

Ques Search in a rotated sorted array.

→ 2, 4, 8, 10, 15

distinct
elements.

$k = 1$, 15, 2, 4, 8, 10

$k = 2$, 10, 15, 2, 4, 8, $x = 2$.

rotated

→ 2, 4, 8, 10, 15

unrotated.

if array is rotated

if $(A[0] > A[m-1])$

yes

else

no

Binary Search →

2

4 5 8 10 1 2 3

if largest element idx is given,

apply B.S. (0, p) & (p+1 to n-1).

Twist:- if largest element idx is not given,

find local maxing using B.S.
 $p \leftarrow$
 4 5 8 10 1 2 3
 then, apply B.S. in both the parts.

Twist:- Do it in 1 B.S.

1 2
 4 5 8 10 1 2 3

Part 1 > Part 2

X,
 $x < 0^{th}$ element
 Part 2
 3 element
 Part 1
 3

Get mid find in which part our middle is and in which part our target, is if both are in different parts, will move mid towards the target else apply normal binary search

m
↓
h

$k = 20$

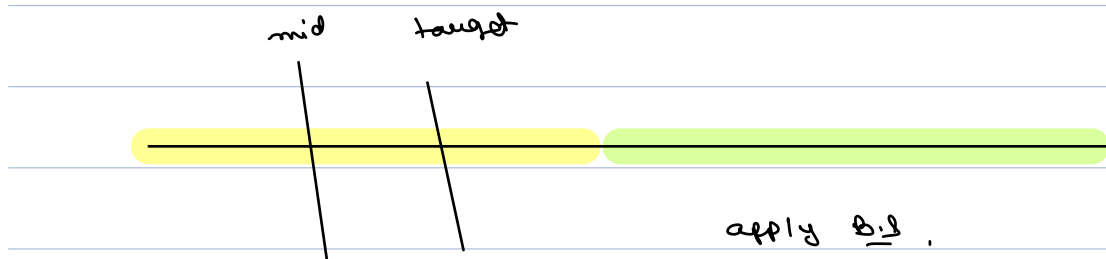
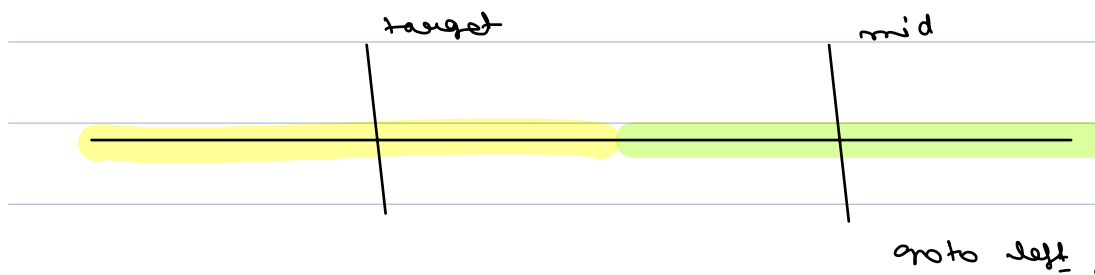
0	1	2	3	4	5	6	7	8	9	10	11
10	20	30	1	2	3	4	5	6	7	8	9

lo	hi	mid	mid Area	Target Area
0	11	5	2	1 goto left
0	4	2	1	1 goto left
0	1	0	1	1 go right
1	1	1	return mid.	

m $k = 60$
↓
h

0	1	2	3	4	5	6
70	80	90	100	40	50	60

lo	hi	mid	mid Area	Target Area
0	6	3	1	2 goto right
4	6	5	2	2 more right
6	6	found.		



$l = 0, \quad r = n - 1$

while ($l \leq r$) {

$m = \frac{l + (r - l)}{2}$

if ($A[m] == target$) {

return m;

if ($target < A[r]$) { // target \rightarrow Part 2

```
if (A[mid] >= A[0]) { // mid → part 1
```

```
    lo = mid + 1;
```

```
else { // mid → part 2
```

```
    if (A[mid] < target) {
```

```
        lo = mid + 1;
```

```
    } else {
```

```
        hi = mid - 1;
```

```
    } else { // target → part 1.
```

```
if (A[mid] < A[0]) { // mid → part 2
```

```
    hi = mid - 1;
```

```
else { // mid → part 1
```

```
    if (A[mid] < target) {
```

```
        lo = mid + 1;
```

```
    } else {
```

```
        hi = mid - 1;
```

T.C → $O(\log n)$

S.C → $O(1)$

Ques Given +ve N , find $\text{sqr}(\text{w})$

int pow

$\text{floor}(\text{sqr}(\text{w}))$

$\text{sqr}(25) \rightarrow 5$

$\text{sqr}(20) \rightarrow 4$

$\text{sqr}(10) \rightarrow 3$

$i = 1$; ①

while ($i*i \leq N$) {

$\text{ans} = i$
 $i++$
}

$N = 20$

T.C $\rightarrow O(\sqrt{N})$

S.C $\rightarrow O(1)$

BB :-

Target $\rightarrow \text{floor}(\text{sqr}(\text{w}))$

Search Space $\rightarrow 1$ to N

Case-1

$\text{mid} * \text{mid} = N$

return mid

Case-2

$\text{mid} * \text{mid} > N$

goto left

Case-3

$\text{mid} * \text{mid} < N$

$\text{ans} = \text{mid}$

goto right

$$\underline{n = 50}$$

$$ans = 7$$

J	hi	m		
1	50	25	$25 \times 25 > 50$	move left
2	24	12	$12 \times 12 > 50$	move left
3	11	6	$6 \times 6 < 50$	ans = 6 move right
4	11	9	$9 \times 9 > 50$	move left
5	8	7	$7 \times 7 < 50$	ans = 7 move right
6	8	8	$8 \times 8 > 50$	move left
7	7		Break	

$$T.C \rightarrow O(\log n)$$

$$S.C \rightarrow O(1)$$

Ath Magical Number

multiples of 3 [1 100]

$$\rightarrow \frac{100}{3} = 33$$

4 from [1 100]

$$\rightarrow \frac{100}{4} = 25$$

6 from [1 100]

$$\rightarrow \frac{100}{6} = 16$$

4 or 6 from [1 100]

$$\frac{100}{4} + \frac{100}{6} - \frac{100}{12} \rightarrow \text{LCM}$$

4 → 4 8 12 16 20 24 ...
6 → 6 12 18 24 30 ...

no. of multiples of A or

$$B \text{ from } 1 \text{ to } x \rightarrow \frac{x}{A} + \frac{x}{B} - \frac{x}{\text{LCM}(A, B)}$$

Ques

A, B & C \rightarrow ^{find} $2^{A^{th}}$ Magical no.

\rightarrow A no. is said to be magical if it is divisible by B or C.

B	C	A
2	3	8

2, 3, 4, 6, 8, 9, 10, 12

\rightarrow

B	C	A
4	6	5

4, 6, 8, 12, 16

1) Brute force.

count = 0;

for (i=1; ; i++) {

if (i % B == 0 || i % C == 0) {

count++;

if (count == A) {

return i;

}

3

3

1) Search Space

$$[\min(b, c), \min(b, c) * A]$$

2) Target \rightarrow Ath Magical number.

B	C	A
4	6	10

is 36 my 10th magical no?

$$\frac{36}{4} + \frac{36}{6} - \frac{36}{12} = 12$$

no left

$$\begin{array}{ccc} 36 & 37 & 38 \\ \times & \times & \times \end{array}$$

is 24 my 10th magical no?

$$\frac{24}{4} + \frac{24}{6} - \frac{24}{12} = 8$$

goto right.

Tracing, d, c, A
5 7 9

lo	hi	mid	
5	20	12	$\frac{12}{5} + \frac{12}{7} - \frac{12}{35} = 9$ move right,

13	20	16	$\frac{16}{5} + \frac{16}{7} - \frac{16}{35} = 5$ move left,
----	----	----	---

13	15	14	$\frac{14}{5} + \frac{14}{7} - \frac{14}{35} = 4$ ans = 4 move left,
----	----	----	---

13	13	13	$\frac{13}{5} + \frac{13}{7} - \frac{13}{35} = 9$ onto right
----	----	----	--

14	13	<u>break</u>	
----	----	--------------	--

$$b = 5, c = 7, a = 3 \quad \downarrow$$

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	0	0	1	1	2	2	2	3	3	3	3	4	5

Ans Magical No (A, B, C) :

$$lo = \min(b, c);$$

$$hi = A * \min(b, c);$$

$$len = len(b, c);$$

while $(lo <= hi)$:

$$m = lo + \frac{(hi - lo)}{2}$$

$$int co = \frac{m}{b} + \frac{m}{c} - \frac{m}{lcm}$$

if $(co < A)$:

$$lo = m + 1;$$

else if $(co > A)$:

$$hi = m - 1;$$

else :

$$ans = m;$$

$$hi = m - 1;$$

return ans;

$$T.C \rightarrow O(\log(\min(b, c) * a))$$

$$S.C \rightarrow O(1)$$

Due

Median of two Sorted Arrays ,

→ Most Important

1) Just after the class → add recording ,

2) Next class → doubt session ,