

Bellman Ford Algorithm Tracing.

main()

num_ver source A[][] Max_value = 999

Enter number of vertices

num_ver

Enter the adjacency matrix

A[sn][dn] => A[5][5]

A[1][1] = 0

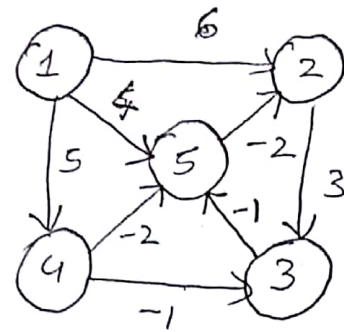
A[1][2] = 6

A[1][3] = 0

A[1][4] = 5

A[1][5] = 4

// indexing starts from 1



A[2][1] = 0

A[3][1] = 0

A[4][1] = 0

A[5][1] = 0

A[2][2] = 0

A[3][2] = 0

A[4][2] = 0

A[5][2] = -2

A[2][3] = 3

A[3][3] = 0

A[4][3] = -1

A[5][3] = 0

A[2][4] = 0

A[3][4] = 0

A[4][4] = 0

A[5][4] = 0

A[2][5] = 0

A[3][5] = -1

A[4][5] = -2

A[5][5] = 0

if A[sn][dn] == 0

then A[sn][dn] = Max_value // 999

All values of adjacency matrix are filled with 999 where.

A[sn][dn] = 0, other than condition where sn == dn,

if sn == dn

then A[sn][dn] = 0

A[sn][dn]	1	2	3	4	5
1	0	6	999	5	4
2	999	0	3	999	999
3	999	999	0	999	-1
4	999	999	-1	0	-2
5	999	-2	999	999	0

Enter source vertex:

source = 1

BellmanFord(S) // calls construction

{
 D[1] = 5 + 1 = 6 // D[6]
}

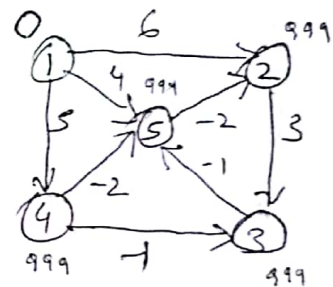
BellmanFordEvaluation(1, A[E][E]) // Function to evaluate

D[source] = 0; // D[1] = 0

Rest all nodes = ~~max~~ value \rightarrow 999

D[6]

0	1	2	3	4	5
0	999	999	999	999	999



If $D[dn] > D[sn] + \text{weight of edge } uv$

then $D[dn] = D[sn] + \text{weight of edge } uv$

This is executed when $A[sn][dn] \neq 999$ // Edge exist

node 1
I $A[1][1] \Rightarrow 0 \neq 999 \checkmark$

$D[1] > D[1] + A[1][1]$

$0 > 0 + 0$ F

$D[1] = 0$

$A[1][2] \Rightarrow 6 \neq 999 \checkmark$

$D[2] > D[1] + A[1][2]$

$999 > 0 + 6$ T

$D[2] = 6$

$A[1][3] \Rightarrow 999 \neq 999 \times$

$D[3] = 999$

$A[1][4] \Rightarrow 5 \neq 999 \checkmark$

$D[4] > D[1] + A[1][4]$

$999 > 0 + 5$ T

$D[4] = 5$

$A[1][5] \Rightarrow 4 \neq 999 \checkmark$

$D[5] > D[1] + A[1][5]$

$999 > 4$ T

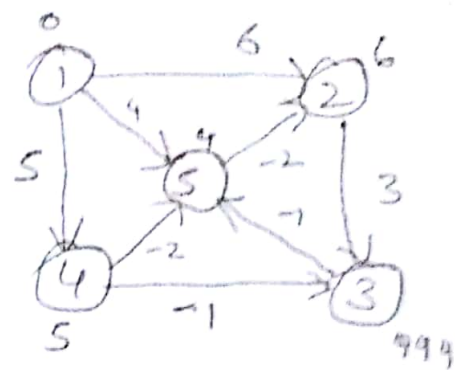
$D[5] = 4$

D[6]

0	1	2	3	4	5
0	6	999	5	4	

~~IV $\Delta[2][1] = 999 = 999$ F~~
 ~~$\Delta[2][2] = 0 = 999$ T~~

Present Graph \rightarrow



II $\Delta[2][1] = 999 = 999$ F

$\Delta[2][2] = 0 = 999$ T

$D[2] > D[2] + \Delta[2][2]$

$6 > 6 + 0$

$\Delta[2][3] = 3 = 999$ T

$D[3] > D[2] + \Delta[2][3]$

$999 > 6 + 3$ T

$\Delta[2][4] = 999 = 999$ F

$\Delta[2][5] = 999 = 999$ F

$D[6]$

0	1	2	3	4	5
0	6	9	5	4	

$D[1] = 0$

$D[2] = 6$

$D[3] = 9$

$D[4] = 5$

$D[5] = 4$

III $\Delta[3][1] = 999 = 999$ F

$\Delta[3][2] = 999 = 999$ F

$\Delta[3][3] = 0 = 999$ T

$D[3] > D[3] + \Delta[3][3]$

$9 > 9 + 0$

$D[3] = 9$

$\Delta[3][4] = 999 = 999$ F

$D[4] = 5$

$\Delta[3][5] = -1 = 999$ T

$D[5] > D[3] + \Delta[3][5]$

$4 > 9 - 1$ F

$D[5] = 4$

IV $\Delta[4][1] = 999 = 999$ F

$\Delta[4][2] = 999 = 999$ F

$\Delta[4][3] = -1 = 999$ T

$D[3] > D[4] + \Delta[4][3]$

$9 > 5 - 1$

$D[3] = 4$

$\Delta[4][4] = 0 = 999$ T

$D[4] > D[4] + \Delta[4][4]$

$D[4] = 5$

$$DE[4][5] \quad -21 = 999 \quad T$$

$$DE[5] > DE[4] + A[4][5]$$

$$4 > 5 - 2$$

$$DE[5] = 2$$

$$DE[6] \quad \begin{array}{|c|c|c|c|c|c|} \hline 0 & 1 & 2 & 3 & 4 & 5 \\ \hline 0 & 6 & 4 & 5 & 3 & \end{array}$$

$$V \quad A[5][1] \quad 9991 = 999 \quad F$$

$$DE[1] = 0$$

$$A[5][2] \quad -21 = 999 \quad T$$

$$DE[2] > DE[5] + A[5][2]$$

$$6 > 3 - 2$$

$$DE[2] = 1$$

$$A[5][3] \quad 9991 = 999$$

$$DE[3] = 4$$

$$A[5][4] \quad 9991 = 999$$

$$DE[4] = 5$$

$$A[5][5] \quad 01 = 999$$

$$DE[5] > DE[5] + A[5][5]$$

$$3 > 3 + 0$$

$$DE[5] = 3$$

$$DE[6]$$

$$\begin{array}{|c|c|c|c|c|} \hline 1 & 2 & 3 & 4 & 5 \\ \hline 0 & -1 & 4 & 5 & 3 \\ \hline \end{array}$$

$$mode = 2$$

$$I \quad A[1][1] \quad 01 = 999 \quad \checkmark$$

$$DE[1] > DE[1] + A[1][1]$$

$$DE[1] = 0$$

$$A[1][2] \quad 61 = 999$$

$$DE[2] > DE[1] + A[1][2]$$

$$1 > 0 + 6$$

$$DE[2] = 1$$

$$A[1][3] \quad 9991 = 999 \quad \times$$

$$DE[3] = 4$$

$$A[1][4] \quad 51 = 999 \quad \checkmark$$

$$DE[4] > DE[1] + A[1][4]$$

$$5 > 0 + 5$$

$$DE[4] = 5$$

$$A[1][5] \quad 41 = 999$$

$$DE[5] > DE[1] + A[1][5]$$

$$3 > 0 + 4 \quad F$$

$$DE[5] = 3$$

$$DE[6]$$

$$\begin{array}{|c|c|c|c|c|} \hline 1 & 2 & 3 & 4 & 5 \\ \hline 0 & 1 & 4 & 5 & 3 \\ \hline \end{array}$$

In similar way in $\Delta[2][1 \dots 5]$

$$D[6] = \begin{array}{|c|c|c|c|c|} \hline 1 & 2 & 3 & 4 & 5 \\ \hline 0 & 1 & 4 & 5 & 3 \\ \hline \end{array}$$

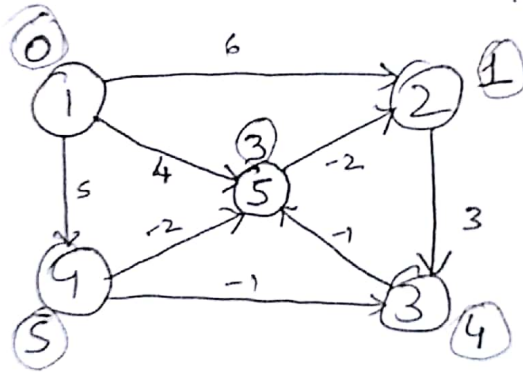
For $\Delta[3][1 \dots 5]$

$\Delta[4][1 \dots 5]$

$\Delta[5][1 \dots 5]$

$$D[6] = \begin{array}{|c|c|c|c|c|} \hline 1 & 2 & 3 & 4 & 5 \\ \hline 0 & 1 & 4 & 5 & 3 \\ \hline \end{array}$$

node = 3, 4

$$D[6] = \begin{array}{|c|c|c|c|c|} \hline 1 & 2 & 3 & 4 & 5 \\ \hline 0 & 1 & 4 & 5 & 3 \\ \hline \end{array}$$


distance of source 1 to 1 is $D[1] = 0$

distance of source 1 to 2 is $D[2] = 1$

distance of source 1 to 3 is $D[3] = 4$

distance of source 1 to 4 is $D[4] = 5$

distance of source 1 to 5 is $D[5] = 3$