



Module 14 – part 1 – Recursion

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Module Overview



- **Recursion**
- **Recursive Data**
- **Recursive Functions**
- **Examples**
- **Merge Sort**



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Recursion

Recursion



- Recursion is the process of defining something in terms of itself, and is sometimes called *circular definition*.
- A recursive process is one in which objects are defined in terms of other objects of the same type.
- The entire class of objects can then be built up from a few initial values and a small number of rules.
- Ex: Fibonacci Number series



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Recursive Data

Recursive Data



Consider the linked list representation of sequential access list:

```
typedef node NODE;  
typedef NODE *LINK;  
struct node {  
    int elem;  
    LINK next;  
};
```

The type is used (referred)
in its own definition

Recursive Data



- Consider a high level description of a sequential access list:
 - *An empty list is a sequential access list;*
 - *Adding an element to a sequential access list produces another sequential access list*
- Such definitions are called **inductive definitions** or **recursive definitions**.



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Recursive Functions

Recursive functions



- A recursive function is one which calls itself (repeatedly)
- Recursive functions are useful in evaluating certain types of mathematical function. (we'll see examples)

Simple Example:

```
main()  
{  
    printf("This is an example of recursive function");  
    main();  
}
```

When this program is executed. The line is printed repeatedly and indefinitely. We might have to abruptly terminate the execution.

Factorial Calculation



```
long int fact(int n)    /* non-recursive */
{
    int t, ans;
    ans = 1;
    for(t=1; t<=n; t++)
        ans = ans*t;
    return(ans);
}
```

```
long int factr(int n)  /* recursive */
{
    int ans;
    if(n==1)
        return(1);
    answer = factr(n-1)*n;
    return(ans);
}
```

Base case

Recursive call

Power function (recursive)

```
double power(double val, unsigned pow)
{
    if(pow == 0) /*pow(x, 0) returns 1*/
        return(1.0);
    else
        return(power(val, pow-1)*val);
}
```

Base case

Recursive call

Summing up the elements of an array



Algorithm Design:

1. If we have only one element, then the sum is simple.
2. Otherwise, we use the sum of the first element and the sum of the rest.

Base case

Recursive call

```
int sum(int first,int last,int array[])
{  if (first == last)
    return (array[first]);
    return (array[first]+sum(first+1,last,array));
}
```

Sum of array elements – execution sequence



For example:

$$\begin{aligned}\text{Sum}(1\ 8\ 3\ 2) &= 1 + \text{Sum}(8\ 3\ 2) = \\ &8 + \text{Sum}(3\ 2) = \\ &3 + \text{Sum}(2) = \\ &2 \\ &3 + 2 = 5 \\ &8 + 5 = 13 \\ &1 + 13 = 14\end{aligned}$$

Answer = 14

Recursive Version of Fibonacci Series



```
int fib(int num)      /*Fibonacci value of a number */
{
    switch(num)
    { case 0: return(0) ;
      break;
      case 1: return(1) ;
      break;
      default:          /*Including recursive calls */
        return(fib(num - 1) + fib(num - 2)) ;
        break;
    }
}
```

Base cases

Recursive call

Analysis



Input Value	Number of time fib is called
0	1
1	1
2	3
3	5
4	9
5	15
6	25
7	41
8	67
9	109

How recursive functions works???



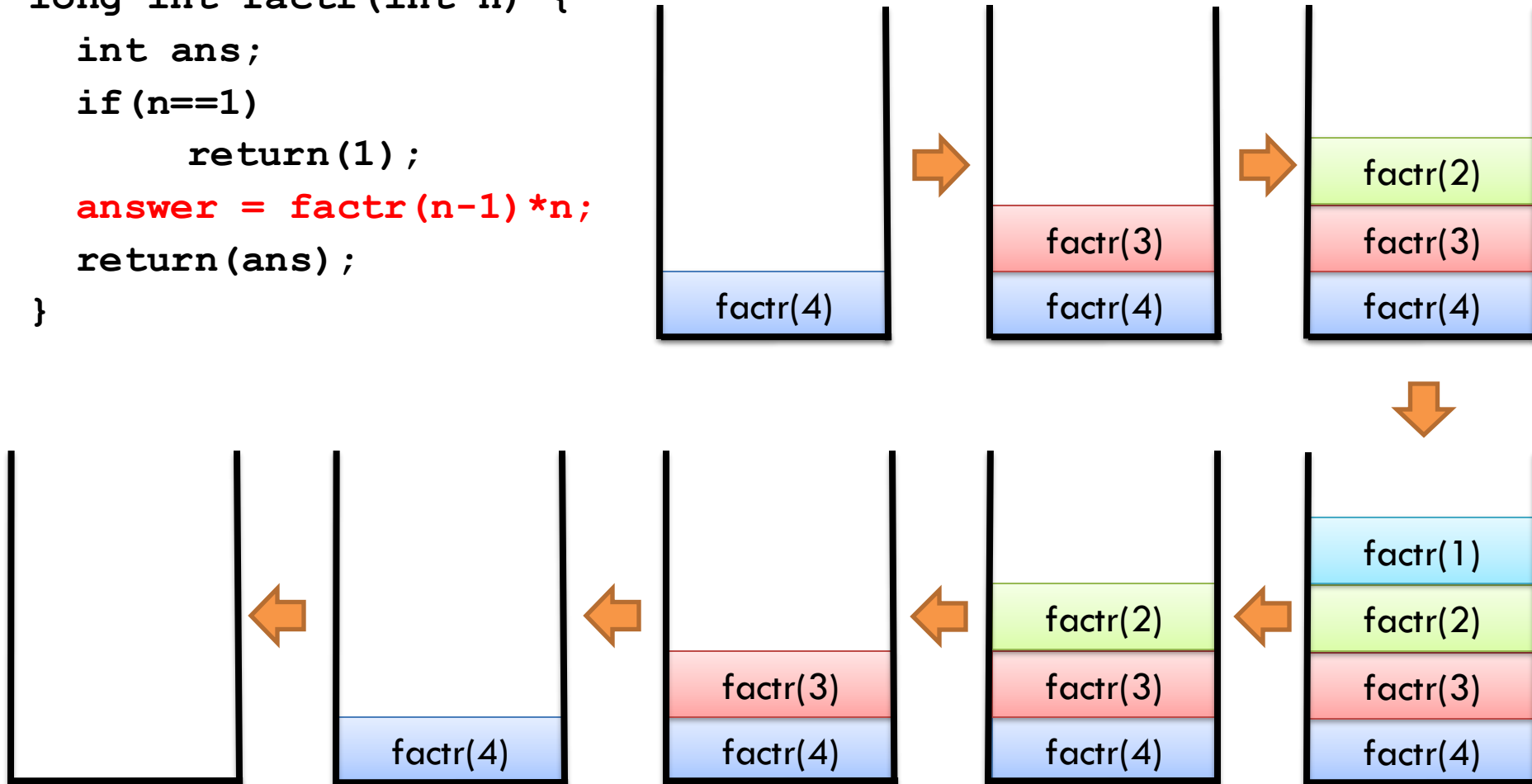
- When a function calls itself, a new set of local variables and parameters are allocated storage on the stack, and the function code is executed from the top with these new variables.
- A recursive call does not make a new copy of the function. Only the arguments are new.
- As each recursive call returns, the old local variables and parameters are removed from the stack and execution resumes at the point of the function call inside the function.

Recursive Call Stack (Example)



factr(4)

```
long int factr(int n) {  
    int ans;  
    if (n==1)  
        return(1);  
    answer = factr(n-1)*n;  
    return(ans);  
}
```



Another Example



```
int main()
{
    static int i=5;
    if (--i){
        printf("%d ",i);
        main();
    }
}
```

Cons of recursion



- No significant reduction in code size as well as no improvement in memory utilization.
- Also, the recursive versions of most routines may execute a bit slower than their iterative equivalents because of the overhead of the repeated function calls.
- In fact, many recursive calls to a function could cause a stack overrun.

Pros of recursion



- The main advantage to recursive functions is that you can use them to create clearer and simpler versions of several algorithms.
- For example, the MergeSort and the Quicksort are quite difficult to implement in an iterative way. Also, some problems, especially ones related to artificial intelligence, lend themselves to recursive solutions.
- Finally, some people seem to think recursively more easily than iteratively.

Precaution



- When writing recursive functions, you must have an **if** statement somewhere to force the function to return without the recursive call being executed.
- If you don't, the function will never return once you call it.

Exercise



Write a function:

`count(int number, int array, int Size)`

that counts the number of times number appears in array. The array has Size elements. The function should be recursive. Write a test program to test it.



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Thank you
Q & A