

# Variable selection using Stepwise Procedure

Srikar

2021-09-09

## Introduction:

Multiple regression is a statistical technique that can be used to analyze the relationship between a single dependent variable and several independent variables. The objective of multiple regression analysis is to use the independent variables whose values are known to predict the value of the single dependent value. Each predictor value is weighed, the weights denoting their relative contribution to the overall prediction.

R-squared (R<sup>2</sup>) is a statistical measure that represents the proportion of the variance for a dependent variable that's explained by an independent variable.

The P value is defined as the probability under the assumption of no effect or no difference (null hypothesis), of obtaining a result equal to or more extreme than what was actually observed. The P stands for probability and measures how likely it is that any observed difference between groups is due to chance.

Stepwise regression is the step-by-step iterative construction of a regression model that involves the selection of independent variables to be used in a final model. It involves adding or removing potential explanatory variables in succession and testing for statistical significance after each iteration.

## Objective:

- 1) To test the regressors using stepwise procedure
- 2) To predict the weight of the fish using the given regressors

## Data Description:

This dataset is a record of a certain type of fish known as Perch Fish. It contains 5 independent variables and 1 dependent variable i.e., the weight of the fish (in grams). The dependent variables are type of species, vertical length (in cms), diagonal length (in cms), cross length (cms), height and width (in cms), The dataset contains a sample of 50 fishes in a market.

```
library(readxl)
dat<- read_excel("C:/Users/Srikar/Desktop/SS/R/Sem 5/Linear Regression/Practical 5/Data.xlsx")
head(dat,10)
```

	Length1	Length2	Length3	Height	Width	Weight
	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>
1	23.2	25.4	30	11.5	4.02	242
2	24	26.3	31.2	12.5	4.31	290
3	23.9	26.5	31.1	12.4	4.7	340
4	26.3	29	33.5	12.7	4.46	363
5	26.5	29	34	12.4	5.13	430
6	26.8	29.7	34.7	13.6	4.93	450
7	26.8	29.7	34.5	14.2	5.28	500
8	27.6	30	35	12.7	4.69	390
9	27.6	30	35.1	14	4.84	450
10	28.5	30.7	36.2	14.2	4.96	500

```
names(dat)
```

```
## [1] "Length1" "Length2" "Length3" "Height" "Width" "Weight"
```

Here the column names represent the following:

Length1 - Vertical Length  
Length2 - Diagonal Length  
Length3 - cross Length  
height - Height  
Width – Width

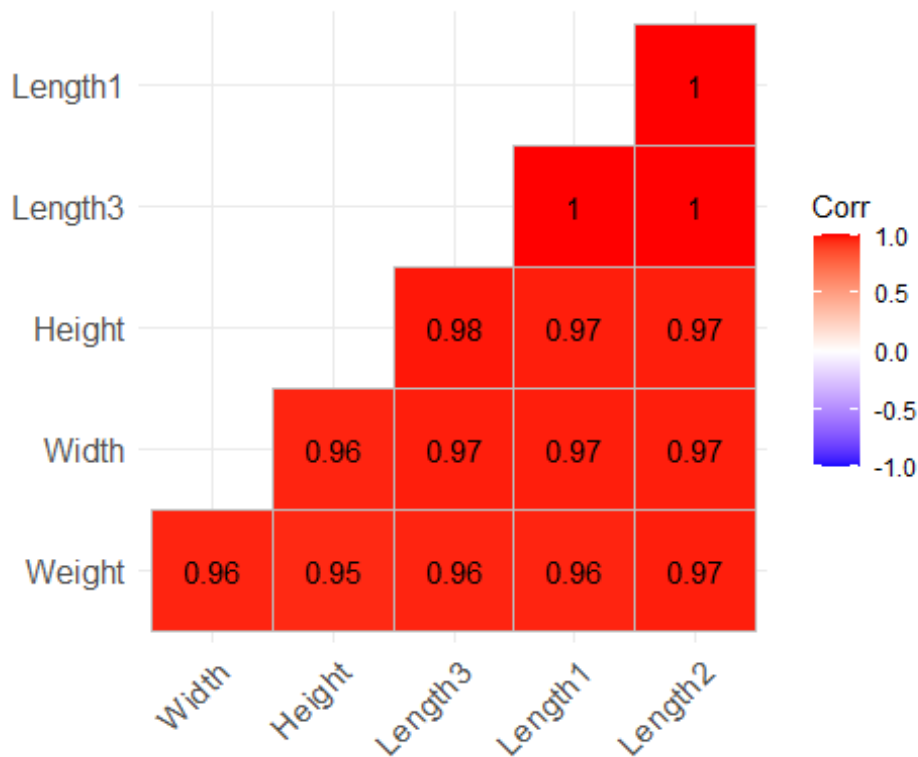
## Procedure:

### 1) Visualizing the correlation matrix

```
r=cor(dat)

library(ggplot2)
library(ggcorrplot)
ggcorrplot(r, hc.order = TRUE, type = "lower", lab = TRUE)
```

Correlation Plot



We can observe that all the variables have high correlation ship with each other and especially with the dependent variable. The correlation value is above 0.90 which shows high correlation with the dependent variable, Weight.

## 2) Constructing the regression model

```
mod=lm(dat$Weight~.,data=dat)
```

The model obtained is:

$$Y = -515.24 + 10.53X_1 + 102.73X_2 - 98.25X_3 + 49.49X_4 + 79.76X_5$$

where  $X_1, X_2, X_3, X_4$  and  $X_5$  are Length1, Length2, Length3, height and Width respectively.

```
summary(mod)
```

```
##  
## Call:  
## lm(formula = dat$Weight ~ ., data = dat)
```

```
##
```

Residuals Table				
Min	1Q	Median	3Q	Max
-170.655	-32.194	-8.474	33.177	176.274

```
##
```

Regresssion Coefficients Table					
	Estimate	Std.Error	t-value	P-value	Significance Code
(Intercept)	-515.24	92.19	-5.589	1.35E-06	***
Length1	10.53	47.25	0.223	0.824699	
Length2	102.73	50.01	2.054	0.045928	*
Length3	-98.25	26.95	-3.645	0.000702	***
Height	49.49	15.44	3.205	0.002515	**
Width	79.76	39.23	2.033	0.048072	*

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
```

```
## Residual standard error: 62.94 on 45 degrees of freedom
```

```
## Multiple R-squared:  0.9574, Adjusted R-squared:  0.9527
```

```
## F-statistic: 202.5 on 5 and 45 DF,  p-value: < 2.2e-16
```

We see that that range of residuals is large which means that values (in grams) will differ from the observed value.

We observe that the intercept p-value is below the significance value (0.05) and hence we can say that the intercept is significant in the prediction. This means that if the values of t

he regressors were all zero, the intercept would tell us the mean estimate of the dependent variable (Weight). Since height, width and length of fish can't be 0, the intercept value has no real meaning.

The p-values of all the regressors except length1 show significance. That means these variables describe the linear relationship with the independent variable. Since most of the variables show significance, we can say that model is a good fit. Also the overall p-value is also lesser than significance level (0.05) and hence we can say that the model is a good fit.

The R-squared value 0.9574 which means that 95.74% of the variation is explained by the regressors. The adjusted R-Squared shows the variation explained by the regressors that truly contribute to the known variation.

To find out which variables really contribute to the model, we can test it out by backward elimination method

## #2) Using stepwise procedure to find the best regressors

```
step(mod, direction="both")
```

```
## Start: AIC=428.12
## dat$Weight ~ Length1 + Length2 + Length3 + Height + Width
##
##           Df Sum of Sq    RSS    AIC
## - Length1  1         201 178452 426.17
## <none>                        178251 428.12
## - Width    1        16750 195001 430.70
## - Length2  1        17094 195345 430.79
## - Height   1        41615 219865 436.82
## - Length3  1        53836 232086 439.58
##
## Step: AIC=426.17
## dat$Weight ~ Length2 + Length3 + Height + Width
##
##           Df Sum of Sq    RSS    AIC
## <none>                        178452 426.17
## + Length1  1         201 178251 428.12
## - Width    1        17835 196286 429.03
## - Height   1        48361 226813 436.40
## - Length3  1        55040 233492 437.88
## - Length2  1        74915 253367 442.05
```

```
##
## Call:
## lm(formula = dat$Weight ~ Length2 + Length3 + Height + Width,
##
```

	Regression Coefficient Table of New Model:			
(Intercept)	Length2	Length3	Height	Width
-521.02	112.24	-96.94	47.98	76.55

#We observe that only Width, lenght2 and height and length3 truly give the estimate values. Using only these variables and excluding length1, we will construct a new model.

### 3) Constructing the new regression model

```
nmod=lm(dat$Weight~dat$Length2+dat$Length3+dat$Height+dat$Width)
```

The new model obtained is:

$$Y = -521.02 + 112.24X_1 - 96.94X_2 + 47.98X_3 + 76.55X_4$$

where X1,X2,X3 and X4 are Length2,Length3,height and Width respectively.

```
summary(nmod)
```

```
##
## Call:
## lm(formula = dat$Weight ~ dat$Length2 + dat$Length3 + dat$Height +
##      dat$Width)
##
```

Residuals:				
Min	1Q	Median	3Q	Max
-170.655	-32.194	-8.474	33.177	176.274

	Regresssion Coefficients Table				
Estimate	Std.	Error	t-value	P-Value	Significance Code
(Intercept)	-521.02	87.53	-5.953	3.67E-07	***
dat\$Length2	112.24	25.82	4.346	7.81E-05	***
dat\$Length3	-96.94	26.02	-3.726	0.000542	***
dat\$Height	47.98	13.74	3.492	0.001086	**
dat\$Width	76.55	36.1	2.121	0.039492	*

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 62.28 on 46 degrees of freedom
## Multiple R-squared:  0.9574, Adjusted R-squared:  0.9537
## F-statistic: 258.5 on 4 and 46 DF,  p-value: < 2.2e-16
```

**We see that all variables are now significant. The r-squared has also increased since we removed an insignificant factor.**

### #3) Constructing the test data for prediction

```
set.seed(123)
x1<-rnorm(50,29.41)
x2=rnorm(50,33.846)
x3=rnorm(50,12.47)
x4<-rnorm(50,4.80)
df<-data.frame(x1,x2,x3,x4)
```

```
A=predict(nmod,df)
```

```
## Warning: 'newdata' had 50 rows but variables found have 51 rows
```

```
df1=data.frame(dat$Weight,A,dat$Weight-A)
head(df1,10)
```

	Observed	Estimated	Difference
1	242	282.1336	-40.13365
2	290	334.7471	-44.74712
3	340	391.8784	-51.87838
4	363	438.2986	-75.29863
5	430	428.045	1.954956
6	450	478.5225	-28.52254
7	500	552.4795	-52.47949
8	390	420.1983	-30.19833
9	450	486.3316	-36.33162
10	500	477.7511	22.248854

From this table, we can compare the observed and expected values are close to each other . As the R-squared value explains only 95.36 of the variation. The rest of the variation is explained by chance or unknow causes.

## Conclusion:

**The newly obtained model which is the best fit for predicting the weight of the fish is**

**$Y = -521.02 + 112.24X_1 + -96.94X_2 + 47.98X_3 + 76.55X_4$  with an R-squared value of 95.36 of the known variation.**

