

Definition :- 2d array , rectangular grid, where each number is an element.

int mat[N][M];
↓ ↗ rows ↘ cols
Type
 ↓
 variable name.

	0	1	2
0			
1			
2			

mat[3][3]
↓
9 elements.

	0	1	2	...	m-1
0					
1					
2					
...					
...					
n-1					

int mat[N][M]

→ 0, m-1

→ mat[n-1][m-1]

Ques

2d matrix $[n][m]$, print row wise sum.

mat[3][4] =

	0	1	2	3
0	1	2	3	4
1	5	6	7	8
2	9	10	11	12

o/p \rightarrow

10
26
42

```
for (i=0; i<n; i++) {  
    sum = 0;  
    for (j=0; j<m; j++) {  
        sum += mat[i][j];  
    }  
    Print (sum);  
}
```

T.C $\rightarrow O(nm)$

S.C $\rightarrow O(1)$

Ques

2d matrix [n][m], Print col wise sum.

mat[3][4] =

	0	1	2	3
0	1	2	3	4
1	5	6	7	8
2	9	10	11	12

o/p → 15
18
21
24

for (col = 0; col < m; col++) { T.C → O(m * m)
S.C → O(1).

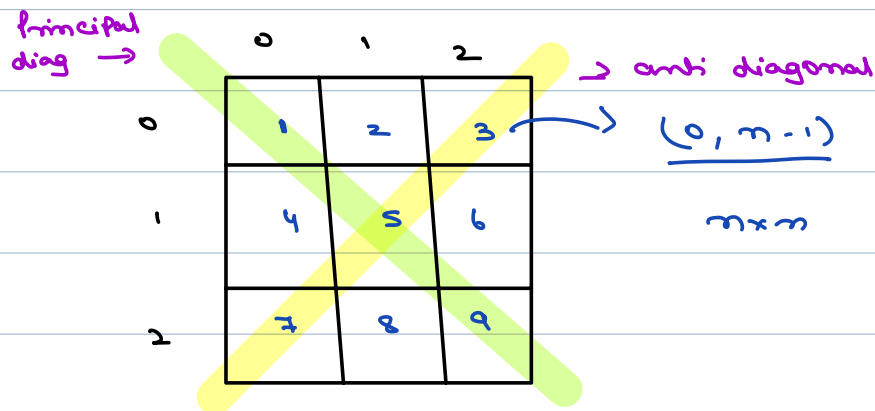
sum = 0;

for (row = 0; row < n; row++) {

sum += mat[row][col];

print(sum);

Ques Given 2d mat $[n][n]$, Print 1) Principal diag.
square matrix. 2) Anti diagonal



1) Print Principal diagonal

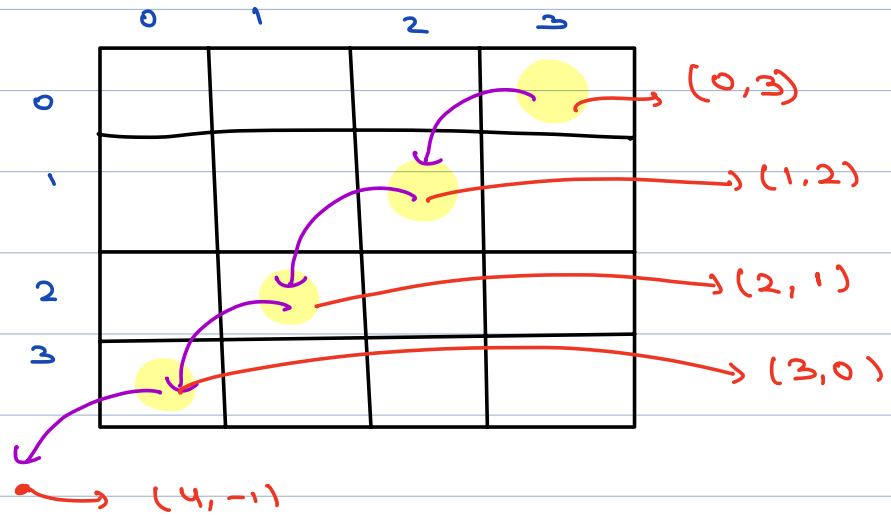
```
i = 0;
T.C  $\rightarrow O(n)$ 
S.C  $\rightarrow O(1)$ 
while (i < n) {
    Print (mat[i][i]);
    i++;
}
```

2) Print anti diagonal element,

```
i = 0, j = n-1
while (i < n && j >= 0) {
    Print (mat[i][j]);
    i++;
    j--;
}
```

\rightarrow only one condⁿ is enough.

3
11



T.C $\rightarrow O(m)$

S.C $\rightarrow O(1)$

Ques

given 2d matrix $n \times m$, print all the diagonals from right to left.

mat[3][4] =

	0	1	2	3
0	1	2	3	4
1	5	6	7	8
2	9	10	11	12

o/p:-

1

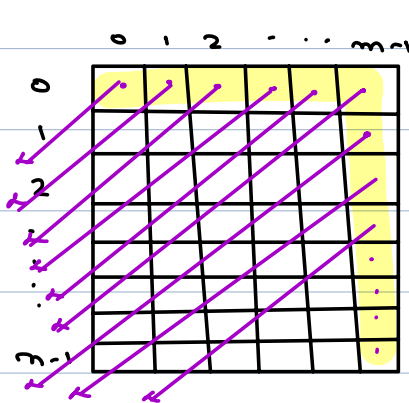
2 5

3 6 9

4 7 10

8 11

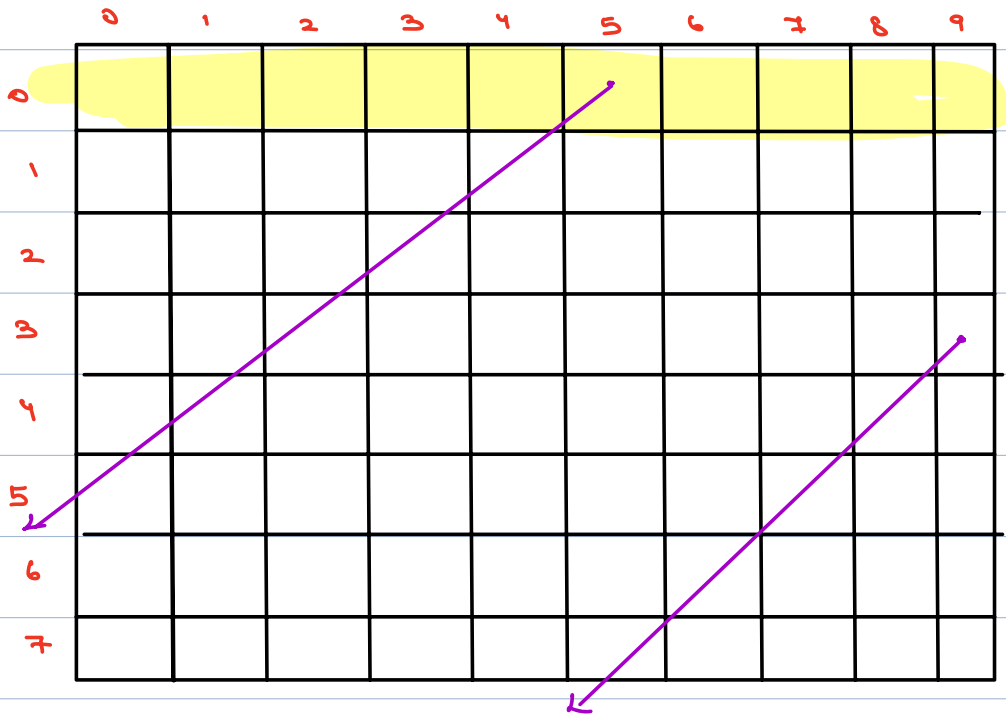
12



int mat[N][M]

$M+N-1$
 \downarrow
R to ↓ diagonals

int mat[4][5] = 4+5-1 = 8 R to 1
diag.



$(0,5) \rightarrow (1,4) \rightarrow (2,3) \rightarrow (3,2) \rightarrow (4,1) \rightarrow (5,0) \rightarrow (6,-1)$
 $(3,9) \rightarrow (4,8) \rightarrow (5,7) \rightarrow (6,6) \rightarrow (7,5) \rightarrow (8,4)$

```
for ( col = 0; col < m; col++ ) {
```

```
    i = 0; j = col;
```

```
    while ( i < n && j >= 0 ) {
```

```
        print (mat[i][j]);
```

```
        i++;
```

```
        j--;
```

```
    }
```

```
}
```

```
for ( row = 1; row < n; row++ ) {
```

```
    i = row
```

```
    j = m - 1;
```

```
    while ( i < n && j >= 0 ) {
```

```
        print (mat[i][j]);
```

```
        i++;
```

```
        j--;
```

```
    }
```

```
}
```

T.C $\rightarrow O(\underline{n \times m})$

S.C $\rightarrow O(\underline{1})$.

Ques

Given a 2d matrix $[N][N]$,

find transpose.

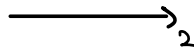
↳ Square matrix

	0	1	2
0	1	2	3
1	4	5	6
2	7	8	9



	0	1	2
0	1	4	7
1	2	5	8
2	3	6	9

	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25



	0	1	2	3	4
0	1	6	11	16	21
1	2	7	12	17	22
2	3	8	13	18	23
3	4	9	14	19	24
4	5	10	15	20	25

$mat[i][j] \Rightarrow mat[j][i]$


```
for (i=0; i < n; i++) {
```

```
    for (j=i+1; j < n; j++) {
```

```
        swap(mat[i][j], mat[j][i]);
```

	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25

i	j	
0	(1 n-1)	n-1
1	(2 n-1)	n-2
2	(3 n-1)	n-3
3	(4 n-1)	n-4
...		...
n-1	1	0

$$1 + 2 + 3 + \dots + (n-1)$$

$$1 + 2 + 3 + \dots + n \Rightarrow \frac{n(n+1)}{2}$$

$$1 + 2 + 3 + \dots + (n-1)$$

$$\frac{(n-1)n}{2} \Rightarrow O(n^2)$$

T.C

$$S.C \rightarrow O(1)$$

Ques Rotate 90° clockwise, $mat[N][N]$

	0	1	2
0	1	2	3
1	4	5	6
2	7	8	9



	0	1	2
0	7	4	1
1	8	5	2
2	9	6	3

	0	1	2
0	7	4	1
1	8	5	2
2	9	6	3

	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25



	0	1	2	3	4
0	21	16	11	6	1
1	22	17	12	7	2
2	23	18	13	8	3
3	24	19	14	9	4
4	25	20	15	10	5

	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25



	0	1	2	3	4
0	1	6	11	16	21
1	2	7	12	17	22
2	3	8	13	18	23
3	4	9	14	19	24
4	5	10	15	20	25

Transpose

$O(n^2)$

	0	1	2	3	4
0	1	6	11	16	21
1	2	7	12	17	22
2	3	8	13	18	23
3	4	9	14	19	24
4	5	10	15	20	25

reverse

every row.

$O(n^2)$

T.C $\rightarrow O(n^2)$, S.C $\rightarrow O(1)$.

Transpose + Reverse Every Row = Rotate 90° .

↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓

$m \times n$

$$\begin{bmatrix} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \\ 9 & 10 & 11 & 12 \end{bmatrix}_{3 \times 4} \xrightarrow{T} \begin{bmatrix} 1 & 5 & 9 \\ 2 & 6 & 10 \\ 3 & 7 & 11 \\ 4 & 8 & 12 \end{bmatrix}_{4 \times 3}$$

10, 20, 30, 40, 50
 $pf[] = 10 \quad 30 \quad 60 \quad 100 \quad 150$
 $df[] = 150 \quad 140 \quad 120 \quad 90 \quad 50$

$pf[i] = \text{sum } 10 \text{ to } i$
 $df[i] = \text{sum } (i \text{ to } n-1)$

diff b/w $n+m$, $n \times m$
 $n=10, m=5$

for ($i=0; i < n; i++$) {
 $\text{print}(-)$ // 10 times
 3
 for ($i=0; i < m; i++$) {
 $\text{print}(-)$ // 5 times
 3
 $n+m$
 $\Rightarrow 15 \text{ times}$

for ($i=0; i < n; i++$) {
 for ($i=0; i < m; i++$) {
 $\text{print}(-)$
 3
 $n \times m$
 $\Rightarrow 50 \text{ times}$

$$1 + 2 + 3 + \dots + n = \frac{n(n+1)}{2}$$

$$\textcircled{5} \rightarrow \frac{5(5+1)}{2}$$

$$\textcircled{10} \rightarrow \frac{10(10+1)}{2}$$

$$(n-1) \rightarrow \frac{(n-1)(n-1+1)}{2} = \frac{(n-1)n}{2} \Rightarrow \frac{n^2 - n}{2}$$

$$\cancel{\frac{n^2}{2}} - \cancel{\frac{n}{2}} \Rightarrow \underline{0(n^2)}$$