Dynamic Programming - 2

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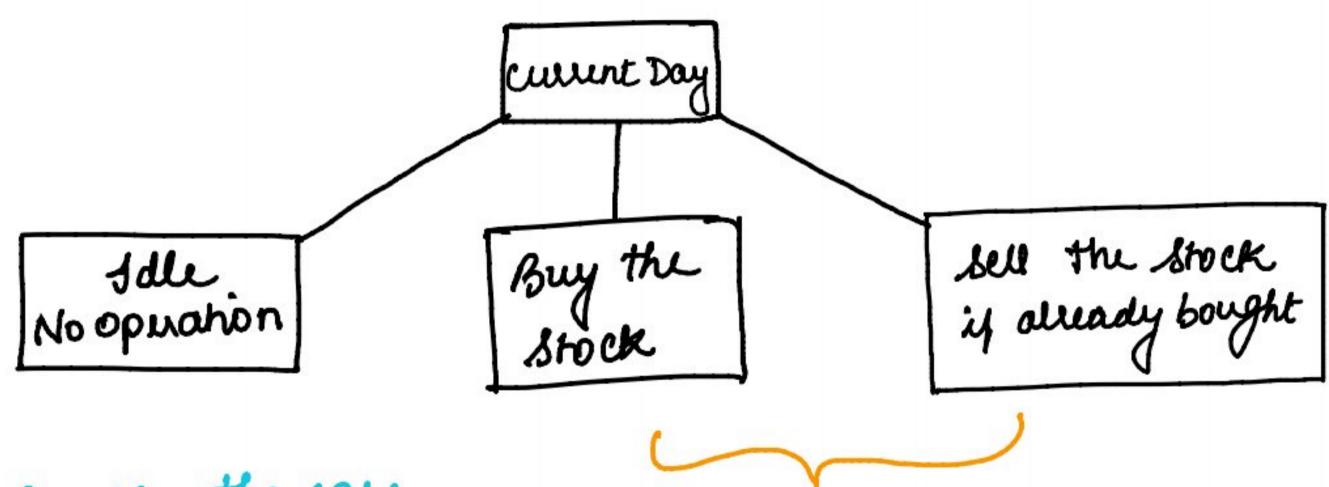
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(6) Best time to Buy & Sell Stock

your an away of prices, spired the max profit if we are allowed to do one transaction

Egg

lets book at choices we have,



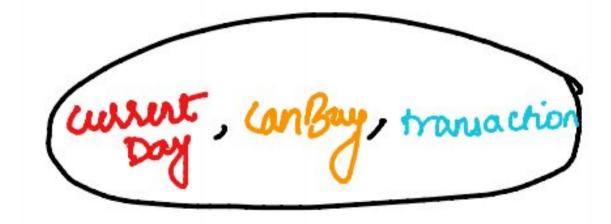
that transaction could occur once, we use a variable called transaction = 1.

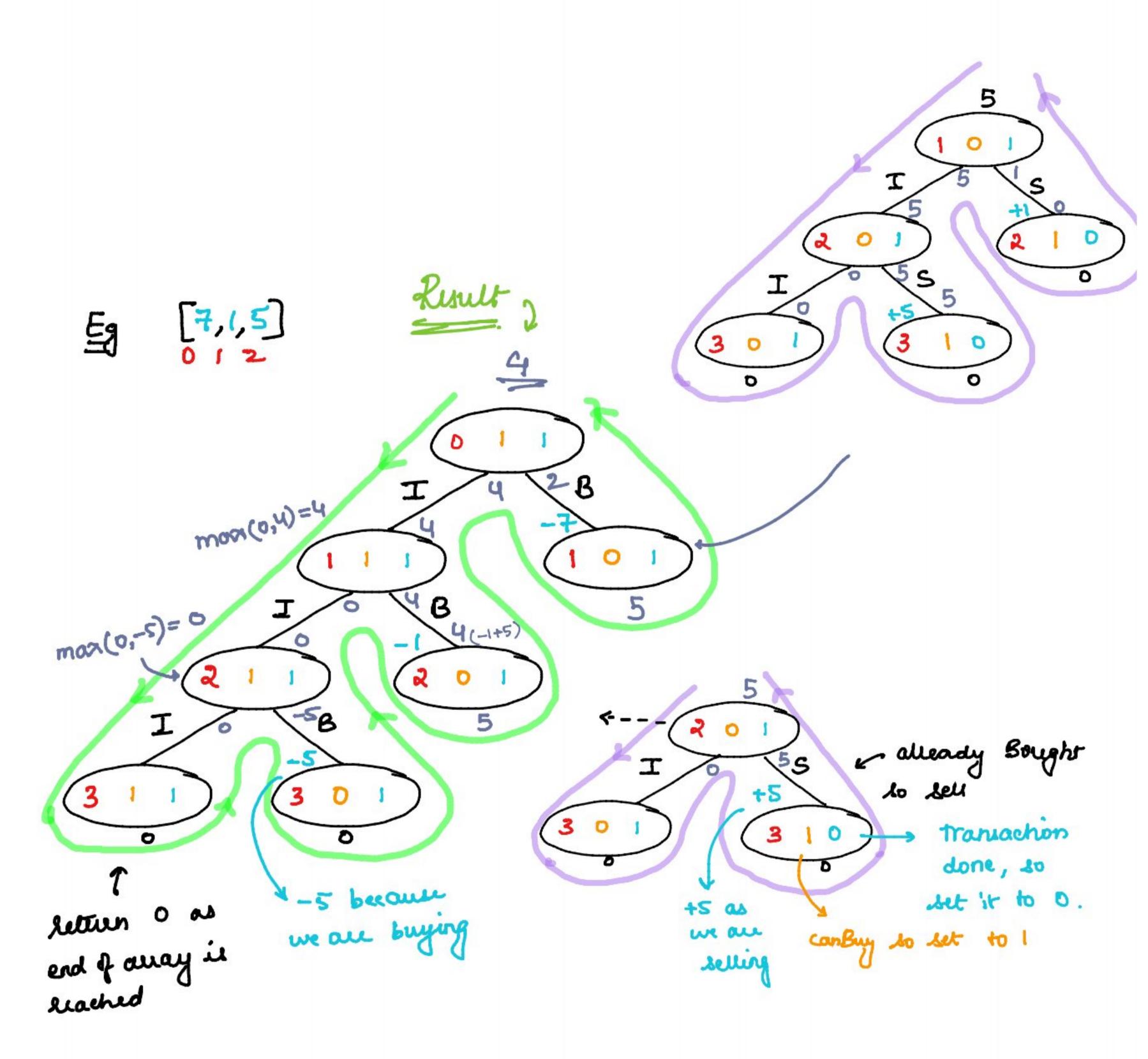
to hardle these cases,
we use a variable called carbing.

-s once bought carring = faller

-s once sold carring = true

. Ou recursive structure would be as follows ->





code_

```
class Solution {
    public:
        int find(vector<int> &prices, int currDay, int k, bool canBuy, vector<vector<int>> &memo){
 4
            if(currDay >= prices.size() || k<=0 ) return 0;</pre>
 5
 6
            if(memo[currDay][canBuy] != -1) return memo[currDay][canBuy];
 8
            if(canBuy)
 9
10
                int idle = find(prices, currDay+1, k, canBuy, memo);
11
                int buy = -prices[currDay] + find(prices, currDay+1, k, !canBuy, memo);
12
13
                return memo[currDay][canBuy] = max(buy, idle);
14
15
            else
16
               int idle = find(prices, currDay+1, k, canBuy, memo);
17
               int sell = prices[currDay] + find(prices, currDay+1, k-1, !canBuy, memo);
18
               return memo[currDay][canBuy] = max(sell, idle);
19
20
21
        int maxProfit(vector<int>& prices) {
22
            int n = prices.size();
23
            vector<vector<int>> memo(n, vector<int> (2,-1));
24
            // canBuy = true and transaction as k = 1
25
            return find(prices,0,1,true,memo);
26
27
28
    };
```

(17) Best time to Buy & Sell Stock - II

In this we can have many transactions that can be done.

Eg., prices = $\begin{bmatrix} \frac{2}{7}, \frac{1}{7}, \frac{5}{5}, \frac{3}{5}, \frac{6}{5}, \frac{4}{3} \end{bmatrix}$

(3) Buy on 1 4 sell on 2 profit = 5-1 = 4

Buy on 3 4 sell on 4 profit = 6-3 = 3

Total Profit = 7 Ans.

wde_

Remove the parameter K is transaction limit.

```
class Solution {
    public:
        int find(vector<int> &prices, int currDay, bool canBuy, vector<vector<int>> &memo){
4
            if(currDay >= prices.size()) return 0;
 5
 6
            if(memo[currDay][canBuy] != -1) return memo[currDay][canBuy];
8
            if(canBuy)
9
10
                int idle = find(prices, currDay+1, canBuy, memo);
11
                int buy = -prices[currDay] + find(prices, currDay+1, !canBuy, memo);
12
                return memo[currDay][canBuy] = max(buy, idle);
13
14
            else
15
16
17
               int idle = find(prices, currDay+1, canBuy, memo);
               int sell = prices[currDay] + find(prices, currDay+1, !canBuy, memo);
18
               return memo[currDay][canBuy] = max(sell, idle);
19
20
21
        int maxProfit(vector<int>& prices) {
22
            int n = prices.size();
23
            vector<vector<int>> memo(n, vector<int> (2,-1));
24
            // canBuy = true and transaction are infinite so ignore k
25
            return find(prices, 0, true, memo);
26
27
28
   };
```

(18) Best time to Buy & Sell Stock - III

In this maximum profit has to be achieved by making atmost 2 transactions.

```
fg prices = [3,3,5,0,0,3,1,4]
```

```
Buy on 6 4 sell on 7 Profir = 3-0=3

Total Profir = 6 Ane
```

code _

In the base condition is no. If transaction 1 = 2then return 0. (3 is possible transactions (2 ine 6)

```
class Solution {
    public:
        int find(vector<int> &prices, int currDay, int transaction, bool canBuy,
        vector<vector<int>>> &memo){
 4
            if(currDay >= prices.size() || transaction>=2) return 0;
            if(memo[currDay][canBuy][transaction] != -1) return memo[currDay][canBuy][transaction];
 8
            if(canBuy)
10
11
                int idle = find(prices, currDay+1, transaction, canBuy, memo);
12
                int buy = -prices[currDay] + find(prices, currDay+1, transaction, !canBuy, memo);
13
                return memo[currDay][canBuy][transaction] = max(buy, idle);
14
15
            else
16
17
               int idle = find(prices, currDay+1, transaction, canBuy, memo);
18
               int sell = prices[currDay] + find(prices, currDay+1, transaction+1, !canBuy, memo);
19
               return memo[currDay][canBuy][transaction] = max(sell, idle);
20
21
22
23
        int maxProfit(vector<int>& prices) {
            int n = prices.size();
24
            vector<vector<vector<int>>> memo(n, vector<vector<int>>(2, vector<int>(2,-1)));
25
            // canBuy = true and transactions are allowed 2 times
26
            return find(prices, 0, 0, true, memo);
27
28
29 };
```

(19) Best time to Buy & Sell Stock - IV

This is a generalised version of previous problem, instead of limiting it to 2 transactions, we need to allow atmost k transactions.

code ->

Pau K as an augument & mu it to limit manuaction in base condition. (Line 6)

```
class Solution {
2 public:
        int find(vector<int> &prices, int currDay, int transaction, int k, bool canBuy,
       vector<vector<int>>> &memo){
            if(currDay >= prices.size() || transaction>=k) return 0;
 6
            if(memo[currDay][canBuy][transaction] != -1) return memo[currDay][canBuy][transaction];
 8
9
            if(canBuy)
10
11
                int idle = find(prices, currDay+1, transaction, k, canBuy, memo);
12
                int buy = -prices[currDay] + find(prices, currDay+1, transaction, k, !canBuy, memo);
13
                return memo[currDay][canBuy][transaction] = max(buy, idle);
14
15
            else
16
17
               int idle = find(prices, currDay+1, transaction, k, canBuy, memo);
18
               int sell = prices[currDay] + find(prices, currDay+1, transaction+1, k, !canBuy, memo);
19
               return memo[currDay][canBuy][transaction] = max(sell, idle);
20
21
22
23
        int maxProfit(int k, vector<int>& prices) {
            int n = prices.size();
24
            vector<vector<vector<int>>> memo(n ,vector<vector<int>>(2,vector<int>(k+1,-1)));
25
            // canBuy = true and transactions are allowed atmost k times
26
27
            return find(prices, 0, 0, k, true, memo);
28
   };
29
```

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(20) Best time to Buy & Sell Stock with Cooldown

In this, cooldown means that we cannot buy a stock on the immediate day after it is sold.

=> The day after sold should be skipped.

code -

To skip day after sell, increment the current Day by 2. (Line 18)

```
class Solution {
 2 public:
        int find(vector<int> &prices, int currDay, bool canBuy, vector<vector<int>> &memo){
 4
            if(currDay >= prices.size()) return 0;
 6
            if(memo[currDay][canBuy] != -1) return memo[currDay][canBuy];
 8
            if(canBuy)
 9
10
                int idle = find(prices, currDay+1, canBuy, memo);
11
                int buy = -prices[currDay] + find(prices, currDay+1, !canBuy, memo);
12
13
                return memo[currDay][canBuy] = max(buy, idle);
14
            else
15
16
               int idle = find(prices, currDay+1, canBuy, memo);
17
               int sell = prices[currDay] + find(prices, currDay+2, !canBuy, memo);
18
               return memo[currDay][canBuy] = max(sell, idle);
19
20
21
22
        int maxProfit(vector<int>& prices) {
            int n = prices.size();
23
            vector<vector<int>> memo(n, vector<int> (2,-1));
24
            // canBuy = true & transaction = infinite so ignore k & while sell, currDay +=2
25
            return find(prices, 0, true, memo);
26
27
28
    };
```

(21) Best time to Buy & Sell Stock with Transaction Fee

In this variation, we do not have limit on transaction but while making a transaction it selling it, some fee has to be paid it transaction fee.

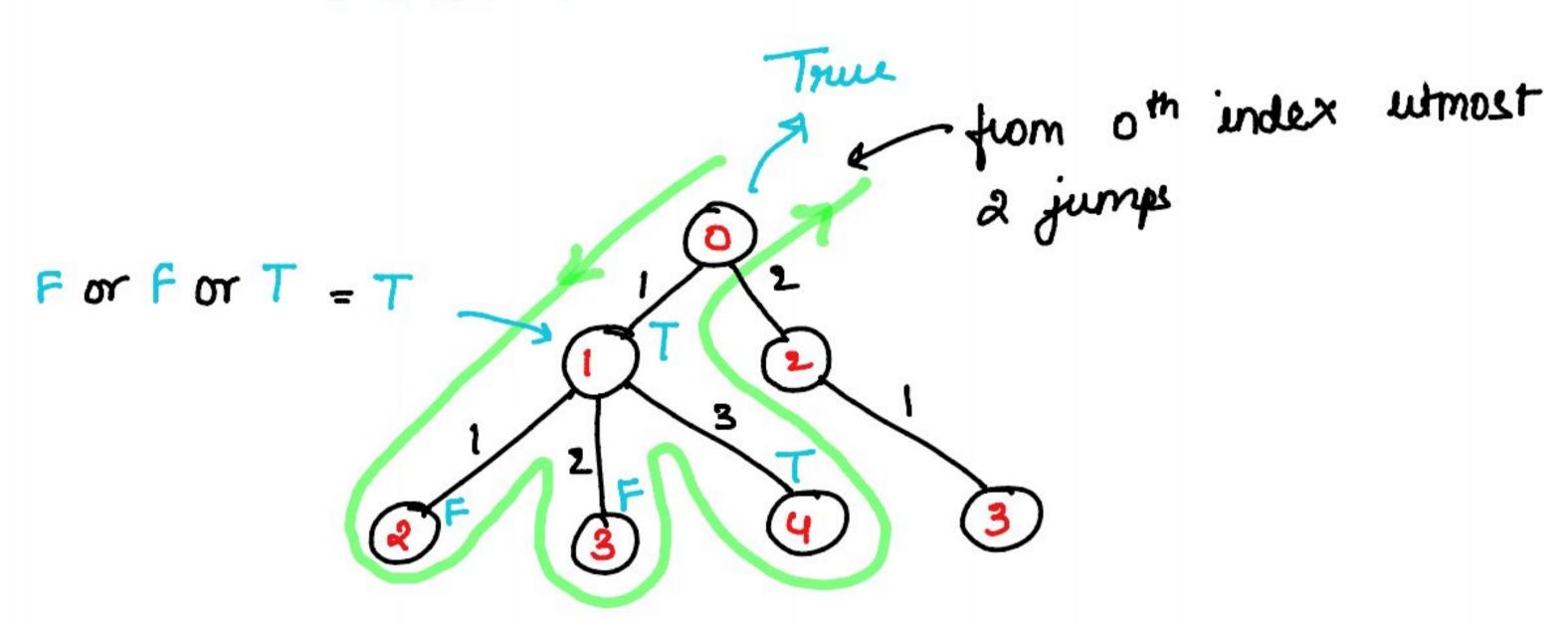
coopr?

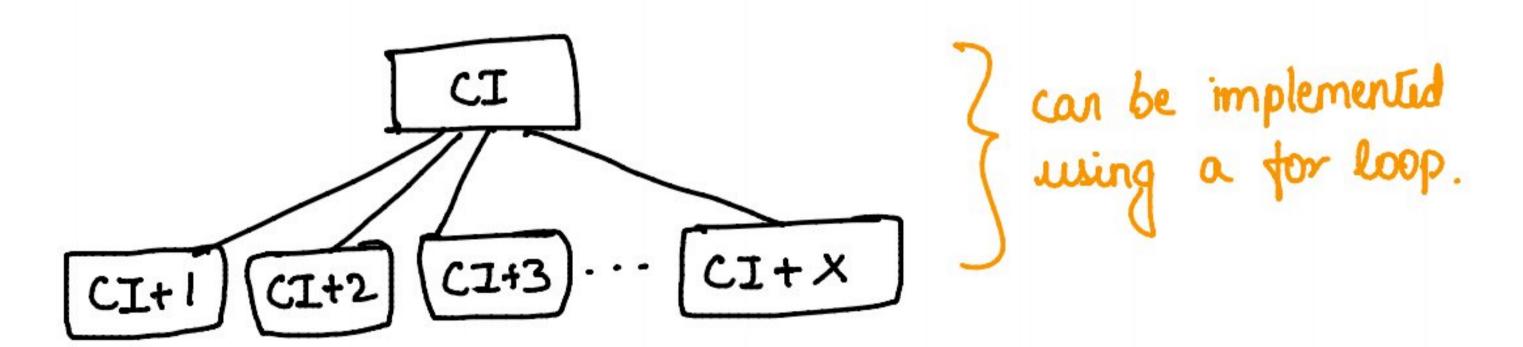
Deduct the fee from the selling day's amount. (Line 18)

```
class Solution {
    public:
        int find(vector<int> &prices, int currDay, int fee, bool canBuy, vector<vector<int>> &memo){
            if(currDay >= prices.size()) return 0;
 6
            if(memo[currDay][canBuy] != -1) return memo[currDay][canBuy];
 7
 8
            if(canBuy)
 9
10
                int idle = find(prices, currDay+1, fee, canBuy, memo);
11
                int buy = -prices[currDay] + find(prices, currDay+1, fee, !canBuy, memo);
12
                return memo[currDay][canBuy] = max(buy, idle);
13
14
15
            else
16
17
               int idle = find(prices, currDay+1, fee, canBuy, memo);
               int sell = (prices[currDay]-fee) + find(prices, currDay+1, fee, !canBuy, memo);
18
               return memo[currDay][canBuy] = max(sell, idle);
19
20
        }
21
22
        int maxProfit(vector<int>& prices, int fee) {
23
            int n = prices.size();
24
            vector<vector<int>> memo(n, vector<int> (2,-1));
25
            // canBuy = true & transaction = infinite so ignore k & while selling deduce fee
26
            return find(prices, 0, fee, true, memo);
27
28
        }
29
    };
```

(22) Jump Grane

given away of nume which indicate more number of jump from any index. Return true if you can reach Last index.





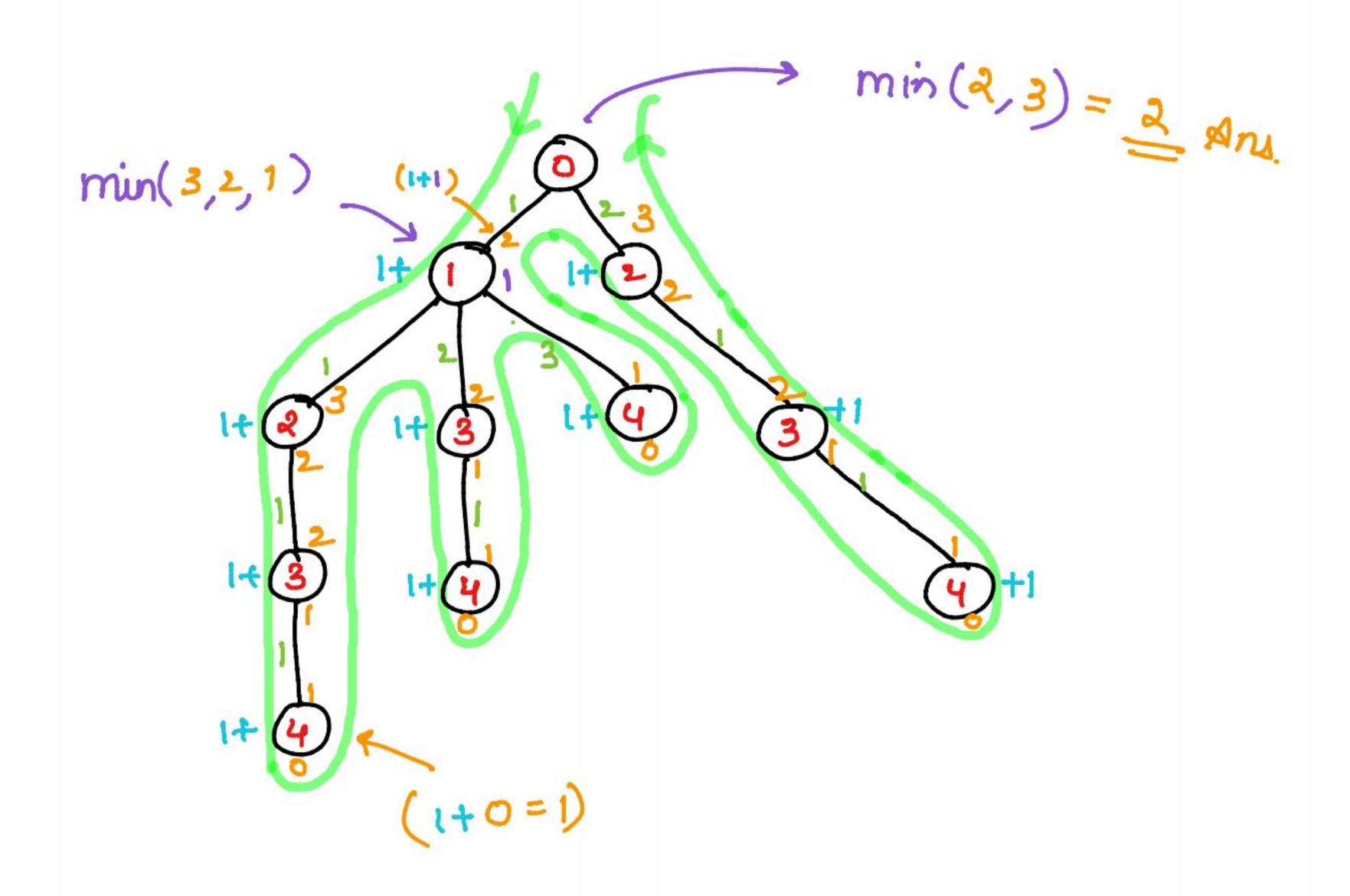
Note: submitting DP solution gives TLE. This is just for undustanding Optimal solution involves Greedy approach.

Tc -> O(max (numi[i]) * n) max time for for loop.

code

```
class Solution {
    public:
        bool isPossible(vector<int>&nums, int curr, unordered_map<int,bool>&memo)
 4
            if(curr >= nums.size()-1) return true;
 6
            int currKey = curr;
8
            if(memo.find(currKey)!=memo.end()) return memo[currKey];
9
10
            int currJump = nums[curr];
11
12
            if(currJump >= nums.size() - curr) return true;
13
14
15
            bool ans = false;
16
            for(int i=1; i<=currJump; i++){</pre>
17
                 bool tempAns = isPossible(nums,curr+i,memo);
18
                 ans = ans || tempAns;
19
20
            return memo[currKey] = ans;
21
22
23
24
        bool canJump(vector<int>& nums){
            unordered_map<int,bool>memo;
25
            return isPossible(nums, 0, memo);
26
27
28
    };
```

given away of nume which indicate max number of jump from any index. Reach last index in minimum number of moves.



-> if current Index >= Last Index then return 0.

while returning add I for counting ways!

Code

```
class Solution {
    public:
        int minJumps(vector<int>& nums,int curr,vector<int>&memo)
        {
            if( curr >= nums.size()-1) return 0;
 6
            int currKey = curr;
 8
            if(memo[currKey]!=-1) return memo[currKey];
10
            int currJump = nums[curr];
11
12
            // some large value
13
            int ans = 10001;
14
15
            for(int i=1;i<=currJump;i++){</pre>
16
                 int tempans = 1 + minJumps(nums,curr+i,memo);
17
                 ans = min(ans, tempans);
18
19
            return memo[currKey] = ans;
20
21
22
23
        int jump(vector<int>& nums) {
            vector<int> memo(nums.size()+1,-1);
24
            return minJumps(nums, 0, memo);
25
26
27
   };
```

(24) Reach a given ascotte ->

given 3 scores [3,5,10] & 'n'.
Return total number of ways to create n using the scores.

Eg n=8 then no. of ways to create 8 from [3, 5, 10] is 1. (3+5)

n = 13 thun no. If ways to create 13 from [3, 5, 10] is a (3+5+5) & (3+10)

n=20 thun no. of ways to create 20 from [3, 5, 10] is 4 (3+3+3+3+3+5) & (5+5+5+5) & (5+5+10) & (10+10)

Let say
$$A = [3,5,10]$$
 thun

 $CI, n = A[CI]$
 CI, n
 $CI, n = A[CI]$

code_

```
typedef long long LL;
 2
    LL ways(int curr, LL n, vector<int>&score, vector<vector<int>>&vec)
 3
 4
 5
        if(n==0) return 1;
 6
        if(curr>=score.size()) return 0;
 8
        if(vec[curr][n]!=-1) return vec[curr][n];
 9
10
        LL consider = 0;
11
12
13
        if(score[curr]<=n)</pre>
          consider = ways(curr,n-score[curr],score,vec);
14
15
        LL notconsider = ways(curr+1,n,score,vec);
16
17
        return vec[curr][n] = consider + notconsider;
18
19
20
    LL count(LL n)
21
22
        vector<int>score{3,5,10};
23
        vector<vector<int>>vec(score.size(),vector<int>(1001,-1));
24
        return ways(0,n,score,vec);
25
26
```

Catalan Numbers are defined using the formula

$$C_n = \frac{(2n)!}{(n+1)! \, n!} = \pi^n \frac{n+k}{k} \quad \text{for } n \ge 0$$

this can be used succusively as follows,

$$C_{n+1} = \sum_{i=0}^{n} C_{i} C_{i-1}$$
 $\begin{cases} n \geq 0 \\ i = 0 \end{cases}$ $\begin{cases} n \geq 0 \end{cases}$ $\begin{cases} n \geq 0 \end{cases}$ $\begin{cases} n \geq 0 \end{cases}$

$$\rightarrow C_1 = 1$$

$$\rightarrow C_2 = C_0.C_1 + C_1.C_0 = 1.1+1.1 = 2$$

$$- > C_4 = C_0C_3 + C_1C_2 + C_2C_1 + C_3C_0$$

$$= 1.5 + 1.2 + 2.1 + 5.1 = 14$$

dpp ns

- 1. No. of possible BST with n Kys.
- 2. No. of vouid combinations for N pair of pounthuis.

To trind Nth caralan Number we can use tormula

$$C_{n+1} = \sum_{i=0}^{n} C_{i} C_{i-1}$$
 $\begin{cases} n \geq 0 \\ i = 0 \end{cases}$ $\begin{cases} n \geq 0 \end{cases}$ $\begin{cases} n \geq 0 \end{cases}$ $\begin{cases} n \geq 0 \end{cases}$

Is this can be implemented by

- i) having bour condition for n==04 p==1
- ii) using a loop to sum values from i=0 to h

Code >

```
class Solution
 2
        public:
 3
        cpp_int ncatalan(int n, vector<cpp_int>& memo) {
 4
            if(n == 0 || n == 1) return 1;
 5
 6
            int curr = n;
            if(memo[curr]!=-1) return memo[curr];
 8
 9
            cpp_int catalan = 0;
10
11
            for(int i=0;i<n;i++) {
12
                 catalan += ncatalan(i, memo)*ncatalan(n-i-1, memo);
13
14
15
            memo[curr] = catalan;
16
            return memo[curr];
17
18
19
        cpp_int findCatalan(int n)
20
21
            vector<cpp_int> memo(1001,-1);
22
            return ncatalan(n, memo);
23
24
25
    };
```

Number of valid Paunthesis Expression given N, find total number of ways in which we can awange N pair of parenthesis in a Balanced way. N=4 => ()()(), ()(()), (())(), ((())) :. Ms=4 ((())) (0)()()(())(nothing is outside identical & (both explusions : Co & 2 types in :- C2 one expression inside C, outside :. C2 & one outside C & nothing inside: Co => Co.C2 => C1.C1

=> 60.62 + 61.61 + 62.60 = 63 => for n we need to find neartalan (n/2)

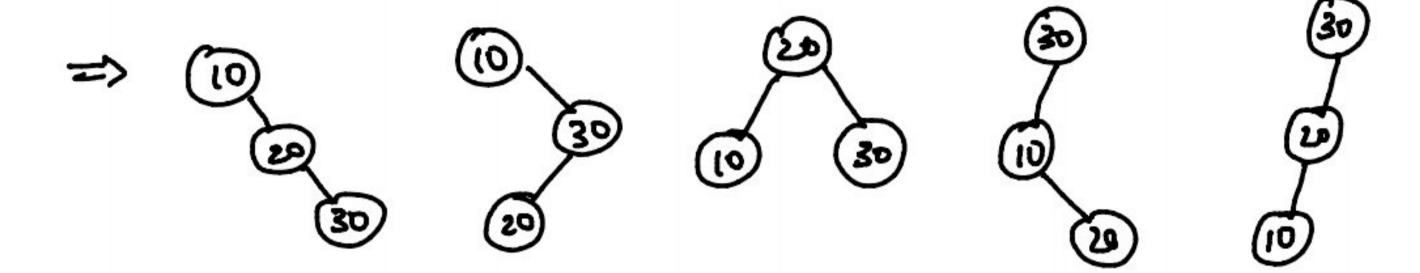
code.

```
#include<bits/stdc++.h>
    using namespace std;
    int ncatalan(int n, unordered_map<int,int>& memo) {
        if(n == 0 || n == 1) return 1;
        int curr = n;
        if(memo[curr]!=-1) return memo[curr];
        int catalan = 0;
10
11
        for(int i=0;i<n;i++) {
12
            catalan += ncatalan(i, memo)*ncatalan(n-i-1, memo);
13
14
15
16
        memo[curr] = catalan;
        return memo[curr];
17
18 }
19
    int countValidParenthesis(int n)
21
        unordered_map<int,int> memo;
22
        return ncatalan(n/2, memo);
23
24
25
    int main(){
        int n;
27
        cin>>n;
28
        cout<<countValidParenthesis(n);</pre>
29
30 }
```

(28) Urique Binary Search Trees -

your intéger N, retuer no. if unique BST that can be formed.

Eg n=3 & ws say elements are [10,20,30]



:. For n=3, the result is 5

:. The catalan number gives us the result.

code__

```
class Solution {
    public:
        int uniqueBST(int n, vector<int>& memo)
 4
        {
             if(n==0||n==1) return 1;
 6
             if( memo[n]!=-1)return memo[n];
 8
 9
             int ans = 0;
10
             for(int i=0;i<n;i++)</pre>
11
                 ans += uniqueBST(i,memo)*uniqueBST(n-i-1,memo);
12
13
14
             return memo[n] = ans;
15
16
        int numTrees(int n) {
17
18
             vector<int> memo(n+1,-1);
             return uniqueBST(n, memo);
19
20
    };
21
```