

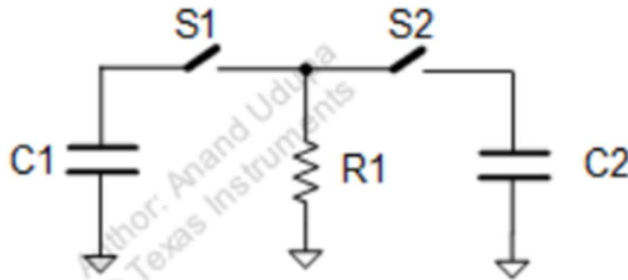
TI BYTE Simulation Exercise

Bonus Simulation Questions

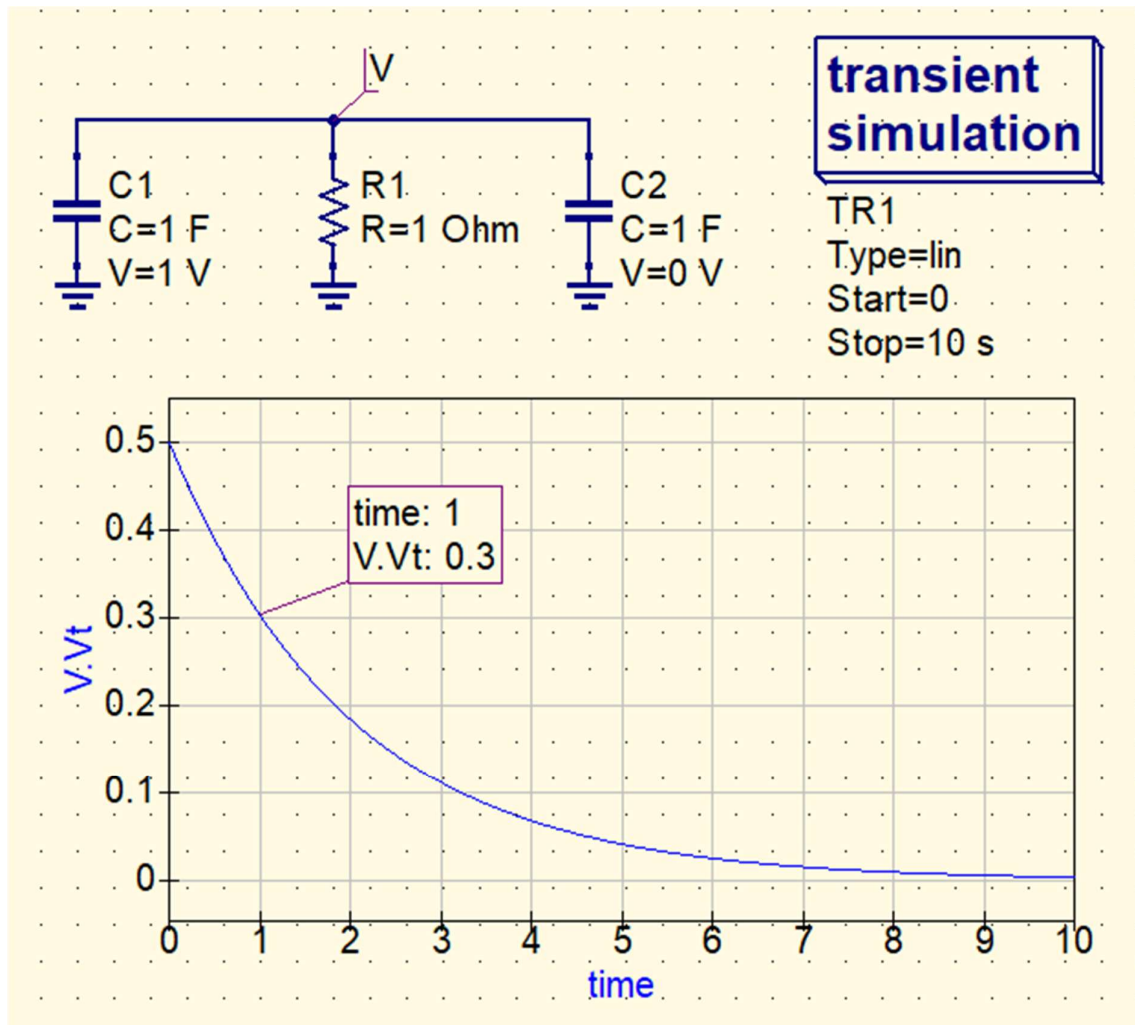
- **Question 1:**

408. $C_1=1F$, $C_2=1F$, $R_1=1\Omega$. Initial charge on the caps is $Q_1=1C$, $Q_2=0C$. Both switches are closed at $t=0$. The voltage across the resistor at $t=1\text{sec}$ is:

- (a) 0.5V
- (b) 0.61V
- (c) 0.30V
- (d) 0.37V
- (e) 0.07V
- (f) 0V
- (g) 1V
- (h) 0.14V



➤ **QUCS Circuit:**



- V is used to label the node and find the voltage at that node.
- Both the capacitors are of 1F. Capacitor C2 is initially uncharged while C1 has an initial charge of 1C.
- At $t = 0$, since both the switches are closed, they are replaced with short-circuits.

➤ **QUCS Result:**

Therefore, from the simulation, we get our answer as:

At $t = 1\text{s}$, $V = 0.30\text{ V}$

Answer: (c)

➤ **Conclusion:**

- In the circuit, at $t = 0$ when the switches are closed, the capacitors share their charges. So, the common voltage of the two capacitors becomes,

$$V = \frac{C_1 V_1 + C_2 V_2}{C_1 + C_2} = \frac{1 \times 1 + 1 \times 0}{1 + 1} = 0.5\text{ V}$$

- Therefore, $V_i = 0.5\text{ V}$
- Now, after ample amount of time, the capacitors discharge through the resistor R1 and thus $V_f = 0\text{ V}$
- For the given circuit, $R_{eq} = 1\ \Omega$ and $C_{eq} = 2\text{ F}$.
- Therefore, the voltage eqn. of the can be written as:

$$V(t) = V_f + (V_i - V_f)e^{-t/\tau}$$

where V_f is the final voltage, V_i is the initial voltage and τ is the time constant $= RC = 2\text{ s}$.

- Therefore, at $t = 1\text{ s}$,

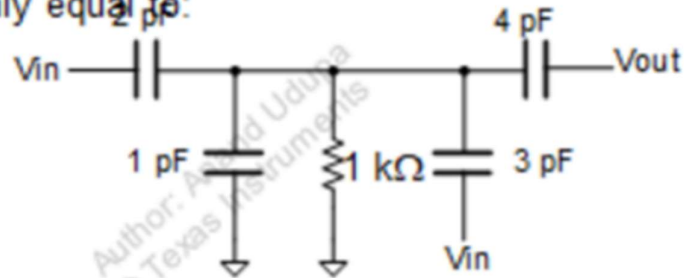
$$\begin{aligned} V(t) &= [0 + (0.5 - 0)e^{\frac{-1}{2}}] \\ &= 0.5e^{-0.5} = 0.303\text{ V} \approx 0.30\text{ V} \end{aligned}$$

- The simulation result almost matches with our calculations.

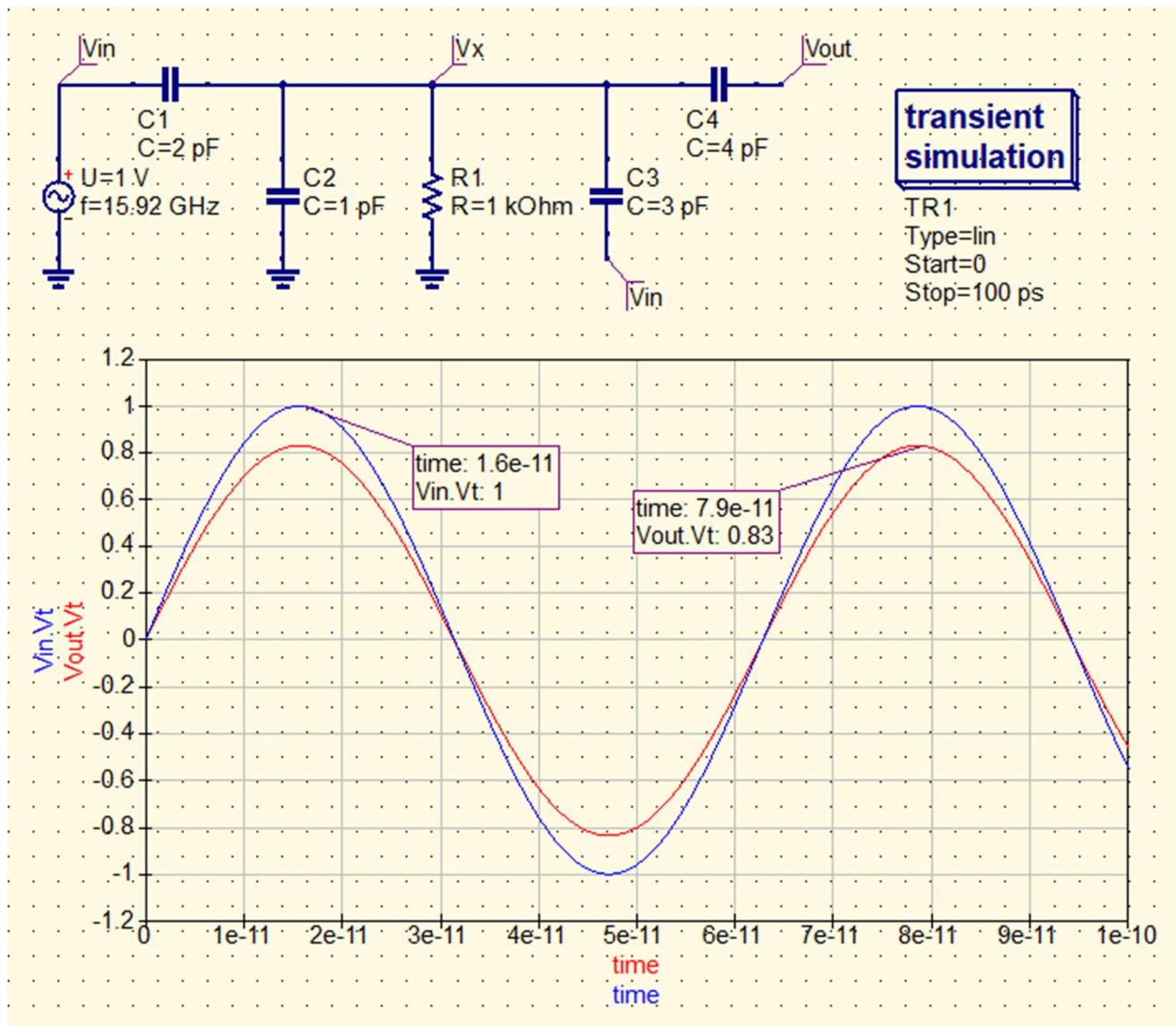
• **Question 2:**

711. A sine wave of amplitude 1V and frequency 100 Grad/s is applied at VIN. The amplitude at VOUT is roughly equal to:

- (a) 1 V
- (b) 0.33 V
- (c) 0.5 V
- (d) 0 V
- (e) 0.99 V
- (f) 0.25 V
- (g) 0.63 V
- (h) 0.83 V



➤ **QUCS Circuit:**



- V_{in} is a sinusoidal input given to the circuit with an amplitude of 1V and frequency of $100 \text{ Grad/s} = 15.915 \text{ GHz}$
- V_{out} is used to label the output node and find the voltage at that node.
- All the capacitors are uncharged.

➤ **QUCS Result:**

Therefore, from the simulation, we get our answer as:

Amplitude of $V_{out} = 0.83 \text{ V}$

Answer: (h)

➤ **Conclusion:**

- Given that the frequency of the input signal(ω) is 100 Grad/s ,

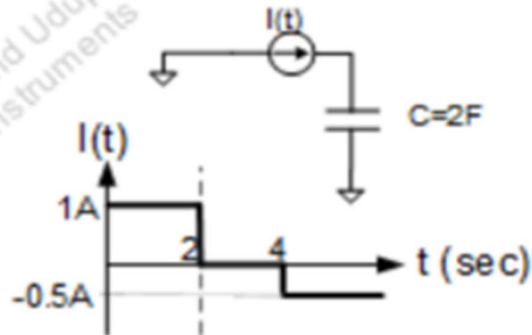
$$f = \frac{\omega}{2\pi} = 15.92 \text{ GHz}$$

- At this frequency, the 4 pF capacitor essentially acts as a short-circuit, so $V_{out} = V_x$.
- Now, the 2 pF and the 3 pF capacitors are then essentially in parallel between V_{in} and V_x . ($C' = 2 \text{ pF} + 3 \text{ pF} = 5 \text{ pF}$)
- So, V_x is thus the voltage division between the 1 pF capacitor and the 5 pF capacitor.
- So, $V_{out} = V_x = \frac{5 \text{ pF}}{1 \text{ pF} + 5 \text{ pF}} \times V_{in} = \frac{5}{6} V = 0.8333 V \approx 0.83 V$
- The simulation result almost matches with our calculations.

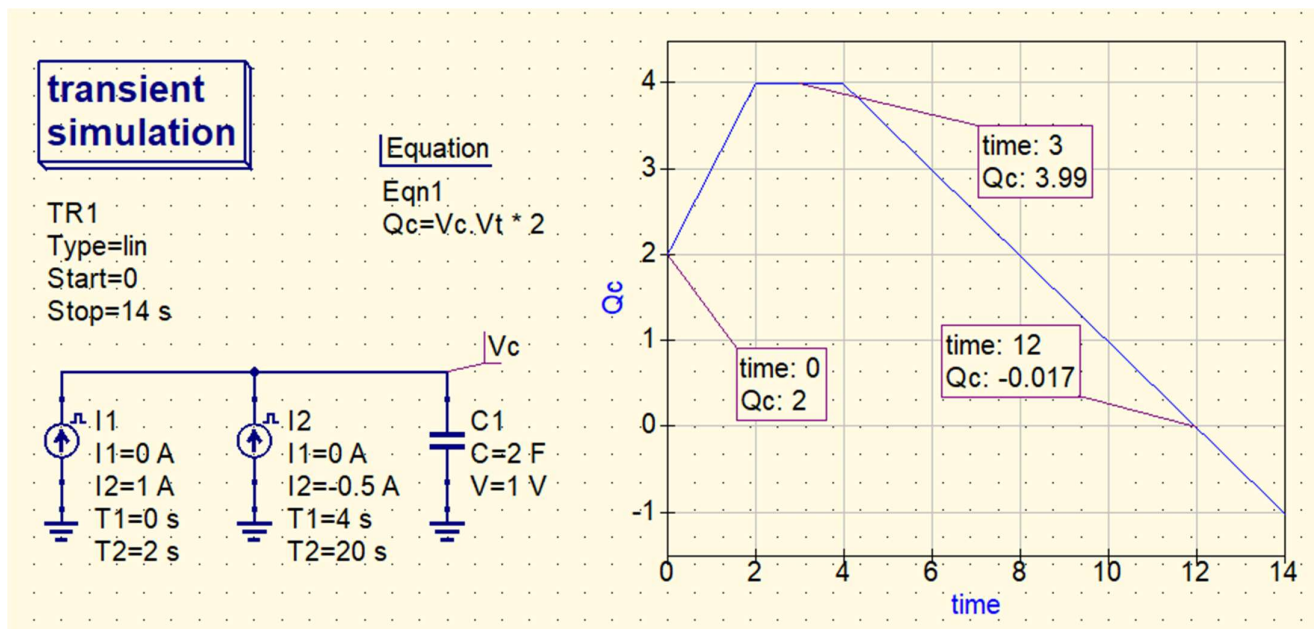
• Question 3:

109. A 2F cap has an initial charge of 2C at $t=0$. It is charged by a current source of value 1A for 2sec. The current source becomes 0A for the next 2sec. Then, the current source switches polarity and its value becomes -0.5A. At what time does charge on the capacitor become 0C?

- (a) $t=4\text{sec}$
- (b) $t=6\text{sec}$
- (c) $t=8\text{sec}$
- (d) $t=10\text{sec}$
- (e) $t=12\text{sec}$
- (f) $t=16\text{sec}$
- (g) $t=20\text{sec}$
- (h) Never



➤ QUCS Circuit:



- V_c is used to label the node and find the voltage at that node.
- The capacitor has an initial charge of 2C.
- The two current DC sources are used to implement the given current waveform. They are thus used to charge and discharge the capacitor.

➤ **QUCS Result:**

Therefore, from the simulation, we get our answer as:

At time $t = 12$ sec, the charge on the capacitor become 0C.

Answer: (e)

➤ **Conclusion:**

- The capacitor has an initial charge of 2C.
- For 2 sec, it is charged using a 1A current source. Thus, the total charge delivered to the capacitor $= 1A \times 2 s = 2C$.
- So, the final charge on the capacitor after $t = 2$ sec, $Q_c = 2C + 2C = 4C$
- Since the current from $t = 2$ sec to $t = 4$ sec is zero, no further charge is delivered to the capacitor and it remains the same.
- After $t = 4$ sec, the current becomes -0.5 A. Thus, the capacitor begins to discharge.
- The total time required by the capacitor to discharge with the -0.5A current source is,

$$\Delta t = \frac{Q_c}{I} = \frac{4 C}{0.5 A} = 8 s$$

- So, the final time when the capacitor charge becomes 0 is,

$$T = t + \Delta t = 4 s + 8 s = 12 s$$

- The simulation result almost matches with our calculations.