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Assignment # 2 - Part 1 & 2
Comp 352- Section X
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Written Questions (50 marks):

Question 1

Consider the following scenario: you have a machine hall containing three pegs named A, B, and C. Each peg can hold many discs, but a disc with a larger diameter can never be placed on top of a disc with a smaller diameter and all discs have different diameters. If there are n discs, then the discs are numbered from 1 to n , where 1 is the smallest disc and n is the largest disk. There exists a robot arm that can move exactly one disc at a time from peg A to B or B to A, or from B to C or C to B. The robot arm cannot do any other move. Initially, all n discs are on peg A stacked by increasing diameters from top to bottom, with the bottommost one of the largest diameter. The goal is to move all discs from peg A to C by using only the robot arm based on the rules and restrictions described above. You are

required to submit the following deliverables:

Algorithm: TowerOfHanoi

Input: Number of disks

Output: The possible movements from A,B, and C

```
TowerOfHanoi(N, Src, Aux, Dst)
if N is 0
    exit
else
    TowerOfHanoi (N-1, source, Aux, Dst) // moves (N-1) small disks from source to Dst
    Move from source to Aux              // moves the largest disk from source to Aux
    TowerOfHanoi (N-1, Dst, Aux, source) // moves (N-1) small disks from Dst to source
    Move from Aux to Dst                 // moves the largest disk from Aux to Dst
    TowerOfHanoi (N-1, source, Aux, Dst) // moves (N-1) small disks from source to Dst
End if
```

B) A hand-run of your algorithm for $n = 4$.

If $n=4$, then then we could equal the formula to $T(4) = 2T(3)+1= 15$,
Hence the Tower of Hanoi code would move the disks 15 times.

C) Formulation and calculation of its complexity using the big-Oh notation. Justify your answers.

We Know that when $n=1$, the code would move the 1 disk directly. Which means $T(1)=1$ // which is the number of disks

In the other cases, the code would follow this procedure.

1. First they would move the $(n-1)$ - disk tower to the spare peg; This takes $T(n-1)$ moves.
2. So, the code would move the n th disk taking 1 move.
3. Finally, they would move the $(n-1)$ - disk again, this time on top of the disk. Meaning it would take $T(n-1)$ moves.

Hence the recurrence formula would be $T(n) = 2(T(n-1)+1)$

With all that said the Big O $\rightarrow O(2^n)$

Question # 2

A) In class, we discussed a recursive algorithm for generating the power set of a set T , i.e., the set of all possible subsets of T . In this assignment, you will develop a well-documented pseudocode that generates all possible subsets of a given set of size n with the following requirements: your solution must be non-recursive, and must use a stack and a queue to solve the problem. For example: if set $T = \{2, 4, 7, 9\}$ then your algorithm would generate: $\{\}, \{2\}, \{4\}, \{7\}, \{9\}, \{2,4\}, \{2,7\}, \{2,9\}, \{4,7\}, \{4,9\}, \{7,9\}, \dots$ etc. (Note: your algorithm's output need not be in this order).

Algorithm: AllPossibleSubsets(T)

Input: A set of T with n elements

Output: All subsets of T stored in a Queue

```
{
  Create an empty queue Q;
  Create an empty stack S;
  Let  $a_1, a_2, \dots$  be all the elements in the subset of  $T$ 
  s.push({}); // push the empty subset into the stack
  s.push ({ $a_1$ })
  for (each element  $a_i$  in  $T - \{a_1\}$ )
    {while (S is not empty)
      { x=s.pop;
        Q.enqueue(x);
         $x = x \cup \{a_i\}$ ;
        Q.enqueue(x);
      }
    if ( $a_i$  is not the last element)
      while (Q is not empty)
```

```

        { x=Q.dequeue();
          S.push();
        }
    } }

```

b) Calculate the time complexity of your algorithm using the big-Oh notation. Show all calculations.

For each element in a_i in T , takes out everything in S , put it back into S twice; once with a_i and once without a_i . So, the total time complexity is $(1+2+4+\dots+2^n)$ times C . And C stands for the time to pop, enqueue, dequeue, and push which, they all are usually (1). Hence, when we add then together the $T(n) = 2^{(n+1)} - 1$. Which would mean that $O(2^n)$ is the o complexity.

Question # 3

Rank the following functions in non-decreasing order (\leq) based on their tight big-Oh complexities and justify your ranking:

$$\log \log n < \binom{n}{2} < n \log n < n/2 < 2^{\log n} < n^{1/2} < n^3 + \log n < n! < 2^n \leq 2^{2^n} < 2^n < n^n < 2^{n!}$$

Written Questions (50 marks):

A) Design and submit the pseudo-code for both the versions of arithmetic calculator.

Algorithm: Calculator Stacks

Input: Expression that needs to resolved Output

Output: The answer of the expression

```

-----
public class StackCalculator
{
    public static void main(String[] args)
    {
        Scanner scan = new Scanner(System.in);
        Stack<Integer> op = new Stack<Integer>(); // Create stack arrays
        Stack<Double> op1 = new Stack<Double>()
        Stack<Integer> optmp = new Stack<Integer>(); // create temporary stacks arrays for the operators
                                                    and operands

        Stack<Double> op1tmp = new Stack<Double>();
        print "Enter expression" // Ask the user to enter the expression to be solved
        String input = scan.next();
        input = "0" + input;
        input = input.replaceAll("-", "+-");
        String temp = "";
        for <int i = 0 to i < input.length()> //Store operands and operators in respective stacks
        {
            char ch = input.charAt(i);
            if (ch == '-')

```

```

        temp = "-" + temp;
    else if (ch != '+' && ch != '*' && ch != '/' && ch != '^' && ch != '!' && ch != '>' && ch != '<' &&
            ch != '=' && ch != '!')
        temp = temp + ch;
    else
    {op1.push(Double.parseDouble(temp));
     op.push((int)ch);
     temp = "";}
    }
}
op1.push(Double.parseDouble(temp));
char operators[] = {'/', '*', '+', '^', '!', '>', '>=', '<=', '<', '==', '!='}; // Create char array of operators as per
                                                                                   precedence

for < int i = 0 to i < 3;>
{
    boolean it = false;
    while (!op.isEmpty())
    {
        int optr = op.pop();
        double v1 = op1.pop();
        double v2 = op1.pop();
        double result = Math.pow(v1,v2);

        if <optr equals operators[i]>
        {
            // if operator matches evaluate and store in temporary stack
            if <i equal 0>
            {
                op1tmp.push(v2 / v1);
                it = true;
                break;
            }
            else if <i equal 1>
            {
                op1tmp.push(v2 * v1);
                it = true;
                break;
            }
            else if <i equal 2>
            {
                op1tmp.push(v2 + v1);
                it = true;
                break;
            }
            else if <i equal 3 >
            {
                op1tmp.push(Math.pow(v2,v1));
                it= true;
                break;
            }
            else if <i equal 4 >
            {
                op1tmp.push (v2 ! v1);
                it = true;
                break;
            }
        }
    }
}

```

```

    }
    else if < i equal 5 >
    {
        op1tmp.push(v2 > v1);
        it = true;
        break;
    }
    else if < i equal 6 >
    {
        op1tmp.push(v2 <= v1);
        it = true;
        break;
    }
    else if < I equal 7>
    {
        op1tmp.push(v2 ==> v1);
        it = true;
        break;
    }
    else if < I equal 8 >
    {
        op1tmp.push(v2 < v1);
        it = true;
        break;
    }
    else if <i equal 9 >
    {
        op1tmp.push(v2 == v1);
        it = true;
        break;
    }
    else if < i equal 10 >
    {
        op1tmp.push(v2 != v1);
        it = true;
        break;
    }
    else
    {
        op1tmp.push(v1);
        op1.push(v2);
        optmp.push(optr);
    }
} // Push back all elements from temporary stacks to main stacks
while (!op1tmp.isEmpty())
    op1.push(op1tmp.pop());

while (!optmp.isEmpty())
    op.push(optmp.pop());
if (it)
    i--;
}
print (" Result = "+op1.pop())
}
End If

```

Algorithm: Recursive Calculator

Input: Expression that needs to be resolved

Output: The answer of the expression

```
DIVIDERS = new ArrayList<Character>
(Arrays.asList('*', '/', '-', '+', '=', '!=', '<=', '>=', '>', '<'));
RIGHT_DIRECTION=1;
LEFT_DIRECTION=-1;
Algorithm main
reader = new BufferedReader(new InputStreamReader(System.in));
expression = "";
// Prompt user to enter expression try expression and catch exceptions
Print ("Expression: " + expression);
expression = prepareExpression(expression);
Print ("Answer: " + calc(expression));
Algorithm calc(expression)
numbers=0;
If numbers which is index of "" is not equals to 1 {
subexp= extractExpressionFromBraces(expression, numbers);
replace ("+"subexp+") in expression by calc(subexp)
return calc(expression);
}
Else If the index of * or / in expression is greater than zero {
multPos = the index of * in expression
divPos = the index of / in expression
numbers= Math.min(multPos, divPos);
If multPos is less than 0 then numbers equals divPos
Else If divPos is less than 0 then numbers equals multPos
divider = to the char at index numbers of expression
leftNum = extractNumber(expression, numbers, LEFT_DIRECTION);
rightNum = extractNumber(expression, numbers, RIGHT_DIRECTION);
expression = expression.replace(leftNum + divider + rightNum, calcShortExpr(leftNum, rightNum, divider));
return calc(expression);
} Else if index of + or - in expression is greater than 0 {
summPos = the index of + in expression
minusPos = index of - in expression
numbers = Math.min(summPos, minusPos);
If summPos is less than 0 then numbers equals minusPos
Else If minusPos is less than 0 then numbers equals summPos
divider = char at index number of expression
leftNum = extractNumber(expression, numbers, LEFT_DIRECTION);
rightNum = extractNumber(expression, numbers, RIGHT_DIRECTION);
expression = expression.replace(leftNum + divider + rightNum, calcShortExpr(leftNum, rightNum, divider));
return calc(expression);
} Else If
Algorithm extractExpressionFromBraces(String expression, int pos)
braceDepth = 1;
subexp="";
For < i = pos+1 to i < expression.length() > do {
switch case is char at index i of expression {
case '(':
braceDepth++;
subexp += "(";
```

```

break;
case ')':
braceDepth--;
If braceDepth is not equals to 0 then subexp += ")";
break;
default:
If braceDepth is less than 0 then subexp += expression.charAt(i);
}
If braceDepth equals 0 and subexp is not equal to "" then return subexp
} return "Failure!";
Algorithm extractNumber(String expression, int pos, int direction)
resultNumber = "";
currPos = pos + direction;
If char at index currPos of expression equals to - {
resultNumber+=expression.charAt(currPos);
currPos+=direction;
}
For currPos >= 0 && currPos < expression.length() && !DIVIDERS.contains(expression.charAt(currPos)) to
currPos += direction do {
resultNumber += expression.charAt(currPos);
}
If direction equals to LEFT_DIRECTION then resultNumber = new
StringBuilder(resultNumber).reverse().toString();
return resultNumber;
Algorithm calcShortExpr(String leftNum, String rightNum, char divider)
switch case is divider {
case '*':
return Double.toString(Double.parseDouble(leftNum) * Double.parseDouble(rightNum));
case '/':
return Double.toString(Double.parseDouble(leftNum) / Double.parseDouble(rightNum));
case '+':
return Double.toString(Double.parseDouble(leftNum) + Double.parseDouble(rightNum));
case '-':
return Double.toString(Double.parseDouble(leftNum) - Double.parseDouble(rightNum));
case '==':
return Double.toString(Double.parseDouble(leftNum) == Double.parseDouble(rightNum));
case '!=':
return Double.toString(Double.parseDouble(leftNum) != Double.parseDouble(rightNum));
case '<=':
return Double.toString(Double.parseDouble(leftNum) <= Double.parseDouble(rightNum));
case '>=':
return Double.toString(Double.parseDouble(leftNum) >=Double.parseDouble(rightNum));
case '>':
return Double.toString(Double.parseDouble(leftNum) > Double.parseDouble(rightNum));
case '<':
return Double.toString(Double.parseDouble(leftNum) < Double.parseDouble(rightNum));
default: return "0";
}
Algorithm prepareExpression(String expression)
return expression;
} End IF

```

B) Implement a Java program for the first version. In your program, you will implement and use your own array-based stack (and not the built-in Java stack) of variable size based on the doubling strategy discussed in class (refer to the code segments provided on your slides and the textbook).

SUBMITTED IN A ECLIPSE FOLDER.

C) Briefly explain the time and memory complexity of both versions of your calculator. You can write your answer in a separate file and submit it together with the other submissions.

Recursion uses your thread stack and that has a much lower limit. The recursive algorithm will add overhead since they store recursive stacks, with that said the big-O complexity for the **recursive calculator is $O(n)$** . However, the calculator that uses stack to calculate the expression takes less time. with that said the **stack calculator has a big-o complexity of $O(n \log n)$** .