

07.10.85

## UNIT - IV

### Filtering

- \* Removes unwanted signal.
- \* To allow/stop set of frequencies.

→ LPF

→ HPF

→ BPF

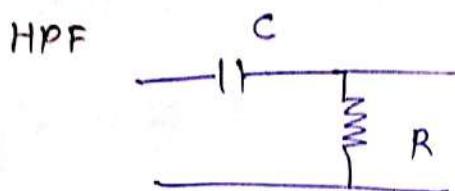
→ BSF

lower order frequencies;

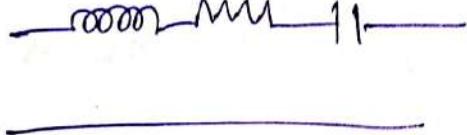
LPF  $\frac{R}{C}$

T or  $\frac{1}{C}$  loops, allows

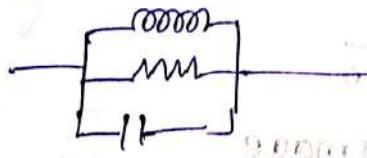
low frequency on  
hence cap takes high  
freq.



BPF



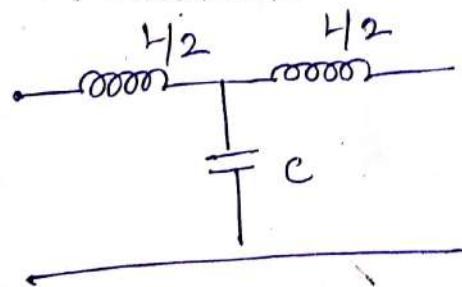
BSF



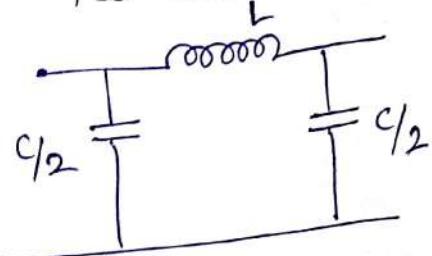
Higher order frequencies

LPF

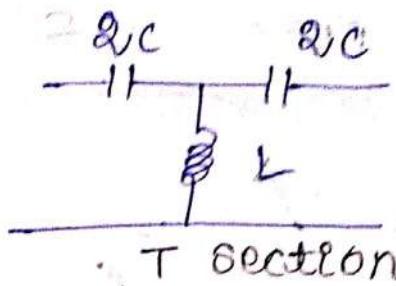
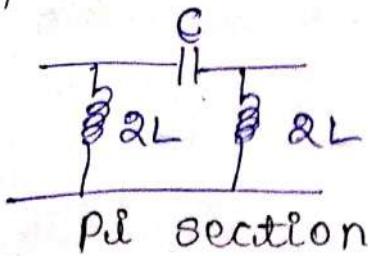
T. section



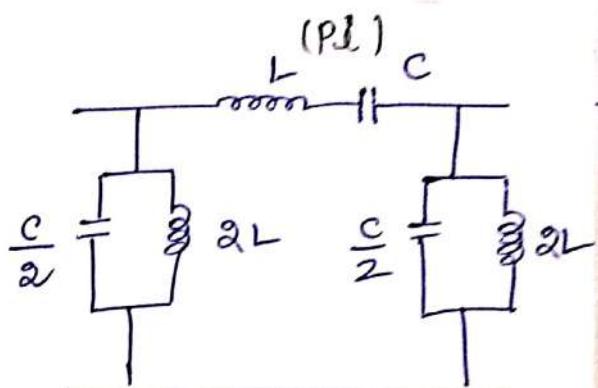
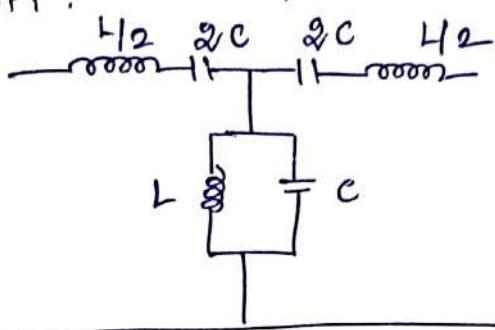
Pi section



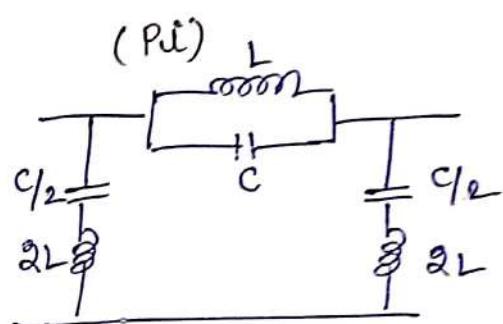
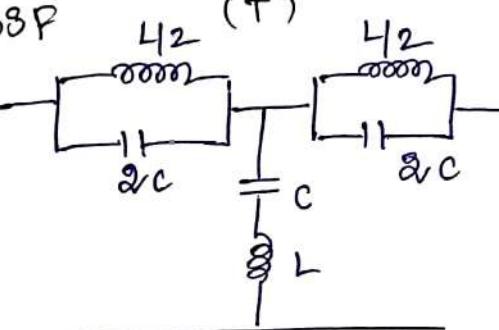
HPF



BPF: (T)



BSP (T)



propagation constant

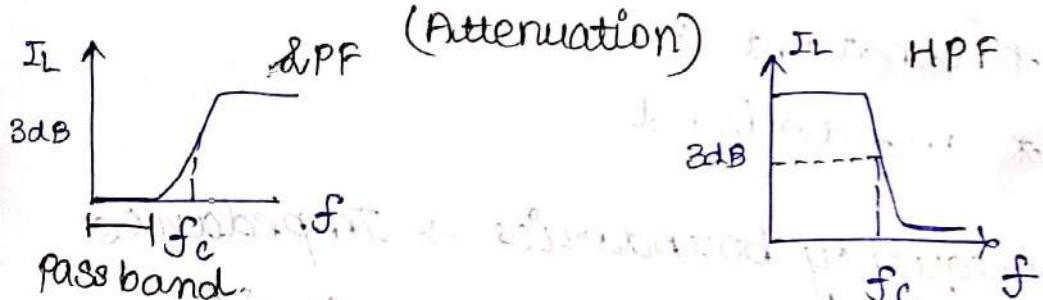
$$\gamma = \alpha + j\beta \quad \alpha = \text{attenuation constant.}$$

$\beta = \text{phase constant}$

pass band  $\alpha = 0$

stop band  $\gamma = \alpha \uparrow$  (higher quantity)

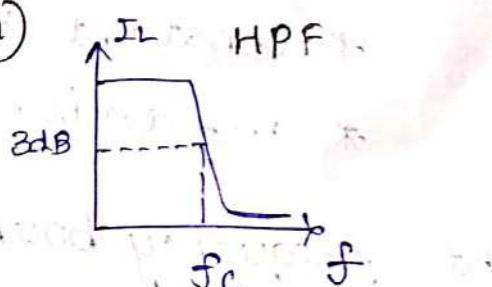
pass band characteristics (wrt insertion loss)



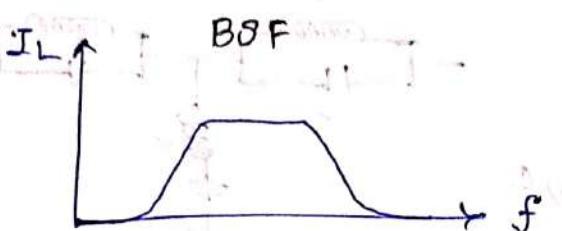
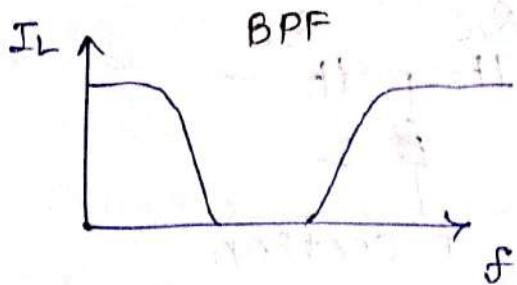
Half power taken (3dB)

Insertion loss less

in pass band

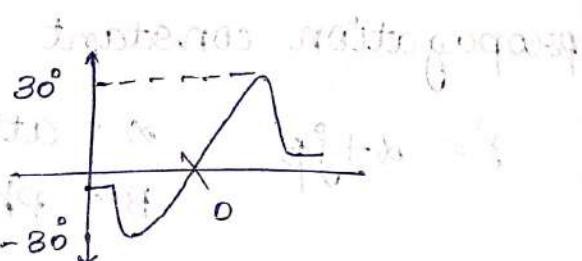
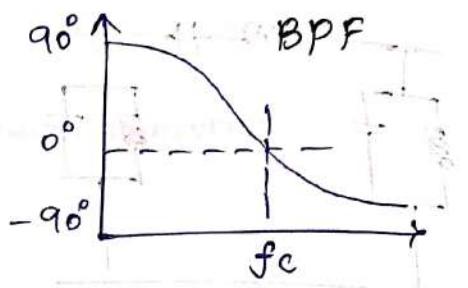
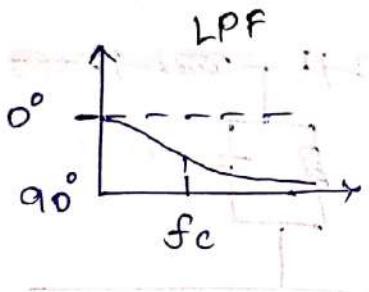


IL is higher



$\therefore$  Realtime loss is more important on purchasing a component if IL w.r.t filter is known.

Phase constant:



With attenuation + phase ~~in BPF band~~ can define pass band characteristics classical methods:

+ Image parameters method

\* constant ( $K_{stability}$ )

\* m - derived

At frequency boundaries  $\rightarrow$  Impedance

match  $\rightarrow$  No reflections  $\rightarrow$  classify

LPF, HPF

- \* Insertion loss method
- \* Tuning for specific frequency.
- \* Involves N/w synthesis for Butterworth and chebyshov.

Impedance Matching :

- \* design filter section T / pi so that input - output impedance match at boundaries ensuring minimum reflections.
- Image parameter methods principles are
  - > Image Impedance
  - > propagation constant.

Let  $Z_{in} = Z_{out} = Z_I \Rightarrow$  symmetrical network.

To find Impedance at input side considering output is matched with Input Impedance (terminated) in Image.



$$Z_{in} = \frac{V_1}{I_1} \quad \begin{array}{l} \text{part 2 terminated with} \\ Z_{I,2} \end{array}$$

$$Z_{out} = \frac{V_2}{I_1} \quad \begin{array}{l} \text{part 1 terminated with} \\ Z_{I,1} \end{array}$$

far series Impedance  $= Z_1$  and,

shunt Impedance  $= Z_2$

Far constant -  $K$

T-section:

$$\text{Image Impedance } Z_I = \sqrt{Z_1 Z_2 + Z_1^2/4}$$

$$\cosh(\gamma) = 1 + \frac{Z_1}{2Z_2}$$

$\Pi$ -section:

$$Z_{\text{img}} = \sqrt{\frac{Z_1}{4} (Z_1 + 4Z_2)}$$

$$\cosh(\gamma) = 1 + \frac{Z_2}{2Z_1}$$

Low pass filter:



series Impedance as  $j\omega L$

shunt Impedance as  $\frac{1}{j\omega C}$

$$Z_{\text{img}} = 50$$

Relation between Input & output

Impedance

$$K^2 = Z_1 Z_2$$

characteristic Impedance  $= K$

$$\omega_c = \frac{1}{\sqrt{LC}}$$

(cut off frequency)

$$K = \sqrt{\frac{L}{C}}$$

$$Z_I = \sqrt{Z_1 Z_2 + Z_1^2/4}$$

$$w_c = \sqrt{j\omega_L \cdot \frac{1}{j\omega_C} + \frac{(j\omega_L)^2}{4}}$$

$$w_c = \frac{1}{\sqrt{Lc}}$$

$w < w_c \Rightarrow$  pass band  $\alpha = 0$

$w > w_c \Rightarrow$  stop band  $\alpha = \text{present}$ .

### HPF

$$w_c = \frac{1}{\sqrt{Lc}}$$

$w < w_c \Rightarrow$  stop band

$w > w_c \Rightarrow$  pass band

### BPF

$$w_1 = \frac{1}{\sqrt{L_1 C_1}} \quad w_2 = \frac{1}{\sqrt{L_2 C_2}}$$

08.10.25

1. design a constant K - T section low pass filter with a cut off frequency of 10MHz with a matched impedance of 50Ω. construct the design to high pass filter

2. design a bandpass filter whose center frequency is 50MHz with a BW of 10MHz terminated with 50Ω impedance.

Design a Band stop filter using the same credential.

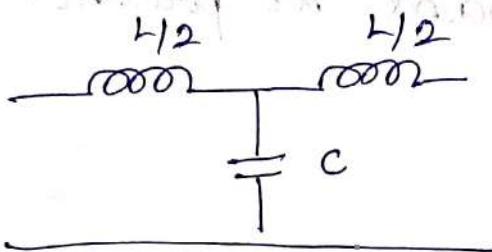
3. construct a low pass and high pass filter using QD credentials

soln

1. T-section:

$$f_c = 10 \text{ MHz} ; R_o = 50 \Omega$$

LPF



$$K = R_o = 50 \Omega$$

$$2\pi f_c = w_c = 2\pi \times 10 \times 10^6 = 62.831 \times 10^6 \text{ rad/s}$$

$$K = Z_1 Z_2 \xrightarrow{\text{series}} \xrightarrow{\text{shunt}}$$

$$= j\omega L \cdot \frac{1}{j\omega C}$$

$$K = \frac{L}{C} \Rightarrow K = \sqrt{\frac{L}{C}} \Rightarrow C = \frac{L}{K^2} \text{ and } L = K^2 C$$

$$w_c = \frac{1}{\sqrt{LC}} \Rightarrow w_c = \frac{1}{\sqrt{K^2 C \cdot C}} = \frac{1}{\sqrt{K^2 C^2}}$$

$$w_c = \frac{1}{K C}$$

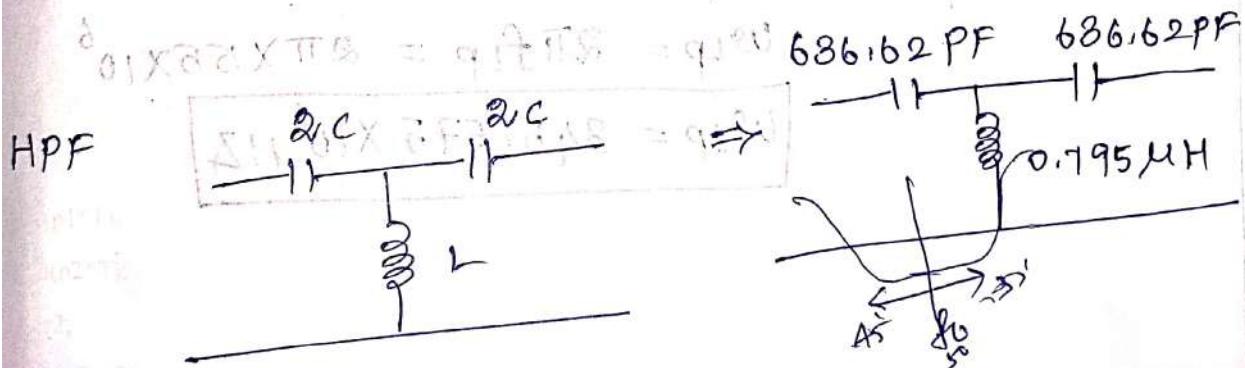
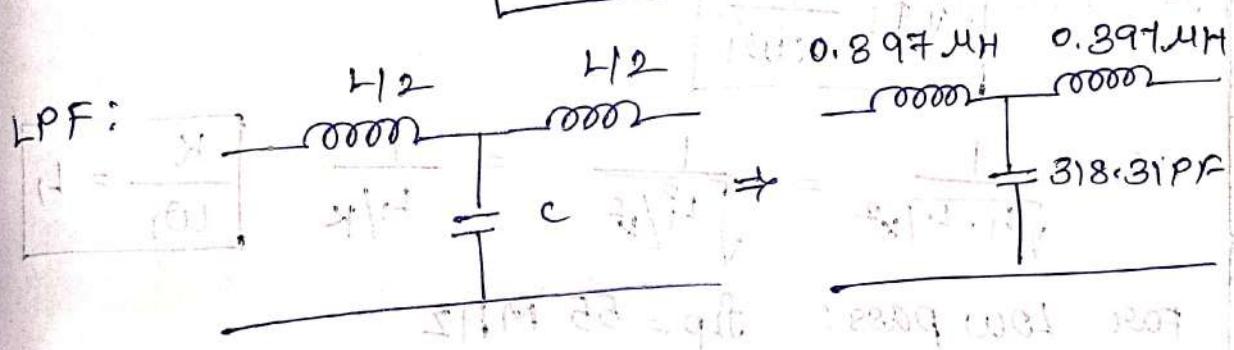
$$\boxed{C = \frac{1}{K w_c}}$$

$$w_c = \frac{1}{\sqrt{L \cdot C / K^2}} = \frac{1}{\sqrt{L^2 / K^2}} = \frac{1}{L/K} = \frac{1}{4K}$$

$$w_c = \frac{K}{L} \Rightarrow L = \frac{K}{w_c}$$

$$C = \frac{1}{50 \times 62.831 \times 10^6} = 318.31 \text{ pF}$$

$$L = \frac{50}{62.831 \times 10^6} = 795.785 \text{ nH}$$



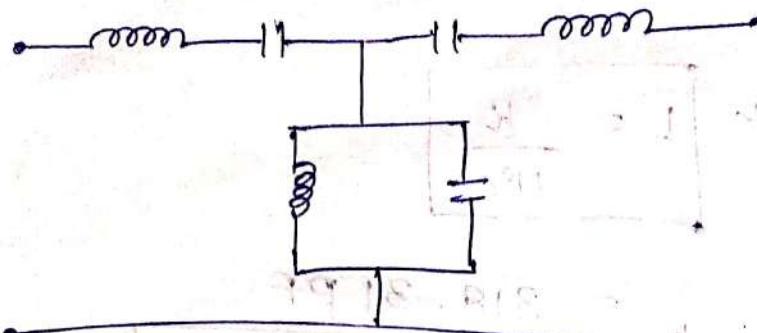
& BPF  $f_0 = 50 \text{ MHz}$   $BW = 10 \text{ MHz}$

$$f_{LP} = 45 \text{ MHz}$$

$$f_{HP} = 55 \text{ MHz}$$

# Constant- $\kappa$ Filter (Bandpass)

⇒ T-section:



$$\kappa^2 = \frac{1}{LC} \Rightarrow \kappa = \sqrt{\frac{1}{LC}} \quad C_1 = \frac{L}{\kappa^2} \quad \text{and} \quad L = \kappa^2 C$$

$$w_1 = \frac{1}{\sqrt{L_1 C_1}} = \frac{1}{\sqrt{L_1 \kappa^2 C_1}} = \frac{1}{\kappa \sqrt{L_1 C_1}}$$

$$C_1 = \frac{1}{\kappa w_1}$$

$$w_1 = \frac{1}{\sqrt{L_1 \cdot 4/\kappa^2}} = \frac{1}{\sqrt{L_1^2/\kappa^2}} = \frac{1}{L_1/\kappa} \quad \frac{\kappa}{w_1} = L_1$$

For low pass:  $f_{LP} = 45 \text{ MHz}$

$$w_{LP} = 2\pi \times 45 \times 10^6$$

$$w_{LP} = 282.74 \text{ MHz}$$

Limitations on constant  $\kappa$

- Amplitudes are not easily shaped (no smooth transition)
- Non linear: phase nearer to cutoff
- Image Impedance are dependable on frequency
- Difficult to match impedances

$$C = \frac{1}{K\omega_c}$$

$$C = \frac{1}{50 \times 2\pi \times 45 \times 10^6}$$

$$C = 70.735 \text{ pF}$$

$$L = \frac{K}{\omega_c}$$

$$= \frac{50}{2\pi \times 45 \times 10^6}$$

$$L = 176.838 \text{ nH}$$

For High pass:

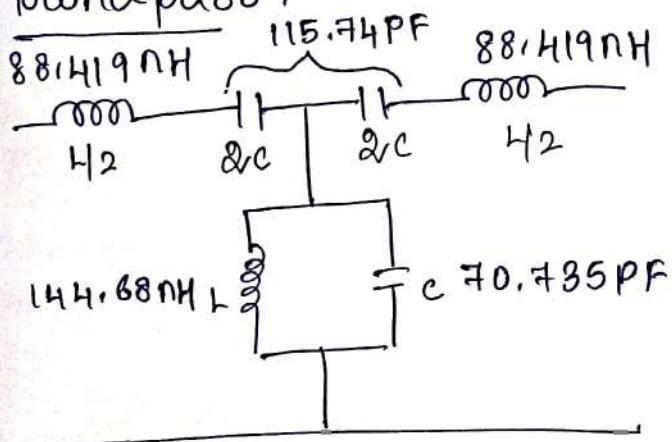
$$C = \frac{1}{K\omega_c} = \frac{1}{50 \times 2\pi \times 55 \times 10^6}$$

$$C = 57.874 \text{ pF}$$

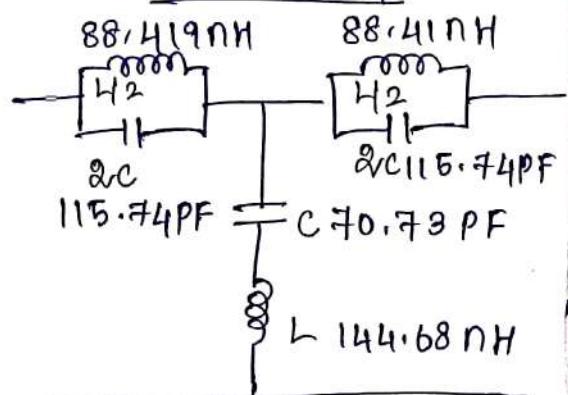
$$L = \frac{K}{\omega_c} = \frac{50}{2\pi \times 55 \times 10^6}$$

$$L = 144.68 \text{ nH}$$

Bandpass:



Band stop:



### $\Pi$ - section

$$C = \frac{1}{\omega C}$$

$$L = \frac{1}{\omega C}$$

### Low pass

$$C = \frac{1}{60 \times 2\pi \times 45 \times 10^6} = 141.471 \text{ PF}$$

$$L = \frac{1}{\omega C} = \frac{50}{2 \times 2\pi \times 45 \times 10^6} = 88.419 \text{ nH}$$

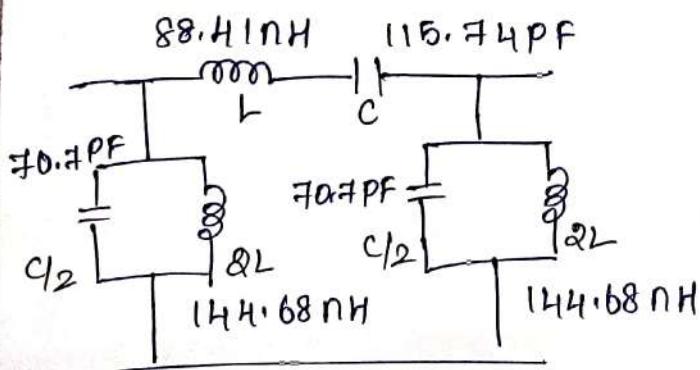
### High pass

$$C = \frac{1}{\omega C} = \frac{1}{50 \times 2\pi \times 55 \times 10^6} = 0.115 \text{ nH}$$

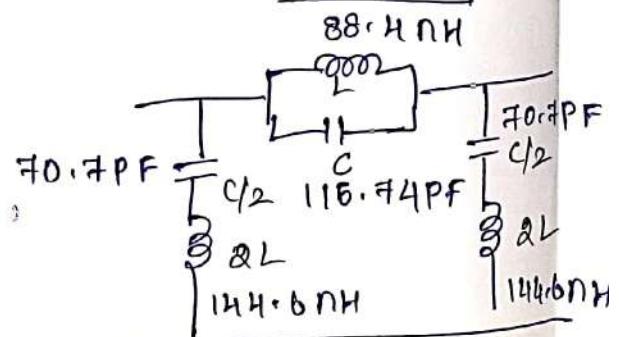
$$= 115.74 \text{ PF}$$

$$L = \frac{1}{\omega C} = \frac{50}{2 \times 2\pi \times 55 \times 10^6} = 78.34 \text{ nH}$$

### Band pass



### Band stop



### 3. Pi network:

FOR  $\pi$  section,

$$K^2 = \frac{4L}{C}$$

$$C = \frac{4L}{K^2} \text{ and } 4L = K^2 C$$

FOR C

$$\omega_c = \frac{1}{\sqrt{LC}}$$

$$L = \frac{K^2 C}{4}$$

$$\omega_c = \frac{1}{\sqrt{\frac{K^2 C}{4} \cdot C}} = \boxed{\frac{1}{\sqrt{\frac{K^2 C^2}{4}}} = \frac{1}{\frac{KC}{2}}}$$

$$\omega_c = \frac{\omega}{KC}$$

$$C = \boxed{\frac{\omega}{KC}}$$

FOR L

$$\omega_c = \frac{1}{\sqrt{LC}} = \frac{1}{\sqrt{L \cdot \frac{4L}{K^2}}}$$

$$= \frac{1}{\sqrt{\frac{4L^2}{K^2}}}$$

$$= \frac{1}{\frac{2L}{K}} = \frac{K}{2L}$$

$$\omega_c = \frac{K}{2L}$$

$$L = \boxed{\frac{K}{2\omega_c}}$$

$$f_c = 10 \text{ MHz}$$

$$Z_0 = 50 \Omega$$

$$C = \frac{\lambda}{2\pi Z_0}$$

$$\omega_c = 2\pi f_c = 2\pi \times 10 \times 10^6 = 62,832 \text{ rad/s}$$

$$C = \frac{\lambda}{2\pi \times 62,832 \times 10^6}$$

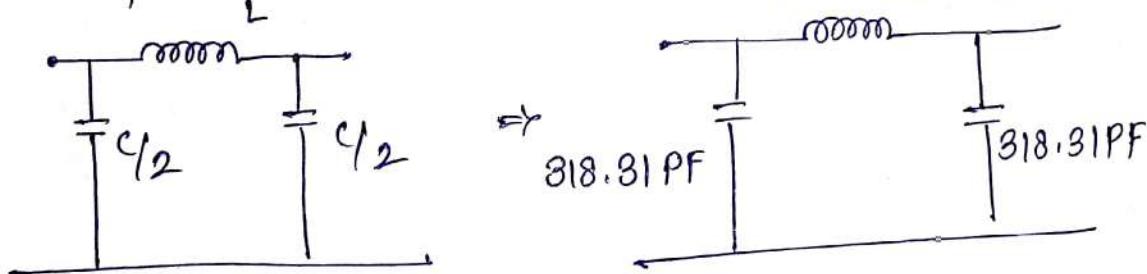
$$C = 636.62 \text{ pF}$$

$$L = \frac{Z_0}{2\pi \omega_c} = \frac{50}{2 \times 62,832 \times 10^6}$$

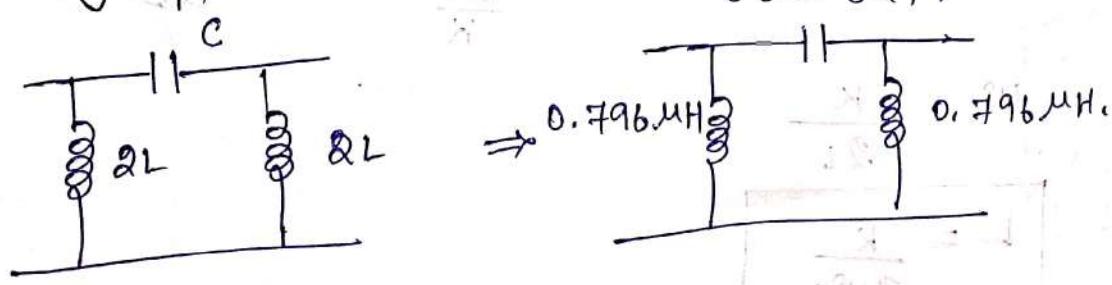
$$L = 397.886 \text{ nH} / 0.398 \mu\text{H}$$

Design:

i) Low pass filter:



ii) High pass filter:



## constant K-section

1) T-section:

$$K = \sqrt{z_1 z_2 + z_1^2/4}$$

constant section width

$$K = \sqrt{j_w L \cdot \frac{1}{j_w c} + \frac{(j_w L)^2}{A}}$$

$$K = \sqrt{\frac{L}{c} + \frac{(-\omega^2 L^2)}{A}}$$

$$K^2 = \frac{L}{c} - \frac{\omega^2 L^2}{A} \quad \omega \ll \omega_c$$

$K^2 = 4c$

2)  $\Pi$ -section:

$$K = \sqrt{\frac{z_1}{A} (z_1 + Hz_2)}$$

$$= \sqrt{\frac{z_1^2}{A} + A z_1 z_2}$$

$$= \sqrt{-\frac{\omega^2 L^2}{4} + \frac{HL}{c}}$$

$$K = \sqrt{HL/c}$$

$K^2 = \frac{HL}{c}$

8.10.25

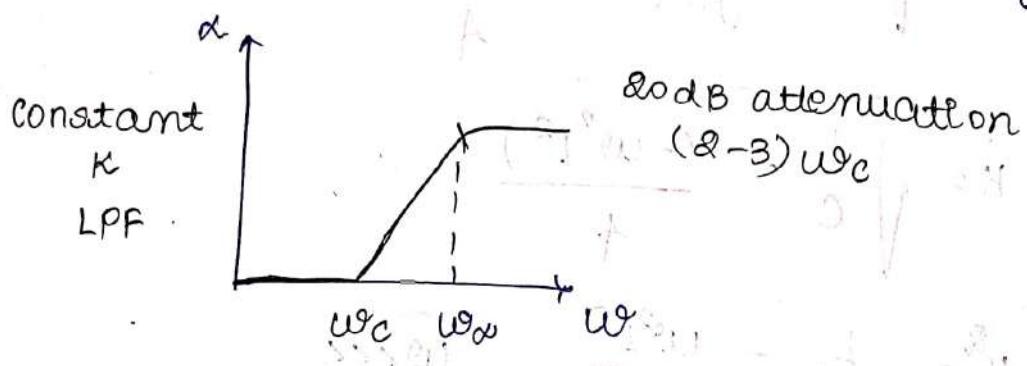
Notes on Filters

m-derived filter:

constant K-filter

1. Non-constant Image Impedance  
(Frequency  $\propto$  Image Impedance)

2. slow attenuation rate near cut-off



To address these drawbacks  $\rightarrow$  m-derived LPF T section:

a) constant K

$$Z_1 = j\omega L$$

$$Z_2 = \frac{1}{j\omega C}$$

For m-derived:

$$z'_1 = mz_1$$

To obtain Image Impedance now over  $Z'_2$  should be

we know that

$$Z_{1T} = \sqrt{Z_1 Z_2 + \frac{Z_1^2}{4}}$$

$$= \sqrt{z'_1 z'_2 + \frac{(z'_1)^2}{4}}$$

$$z_1' z_2' + \frac{(z_1')^2}{4} = z_1 z_2 + \frac{z_1^2}{4}$$

$$z_1' z_2' = z_1 z_2 + \frac{z_1^2}{4} - \frac{(z_1')^2}{4}$$

$$(m z_1) z_2' = z_1 z_2 + \frac{z_1^2}{4} - \frac{m^2 z_1^2}{4}$$

$$m z_1 z_2' = z_1 z_2 + \frac{z_1^2}{4} (1 - m^2)$$

$$z_2' = \frac{z_1 z_2}{m z_1} + \frac{z_1^2}{4} (1 - m^2)$$

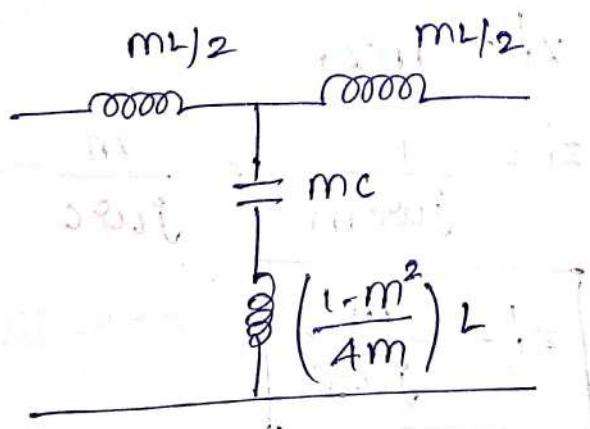
$$z_2' = \frac{z_2}{m} + \frac{z_1 (1 - m^2)}{4m}$$

$$z_1' = m z_1 = m j w L$$

$$z_2' = \frac{1}{j w cm} + j w L \frac{(1 - m^2)}{4m} \quad (\text{Bath } L \text{ & } c) \text{ component.}$$

m-derived

T-section:



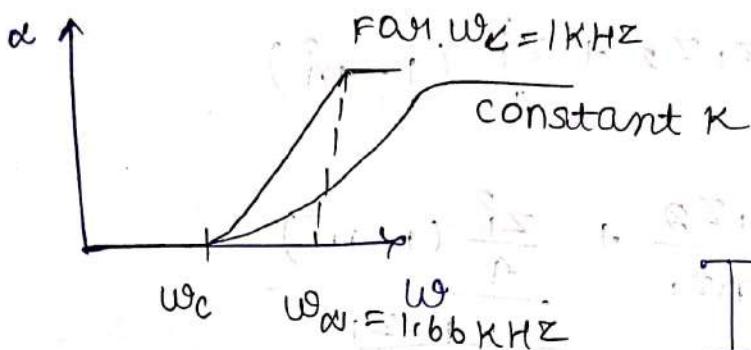
$$0 < m < 1$$

If  $m=1$  then constant K filter

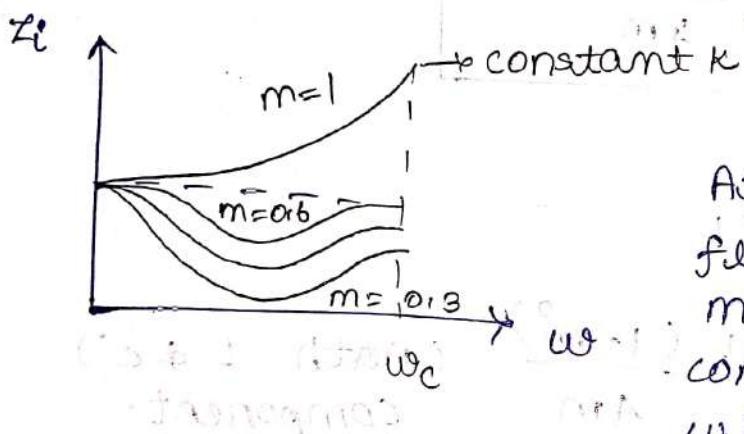
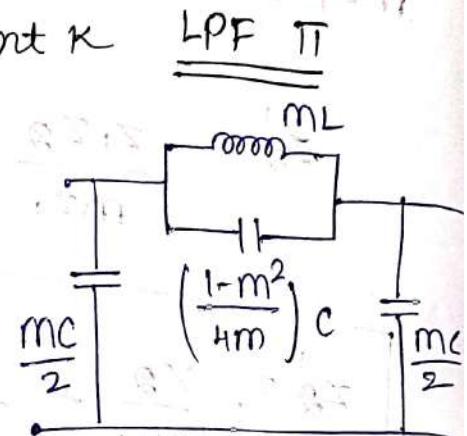
$$\omega_o = \frac{\omega_c}{\sqrt{1-m^2}} \quad m < 1$$

If  $\omega_c = 1 \text{ kHz}$  and  $m = 0.8$  then

$$\omega_o = \frac{1 \text{ kHz}}{\sqrt{1-(0.8)^2}} = 1.66 \text{ kHz}$$



$m = 0.6$  for real time



High pass filter

For constant  $k$

$$Z_1 = \frac{1}{j\omega c}$$

$$Z_2 = j\omega L$$

negative feedback

At pass band,  
fluctuations when:  
 $m = 0.3$  but  
compensated by  $m = 0.6$   
with short circuit  
(better)  
in attenuation

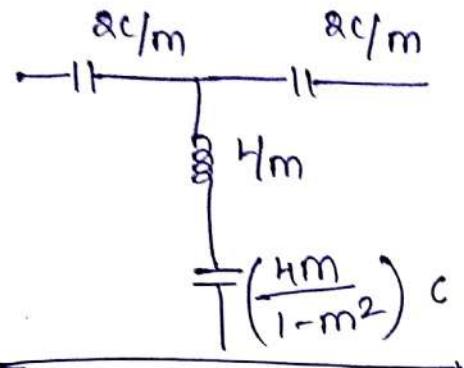
$$Z_1' = mz_1$$

$$Z_1' = \frac{1}{j\omega cm} = \frac{m}{j\omega c}$$

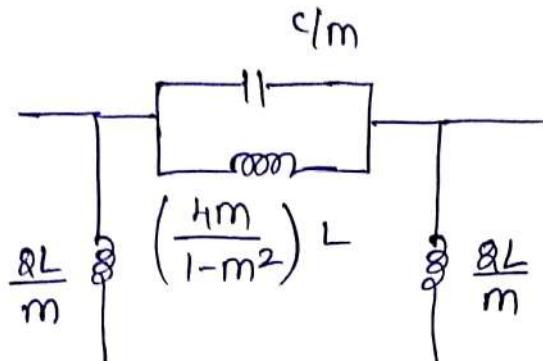
$$Z_1' = \frac{m}{j\omega c}$$

$$Z_0' = \frac{g_{WL}}{m} + \frac{1}{g_{WC}} \left( \frac{1-m^2}{4m} \right)$$

For  $m^2$ -derived



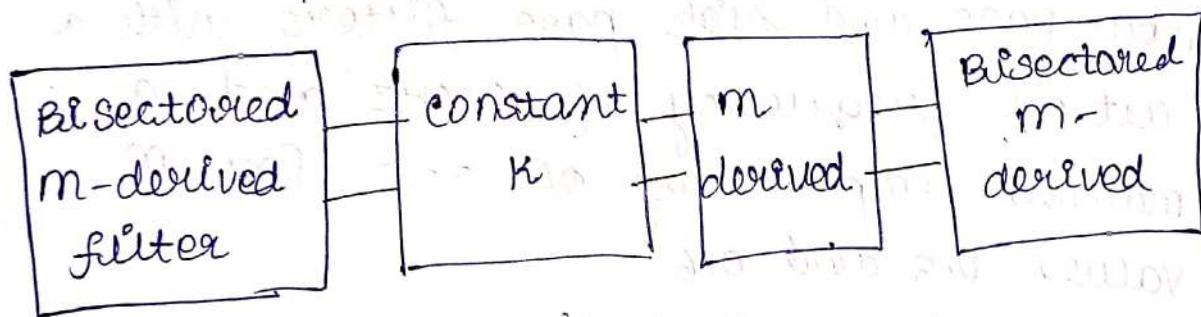
T-section



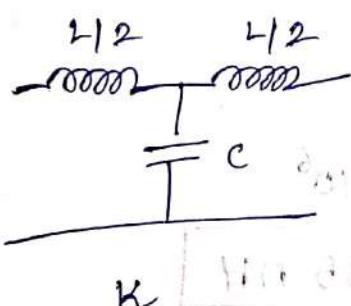
Pi section

composite filter:

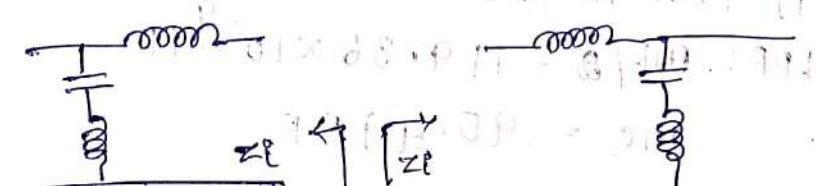
constant  $\kappa$  with m-derived along  
with Impedance matching network.

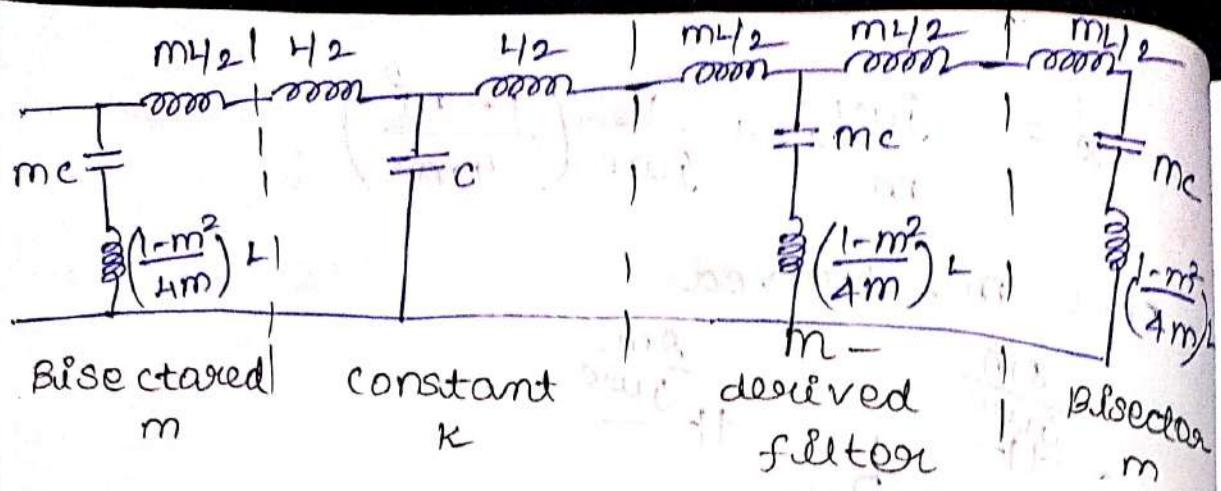


composite low pass filter

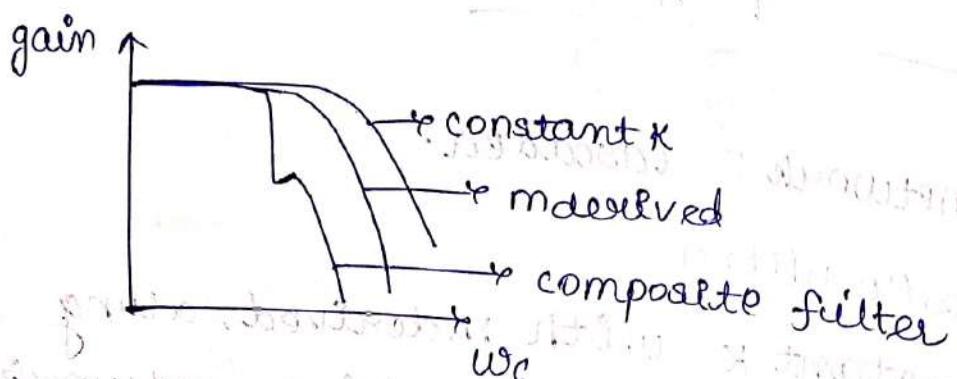


Bisected m





sharp cut off - freq un feasible way  
for composite



4. Design a  $m$ -derived T and pi section low pass and high pass filters with a cut off frequency of 10 MHz and a matched impedance of  $50\Omega$  for  $m$  values 0.3 and 0.6.

Low pass filter - T section

T-section:

$$C = \frac{1}{K w_c} \quad L = \frac{K}{w_c}$$

$$C = \frac{1}{50 \times 2\pi \times 10 \times 10^6}$$

$$C = 318.309 \text{ pF}$$

$$L = \frac{50}{2\pi \times 10 \times 10^6}$$

$$L = 795.785 \text{ nH}$$

i) For  $m = 0.3$

$$\text{LPF: } m_{L/2} = 119.36 \times 10^{-9} \text{ H}$$

$$m_c = 95.49 \text{ pF}$$

$$\left(\frac{1-m^2}{4m}\right) L = \left(\frac{1-0.3^2}{4 \times 0.3}\right) L = 54.3123 \text{ nH}$$

$$\text{HPF: } \frac{\omega c}{m} = 8122.06 \text{ PF} \quad L/m = 8658.61 \text{ nH}$$

$$\left(\frac{4m}{1-m^2}\right) C = \left(\frac{4 \times 0.3}{1-0.3^2}\right) C = 419.748 \text{ PF}$$

iii) FOR  $m=0.6$

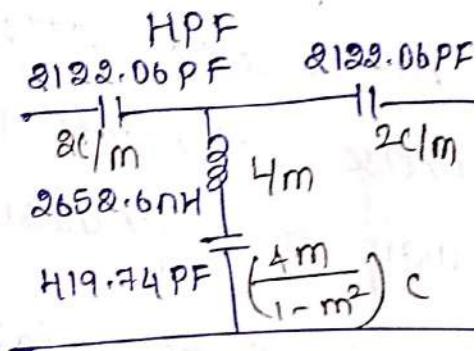
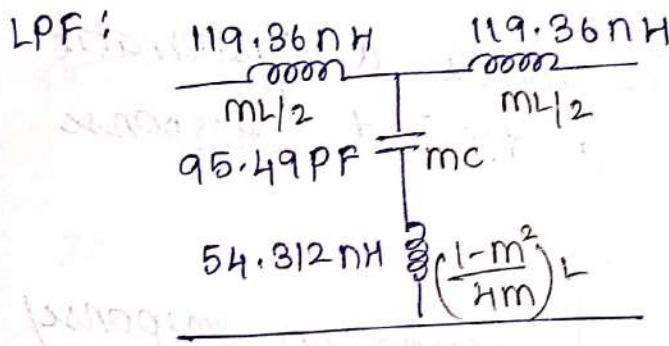
$$\text{LPF: } m L/2 = 888.73 \text{ nH} \quad m c = 190.98 \text{ PF}$$

$$\left(\frac{1-m^2}{4m}\right) L = \left(\frac{1-0.6^2}{4 \times 0.6}\right) L = 76.395 \text{ nH}$$

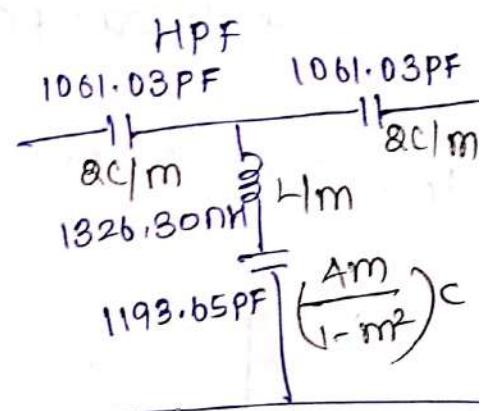
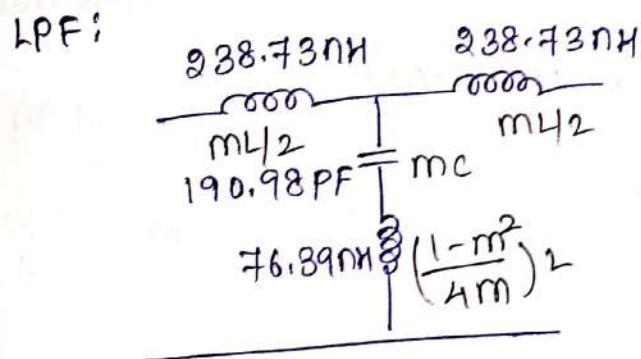
$$\text{HPF: } \frac{\omega c}{m} = 1061.03 \text{ PF} \quad L/m = 1826.30 \text{ nH}$$

$$\left(\frac{4m}{1-m^2}\right) C = \left(\frac{4 \times 0.6}{1-0.6^2}\right) C = 1193.658 \text{ PF}$$

FOR  $m=0.3$



FOR  $m=0.6$



14.10.25

Filter design:

- pass band → zero insertion loss
- stop band → infinite attenuation
- pass band → linear phase → to avoid signal distortion

In Images parameter method; there is no methodical way of improving the design

Insertion loss method:

→ high degree of control over the pass band and stop band amplitude and phase characteristics with a systematic way to synthesize a desired response

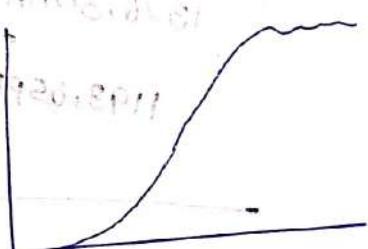
\* Binomial

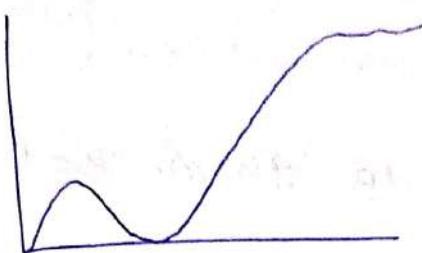
\* Chebyshev

\* Linear phase

} depends on response polynomial

Fair flat response → binomial





For sharp cutoff  
chebyshev.

ripples  $\rightarrow$  chebyshev.

define insertion loss and then with  
matching L, C components.

for linear phase and flat response  
we go for linear phase method.

Insertion loss:

$$IL = 10 \log (\text{power loss ratio})$$

$$\text{power loss ratio} = \frac{P_{in}}{P_{load}}$$

In terms of reflection coefficients

$$= \frac{1}{1 - |r|^2} \quad r = \frac{z_{in} - z_0}{z_{in} + z_0}$$

binomial (flat response):

$$\text{power loss ratio } PLR = 1 + K^2 \left( \frac{\omega}{\omega_c} \right)^{2N}$$

$N$  = order of filter (highest degree  
of pole  $\rightarrow$  order  
of system)

At the edge of boundary ( $\omega = \omega_c$ )

$$PLR = 1 + K^2$$

$K = 0$  (ideal case)  
 $K = 1$  (3dB loss expected)

$$(PLR)_{dB} = 3$$

For reference of  $-3 \text{ dB}$  then  $\kappa=1$

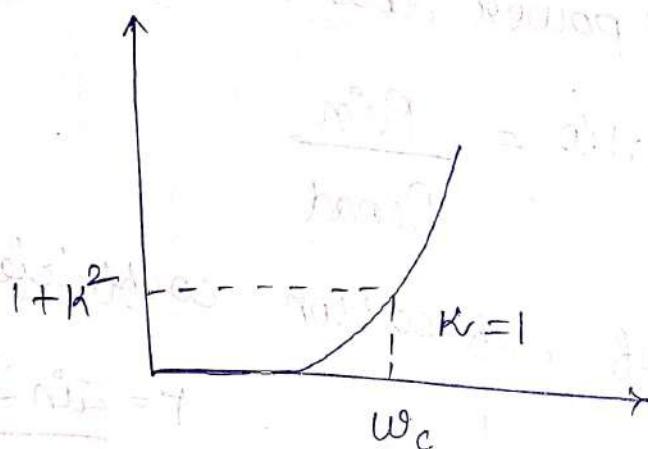
If  $\kappa=1$  then

$$PLR = 1 + \left( \frac{\omega}{\omega_c} \right)^{2N}$$

if  $\omega \gg \omega_c$

$\Rightarrow$   $20 \text{ dB/decade}$

if  $\omega \ll \omega_c = 0$ .



Chebyshev Response:

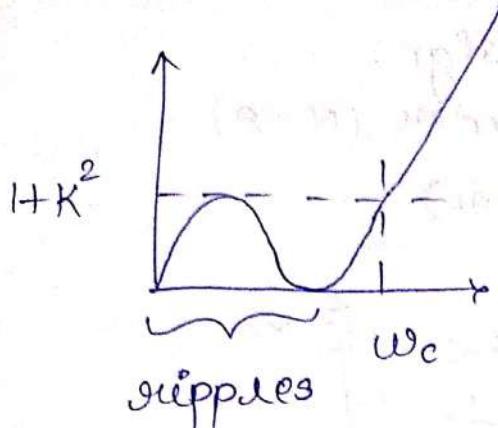
$$PLR = 1 + \kappa^2 T_N^2 \left( \frac{\omega}{\omega_c} \right)$$

$$PLR = 1 + T_N^2 \left( \frac{\omega}{\omega_c} \right) \quad 3 \text{ dB reference } \kappa=1$$

At Edge of Boundary  $\omega = \omega_c$

$$PLR = 1 + T_N^2 (1)$$

$= 20 \text{ dB/decade}$



Equiripple in passband response

Linear phase response:

$$\phi(w) = Aw \left[ 1 + P \left( \frac{w}{w_c} \right)^{2N} \right]$$

$P = \text{constant}$

$$\text{group delay: } \tau_d = \frac{d(\phi(w))}{dw}$$

$$\tau_d = A \left[ 1 + P(2N+1) \left( \frac{w}{w_c} \right)^{2N} \right]$$

phase change depends on order and constant.

Amplitude vary:  $20N$  slope/decade  
design steps involved in: Insertion loss method:

→ filter specification

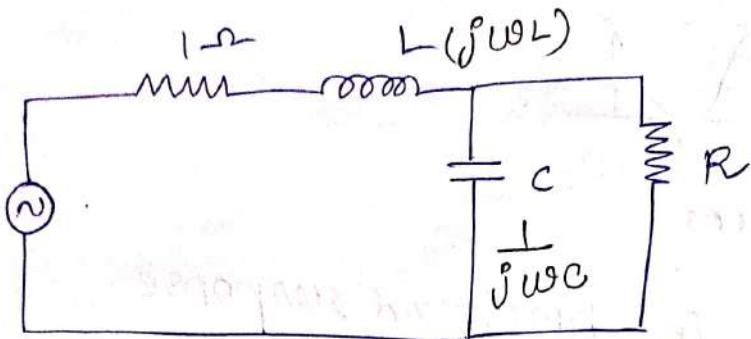
→ low pass filter design

→ scaling of frequency/conversion

→ Implementation.

Low pass filter design:

Let it be second order ( $N=2$ )



$$\omega_c = 1 \text{ rad/sec}$$

Acceptable range of loss = 3 dB

$$so \boxed{k=1}$$

Binomial method:

$$(PLR) = 1 + k^2 \left( \frac{\omega}{\omega_c} \right)^{2N} = \frac{1}{1 - \tau^2}$$

Suppose  $k=1$  then

$$= 1 + \left( \frac{\omega}{\omega_c} \right)^{2N} = 1 + \left( \frac{\omega}{\omega_c} \right)^4$$

Butterworth

$$(PLR) = 1 + \omega^4 \quad \text{--- (1)}$$

$$Z_{in} = j\omega L + \frac{R(1-j\omega RC)}{1 + \omega^2 R^2 C^2}$$

$Z_0 = R = 1 \Omega = \text{normalised impedance}$   
( $50 \Omega$ )

$$\Gamma = \frac{Z_{in} - 1}{Z_{in} + 1} = \frac{(Z_{in} + 1)^2}{2(Z_{in} + Z_{in}^*)}$$

$$PLR = \frac{1}{1 - |\Gamma|^2}$$

$$= 1 + \frac{1}{4R} \left[ (1-R)^2 + (R^2 C^2 + L^2 - 2LCR^2) w^2 + (L^2 C^2 R^2) w^4 \right] \quad \text{--- (2)}$$

If no frequency component through

① then  $w=0$  and  $PLR=1$

If  $R=1$  then from ②  $PLR=1$

Equate  $w^2$  in ① and ②

$$RC^2 + L^2 - 2LCR^2 = 0$$

wkt  $\boxed{R=1}$

$$C^2 + L^2 - 2LC = 0$$

$$(C-L)^2 = 0$$

$\boxed{C=L} \quad \text{--- (3)}$

Equating  $w^4$  from ② and ①

$$L^2 C^2 R^2 = 1/4 \quad \frac{1}{4} L^2 C^2 R^2 = 1$$

$$L^2 C^2 = 1/4$$

$$L^2 C^2 = 4$$

From ③

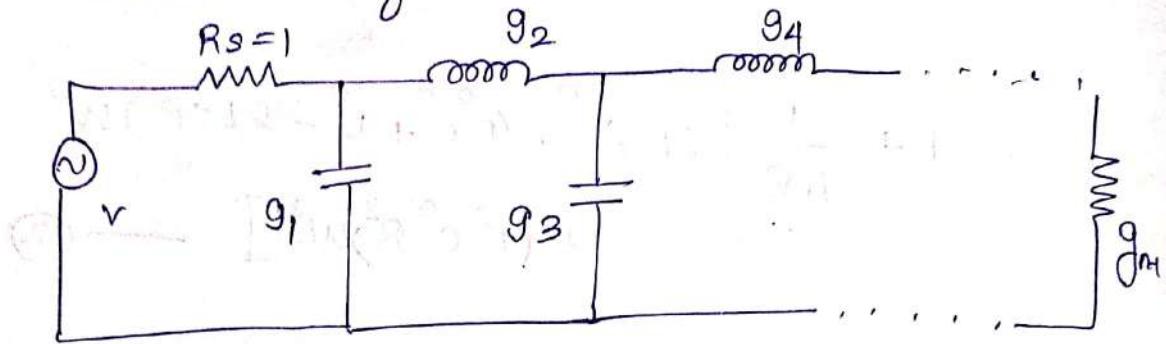
$$L^4 = 4$$

$$L = \sqrt{2} = C$$

$$L = C = \frac{1}{\sqrt{2}}$$

$\boxed{L=C=1.414}$

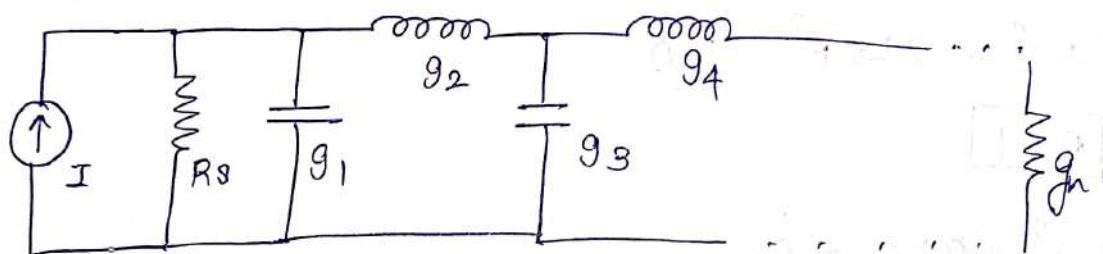
For n - order it goes in a ladder way



Irrespective of order n; R=1

In chebyshev  
odd number = 1

Even number = 1, 9, 8



Filter Transformation:

- Impedance Transformation;
- Frequency Transformation
- Low pass filter converted to High pass, Bandpass and Band stop.

## Impedance Transformation:

$$R_S = R_0$$

$$R'_S = R_0$$

far Butterworth with  $R_0 = 1$   
for all (at least)

$$R'_L = R_0 R_L$$

If  $R_{0 \rightarrow 2}$  is varied  
then new  $R_L$  found

$$L' = R_0 L$$

$$C' = \frac{C}{R_0}$$

Due to Impedance change

frequency Transformation: change in frequency

$$PLR'(w) = PLR \left( \frac{w}{w_c} \right)$$

$$jX_L = jwL$$

$$jB_K = \frac{1}{jw_c}$$

$$\left. \begin{array}{l} w=w_c=1 \\ w \leftarrow \frac{w}{w_c} \end{array} \right\}$$

$$w' = 1/w_c$$

Due to change

other than  $w_c = 1 \text{ rad/s}$   
and  $w=1$

$$jX_L = jwL' = j \left( \frac{w}{w_c} \right) L$$

$$jB_K = \frac{1}{jw_c'} = j \left( \frac{w}{w_c} \right) C_K$$

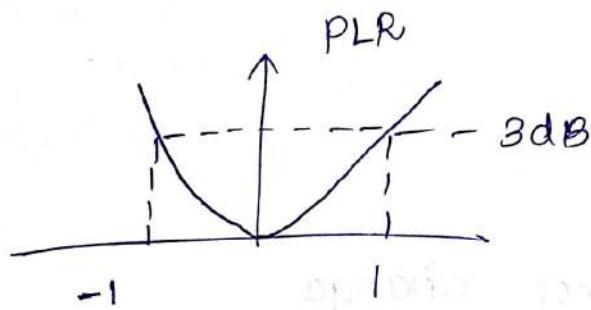
$$jB_K = jwC' = j \left( \frac{w}{w_c} \right) C_K$$

Impedance & frequency change:

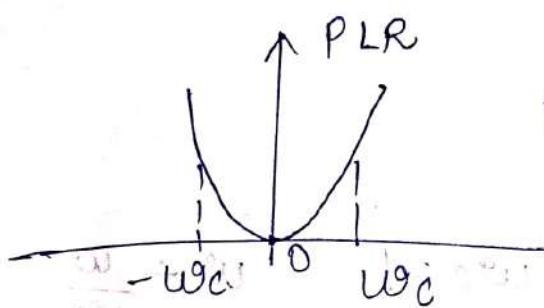
$$j\omega L' = j\left(\frac{\omega}{\omega_c}\right) L R_0$$

$$j\omega C' = j\left(\frac{\omega}{\omega_c}\right) \cdot \frac{C}{R_0}$$

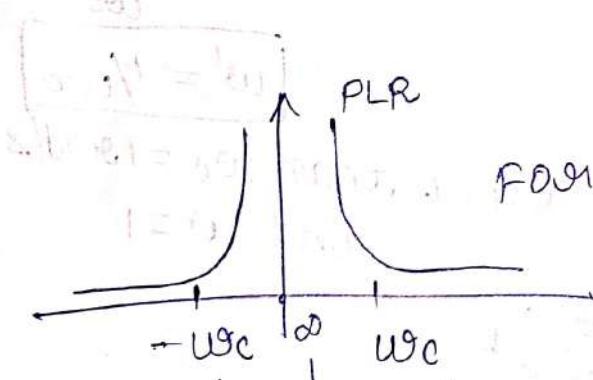
conversion from LPF to HPF



due to frequency translation



for LPF



for HPF

Frequency Translation:

$$\text{LPF: } \omega \leftarrow \frac{\omega}{\omega_c} = 1 \leftarrow \frac{1}{\omega_c} \quad \omega = 1$$

$$\text{HPF: } \frac{-\omega_c}{\omega} \quad \text{for } \omega = 1 \text{ then } -\omega_c$$

# Impedance Translation Frequency

LPF:

$$L_K' = \frac{L_K R_0}{w_c}$$

\$L\_K, C\_K\$ from  
\$g\_1, g\_2\$ in table

$$C_K' = \frac{C_K}{R_0 w_c}$$

\$R\_0\$: last value  
in table

$w_c$ : new frequency

HPF:

series and shunt changes

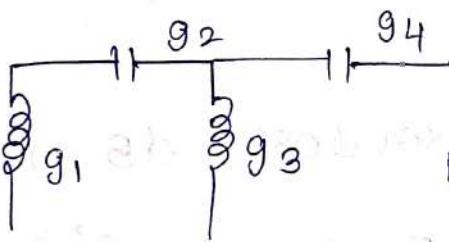
$$C_K' = \frac{R_0 (w_c L_K)}{w_c C_K} \quad \left[ jX_K = j\left(\frac{w_c}{w}\right) L = \frac{1}{j w C_K} \right]$$

Reverse since HPF

$$L_K' = \frac{R_0}{w_c C_K}$$

IT no changes

For HPF



But we have \$g\_1\$ &  
\$g\_2\$ as (\$C\$ and \$L\$)

(changing component  
value alone)

15.10.25

1. Design maximally flat LPF with a cut off frequency of 20 Hz impedance of 50 \$\Omega\$ and atleast 15dB insertion loss at 30 Hz compare with an equiripple of 3dB and linear phase filter has the same order.

To design filter:

→ LPF

→ flat, Equiripple and linear phase given

$$f_0 = 2 \text{ GHz}$$

$$w = \underbrace{3 \text{ GHz}}^f \times \pi; I_L = 15 \text{ dB} \quad (\text{Insertion loss})$$

$$Z = 50 \Omega$$

$$Z_S = 50 \Omega$$

i) Butterworth filter: a) LPF

Table 8.3

$$L_K = \frac{R_O L_K}{w_C} \quad C_K = \frac{C_K}{R_O w_C} \quad \text{Fig 8.26}$$

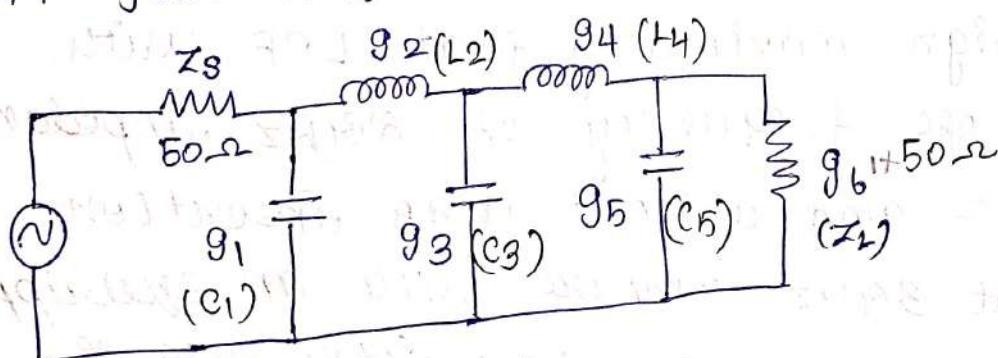
N → depends on IL

$$\frac{w}{w_C} - 1 = \frac{3 \times 10^9}{2 \times 10^9} - 1 = 0.5$$

Attenuation (Insertion loss) dB = 15 dB

comes between 4 and 5 go to higher value hence  $\boxed{n=5}$

LPF for n=5



From Table 8.3 (pozai)

$$n=5$$

$$g_1 = 0.6180$$

$$= C_1$$

$$g_2 = 1.6180$$

$$= L_2$$

$$g_3 = 8.0000 = C_3$$

$$g_4 = 1.6180 = L_4$$

$$g_5 = 0.6180 = C_5$$

$$g_6 = 1.0000$$

$$g_6 \times 50 = 50 \Omega \text{ hence last } R = 50 \Omega$$

For  $g_1$

$$C_K' = \frac{C_K}{R_0 \times w_c} = \frac{0.6180}{50 \times 2\pi \times 2 \times 10^9} = 0.983 \text{ PF}$$

For  $g_2$

$$L_K' = \frac{R_0 L_K}{w_c} = \frac{50 \times 1.6180}{2\pi \times 2 \times 10^9} = 6.437 \text{ nH}$$

For  $g_3$

$$C_K' = \frac{C_K}{R_0 \times w_c} = \frac{8}{50 \times 2\pi \times 2 \times 10^9} = 3.183 \text{ PF}$$

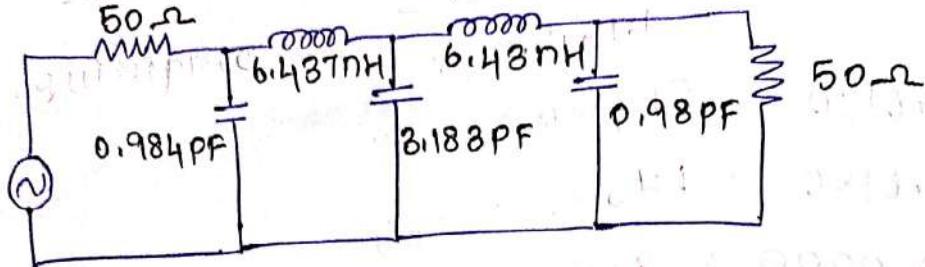
For  $g_4$

$$L_K' = \frac{R_0 L_K}{w_c} = \frac{50 \times 1.6180}{2\pi \times 2 \times 10^9} = 6.43 \text{ nH}$$

For  $g_5$

$$C_K' = \frac{C_K}{R_0 \times w_c} = \frac{0.6180}{50 \times 2\pi \times 2 \times 10^9} = 0.98 \text{ PF}$$

## Butterworth Low pass filter:



## b) High pass Filter:

Now,  $g_1 = 0.6180$  From maximally flat table

$$g_2 = 1.6180$$

$$g_3 = \infty$$

$$g_4 = 1.6180$$

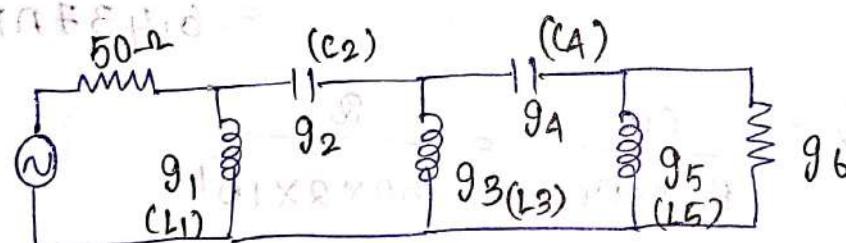
$$L_1 = g_5 = 0.6180$$

$$C_K = \frac{R_0 \times 10^9}{8\pi f \times 10^9} = \frac{50}{8\pi \times 10^9 \times 10^9} = 10^{-10}$$

$$C_K = \frac{1}{R_0 \omega_c L_K}$$

Take respective  
( $g_n$ ) values from  
LPF

$$H_{HPF}(s) = \frac{R_0 \times 10^9}{\omega_c C_K} =$$



For  $g_1$

$$L_1 = \frac{R_0}{\omega_c C_K} = \frac{50}{8\pi \times 2 \times 10^9 \times 0.6180}$$

$$L_1 = 6.438 \text{ nH}$$

For  $g_2$

$$C_2 = \frac{1}{R_0 \omega_c L_2} = \frac{1}{50 \times 2\pi \times 2 \times 10^9 \times 1.6180}$$

$$= 0.984 \text{ pF}$$

for 93

$$L_3 = \frac{R_o}{w_c C_K} = \frac{50}{2\pi \times 2 \times 10^9 \times 2} = 1.989 \text{ nH.}$$

for 94

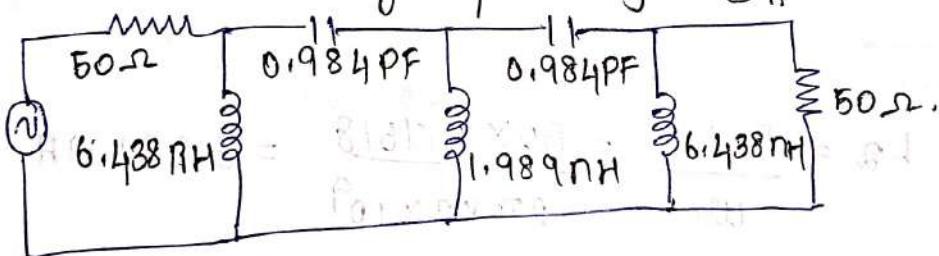
$$C_4 = \frac{1}{R_o w_c L_K} = \frac{1}{50 \times 2\pi \times 2 \times 10^9 \times 1.6180} = 0.984 \text{ PF.}$$

for 95

$$L_5 = \frac{R_o}{w_c C_K} = \frac{50}{2\pi \times 2 \times 10^9 \times 0.6180} = 6.438 \text{ nH.}$$

$$Z_6 = 1 \times 50 = 50 \Omega$$

Butterworth High pass filter:



ii) Chebyshev filter: (From Table 8.4)

a) LPF:

For a Equiripple of 3dB

From the Table,

since, same order  $n=5$

$$g_1 = 3.4817$$

$$g_2 = 0.7618$$

$$g_3 = 4.5381$$

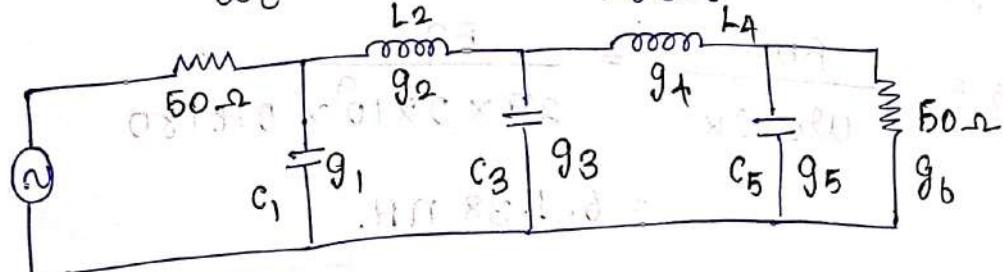
$$g_4 = 0.7618$$

$$g_5 = 3.4817$$

$$g_6 = 1$$

$$g_6 \times 50 = 50 \Omega$$

$$L_K = \frac{R_0 L_K}{w_C} ; C_K = \frac{C_K}{R_0 w_C}$$



$$\text{For } g_1 \quad C_1 = \frac{C_K}{R_0 w_C} = \frac{3.4817}{50 \times 2\pi \times 2 \times 10^9} = 5.541 \text{ pF}$$

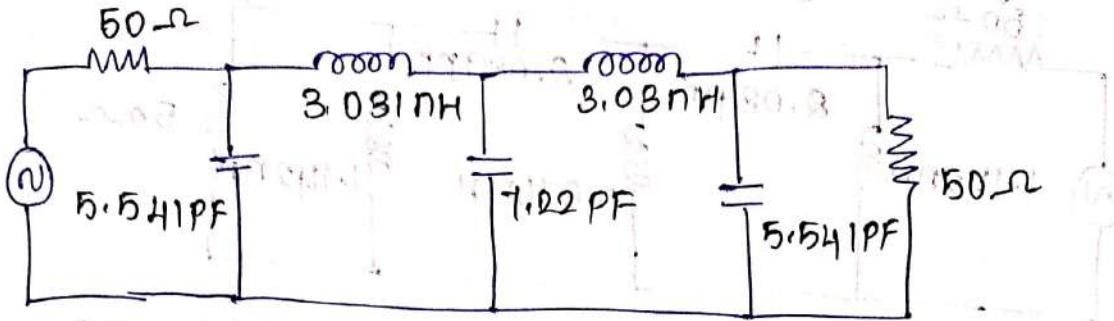
$$\text{For } g_2 \quad L_2 = \frac{R_0 L_K}{w_C} = \frac{50 \times 0.7618}{2\pi \times 2 \times 10^9} = 3.031 \text{ nH}$$

$$\text{For } g_3 \quad C_3 = \frac{C_K}{R_0 w_C} = \frac{4.5381}{50 \times 2\pi \times 2 \times 10^9} = 7.222 \text{ pF}$$

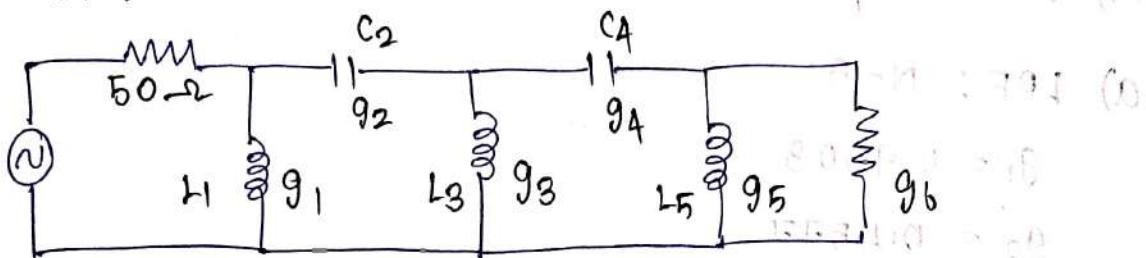
$$\text{For } g_4 \quad L_4 = \frac{R_0 L_K}{w_C} = \frac{50 \times 0.7618}{2\pi \times 2 \times 10^9} = 3.03 \text{ nH}$$

$$\text{For } g_5 \quad C_5 = \frac{C_K}{R_0 w_C} = \frac{3.4817}{50 \times 2\pi \times 2 \times 10^9} = 5.541 \text{ pF}$$

chebyshov low pass filter: (not yet calculated)



b) HPF:



$$C_K' = \frac{1}{R_0 \omega_c L_K} ; \quad L_K' = \frac{R_0}{\omega_c C_K}$$

for g1

$$L_1 = \frac{R_0}{\omega_c C_{K1}} = \frac{50}{2\pi \times 2 \times 10^9 \times 3.4817} = 1.142 \text{ nH}$$

$$L_1 = 1.142 \text{ nH}$$

for g2

$$C_2 = \frac{1}{R_0 \omega_c L_K} = \frac{1}{50 \times 2\pi \times 2 \times 10^9 \times 0.7618} = 2.08 \text{ pF}$$

for g3

$$L_3 = \frac{R_0}{\omega_c C_K} = \frac{50}{2\pi \times 2 \times 10^9 \times 1.5381} = 0.876 \text{ nH}$$

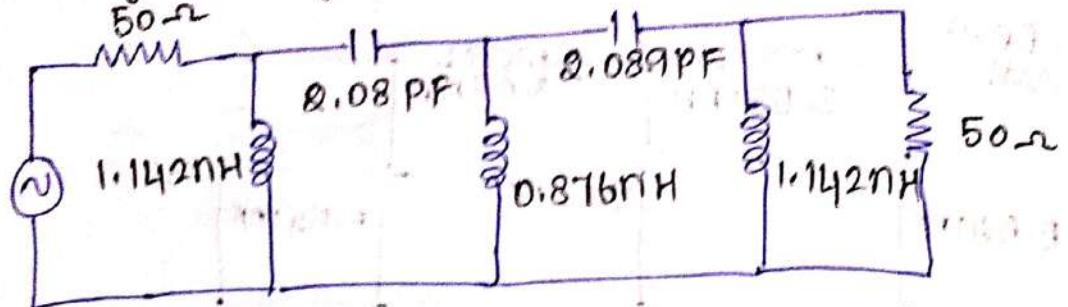
for g4

$$C_4 = \frac{1}{R_0 \omega_c L_K} = \frac{1}{50 \times 2\pi \times 2 \times 10^9 \times 0.7618} = 2.089 \text{ pF}$$

for g5

$$L_5 = \frac{R_0}{\omega_c C_K} = \frac{50}{2\pi \times 2 \times 10^9 \times 3.4817} = 1.142 \text{ nH}$$

# Chebyshev Highpass Filter:



iii) Linear phase filters (from Table 8.5)

a) LPF: N=5

$$g_1 = 0.9303$$

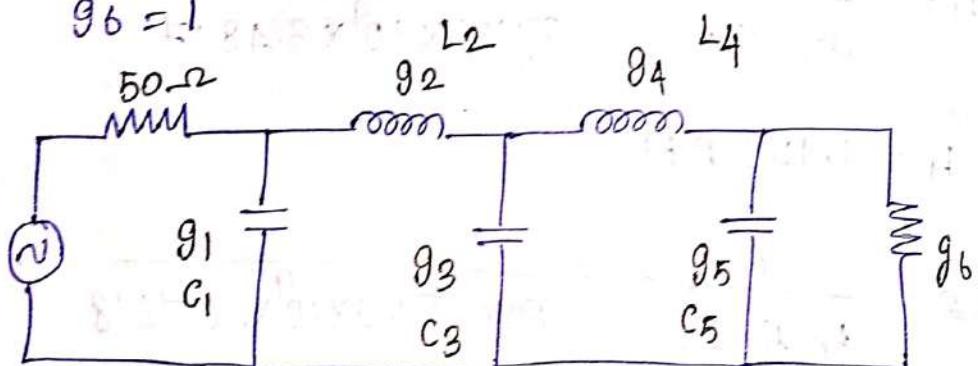
$$g_2 = 0.4577$$

$$g_3 = 0.3312$$

$$g_4 = 0.2090$$

$$g_5 = 0.0718$$

$$g_6 = 1$$



$$L_K^1 = \frac{R_0 L_K}{w_0 C}$$

$$C_K^1 = \frac{C_K}{R_0 w_0 C}$$

For  $g_1$

$$C_1 = \frac{C_K}{R_0 w_0 C} = \frac{0.9303}{50 \times 2\pi \times 2 \times 10^9} = 1.4806 \text{ PF}$$

For  $g_2$

$$L_{g_2} = \frac{R_0 L_K}{w_0 C} = \frac{50 \times 0.4577}{2\pi \times 2 \times 10^9} = 1.821 \text{ nH}$$

for 93

$$C_3 = \frac{CK}{R_0 \omega_C} = \frac{0.3312}{50 \times 2\pi \times 2 \times 10^9} = 0.1527 \text{ pF}$$

for 94

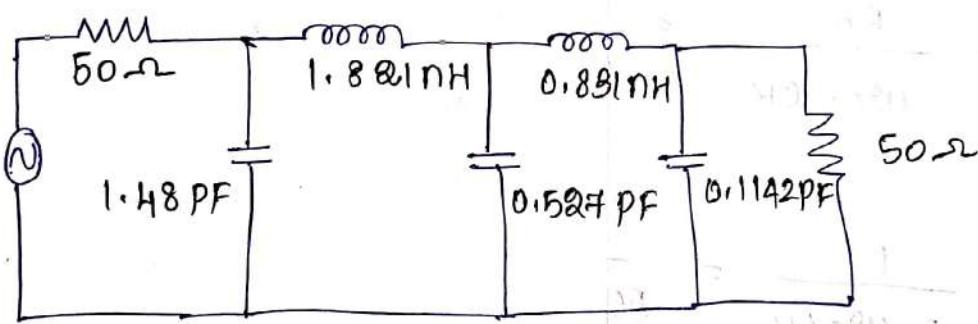
$$L_4 = \frac{R_0 K}{\omega_C} = \frac{50 \times 0.2090}{2\pi \times 2 \times 10^9} = 0.831 \text{ nH}$$

for 95

$$C_5 = \frac{CK}{R_0 \omega_C} = \frac{0.0718}{50 \times 2\pi \times 2 \times 10^9} = 0.1142 \text{ pF}$$

$$g_6 \times 50 = 50 \Omega$$

linear phase Low pass filter:



b) HPF:

$$g_1 = 0.9303$$

$$g_2 = 0.4577$$

$$g_3 = 0.3312$$

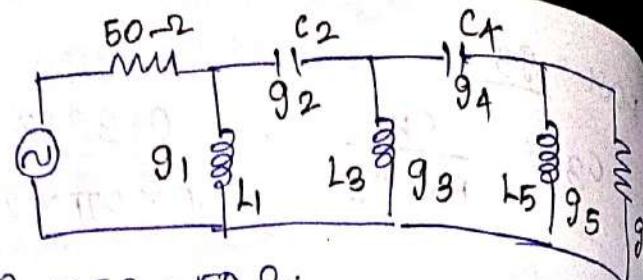
$$g_4 = 0.2090$$

$$g_5 = 0.0718$$

$$g_6 = 1$$

$$C_K = \frac{1}{\omega_C R_0 L_K}$$

$$L_K = \frac{R_0}{\omega_C C_K}$$



$$g_b \times 50 = 50 \Omega$$

For g1

$$L_1 = \frac{R_0}{\omega_C \cdot C_K} = \frac{50}{2\pi \times 2 \times 10 \times 0.9303} = 4.876 \text{ nH}$$

For g2

$$C_2 = \frac{1}{R_0 \omega_C L_K} = \frac{1}{50 \times 2\pi \times 2 \times 10 \times 0.4577} = 3.477 \text{ pF}$$

For g3

$$L_3 = \frac{R_0}{\omega_C \cdot C_K} = \frac{50}{2\pi \times 2 \times 10 \times 0.3312} = 12.01 \text{ nH}$$

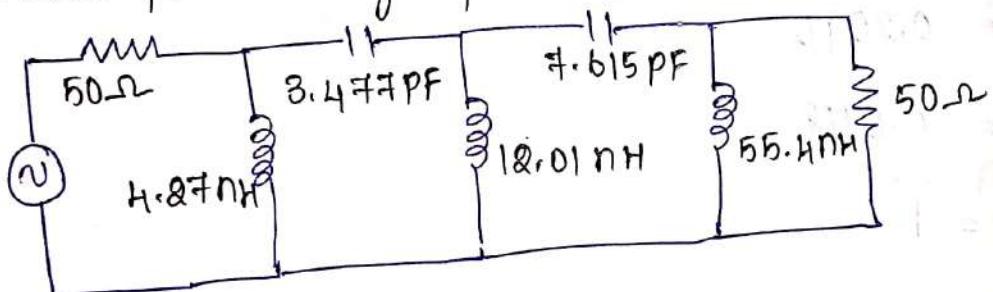
For g4

$$C_4 = \frac{1}{R_0 \omega_C L_K} = \frac{1}{50 \times 2\pi \times 2 \times 10 \times 0.2090} = 4.615 \text{ pF}$$

For g5

$$L_5 = \frac{R_0}{\omega_C \cdot C_K} = \frac{50}{2\pi \times 2 \times 10 \times 0.0718} = 55.41 \text{ nH}$$

linear phase High pass filter:



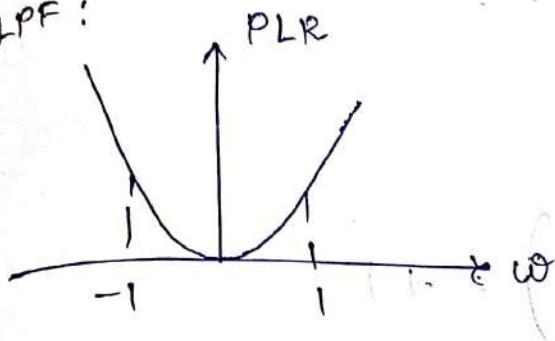
16.10.85

## Frequency Translation:

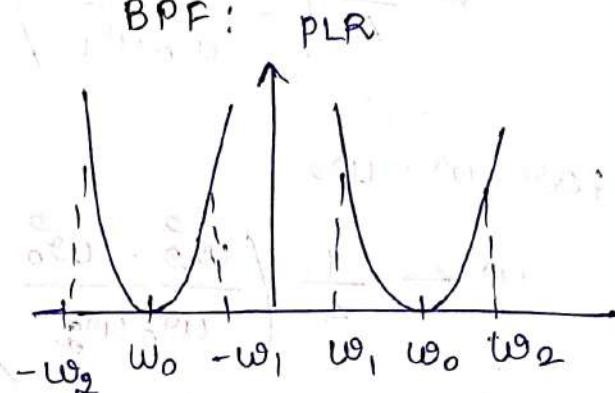
LPF to BPF and BBF

$$\omega_c = 1 ; K = 1$$

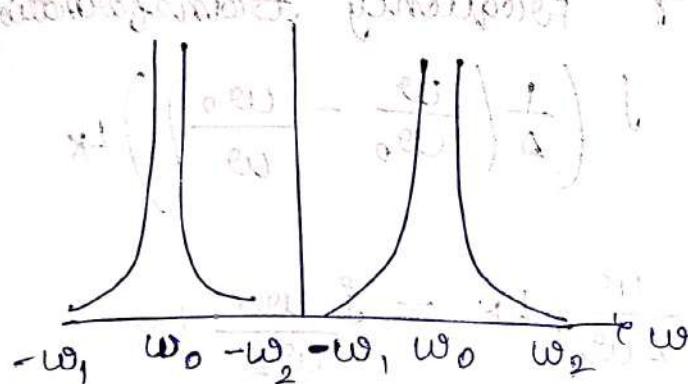
LPF:



BPF: PLR



BBF:



$$w \leftarrow \frac{\omega_0}{\omega_2 - \omega_1} \left( \frac{w}{\omega_0} - \frac{\omega_0}{w} \right)$$

$$\Delta = \frac{\omega_2 - \omega_1}{\omega_0}$$

$$w \leftarrow \frac{1}{\Delta} \left( \frac{w}{\omega_0} - \frac{\omega_0}{w} \right)$$

$$\text{If } w = \omega_0$$

$$w \leftarrow 0 \text{ (LPF)}$$

For  $\omega = \omega_1$

$$\omega \leftarrow \frac{1}{\Delta} \left( \frac{\omega_1}{\omega_0} - \frac{\omega_0}{\omega_1} \right)$$

$$\Rightarrow \frac{1}{\Delta} \left( \frac{\omega_1^2 - \omega_0^2}{\omega_0 \omega_1} \right) = -1$$

For  $\omega = \omega_2$

$$\omega \leftarrow \frac{1}{\Delta} \left( \frac{\omega_2^2 - \omega_0^2}{\omega_0 \omega_2} \right) = +1$$

For LPF generally

$$\begin{aligned} jX_K &= j\omega L_K = j \left( \frac{1}{\Delta} \left( \frac{\omega}{\omega_0} - \frac{\omega_0}{\omega} \right) \right) L_K \\ &= j \frac{\omega}{\Delta \omega_0} L_K - j \frac{\omega_0}{\Delta \omega_0} L_K \end{aligned}$$

LPF  $\rightarrow$  HPF

$$j \frac{\omega_0}{\Delta \omega_0} L_K = \frac{1}{j\omega C_K}$$

$$= j\omega L_K' - j \frac{1}{\omega C_K} + j \frac{\omega}{\Delta \omega_0} L_K$$

series sum

For  $L_K'$

$$\frac{j\omega}{\Delta \omega_0} L_K = j\omega L_K'$$

$$L_K' = R_0 \frac{L_K}{\Delta \omega_0}$$

$$\frac{-j\omega_0}{\Delta\omega} L_K = \frac{-j}{\omega_{CK}}$$

$$C_K' = \frac{\Delta}{R_0 \omega_0 L_K}$$

$$\omega_0 = \sqrt{\omega_1 \omega_2}$$

$$\Delta = \frac{\omega_2 - \omega_1}{\omega_0}$$

shunt arm:

$$jB_K = j\omega_{CK}$$

$$= j \left( \frac{1}{\Delta} \left( \frac{\omega}{\omega_0} - \frac{\omega_0}{\omega} \right) \right) C_K$$

$$\frac{j\omega}{\Delta\omega_0} C_K - \frac{j\omega_0}{\Delta\omega} C_K$$

Equate:

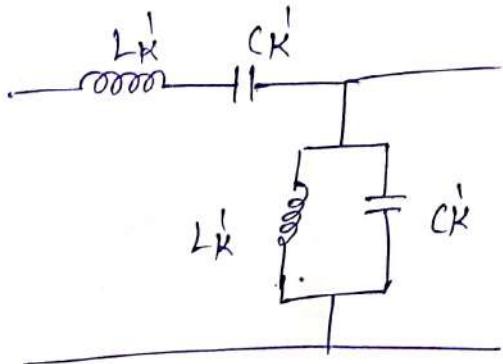
$$j\omega_{CK}' = j/\omega_{CK}'$$

$$\frac{j\omega_{CK}}{\Delta\omega_0} = j\omega_{CK}'$$

$$C_K' = \frac{C_K}{\Delta\omega_0 R_0}$$

$$\frac{-j\omega_0}{\Delta\omega} C_K = \frac{-j}{\omega L_K'}$$

$$L_K' = \frac{\Delta R_0}{\omega_0 C_K}$$



Band stop filter:

$$\omega \leftarrow -\frac{1}{\Delta} \left( \frac{\omega}{\omega_0} - \frac{\omega_0}{\omega} \right)^{-1}$$

series arm:

$$L_K = \frac{\Delta L_K R_0}{\omega_0}$$

$$C_K = \frac{1}{\omega_0 \Delta L_K \cdot R_0}$$

shunt arm

$$L_K' = \frac{R_0}{\omega_0 \Delta C_K}$$

$$C_K' = \frac{\Delta C_K}{R_0 \omega_0}$$

|                   | series   | shunt  | series structure | shunt structure                           |
|-------------------|--|--|------------------|---|
| Lowpass filter:   | $L_K' = \frac{L_K}{\omega_0 C} \cdot R_0$  | $C_K' = \frac{C_K}{R_0 \omega_0}$  | —  —             | $\frac{1}{1 + \frac{R_0}{L_K' \omega_0}}$ |
| High pass filter: | $C_K' = \frac{1}{R_0 \omega_0 L_K}$  | $L_K' = \frac{R_0}{\omega_0 C_K}$  | —II—             | $\frac{1}{1 + \frac{R_0}{C_K' \omega_0}}$ |
| Bandpass filter:  | $L_K' = \frac{L_K R_0}{\Delta \omega_0}$ (LPF)<br>$C_K' = \frac{\Delta}{R_0 \omega_0 L_K}$ (HPF) | $L_K' = \frac{\Delta R_0}{\omega_0 C_K}$<br>$C_K' = \frac{C_K}{\Delta \omega_0 R_0}$ (LPF) | —  —<br>—II—     |   |
| Bandstop filter:  | $L_K' = \frac{\Delta L_K R_0}{\omega_0}$<br>$C_K' = \frac{1}{\omega_0 \Delta L_K R_0}$           | $L_K' = \frac{R_0}{\omega_0 \Delta C_K}$<br>$C_K' = \frac{\Delta C_K}{R_0 \omega_0}$       | —  —<br>—II—     |   |

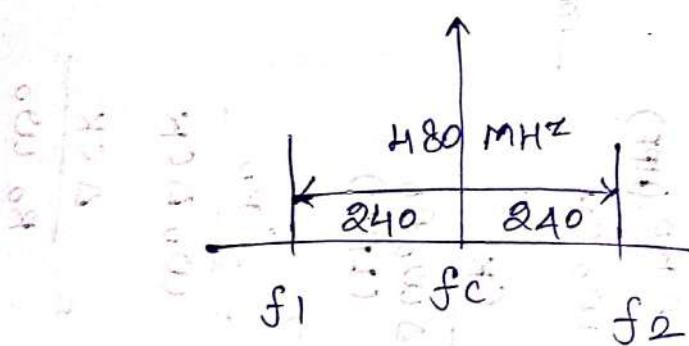
2. consider order of filter is 4, to design BPF save for Butterworth and chebyshov filter of 0.5 dB ripple  $f_c = 2.4 \text{ GHz}$  with Impedance  $B_w$  ratio of 20%.

Given:  $N = 4$

$$(2.4 \times 10^9) \times 20/100$$

$$f_c = 2.4 \text{ GHz} \Rightarrow 480 \text{ MHz}$$

$$f_c = 480 \text{ MHz}$$



$$\begin{array}{l} 2.4 \text{ GHz} \\ -48 \text{ GHz} \end{array}$$

$$\begin{array}{c} 2.4 \text{ GHz} \\ 0.48 \text{ GHz} \end{array} \xrightarrow{-} \underline{0.16 \text{ GHz}}$$

$$\begin{array}{c} 2.4 \text{ GHz} \\ 0.48 \text{ GHz} \end{array} \xrightarrow{+} \underline{0.64 \text{ GHz}}$$

$$\begin{array}{l} f_1 = 0.16 \text{ GHz} \\ f_2 = 0.64 \text{ GHz} \end{array}$$

$$\begin{array}{l} \omega_c = 2\pi \times 0.4 \times 10^9 \\ \omega_c = 15.07 \times 10^9 \text{ rad/s} \end{array}$$

$$\omega_1 = 2\pi \times 0.16 \times 10^9 = 13.5716 \times 10^9 \text{ rad/s}$$

$$\omega_2 = 2\pi \times 0.64 \times 10^9 = 40.192 \times 10^9 \text{ rad/s}$$

$$\begin{aligned} \omega_0 &= \sqrt{\omega_1 \omega_2} = 15.004 \times 10^9 \text{ rad/s} \\ &= 15 \times 10^9 \text{ rad/s.} \end{aligned}$$

$$\Delta = \frac{\omega_2 - \omega_1}{\omega_0}$$

$$\Delta = \frac{(16.5876 - 13.5716) \times 10^9}{15 \times 10^9}$$

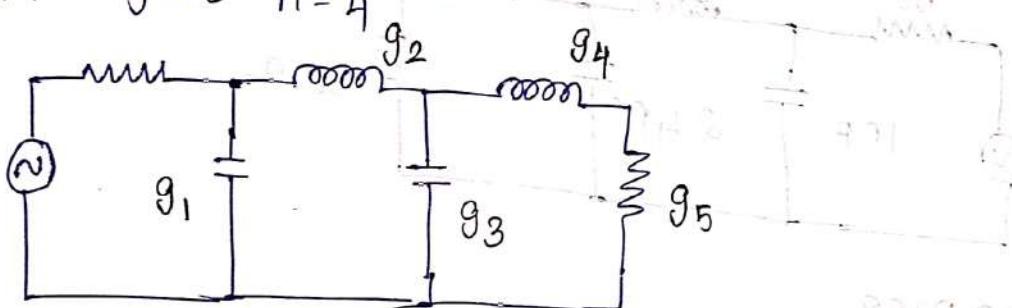
$$\boxed{\Delta = 0.801}$$

i) Butterworth filter:

low pass:

$$L_K^1 = \frac{R_o L_K}{\omega_c} \quad C_K^1 = \frac{C_K}{R_o \omega_c}$$

HPF for  $n=4$



$$g_1 = 0.7654 \quad g_5 = 1$$

$$g_2 = 1.8478$$

$$g_3 = 1.8478$$

$$g_4 = 0.7654$$

For  $g_1$

$$C_K^1 = \frac{C_K}{R_o \omega_c} = \frac{0.7654}{50 \times 2\pi \times 0.4 \times 10^9}$$

$$C_K^1 = 1.015 \times 10^{-12} F$$

For  $g_2$

$$L_K^1 = \frac{R_o L_K}{\omega_c} = \frac{50 \times 1.8478}{2\pi \times 0.4 \times 10^9}$$

$$= 6.126 \text{ nH}$$

Part 93

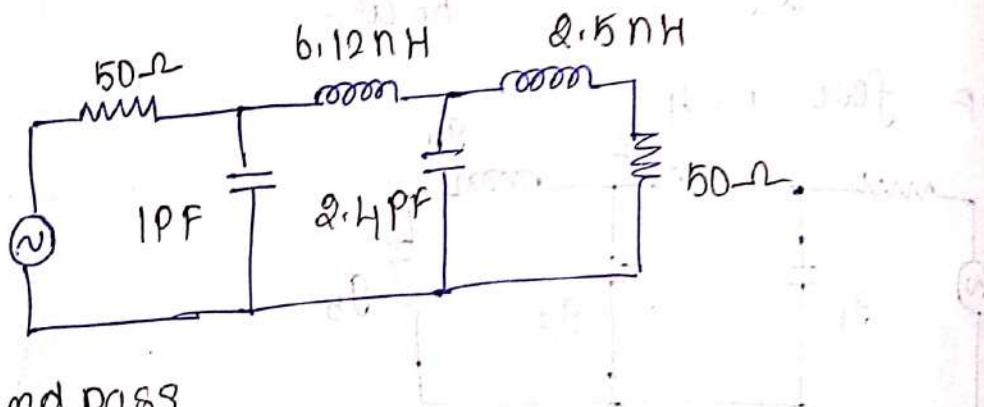
$$C_K' = \frac{C_K}{R_0 w_c} = \frac{1.8478}{50 \times 2\pi \times 0.4 \times 10^9}$$

$$C_K' = 0.4507 \text{ pF}$$

Part 94

$$L_K' = \frac{R_0 L_K}{w_c} = \frac{50 \times 0.7654}{2\pi \times 2.4 \times 10^9}$$

$$L_K' = 2.5378 \text{ nH}$$



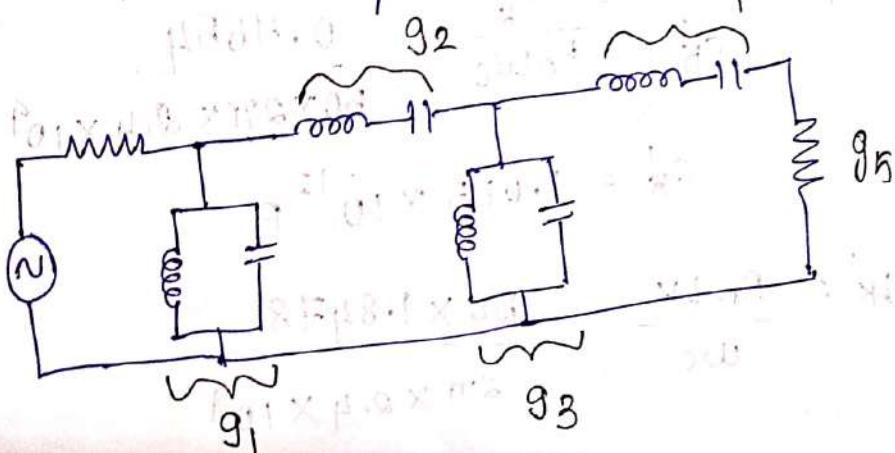
Band pass

$$g_1 = 0.7654$$

$$g_2 = 1.8478 \quad g_5 = 1$$

$$g_3 = 1.8478$$

$$g_4 = 0.7654$$



series

$$L_K' = \frac{L_K R_0}{\Delta w_0}$$

shunt

$$L_K' = \frac{\Delta R_0}{w_0 C_K}$$

$$C_K' = \frac{A}{R_0 w_0 L_K}$$

$$C_K' = \frac{C_K}{\Delta w_0 R_0}$$

Shunt (g<sub>1</sub>)

$$L_K' = \frac{\Delta R_0}{w_0 C_K} = \frac{0.201 \times 50}{2\pi \times 90 \times 2.4 \times 10^9 \times 0.7654}$$

$$L_K' = 0.8704 \text{ nH}$$

$$C_K' = \frac{C_K}{R_0 w_0} = \frac{100 \times 0.7654}{0.201 \times 2\pi \times 2.4 \times 10^9 \times 50}$$

$$C_K' = 5.050 \text{ pF}$$

Series (g<sub>2</sub>)

$$L_K' = \frac{L_K R_0}{\Delta w_0} = \frac{1.8478 \times 50}{0.201 \times 2\pi \times 2.4 \times 10^9}$$

$$L_K' = 30.481 \text{ nH}$$

$$C_K' = \frac{A}{R_0 w_0 L_K} = \frac{0.201}{50 \times 2\pi \times 2.4 \times 10^9 \times 1.8478}$$

$$C_K' = 0.14427 \text{ pF}$$

shunt (g<sub>3</sub>)

$$L_K' = \frac{\Delta R_0}{w_0 C_K} = \frac{0.201 \times 50}{2\pi \times 2.4 \times 10^9 \times 1.8478}$$

$$L_K' = 0.3606 \text{ nH}$$

$$C_K = \frac{C_K}{\Delta W_0 R_0}$$

$$C_K = \frac{1.8478}{0.201 \times 2\pi \times 2.4 \times 10^9 \times 50}$$

$$C_K = 12.1926 \text{ pF}$$

Series (g4)

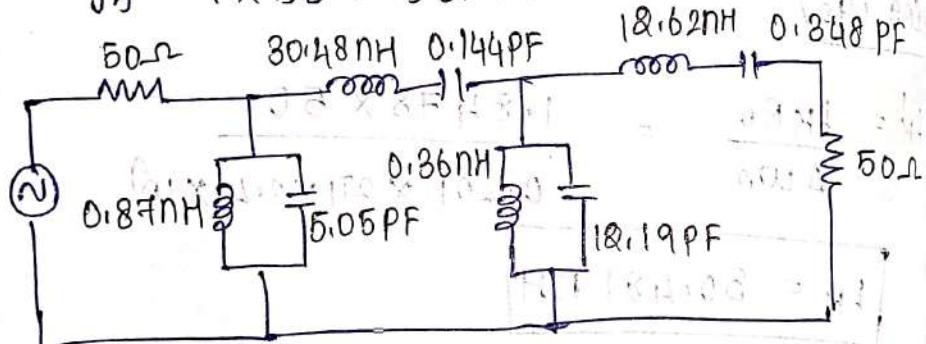
$$L_K = \frac{L_K R_0}{\Delta W_0} = \frac{0.7654 \times 50}{0.201 \times 2\pi \times 2.4 \times 10^9}$$

$$L_K = 12.6261 \text{ nH}$$

$$C_K = \frac{\Delta}{R_0 W_0 L_K} = \frac{0.201}{50 \times 2\pi \times 10^9 \times 2.4 \times 10^9 \times 0.765}$$

$$C_K = 0.3482 \text{ pF}$$

$$g_5 = 1 \times 50 = 50 \Omega$$



ii) chebyshev filter: (0.5 dB ripple)

$$g_1 = 1.6703$$

$$g_2 = 1.1926$$

$$g_3 = 2.3661$$

$$g_4 = 0.8419$$

$$g_5 = 1.9841$$

shunt (g1)

$$L_K^1 = \frac{\Delta R_0}{\omega_0 C_K} = \frac{0.201 \times 50}{2\pi \times 2.4 \times 10^9 \times 1.6703} = 0.899 \text{ nH}$$

$$C_K^1 = \frac{C_K}{\Delta \omega_0 R_0} = \frac{1.6703}{0.201 \times 2\pi \times 2.4 \times 10^9 \times 50} = 11.02 \text{ pF}$$

series (g2)

$$L_K^1 = \frac{L_K R_0}{\Delta \omega_0} = \frac{1.1926 \times 50}{2\pi \times 2.4 \times 10^9 \times 0.201} = 19.67 \text{ nH}$$

$$C_K^1 = \frac{\Delta}{R_0 \omega_0 L_K} = \frac{0.201}{50 \times 2\pi \times 2.4 \times 10^9 \times 1.1926} = 0.82 \text{ pF}$$

shunt (g3)

$$L_K^1 = \frac{\Delta R_0}{\omega_0 C_K} = \frac{0.201 \times 50}{2\pi \times 2.4 \times 10^9 \times 2.3661} = 0.281 \text{ nH}$$

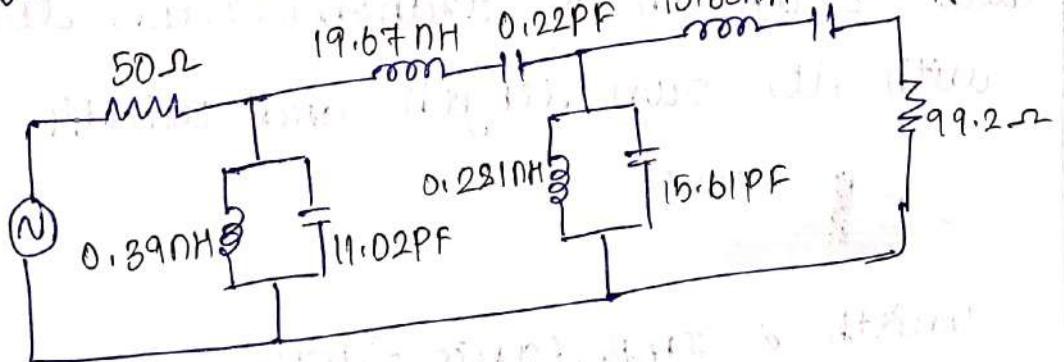
$$C_K^1 = \frac{C_K}{\Delta \omega_0 R_0} = \frac{2.3661}{0.201 \times 2\pi \times 2.4 \times 10^9 \times 50} = 15.61 \text{ pF}$$

series (g4)

$$L_K^1 = \frac{L_K R_0}{\Delta \omega_0} = \frac{0.8419 \times 50}{0.201 \times 2\pi \times 2.4 \times 10^9} = 13.88 \text{ nH}$$

$$C_K^1 = \frac{C_K}{R_0 \omega_0 L_K} = \frac{0.201}{50 \times 2\pi \times 2.4 \times 10^9 \times 0.8419} = 0.316 \text{ pF}$$

$$g_5 = 1.9841 \times 50 = 99.205 \Omega$$



25.10.25

- Limited range of lumped components
- connection line: frequency variation

To overcome this we go for filter implementation

→ Richard's transformation

→ Kuroda's transformation

→ Translating  $\omega \rightarrow \omega_2$  (ohm)

$$j\omega_2 = j\tan(\beta L)$$

$$= j \tan\left(\frac{\omega}{V_p} L\right)$$

$$jX_L = j\omega L = j\omega_2 L = L \tan(\beta L)$$

$$j\omega C = j\omega c = j\omega_2 c = c \tan(\beta L)$$

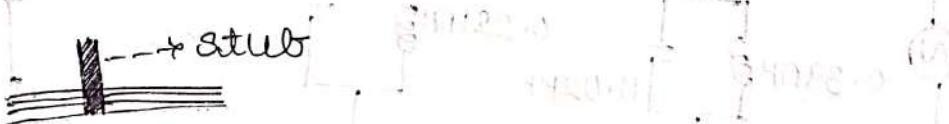
$L \tan(\beta L) \rightarrow$  representation of short

circuit stub, impedance  $L \tan(\beta L)$

$C \Rightarrow$  open circuited stub, impedance  $\frac{1}{L \tan(\beta L)}$

stub: Extension of transmission line

with its own length and width



width & impedance factor

Length depends on frequency

Let  $\omega_c = 1$  | Impedance = 1

$$\tan \phi = -\frac{Z}{1} = -1$$

$$\phi = \tan^{-1}(-1) = \pi/4$$

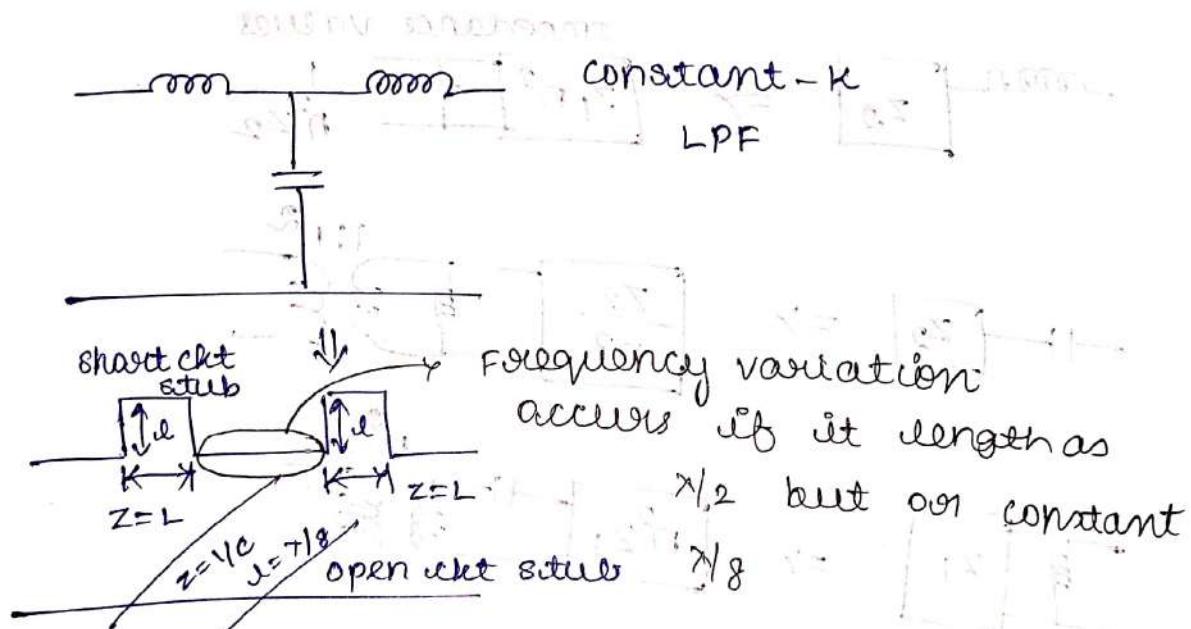
$$d = \frac{\pi/4}{\beta}$$

$$d = \frac{\pi/4}{8\pi/\lambda} \Rightarrow \frac{\pi/4}{8\pi} \times \frac{\lambda}{2\pi}$$

$$d = \frac{\lambda}{8}$$

= Normalised Impedance  
Repeats every  $4\omega_c$ .

frequency changes, in terms of  $\lambda$   
it varies (length varies)



Kuroda's transformation:

- physically separate Tx line stubs
- Transform series stub to shunt stub and shunt stub to series stub

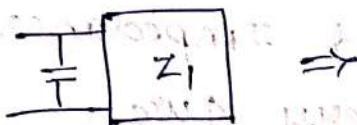
→ change impractical characteristic impedance into more realistic

1)

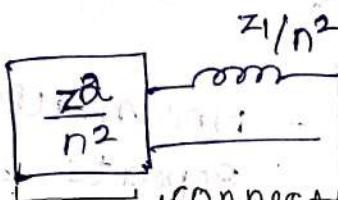


physical separation

2)



$\Rightarrow$



$\frac{Z_1}{n^2}$

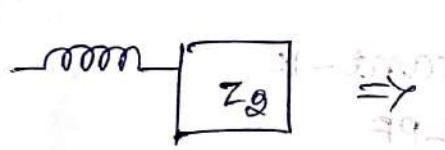
$\frac{Z_2}{n^2}$

$n^2 = 1 + \frac{Z_2}{Z_1}$

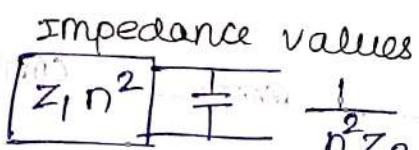
$\frac{Z_2}{n^2}$

connecting line  $\frac{Z_2}{n^2}$

can nullify frequency variations



$\Rightarrow$



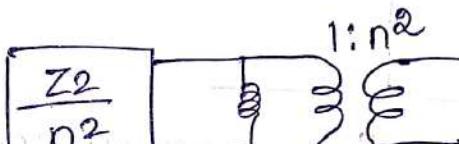
Impedance values

$Z_1 n^2$

$\frac{1}{n^2 Z_2}$



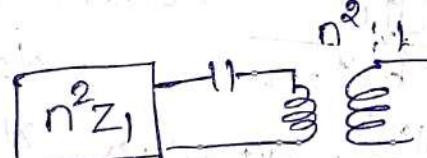
$\Rightarrow$



$1:n^2$

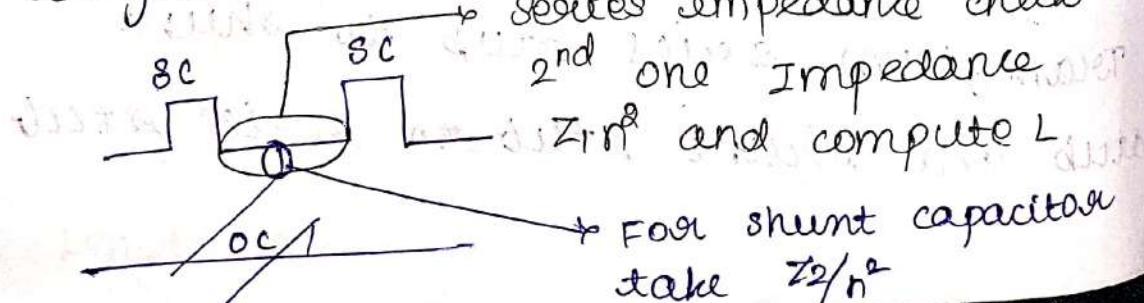


$\Rightarrow$



$n^2 : 1$

Take impedance value and compute  
length between impedances.



series impedance check

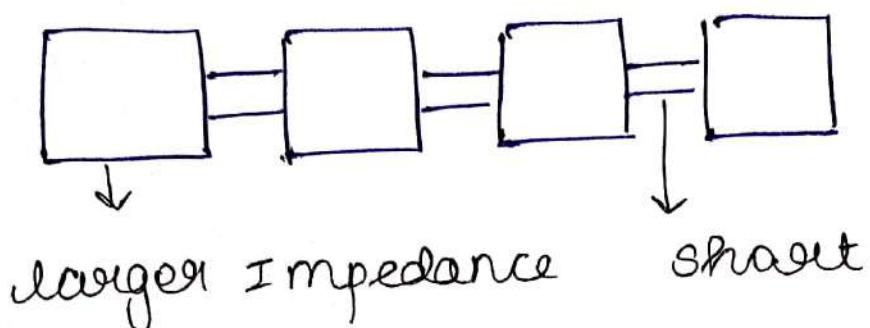
2nd one impedance

$Z_1 n^2$  and compute L

For shunt capacitor

take  $Z_2 / n^2$

stepped Impedance:



Higher Impedance = L

smaller Impedance = C

$$\beta l = \frac{L R_0}{Z_0}$$

$$\beta l = \frac{C Z_L}{R_0}$$

Coupled line BP filter design.