ASSIGNMENT 1 INTRODUCTION TO NLP

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Creating a Language model

First part of the language modelling is to clean the text. As a part of cleaning the text, following operations are done on the sentences using regex.

Text cleaning:

- 1) Convert the sentences to lower case.
- 2) Remove punctuations from the sentences. "Dr." now becomes "dr" and "B.P." becomes "bp"
- 3) Consider only alphabets. (Removes numbers and other languages)
- 4) Remove the lines with the "_" string. (To remove the sentences with POS tags)

Kneyser-ney's model of smoothing:

I have implemented the following recursion formula, taking n=4 (as the model we are building is 4-gram LM).

$$P_{\text{KN}}(w_i|w_{i-n+1:i-1}) = \frac{\max(c_{\text{KN}}(w_{i-n+1:i}) - d, 0)}{\sum_{v} c_{\text{KN}}(w_{i-n+1:i-1} \ v)} + \lambda(w_{i-n+1:i-1}) P_{\text{KN}}(w_i|w_{i-n+2:i-1})$$

Lambda for a bigram is:

$$\lambda(w_{i-1}) = \frac{d}{\sum_{v} C(w_{i-1}v)} |\{w : C(w_{i-1}w) > 0\}|$$

The same approach is used to find the lambda for other grams.

 $c_{KN}(.)$ is count(.) for 4-grams and continuation count for all other lower order grams (trigram, bigram and unigram) where the continuation count is the number of unique single word contexts for \cdot .

The termination condition for recursion is when P_{KN} of a unigram is called. It is as follows,

$$P_{KN}(w) = \frac{\max(c_{KN}(w) - d, 0)}{\sum_{w'} c_{KN}(w')} + \lambda(\epsilon) \frac{1}{V}$$

The Lambda of epsilon is 'd'.

Value of d is taken as 0.75.

Code snippet:

```
def calc_kneyser_probability(sentence):
    length = len(sentence.split())
    if (length >=2): return first_term(sentence) + kneyser_lambda(sentence)*calc_kneyser_probability(gen_post_string(sentence))
    else: return first_term(sentence) + (kneyser_lambda(sentence)/len(unigrams))
```

Witten bell's model of smoothing:

I have implemented the following recursion formula taking n=4.

$$p_{\mathrm{WB}}(w_{\,i}|w_{\,i-n+1}^{\,i-1}) = \lambda_{w_{\,i-n+1}^{\,i-1}} \; p_{\mathrm{ML}}(w_{\,i}|w_{\,i-n+1}^{\,i-1}) + (1 - \lambda_{w_{\,i-n+1}^{\,i-1}}) \; p_{\mathrm{WB}}(w_{\,i}|w_{\,i-n+2}^{\,i-1})$$

The formula for p_{ML} is as follows,

$$P(w_{i}|w_{i-n+1}...w_{i-1}) = \frac{C(w_{i-n+1}...w_{i})}{C(w_{i-n+1}...w_{i-1})}$$

Formula used to compute lambda is as follows,

$$1 - \lambda_{w_{i-n+1}^{i-1}} = \frac{N_{1+}(w_{i-n+1}^{i-1} \bullet)}{N_{1+}(w_{i-n+1}^{i-1} \bullet) + \sum_{w_i} c(w_{i-n+1}^{i})}$$

$$N_{1+}(w_{i-n+1}^{i-1}\bullet) = \big| \{w_i : c(w_{i-n+1}^{i-1}w_i) > 0\} \big|$$

Recursion terminates when p_{WB} (unigram) is called.

Code snippet:

```
def calc_witten_probability(sentence):
    length = len(sentence.split())
    if (length >=2): return witten_lambda(sentence)*mle_probability(sentence) + (1-witten_lambda(sentence))*calc_witten_probability(gen_post_string(sentence))
    else: return witten_lambda(sentence)*mle_probability(sentence) + (1-witten_lambda(sentence))*(1/(2*len(unigrams)))
```

Computing perplexity - to evaluate the language model:

I have used the following formula to compute the perplexity of a sentence $W = w_1 w_2 ... w_N$

$$PP(W) = P(w_1 w_2 ... w_N)^{-\frac{1}{N}}$$
$$= \sqrt[N]{\frac{1}{P(w_1 w_2 ... w_N)}}$$

 $P(w_1w_2...w_N)$ can be expanded using chain rule based on the LM we are building (4-gram in our case)...

Code snippet:

```
perplexity = probability**(-1/len(input.split()))
```

Observations:

Splitting the corpus into test and train:

Random 1000 lines from the corpus are taken as the test set and the model is trained on the other lines, i.e the training set.

```
for x in file:
    r1 = random.randint(1, 10)
    if(r1%2==0): f_train.write(x)
    elif(r1%2!=0 and counter<1000):
        f_test.write(x)
        counter+=1
    else: f_train.write(x)</pre>
```

Average perplexities of train sentences:

	Kneyser-Ney	Witten-bell
Health Corpus	17.5307580665028	10.8926669926752935
Technical Corpus	3.777256590678746	2.615631941089133

- Average perplexities for both the train corpuses are computed after training both the models on the same set.
- Average of only a few (500-1000) sentences from the train set is computed due to the time constraint.

- From the above table, the average perplexities of training sets of both the corpuses from Kneyser-ney model are higher than the average perplexities from Witten-bell model. Thus, the probabilities given by the Kneyser-ney model must have been lesser than those given by the Witten-bell model.
- This tells that Witten-bell is more conservative and deducts lesser value from probabilities of seen sentences, i.e the sentences in the training set. Whereas the penalty imposed by Kneyser-ney on seen sentences is higher.

Average perplexities of test sentences:

	Kneyser-Ney	Witten-bell
Health Corpus	101.74828224499177	331.2303428948926
Technical Corpus	48.40029692335503	134.526656369984

- Average perplexities for both the test corpuses are computed after training both the models on a separate training set.
- From the table above, the average perplexities of both the corpuses given by Witten-bell are higher than Kneyser-Ney. This means that the average probabilities for both the corpuses given by Witten-bell are lesser than those given by Kneyser-Ney's. This proves that Witten-bell is conservative and takes less probabilities from seen sentences and hence gives lesser probabilities to unseen sentences. Comparatively, penalty on seen sentences is more when the Kneyser-ney model is used and hence probabilities for them are high.
- The lower the perplexity on the test corpus, better is the model.
- Hence, my conclusion is that the Kneyser-Ney model is better than the Witten-bell model.

RESULTS FOR A SEEN SENTENCE

For the sentence - "drink plenty of water" - from the health domain corpus, after both the models are trained on the corpus, the probability given by Kneyser-Ney is 0.102 which is **lower** than the one given by Witten-Bell, i.e, 0.172.

```
dolly@sriharshitha:~/Acads/Sem6/NLP/Assignment1$ python3 language_model.py k ./Health_English.txt
Enter the sentence: drink plenty of water
Probability of the sentence is 0.10295910732224445
Perplexity of the sentence is 1.4606826539558615

dolly@sriharshitha:~/Acads/Sem6/NLP/Assignment1$ python3 language_model.py w ./Health_English.txt
Enter the sentence: drink plenty of water
Probability of the sentence is 0.17203588542540582
Perplexity of the sentence is 1.340901342222623
```

RESULTS FOR A PARTIALLY SEEN SENTENCE - seen phrases + unseen words

For the sentence - "drink plenty of juice" - not from the health domain corpus, after both the models are trained on the corpus, the probability given by Kneyser-Ney is 6.11×10^{-5} which is **higher** than the one given by Witten-Bell, i.e, 7.44×10^{-6} .

```
dolly@sriharshitha:~/Acads/Sem6/NLP/Assignment1$ python3 language_model.py k ./Health_English.txt
Enter the sentence: drink plenty of juice
Probability of the sentence is 6.112000976708643e-05
Perplexity of the sentence is 5.038517417179293

dolly@sriharshitha:~/Acads/Sem6/NLP/Assignment1$ python3 language_model.py w ./Health_English.txt
Enter the sentence: drink plenty of juice
Probability of the sentence is 7.440107430710179e-06
Perplexity of the sentence is 7.157095280669682
```

RESULTS FOR AN UNSEEN SENTENCE

For the sentence - "all that glitters is not gold" - not from the health domain corpus, after both the models are trained on the corpus, the probability given by Kneyser-Ney is $1.90x10^{-15}$ which is **quite higher** than the one given by Witten-Bell, i.e, $3.28x10^{-19}$.

```
dolly@sriharshitha:~/Acads/Sem6/NLP/Assignment1$ python3 language_model.py k ./Health_English.txt
Enter the sentence: all that glitter is not gold
Probability of the sentence is 1.901161275809059e-15
Perplexity of the sentence is 69.20263481127145

dolly@sriharshitha:~/Acads/Sem6/NLP/Assignment1$ python3 language_model.py w ./Health_English.txt
Enter the sentence: all that glitters is not gold
Probability of the sentence is 3.2889453804033326e-19
Perplexity of the sentence is 204.34683583038097
```

Hence,

- 1) Both the models do not give 0 probability for any unseen sentence.
- 2) The table below compares the probabilities and perplexities computed by both the models for different types of input sentences.

	Kneyser-ney probability	Witten-bell probability
Seen	Comparatively lower	Higher
Partially seen	Higher	Comparatively lower
Completely unseen	Quite higher	Lower

	Kneyser-ney perplexity	Witten-bell perplexity
Seen	Comparatively higher	Lower
Partially seen	Lower	Comparatively higher
Completely unseen	Lower	Quite higher

- 3) Witten-bell is conservative.
- 4) When evaluated based on average perplexity, Kneyser-ney is a better model than Witten-bell.

References:

 $https://web.stanford.edu/~jurafsky/slp3/3.pdf \\ https://www.microsoft.com/en-us/research/wp-content/uploads/2016/02/tr-10-98.pdf? from=https%3A%2F%2Fresearch.microsoft.com%2F%7Ejoshuago%2Ftr-10-98.pdf$