

Some Important Formula

Unit - III

* Correlation coefficient [Quantitative data]

$$r_{xy} = \frac{n \sum xy - \sum x \sum y}{\sqrt{n(\sum x^2) - (\sum x)^2} \sqrt{n(\sum y^2) - (\sum y)^2}}$$

$$-1 \leq r_{xy} \leq 1$$

* Rank correlation coefficient [Qualitative Data]

$$r = 1 - \frac{6 \sum d^2}{n(n^2-1)} \quad [\text{Non-tied Rank}]$$

where $d = \text{Rank in } x - \text{Rank in } y$

$$r = 1 - \frac{6 \left[\sum d^2 + \frac{1}{12} m_1(m_1^2 - 1) + \frac{1}{12} m_2(m_2^2 - 1) + \dots \right]}{n(n^2-1)}$$

where $m_1, m_2 \& m_3$ are the repetition of a number.

* Regression line

→ y on x

$$y - \bar{y} = b_{yx} (x - \bar{x})$$

$$\text{when } b_{yx} = \frac{n \sum xy - \sum x \sum y}{n \sum x^2 - (\sum x)^2}$$

→ n on y

$$n - \bar{n} = b_{ny} (y - \bar{y})$$

$$\text{where } b_{ny} = \frac{n \sum ny - \bar{n} \sum y}{n \sum y^2 - (\bar{y})^2}$$

* Curve Fitting

→ Straight line

$$y = a + bn$$

The normal equations are

$$\sum y = an + bn$$

$$\sum ny = a \sum n + b \sum n^2$$

Note: To make the normal equⁿ multiply the coefficient of constant & take the summation

→ Second Degree Parabola

$$y = a + bn + cn^2$$

The normal equⁿ are

$$\sum y = an + bn + cn^2$$

$$\sum ny = a \sum n + b \sum n^2 + c \sum n^3$$

$$\sum n^2 y = a \sum n^2 + b \sum n^3 + c \sum n^4$$

→ $y = a e^{bn}$

$$\log y = \log a + bn$$

$$y = A + bn$$

The normal equⁿ are

$EY = An + bn$

$E(XY) = abn^2 + bn^2$

* Moments about Mean

$$\mu_r = \frac{\sum (x_i - \bar{x})^r}{n} \quad [\text{If data is given in series form}]$$

$$\mu_r = \frac{\sum f_i (x_i - \bar{x})^r}{\sum f_i} \quad [\text{If data is given in frequency form}]$$

* Skewness

$$\beta_1 = \frac{\mu_3^2}{\mu_2^3}$$

+ve skewed if $\beta_1 > 0$

-ve skewed if $\beta_1 < 0$

Symmetric if $\beta_1 = 0$

* Kurtosis

$$\beta_2 = \frac{\mu_4}{\mu_2^2}$$

Meso-kurtosis if $\beta_2 = 3$

Lepto-kurtosis if $\beta_2 > 3$

Poly-kurtosis if $\beta_2 < 3$

* Karl Pearson's coefficient

$$Y_1 = \sqrt{\beta_1}$$

$$Y_2 = \beta_2 - 3$$

* Multiple Linear Regression

If n depends on y & z

$$n = a + by + cz$$

the normal equations are

$$\sum n = an + b \sum y + c \sum z$$

$$\sum ny = a \sum y + b \sum y^2 + c \sum yz$$

$$\sum nz = a \sum z + b \sum yz + c \sum z^2$$

It is very similar as curve fitting.

Unit - IV

- * Binomial Distribution

$$P(r) = {}^n C_r p^r q^{n-r}$$

where n = no. of trial

p = probability of success

q = " " failure

The general form of Binomial distribution

$$(q+p)^n$$

→ If trials are repeated N times then the general form will be $N \cdot (q+p)^n$

l Probability of r success will becomes Frequency of r success & can be calculated as $N \cdot P(r)$.

$$\therefore N \cdot {}^n C_r p^r q^{n-r}$$

Note: $\rightarrow P(0) + P(1) + P(2) + \dots + P(n) = 1$

\rightarrow At least 2 success i.e [lower limit given]
 $P(2) + P(3) + \dots + P(n)$

\rightarrow At most 2 success i.e [upper limit given]
 $P(0) + P(1) + P(2)$

\rightarrow Exactly 2 success

$$\rightarrow p+q=1 \quad P(2)$$

\rightarrow Binomial Distribution is applicable only when
 n - finite
 p - constant

* Poisson Distribution

Probability of r success

$$P(r) = \frac{e^{-\lambda} \lambda^r}{r!}$$

where $\lambda = np$ = Mean, it is given either in question or you have to calculate $n.p$

→ Frequency of r success $N \cdot P(r)$

$$= N \cdot \frac{e^{-\lambda} \lambda^r}{r!}$$

→ Applicable only when p is small & n is large

* Normal Distribution

$$z = \frac{x - \mu}{\sigma}$$

where μ = Mean

σ = Std deviation

→ You have to use table of Normal Distribution

* Addition Law of Probability

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

→ If Events A & B are ~~independent~~, then
 $P(A \cap B) = 0$ mutually exclusive

$$\Rightarrow P(A \cup B) = P(A) + P(B)$$

* Multiplication Law of Probability

$$P(A \cap B) = P(A) \cdot P(B/A) = P(B) \cdot P(A/B)$$

If events are independent, then

$$P(A \cap B) = P(A) \quad \& \quad P(B/A) = P(B)$$

$$P(A \cap B) = P(A) \cdot P(B)$$

* Baye's Theorem

$$P\left(\frac{E_i}{A}\right) = \frac{P(A) \cdot P\left(\frac{A}{E_i}\right)}{\sum P(A) \cdot P\left(\frac{A}{E_i}\right)}$$

* Random Variable : $S \rightarrow R$

Discrete R.V.

→ If Range set is finite

Probability Mass function

$$\rightarrow (i) \sum p_i = 1$$

$$(ii) p_i > 0$$

Continuous R.V.

→ If Range set is an interval.

Probability Density function

$$(i) f(x) > 0$$

$$(ii) \int_{-\infty}^{\infty} f(x) dx = 1$$

* Expectation

$$E(X) = \sum x_i p_i$$

* Variance

$$\text{Var}(X) = E(X^2) - [E(X)]^2$$

Unit - IV

* t-test [If sample size $n < 30$ & compare the mean]

$$t = \frac{\bar{x} - \mu}{\frac{s}{\sqrt{n}}} \quad \text{or} \quad \frac{\bar{x} - \mu}{\frac{s}{\sqrt{n-1}}}$$

where μ = Mean of Population

s = Std deviation of Population

n = Sample size

s = Std deviation of Sample

→ If data \bar{x} is given

$$s^2 = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n-1}}$$

* Relation b/w s & S

$$(n-1) S^2 = n s^2$$

* Degree of freedom = $n-1$

* F-test [comp]

* For two samples

$$t = \frac{\bar{x} - \bar{y}}{\sqrt{\frac{s^2}{n_1} + \frac{s^2}{n_2}}} \quad \text{where } s^2 = \frac{n_1 s_1^2 + n_2 s_2^2}{n_1 + n_2 - 2}$$

\bar{x} = Mean of sample 1 $s = \sqrt{\frac{\sum (x_i - \bar{x})^2 + \sum (y_i - \bar{y})^2}{n_1 + n_2 - 2}}$

n_1 = Size of sample 1

\bar{y} = Mean of sample 2

n_2 = Size of sample 2

D.O.F = $n_1 + n_2 - 2$

* F - Test [Compare the variances]

$$F = \frac{s_1^2}{s_2^2} \quad [s_1^2 > s_2^2]$$

$$S_{\text{P}}^2 = \frac{\sum (x_i - \bar{x})^2}{n_1 + n_2 - 2}$$

$$s_1^2 = \frac{\sum (x_i - \bar{x})^2}{n_1 - 1} \quad \text{or} \quad \frac{n_1 s_1^2}{(n_1 - 1)}$$

$$s_2^2 = \frac{\sum (y_i - \bar{y})^2}{n_2 - 1} \quad \text{or} \quad \frac{n_2 s_2^2}{(n_2 - 1)}$$

D. o.f is ~~n_1 + n_2 - 2~~ $(n_1 - 1), (n_2 - 1)$

* Chi-Square Test [Compare the frequency]

$$\chi^2 = \sum \left(\frac{(O_i - E_i)^2}{E_i} \right)$$

O_i = Observed Frequency

E_i = Expected Frequency

Expected frequency can be calculated as

→ Average - D.o.f. $n-1$

→ B. D. - $n-1$

→ P. D. - $n-2$

→ N. D. -

Contingency Table

| | | |
|-------|-------|---------------|
| a | b | $a+b$ |
| c | d | $c+d$ |
| $a+c$ | $b+d$ | $N = a+b+c+d$ |
| | | |

| | |
|------------------------|------------------------|
| $\frac{(a+b)(a+c)}{N}$ | $\frac{(a+b)(b+d)}{N}$ |
| $\frac{(a+c)(c+d)}{N}$ | $\frac{(b+d)(c+d)}{N}$ |

D.O.F is $(m-1)(n-1)$ where

m = no. of rows

n = no. of columns

* Anova Test

| | Sum of squares | D.O.F | Mean of sum of squares | F = |
|---------------|----------------|-------|------------------------|-----|
| within Sample | | | | |
| btw Sample | | | | |
| Total | | | | |

* Control charts

→ X chart [Mean]

$$CL = \bar{\bar{x}}$$

$$LCL = \bar{\bar{x}} - A_2 \bar{R}$$

$$UCL = \bar{\bar{x}} + A_2 \bar{R}$$

→ R chart [Range]

$$CL = \bar{R}$$

$$LCL = D_3 \bar{R}$$

$$UCL = D_4 \bar{R}$$

→ C chart

$$CL = \bar{c} = \frac{\Sigma c}{n} = \frac{\text{Sum of defect in sample}}{\text{Total no of sample}}$$

$$LCL = \bar{c} - 3 \sqrt{c}$$

$$UCL = \bar{c} + 3 \sqrt{c}$$

→ np chart

$$CL = n \bar{p}$$

$$LCL = n \bar{p} - 3 \sqrt{n \bar{p} (1 - \bar{p})}$$

$$UCL = n \bar{p} + 3 \sqrt{n \bar{p} (1 - \bar{p})}$$

where $\bar{p} = \frac{\text{No. of defective items}}{\text{Total no. of inspected items}}$

→ p chart

$$CL = \bar{p}$$

$$LCL = \bar{p} - 3 \sqrt{\frac{\bar{p} (1 - \bar{p})}{n}}$$

$$UCL = \bar{p} + 3 \sqrt{\frac{\bar{p} (1 - \bar{p})}{n}}$$