

1. a). Determine a minimum cost staffing plan for the center. In your solution, how many consultants will be paid to work full time and how many will be paid to work part time? What is the minimum cost ?

Linear Programming Model

Let F1 = number of full time consultants for the morning shift

F2 = number of full time consultants for the afternoon shift

F3 = number of full time consultants for the evening shift

P1 = number of part-time consultants for the first shift

P2 = number of part-time consultants for the second shift

P3 = number of part-time consultants for the third shift

P4 = number of part-time consultants for the fourth shift

$$\text{Minimum Cost} = (8 \times 14) \times (F1 + F2 + F3) + (4 \times 12) \times (P1 + P2 + P3 + P4)$$

1. b) After thinking about this problem for a while, you have decided to recognize meal breaks explicitly in the scheduling of full -time consultants. In particular, full - time consultants are entitled to a one - hour lunch break during their eight - hour shift. In Addition, employment rules specify that the lunch break can start after three hours of work or after four hours of work, but those are the only alternatives. Part-time consultants do not receive a meal break. Under these conditions, find a minimum-cost staffing plan. What is the minimum cost

S.T

$$(8\text{AM to } 12\text{PM}) : P1 + F1 \geq 4$$

$$(12\text{PM to } 4\text{PM}) : P2 + F1 + F2 \geq 8$$

$$(4\text{PM to } 8\text{PM}) : P3 + F2 + F3 \geq 10$$

$$(8\text{PM to } 12\text{AM}) : F3 + P4 \geq 6$$

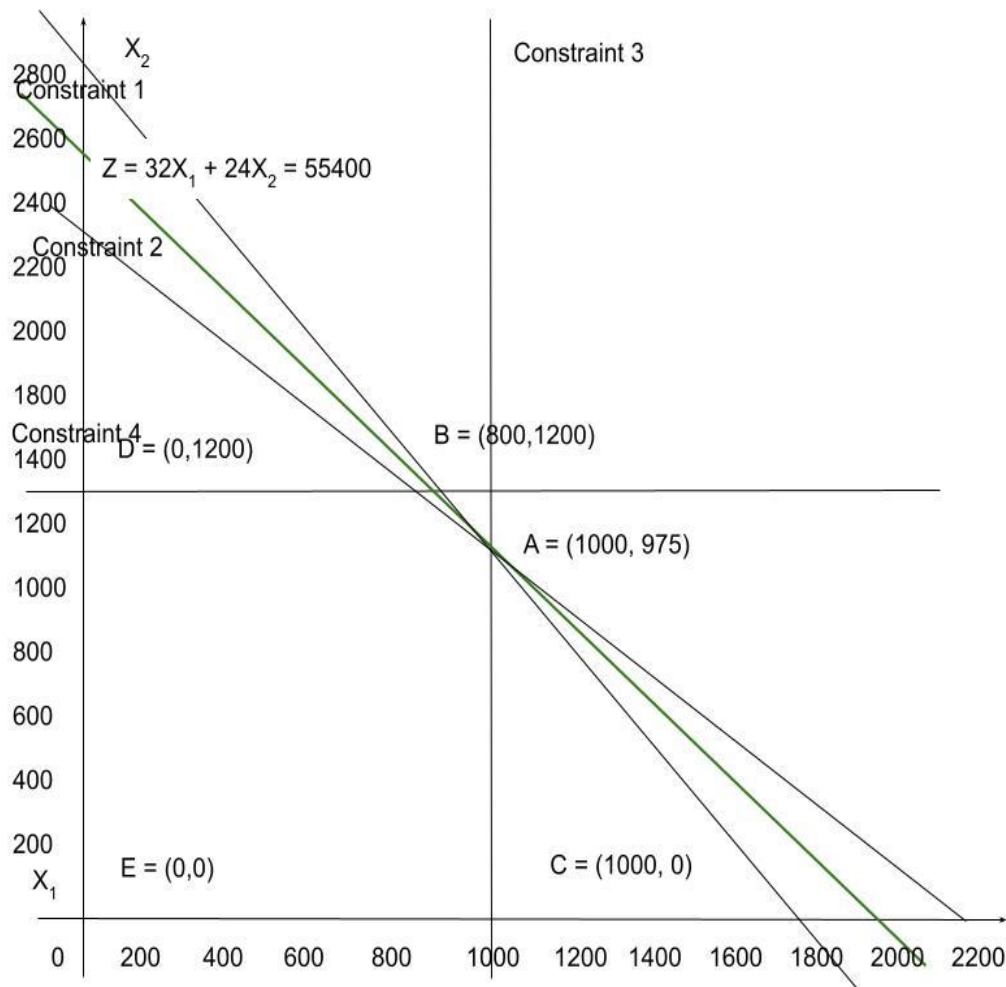
$$F1 \geq P1$$

$$F1 + F2 \geq P2$$

$$F2 + F3 \geq P3$$

$$F4 \geq P4$$

$$F1, F2, F3, P1, P2, P3, P4 \geq 0$$



3. a. Define the decision variables
- b. Formulate a linear programming model for this problem.
- c. Solve the problem using lpsolve, or any other equivalent library in R.

a).

Decision Variables:

SPL1 = Number of large size units produced in the plant 1
 SPM1 = Number of medium size units produced in the plant 1
 SPS1 = Number of small size units produced in the plant 1
 SPL2 = Number of large size units produced in the plant 2
 SPM2 = Number of medium size units produced in the plant 2
 SPS2 = Number of small size units produced in the plant 2
 SPL3 = Number of large size units produced in the plant 3

SPM3 = Number of medium size units produced in the plant 3

SPS3 = Number of small size units produced in the plant 3

b).

Maximizing the profit::

$$Z = 420 (SPL1 + SPL2 + SPL3) + 360 (SPM1 + SPM2 + SPM3) + 300 (SPS1 + SPS2 + SPS3)$$

$$= 420SPL1 + 420SPL2 + 420SPL3 + 360SPM1 + 360SPM2 + 360SPM3 + 300SPS1 + 300SPS2 + 300SPS3$$

Storage:

$$20SPL1 + 15SPM1 + 12SPS1 \leq 13000 ;$$

$$20SPL2 + 15SPM2 + 12SPS2 \leq 12000 ;$$

$$20SPL3 + 15SPM3 + 12SPS3 \leq 5000 ;$$

Excess Capacity:

$$SPL1 + SPM1 + SPS1 \leq 750 ;$$

$$SPL2 + SPM2 + SPS2 \leq 900 ;$$

$$SPL3 + SPM3 + SPS3 \leq 450 ;$$

Sales:

$$SPL1 + SPL2 + SPL3 \leq 900 ;$$

$$SPM1 + SPM2 + SPM3 \leq 1200 ;$$

$$SPS1 + SPS2 + SPS3 \leq 750 ;$$

$$1/750(SPL1 + SPM1 + SPS1) - 1/900(SPL2 + SPM2 + SPS2) = 0$$

$$1/750(SPL1 + SPM1 + SPS1) - 1/450(SPL3 + SPM3 + SPS3) = 0$$

$$SPL1, SPM1, SPS1, SPL2, SPM2, SPS2, SPL3, SPM3, SPS3 \geq 0$$