

Similarity of  
Triangles

Srihari S

Question

Construction

Codes and figures

Construction  
methods

Construction  
methods

Construction  
methods

Solution

a

b

# Similarity of Triangles

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# Question

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## Exercise 8.1(Q no.51)

O is a point in the interior of  $\triangle ABC$ . D is a point on OA. If  $DE \parallel OB$  and  $DF \parallel OC$ . Show that  $EF \parallel BC$ .

# Codes and Figures

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### Construction methods

### Solution

The python code for the figure is

```
./codes/similartriangle.py
```

The latex- tikz code is

```
./figs/constructionpic.tex
```

The above latex code can be compiled as standalone document

```
./figs/constructionpic_standalone.tex
```

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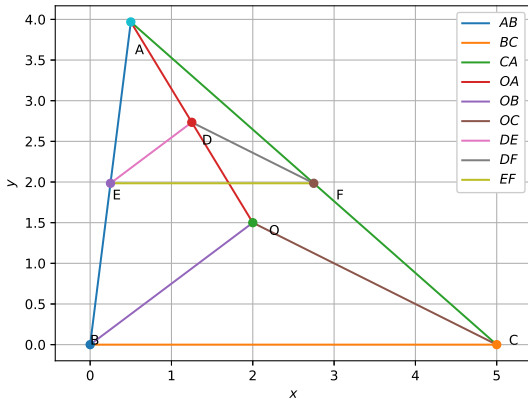
Construction methods

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(a) By Python

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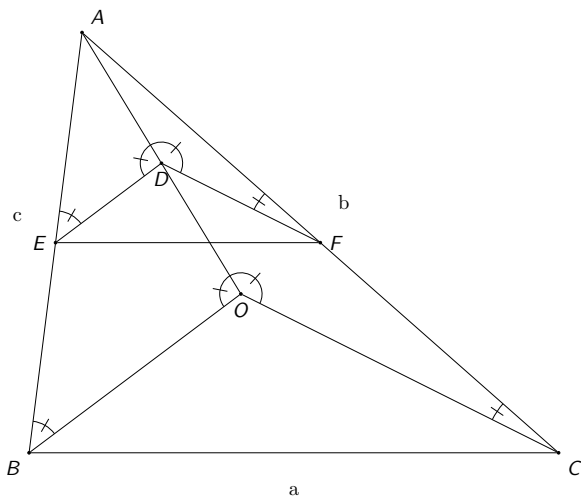


Figure: By Latex-tikz

# Construction method

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The values used for constructing the triangles in both Python and  $\text{\LaTeX}$ -Tikz is given below:

Initial Input Values	
Parameter	Value
<b>a</b>	<b>5</b>
<b>b</b>	<b>6</b>
<b>c</b>	<b>4</b>

**Table:** To construct  $\triangle ABC$

Finding the coordinates of various points of  $\triangle ABC$ :

From the information provided, let

$$B = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \quad C = \begin{pmatrix} a \\ 0 \end{pmatrix} \quad A = \begin{pmatrix} p \\ q \end{pmatrix}$$

Given a point  $O$ , we need to determine whether it lies inside  $\triangle ABC$ .

A point  $O$  is said to lie inside  $\triangle ABC$  if and only if all of the cross products  $AB \times AO$ ,  $BC \times BO$  and  $CA \times CO$  are  $\geq 0$ .

Let the arbitrary interior point  $O$  be represented as  $\begin{pmatrix} 2 \\ 1.5 \end{pmatrix}$ .

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D is a point on line AO such that  $DE \parallel OB$  and  $DF \parallel OC$ .

**Determination of points D, E and F:**

As  $DE \parallel OB$ , by basic proportionality theorem the points E and D, divide the lines AB and AO respectively in the same ratio.

Hence we choose points E and D such that

$$\frac{AE}{EB} = \frac{AD}{DO} \quad (1)$$

Similarly point F is chosen such that the points F and D, divide the lines AC and AO respectively in the same ratio such that

$$\frac{AF}{FC} = \frac{AD}{DO} \quad (2)$$

Derived Values	
Parameter	Value
p	0.5
q	3.96

Table: To construct  $\triangle ABC$

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If the point D divides the line AO in the ratio  $x:y$ , the coordinates of D is given by section formula as:

$$D = \frac{yA + xO}{x + y} \quad (3)$$

Similarly the coordinates of points E and F is given by

$$E = \frac{yA + xB}{x + y} \quad (4)$$

$$F = \frac{yA + xC}{x + y} \quad (5)$$

Let us assume the points divide the respective lines in the ratio 1:1. Then the coordinates of points D, E and F is

$$D = \begin{pmatrix} 1.25 \\ 2.73 \end{pmatrix}$$

$$E = \begin{pmatrix} 0.25 \\ 1.98 \end{pmatrix}$$

$$F = \begin{pmatrix} 2.75 \\ 1.98 \end{pmatrix}$$



# Solution

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$\triangle EAD \sim \triangle BAO$  by AAA Similarity:

Since  $DE \parallel OB$ ,

①  $\angle DEA = \angle OBA$  {Alternate Interior Angles}

②  $\angle ADE = \angle AOB$  {Alternate Interior Angles}

③  $\angle EAD = \angle BAO$  {Common angle}

Therefore

$$\frac{AE}{AB} = \frac{AD}{AO} \quad (6)$$

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Similarly  $\triangle FDA \sim \triangle COA$  by AAA Similarity:

Since  $DF \parallel OC$ ,

- ①  $\angle DFA = \angle OCA$  { *Alternate Interior Angles*}
- ②  $\angle ADF = \angle AOC$  { *Alternate Interior Angles*}
- ③  $\angle FAD = \angle CAO$  { *Common angle*}

Therefore

$$\frac{AF}{AC} = \frac{AD}{AO} \quad (7)$$

Hence from the above we conclude,

$$\frac{AF}{AC} = \frac{AE}{AB} = \frac{AD}{AO} \quad (8)$$

As the ratio of the sides is the same,  $\triangle ABC \sim \triangle AEF$ , which means  $\angle AFE = \angle ACB$  and  $\angle AEF = \angle ABC$  as similar triangles have same angles. i.e.

$$EF \parallel QR \quad (9)$$

Hence Proved.