

Johnson Algorithm

Parallel Implementation in Rust

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Killamsetty Bhagyaraj - IIT2013042 Vishnu Ks - IIT2013075

Overview

Johnson's algorithm is a way to find the shortest paths between all pairs of vertices in a sparse, edge weighted, directed graph. It allows some of the edge weights to be negative numbers, but no negative-weight cycles may exist.

Goals

- 1. Formulate a parallel approach for Johnson algorithm and implement in Rust
- 2. Analyze and improve the performance.

Algorithm

```
procedure JOHNSON_SINGLE_SOURCE_SP(V, E, s)
1.
2.
         begin
3.
              Q := V;
4.
              for all v \in Q do
5.
                   l[v] := \infty;
6.
              l[s] := 0;
7.
              while Q \neq \emptyset do
8.
              begin
9.
                   u := extract\_min(Q);
10.
                   for each v \in Adj[u] do
                       if v \in Q and l[u] + w(u, v) < l[v] then
11.
12.
                            l[v] := l[u] + w(u, v);
13.
              endwhile
         end JOHNSON_SINGLE_SOURCE_SP
14.
```

Implementation in Rust

```
while let Some(que_node { cost , vertex }) = heap.pop() {
   if cost > distance[vertex as usize] {
      continue;
   }

   for i in 0..nodes {
      let mut weigh = adj_matrix[vertex as usize][i as usize];
      if(i != vertex && weigh != 0 ){
        let next = que_node { cost: cost + weigh, vertex: i };
        if next.cost < distance[next.vertex as usize] {
            heap.push(next);
            distance[next.vertex as usize] = next.cost;
      }
    }
}</pre>
```

The algorithm

Parallelizing Step

How to run the code

```
git clone <a href="https://github.com/praneelrathore/etig">https://github.com/praneelrathore/etig</a>
cd etig/src
uncomment parallel::johnson(&mut gra, na);
cargo build
cargo run input_file
Make sure the main.rs contains extern crate algorithms; use algorithms::parallel;
```

Sample Input and Output

```
/rust-algo master*
) more input.in
5
3 1 0 0 3
1 4 4 2 4
2 1 0 4 3
2 2 4 0 2
0 0 2 0 0

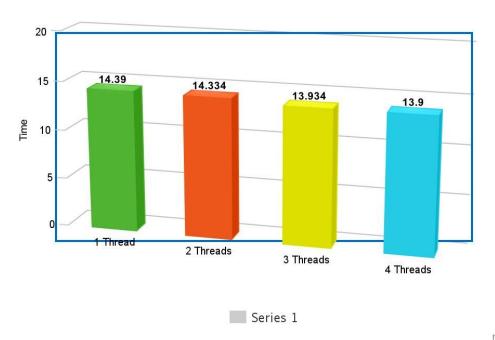
/rust-algo master*
) cargo run input.in
    Running `target/debug/etig input.in`
min distance of 0 = 0
min distance of 1 = 1
min distance of 2 = 5
min distance of 3 = 3
min distance of 4 = 3
```

Analysis of Performance

Nodes = 500

Threads	Time Taken
1	14.39
2	14.33
3	13.93
4	13.90

Time Vs Parallel Threads 500 Nodes



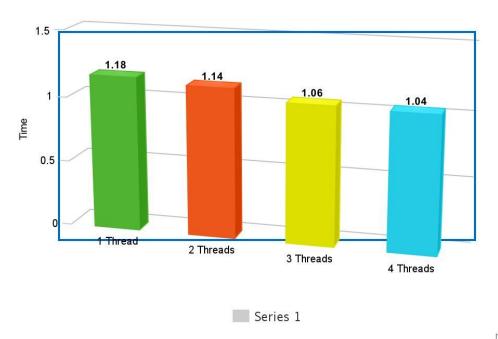
meta-chart.com

Analysis of Performance

Nodes = 100

Threads	Time Taken
1	1.18
2	1.14
3	1.06
4	1.04

Time Vs Parallel Threads 100 Nodes



meta-chart.com

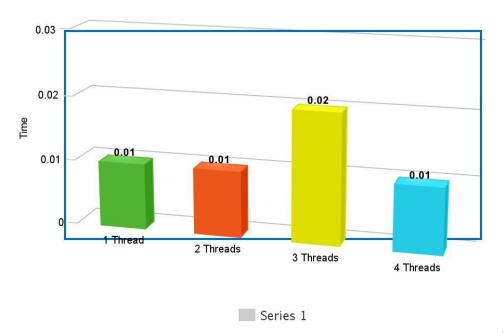
Analysis of Performance

Nodes = 10

Thread creation overhead comes to play as time for 3 threads became greater than for 2

Threads	Time Taken
1	0.01
2	0.01
3	0.02
4	0.01

Time Vs Parallel Threads 10 Nodes



Time Complexity

Without parallelization

The time complexity of this algorithm, using Fibonacci heaps in the implementation of Dijkstra's algorithm, is $O(V2log\ V\ +\ VE)$ and $O(V\ log\ V\ +\ E)$ for each of V instantiations of Dijkstra's algorithm. Thus, when the graph is sparse, the total time can be faster than the Floyd–Warshall algorithm, which solves the same problem in time O(V3).

After Parallelization

The time complexity after parallelization is

$$O(K2 * LogV + KE) + O(K * Log V + V)$$

K = V / NO OF THREADS

V = No of Vertices