

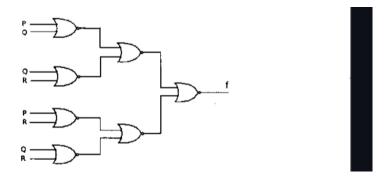
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GATE 2010 CS, 31th Question Analysis

Q.31

What is the boolean expression for the output f of the combinational logic circuit of NOR gates given below?



Solution

Each gate in the circuit is a NOR gate, which performs the operation: $A \downarrow B = \overline{A+B}$

• Gate A:
$$A = \overline{P + Q}$$

• Gate B:
$$B = \overline{Q + R}$$

• Gate C:
$$C = \overline{A + B} = \overline{\overline{P + Q} + \overline{Q + R}}$$

• Gate D:
$$D = \overline{P + R}$$

• Gate E:
$$E = \overline{Q + R}$$

• Gate F:
$$F = \overline{D + E} = \overline{\overline{P + R} + \overline{Q + R}}$$

• Final Output:
$$f = \overline{C + F} = \overline{\overline{P + Q} + \overline{Q + R}} + \overline{\overline{P + R} + \overline{Q + R}}$$

Truth Table

Р	Q	R	$f = \overline{Q + R}$
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	0

Hardware Implementation

The above problem is implemented and tested in hardware using Arduino UNO board. Here we implemented a FSM using the 7474 IC and blinked the LED as per truth table and verified the expression.

Required Components & Pin Connections

S.No	Component
1	Arduino Uno Board
2	Breadboard
3	LEDs (1)
4	7447 IC (1)
5	Seven segment (1)
6	Resistors: 220Ω (2)
7	Jumper Wires
8	USB Cable

Component	Arduino Pin
Input P	Digital 2
Input Q	Digital 3
Input R	Digital 4
Output sevensegment(a)	7447(a)
Output sevensegment(b)	7447(b)
Output sevensegment(c)	7447(c)
Output sevensegment(d)	7447(d)
Output sevensegment(e)	7447(e)
Output sevensegment(f)	7447(f)
Output sevensegment(g)	7447(g)
Output F (LED)	Digital 5
GND	GND
VCC	$\int V$

Code Uploading Steps

- 1. Create a avr-gcc project
- 2. Write The code in main.c in src
- 3. Run the PIO project with command "make hex". It will compile the code and creates .hex file
- 4. Copy the .hex file to ArduinoDriod folder
- 5. connect the Arduino UNO to mobile with OTG cable
- 6. Upload the hex file using "upload precomplied" option
- 7. Observe the ouput and verify the expression

Answer:

$$f = \overline{Q + R}$$

Correct option: (A)