

India-map

Step1:- Basic K center with k=5

Initial centers: Thiruvanthepuram(South)

Itanagar(Northeast)

Jaipur(Northwest)

Bhubaneshwar(East)

Mumbai(West)

Initial $r' = 709.788 \text{ km}$

Step2:- Distance SetR: Client to facility distances ($128 \times 28 = 784$)
client-facility distance

Total distances = 784

Unique sample = 30 values

Min=50, 25th percentile = 400km, Median = 800km,

Max = 2500km

Step3: Generate partitions :-

How many facilities place near each center?

$${}^n C _r = \frac{(n+r-1)!}{(r-1)!} = \frac{12!}{3!} = \frac{9!}{9!(85!)} = 3630$$

= 120 partitions.

Combinations

(1,1,1,1,1)

(0,0,0,1,4)

(2,2,1,0,0)

Skip degenerate partitions
like (5,0,0,0,0)

= 121 partitions \times 30 radii

= 3630 combinations

Step 4:- Build Network Flow graph with radius = 600km

Edge capacities: Source - Client ($w=1$)

Client - Facility ($w=1$) if

$$(\text{distance } r + r' = 600 + 710 = 1310 \text{ km})$$

Facility - Sink = ∞ (Capacity constraint)

Step 5: Run max flow:

flowmax = 28 (all clients served feasible)

flowmax < 28 (some clients unassigned infeasible).

Iteration 150: partition $(0, 0, 0, 1, 4)$ $r = 965.2 \text{ km}$

feasible ✓

flow value = 28, New best = 965.2 km

Iteration 318: partition $(0, 0, 0, 2, 3)$ $r = 799.7 \text{ km}$

flow value = 28 feasible ✓

Iteration: 845 : partition $(0, 0, 1, 1, 3)$ $r = 601.2 \text{ km}$

flow value = 28, feasible ✓

Iteration: 2310 :

partition $(1, 1, 1, 1, 1)$ $r = 55.8 \text{ km}$

flow value = 28, feasible ✓

New best = 55.8 km optimal.