plt.plot(x, 'bo', x, 'r')
  plt.show()
main()
```

Enter the size of the array: 5

Enter the Element 0 of array: 4

Enter the Element 1 of array: 67

Enter the Element 2 of array: 21

Enter the Element 3 of array: 45

Enter the Element 4 of array: 8

[4, 67, 21, 45, 8]

Results after performing Selection sort: [4, 8, 21, 45, 67]

Run time of Selection Sort = 9.99999999621423e-06

Results after performing Bubble sort: [4, 8, 21, 45, 67]

Runtime of Bubble sort = 7.89999999949614e-06

Results after performing Merge sort: [4, 8, 21, 45, 67]

Runtime of Merge sort= 1.729999999664806e-05

Results after performing Insertion sort: [4, 8, 21, 45, 67]

Runtime of Insertion sort= 5.60000001493299e-06

Results after performing Quick sort: [4, 8, 21, 45, 67]

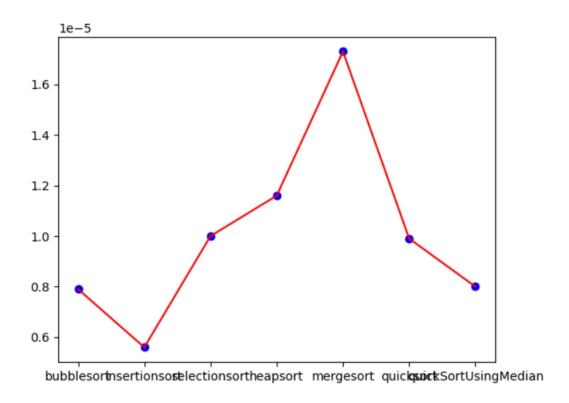
Runtime of Quick sort= 9.89999998452813e-06

Result after performing Quick sort using Median: [4, 8, 21, 45, 67]

Runtime of Quick sort using Median= 8.000000001118224e-06

Results after performing Heap sort: [4, 8, 21, 45, 67]

Runtime of Heap sort= 1.16000000055561e-05



x= y=1.059e-05

Enter the size of the array: 5

Enter the Element 0 of array: 1

Enter the Element 1 of array: 2

Enter the Element 2 of array: 3

Enter the Element 3 of array: 4

Enter the Element 4 of array: 5

[1, 2, 3, 4, 5]

Results after performing Selection sort: [1, 2, 3, 4, 5]

Run time of Selection Sort = 1.040000000743148e-05

Results after performing Bubble sort: [1, 2, 3, 4, 5]

Runtime of Bubble sort = 6.600000006073969e-06

Results after performing Merge sort: [1, 2, 3, 4, 5]

Runtime of Merge sort= 1.4100000001349144e-05

Results after performing Insertion sort: [1, 2, 3, 4, 5]

Runtime of Insertion sort= 3.90000002943216e-06

Results after performing Quick sort: [1, 2, 3, 4, 5]

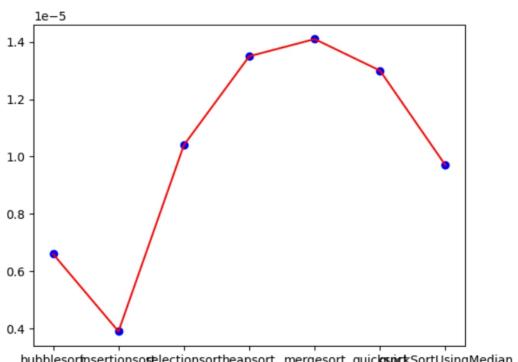
Runtime of Quick sort= 1.299999995599865e-05

Result after performing Quick sort using Median: [1, 2, 3, 4, 5]

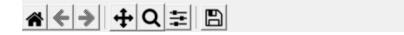
Runtime of Quick sort using Median= 9.69999999668307e-06

Results after performing Heap sort: [1, 2, 3, 4, 5]





bubbles or f nsertions o s e lections or the apsort merges or t quick S o r t V S o r t U s i n g M e d i a n



x = y = 6.83e - 06

Enter the size of the array: 40

Enter the Element 0 of array: 6

Enter the Element 1 of array: 12

Enter the Element 2 of array: 98

Enter the Element 3 of array: 534

Enter the Element 4 of array: 234

Enter the Element 5 of array: 61

Enter the Element 6 of array: 90

Enter the Element 7 of array: 29

Enter the Element 8 of array: 11

Enter the Element 9 of array: 456

Enter the Element 10 of array: 75

Enter the Element 11 of array: 13

Enter the Element 12 of array: 42

Enter the Element 13 of array: 78

Enter the Element 14 of array: 19

Enter the Element 15 of array: 33

Enter the Element 16 of array: 26

Enter the Element 17 of array: 84

Enter the Element 18 of array: 93

Enter the Element 19 of array: 25

Enter the Element 20 of array: 71

Enter the Element 21 of array: 43

Enter the Element 22 of array: 81

Enter the Element 23 of array: 22

Enter the Element 24 of array: 56

Enter the Element 25 of array: 39

Enter the Element 26 of array: 11

Enter the Element 27 of array: 77

Enter the Element 28 of array: 239

Enter the Element 29 of array: 871

Enter the Element 30 of array: 123

Enter the Element 31 of array: 44

Enter the Element 32 of array: 64

Enter the Element 33 of array: 37

Enter the Element 34 of array: 114

Enter the Element 35 of array: 121

Enter the Element 36 of array: 2

Enter the Element 37 of array: 1

Enter the Element 38 of array: 5

Enter the Element 39 of array: 9

[6, 12, 98, 534, 234, 61, 90, 29, 11, 456, 75, 13, 42, 78, 19, 33, 26, 84, 93, 25, 71, 43, 81, 22, 56, 39, 11, 77, 239, 871, 123, 44, 64, 37, 114, 121, 2, 1, 5, 9]

Results after performing Selection sort: [1, 2, 5, 6, 9, 11, 11, 12, 13, 19, 22, 25, 26, 29, 33, 37, 39, 42, 43, 44, 56, 61, 64, 71, 75, 77, 78, 81, 84, 90, 93, 98, 114, 121, 123, 234, 239, 456, 534, 871]

Run time of Selection Sort = 5.2699999997685154e-05

Results after performing Bubble sort: [1, 2, 5, 6, 9, 11, 11, 12, 13, 19, 22, 25, 26, 29, 33, 37, 39, 42, 43, 44, 56, 61, 64, 71, 75, 77, 78, 81, 84, 90, 93, 98, 114, 121, 123, 234, 239, 456, 534, 871]

Runtime of Bubble sort = 8.910000001094431e-05

Results after performing Merge sort: [1, 2, 5, 6, 9, 11, 11, 12, 13, 19, 22, 25, 26, 29, 33, 37, 39, 42, 43, 44, 56, 61, 64, 71, 75, 77, 78, 81, 84, 90, 93, 98, 114, 121, 123, 234, 239, 456, 534, 871]

Runtime of Merge sort= 6.8400000035212e-05

Results after performing Insertion sort: [1, 2, 5, 6, 9, 11, 11, 12, 13, 19, 22, 25, 26, 29, 33, 37, 39, 42, 43, 44, 56, 61, 64, 71, 75, 77, 78, 81, 84, 90, 93, 98, 114, 121, 123, 234, 239, 456, 534, 871]

Runtime of Insertion sort= 4.859999999510146e-05

Results after performing Quick sort: [1, 2, 5, 6, 9, 11, 11, 12, 13, 19, 22, 25, 26, 29, 33, 37, 39, 42, 43, 44, 56, 61, 64, 71, 75, 77, 78, 81, 84, 90, 93, 98, 114, 121, 123, 234, 239, 456, 534, 871]

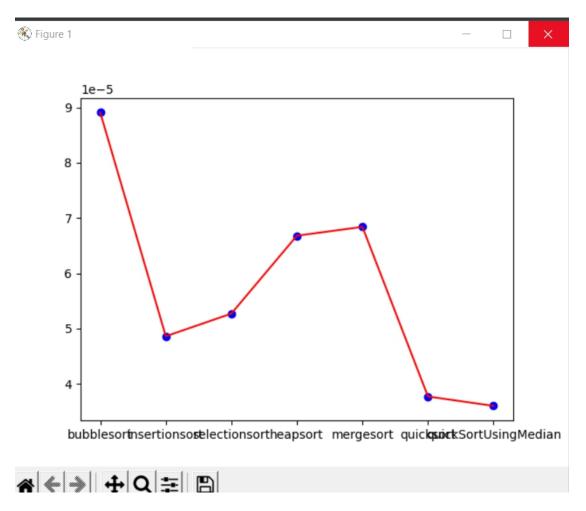
Runtime of Quick sort= 3.7700000007134804e-05

Result after performing Quick sort using Median: [1, 2, 5, 6, 9, 11, 11, 12, 13, 19, 22, 25, 26, 29, 33, 37, 39, 42, 43, 44, 56, 61, 64, 71, 75, 77, 78, 81, 84, 90, 93, 98, 114, 121, 123, 234, 239, 456, 534, 871]

Runtime of Quick sort using Median= 3.600000000858472e-05

Results after performing Heap sort: [1, 2, 5, 6, 9, 11, 11, 12, 13, 19, 22, 25, 26, 29, 33, 37, 39, 42, 43, 44, 56, 61, 64, 71, 75, 77, 78, 81, 84, 90, 93, 98, 114, 121, 123, 234, 239, 456, 534, 871]

Runtime of Heap sort= 6.6799999999343e-05



Conclusion:

From the above graphs, we observed that,

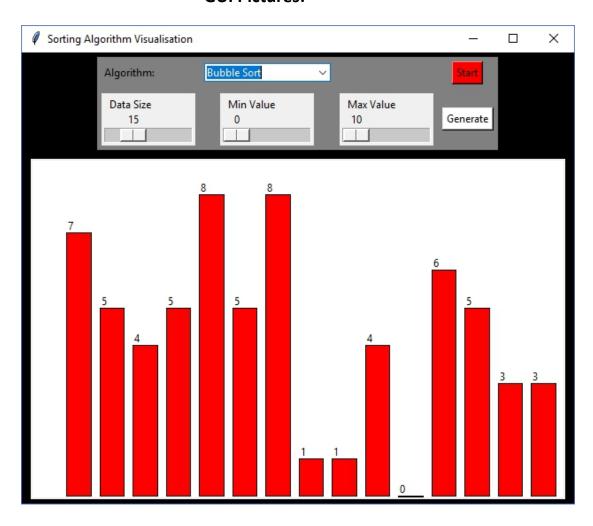
for smaller data Insertion sort is more efficient.

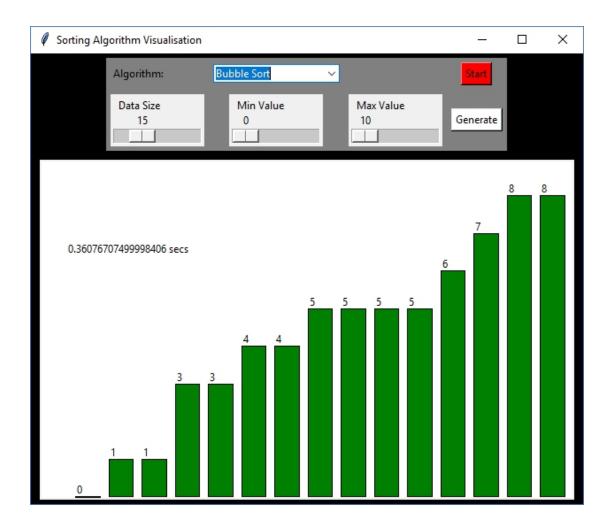
For larger data quick Sort Using Median is more efficient.

Time Complexity of all the above sorting Algorithms are given in the following table in Best Case, Average Case and Worst Case.

Name Algorithm	Time Complexity of Algorithm			
	Best	Average	Worst	
Merge Sort	Ω(n log(n))	Θ(n log(n))	O(n log(n))	
Heap Sort	Ω(n log(n))	Θ(n log(n))	O(n log(n))	
Quick Sort	Ω(n log(n))	Θ(n log(n))	O(n^2)	
Insertion Sort	Ω(n)	Θ(n^2)	O(n^2)	
Selection Sort	Ω(n^2)	Θ(n^2)	O(n^2)	
Bubble Sort	Ω(n)	Θ(n^2)	O(n^2)	

GUI Pictures:





Here, I have built a simple GUI using tkinter package which is a Python interface to take the number of inputs, maximum value and minimum value.

First graph indicates values before sorting.

Second graph indicates values after sorting.

Data Size: Here we give the number of inputs.

Min Value: It takes the minimum value of the input data set.

Max Value: It takes the maximum value of the input data set.

Start: Start Button is used to start the sorting algorithm and to sort out.

Generate: Generate Button is used to generate the values between minimum and maximum values of the data set.