

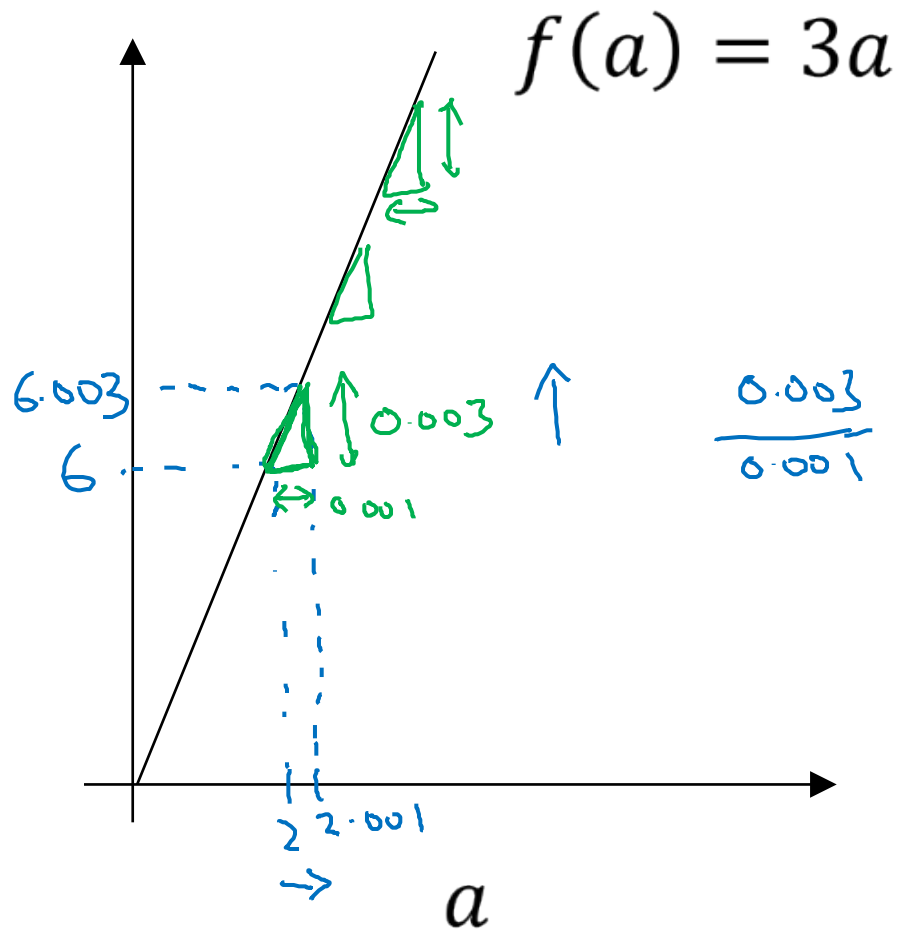


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Basics of Neural Network Programming

Derivatives

Intuition about derivatives



$$\frac{0.003}{0.001} \quad \frac{\text{height}}{\text{width}}$$

$\rightarrow a = 2 \quad f(a) = 6$
 $a = 2.001 \quad f(a) = 6.003$

slope (derivative) of $f(a)$ at $a = 2$ is 3

$\rightarrow a = 5 \quad f(a) = 15$
 $a = 5.001 \quad f(a) = 15.003$
 slope at $a = 5$ is also 3

$\frac{df(a)}{da} = 3 = \frac{d}{da} f(a)$
 $\frac{0.003}{0.001}$

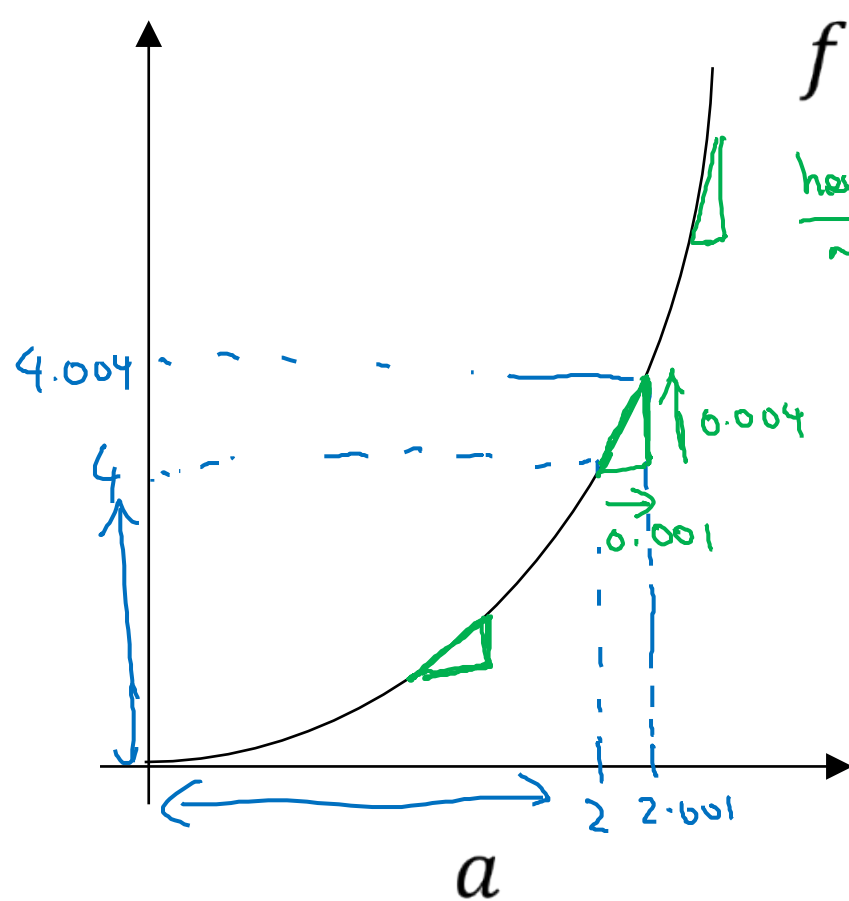


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Basics of Neural Network Programming

More derivatives
examples

Intuition about derivatives



$$f(a) = a^2$$

height
width

$$\frac{d}{da} a^2 = 2a$$

$$0.001$$

$$(2a) \times 0.001$$

0.001 ←
0.000000...01 ←

$a=2$ $f(a)=4$
 $a=2.001$ $f(a) \approx 4.004$
 (4.004004) ←
 slope (derivative) of $f(a)$ at
 $a=2$ is 4.

$$\frac{d}{da} f(a) = 4 \quad \text{when } a=2$$

$a=5$ $f(a)=25$
 $a=5.001$ $f(a) \approx 25.010$
 $\frac{d}{da} f(a) = 10$ when $a=5$

$$\frac{d}{da} f(a) = \frac{d}{da} a^2 = 2a$$

More derivative examples

$$f(a) = a^2$$

$$\frac{d}{da} f(a) = \frac{2a}{4}$$

$$a = 2$$

$$f(a) = 4$$

$$a = 2.001$$

$$f(a) \approx 4.004$$

$$f(a) = a^3$$

$$\frac{d}{da} f(a) = \frac{3a^2}{3 \times 2^2 = 12}$$

$$a = 2$$

$$f(a) = 8$$

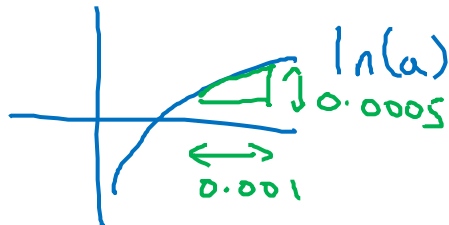
$$a = \underline{2.001}$$

$$f(a) \approx \underline{8.012}$$

$$f(a) = \log_e(a)$$

$$\ln(a)$$

$$\frac{d}{da} f(a) = \frac{1}{a}$$



$$\frac{d}{da} f(a) = \frac{1}{2}$$

$$a = 2$$

$$f(a) \approx 0.69315$$

$$\downarrow$$

$$a = \underline{2.001}$$

$$\downarrow$$

$$\underline{f(a) \approx 0.69365}$$

$$\downarrow$$

$$0.0005$$

$$\swarrow$$

$$\underline{0.0005}$$