

India-map

Step 1: Basic K center with $k=5$

Initial centers: Thiruvanthapuram (South)

Itanagar (Northeast)

Jaipur (Northwest)

Bhuvaneshwar (East)

Mumbai (West)

Initial $r = 709.788 \text{ km}$

Step 2: Distance Set R: Client to facility distances ($28 \times 28 = 784$)
client-facility distance

Total distances = 784

Unique sample = 30 values.

Min = 50, 25th percentile = 400 km, Median = 800 km,

Max = 2500 km

Step 3: Generate partitions:-

How many facilities place near each center?

$$nCr = {}^9C_4 = \frac{(9+4-1)!}{(4-1)!} = \frac{12!}{3!} = \frac{9!}{4!(5!)}$$

= 126 partitions.

= 3630
Combinations

(1,1,1,1,1)

(0,0,0,1,4)

(2,2,1,0,0)

Skip degenerate partitions
like (5,0,0,0,0)

= 121 partitions \times 30 radii

= 3630 combinations

Step 4:- Build Network Flow graph with radius = 600km

Edge capacities: Source - Client ($w=1$)

Client - Facility ($w=1$) if

(distance $r+r' = 600+710=1310$ km)

Facility - Sink = 8 (Capacity constraint)

Step 5: Run max flow:->

flowmax = 28 (all clients served Feasible)

flowmax < 28 (some clients unassigned infeasible).

Iteration 150: Partation (0,0,0,1,4) $r=965.2$ km
feasible ✓

flow value = 28, New best = 965.2 km

Iteration 318: Partation (0,0,0,2,3) $r=799.7$ km
flow value = 28 feasible ✓

Iteration: 845: Partation (0,0,1,1,3) $r=601.2$ km
flow value = 28, feasible ✓

Iteration: 2310:

Partation (1,1,1,1,1) $r=55.8$ km

flow value = 28, feasible ✓

New best = 55.8 km optimal.