

AI1110 Assignment 1

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29 March, 2022

Paper 2018

Q4 (b)

If the straight lines $3x - 5y = 7$ and $4x + ay + 9 = 0$ are perpendicular to one another, find the value of a .

Solution

Given,

The pair of lines $3x - 5y = 7$ and $4x + ay + 9 = 0$ are perpendicular to one another.

Slope of any line of form $ax + by + c = 0$ is $\frac{-a}{b}$

$$\Rightarrow \text{Slope of line } 3x - 5y = 7 = \frac{3}{5}$$

$$\Rightarrow \text{Slope of line } 4x + ay + 9 = 0 = \frac{-4}{a}$$

Since the two lines are perpendicular the product of their slopes should be -1.

So,

$$\frac{3}{5} \cdot \frac{-4}{a} = -1$$

$$\Rightarrow 5a = 12$$

$$\Rightarrow a = \frac{12}{5}$$

So,

The value of a such that the given two lines are perpendicular is:
 $\frac{12}{5}$ or 2.4