Collinearity of points

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Question

For what value of P are the points (2,1),(P,-1), and (-1,3) collinear? (10, 2019)

Variable name	Description	Formula
Α	The point in 2-D plane with coordinates	$\begin{pmatrix} 2 \\ 1 \end{pmatrix}$
В	The point with unknown coordinate	$\begin{pmatrix} P \\ -1 \end{pmatrix}$
С	The point in 2-D plane with coordinates	$\begin{pmatrix} -1 \\ 3 \end{pmatrix}$

Collinearity Condition

Three points **A**, **B**, and **C** are collinear if:

$$\mathsf{rank} \begin{pmatrix} \mathbf{C} - \mathbf{B} & \mathbf{B} - \mathbf{A} \end{pmatrix} = 1$$

Setting Up the Matrix

$$\begin{pmatrix} -1-P & P-2 \\ 4 & -2 \end{pmatrix} \stackrel{R_1 \to R_1/(-P-1)}{\longleftrightarrow} \tag{0.1}$$

Row Reduction

$$\begin{pmatrix} 1 & \frac{2-P}{P+1} \\ 4 & -2 \end{pmatrix} \stackrel{R_2 \to R_2 - 4R_1}{\longleftrightarrow} \tag{0.2}$$

$$\begin{pmatrix} 1 & \frac{2-P}{P+1} \\ 0 & \frac{2P-10}{P+1} \end{pmatrix} \tag{0.3}$$

Finding P

For the rank to be one:

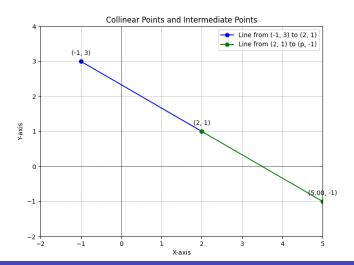
$$2P - 10 = 0$$

 $P - 5 = 0$ (0.4)
 $P = 5$

Conclusion

The value of P for which the points are collinear is P = 5.

Plotting of Points



└ Code

```
#include <stdio.h>
#include <stdlib.h>
#include "libs/matfun.h"
#include "libs/geofun.h"
void calculate_p(double *p, double points[5][2]) {
   double x1 = 2.0, y1 = 1.0;
   double x3 = -1.0, y3 = 3.0;
   double **matrix = createMat(3, 3);
   matrix[0][0] = x1: matrix[0][1] = v1: matrix[0][2] = 1.0: // Point (2, 1)
   matrix[1][0] = *p: matrix[1][1] = -1.0: matrix[1][2] = 1.0: // Point (p. -1)
   matrix[2][0] = x3; matrix[2][1] = y3; matrix[2][2] = 1.0; // Point (-1, 3)
   int rank = 3;
   for (int i = 0; i < 3; i++) {
       if (matrix[i][0] == 0 && matrix[i][1] == 0 && matrix[i][2] == 0) {
          rank--;
          continue:
       for (int j = i + 1; j < 3; j++) {
          if (matrix[j][i] != 0) {
              double ratio = matrix[j][i] / matrix[i][i];
              for (int k = 0; k < 3; k++) {
                 matrix[j][k] -= ratio * matrix[i][k];
          }
   if (rank < 3) {
       *p = (y3 - y1) / (x3 - x1) * (x3 - x1) + y1;
   } else {
```

```
Code
```

```
*p = 5.0;
}

for (int i = 0; i < 5; i++) {
    double t = (double)i / 4;
    points[i][0] = (1 - t) * x1 + t * x3;
    points[i][1] = (1 - t) * y1 + t * y3;
}

for (int i = 0; i < 3; i++) {
    free(matrix[i]);
}

free(matrix);
}</pre>
```

└ Code

```
import ctypes
import numpy as np
import matplotlib.pvplot as plt
lib = ctypes.CDLL('./libcalculate_p.so')
lib.calculate p.argtypes = [ctypes.POINTER(ctypes.c double), ctypes.POINTER(ctypes.c double * 10)]
p = ctypes.c_double(0.0)
points array type = ctypes.c double * 10
points = points_array_type()
lib.calculate_p(ctypes.byref(p), points)
points_list = np.array([[points[i * 2], points[i * 2 + 1]] for i in range(5)])
original points = np.array([[2, 1], [p.value, -1], [-1, 3]])
plt.figure(figsize=(8, 6))
plt.plot([2, -1], [1, 3], label='Line_from_(-1, 3), to_(2, 1)', color='blue', marker='o')
plt.plot([2, p.value], [1, -1], label='Line_from (2, 1), to (p, 1-1)', color='green', marker='o')
plt.scatter(original_points[:, 0], original_points[:, 1], color='red')
plt.annotate('(-1,13)', xy=(-1, 3), textcoords="offset_points", xytext=(0,10), ha='center')
plt.annotate('(2,11)', xy=(2, 1), textcoords="offset_points", xytext=(0,10), ha='center')
plt.annotate(f'({p.value: .2f}, -1)', xv=(p.value, -1), textcoords="offset points", xvtext=(0.10), ha='
      center')
plt.xlim(-2, 5)
```

```
└ Code
```

```
plt.ylim(-2, 4)

plt.title('Collinear_Points_and_Intermediate_Points')
plt.xlabel('X-axis')
plt.ylabel('Y-axis')
plt.axhline(0, color='black', linewidth=0.5, ls='-')
plt.axvline(0, color='black', linewidth=0.5, ls='-')
plt.grid(color='gray', linestyle='--', linewidth=0.5)
plt.legend()
plt.savefig('../figs/fig.png')
plt.show()
```