

Name: Sri Hari Vadhry

Student ID: 811297316

Subject: Quantitative Management Modelling

Problem1:

A). Decision Variables:

Let,

X= Number of Collegiate produced per week

Y= Number of Mini produced per week

B) Objective Function:

The main objective is to check what quantity of each product to be produced to get the maximum profit

$$Z = 32X + 24Y$$

Where,

Z= Maximizing profit

Profit per unit of X = 32

Profit per unit of Y = 24

C) Constraints:

- **Material Constraint:** It is given that total nylon receives only 5000 square foot of shipment per week and Each Collegiate requires 3 Square feet whereas each Mini requires 2 Square feet.
 $3X + 2Y \leq 5000$
- **Production Constraint:** The quantity of Collegiate bags produced should be less than 1000 per week and the quantity of Mini bags produced should be less than 1200 per week
 $X \leq 1000$
 $Y \leq 1200$
- **Labor Constraint:** There are 35 laborers working 40 hours per week and the time required for X is 45 mins and for Y is 40 mins ($35 \times 40 = 1400$ hours, convert it into minutes, $1400 \times 60 = 84000$)
 $45X + 40Y \leq 84000$
- **Non-Negative Constraint:** The number of bags produced per week cannot be negative
 $X \geq 0$
 $Y \geq 0$

D) Mathematical Formulation:

$$Z = 32X + 42Y$$

Subjected to,

$$X \leq 1000, Y \leq 1200$$

$$3X + 2Y \leq 5000$$

$$45X + 40Y \leq 84000$$

$$X \geq 0, Y \geq 0$$

Problem 2:

A) Decision Variables:

Let,

X_1, X_2, X_3 be the quantity of the products produced by Plant1, Plant2 and Plant3 respectively

Y_1, Y_2, Y_3 be the quantity of the products produced by Plant1, Plant2 and Plant3 respectively

Z_1, Z_2, Z_3 be the quantity of the products produced by Plant1, Plant2 and Plant3 respectively

B) Formulation of Linear Programming Model:

Objective Function:

How many products to be produced by each plant to maximize the profit and to check on avoiding layoff by using same percentage of excess production capacity

$$Z = 420 (X_1 + X_2 + X_3) + 360 (Y_1 + Y_2 + Y_3) + 300 (Z_1 + Z_2 + Z_3)$$

Subject to constraint,

Excess Production Capacity Constraints:

$$\text{Plant1- } X_1 + Y_1 + Z_1 \leq 750$$

$$\text{Plant2- } X_2 + Y_2 + Z_2 \leq 900$$

$$\text{Plant3- } X_3 + Y_3 + Z_3 \leq 450$$

Storage Capacity Constraints:

$$\text{Plant1- } 20X_1 + 15Y_1 + 12Z_1 \leq 13000$$

$$\text{Plant2- } 20X_2 + 15Y_2 + 12Z_2 \leq 12000$$

$$\text{Plant3- } 20X_3 + 15Y_3 + 12Z_3 \leq 5000$$

Sales Constraint:

$$\text{Large Size- } X_1 + X_2 + X_3 \leq 900$$

$$\text{Medium Size- } Y_1 + Y_2 + Y_3 \leq 1200$$

$$\text{Small Size- } Z_1 + Z_2 + Z_3 \leq 750$$

Percentage of Excess Capacity to avoid layoffs:

The management has decided that the plants use same percentage of excess capacity to produce the new product

$$(X1 + Y1 + Z1)/750 = (X2 + Y2 + Z2)/900 = (X3 + Y3 + Z3)/450$$

Non-Negative Constraints:

$$X1 \geq 0, X2 \geq 0, X3 \geq 0,$$

$$Y1 \geq 0, Y2 \geq 0, Y3 \geq 0,$$

$$Z1 \geq 0, Z2 \geq 0, Z3 \geq 0.$$