

198. Given a graph represented by an adjacency matrix, implement Dijkstra's Algorithm to find the shortest path from a given source vertex to all other vertices in the graph. The graph is represented as an adjacency matrix where $graph[i][j]$ denote the weight of the edge from vertex i to vertex j . If there is no edge between vertices i and j , the value is Infinity (or a very large number).

Program:

```
import heapq

def dijkstra(graph, source):
    n = len(graph)
    dist = [float('inf')] * n
    dist[source] = 0
    heap = [(0, source)] # (distance, vertex)
    while heap:
        d, u = heapq.heappop(heap)
        # If current distance is greater than known shortest distance, skip it
        if d > dist[u]:
            continue
        for v in range(n):
            if graph[u][v] != float('inf'): # There is an edge from u to v
                if dist[u] + graph[u][v] < dist[v]:
                    dist[v] = dist[u] + graph[u][v]
                    heapq.heappush(heap, (dist[v], v))
    return dist

# Example 1
graph1 = [
    [0, 10, 3, float('inf'), float('inf')],
    [float('inf'), 0, 1, 2, float('inf')],
    [float('inf'), 4, 0, 8, 2],
```

```

[ float('inf'), float('inf'), float('inf'), 0, 7],
[ float('inf'), float('inf'), float('inf'), 9, 0]
]

source1 = 0

print(dijkstra(graph1, source1)) # Output: [0, 7, 3, 9, 5]

# Example 2

graph2 = [

    [0, 5, float('inf'), 10],

    [float('inf'), 0, 3, float('inf')],

    [float('inf'), float('inf'), 0, 1],

    [float('inf'), float('inf'), float('inf'), 0]

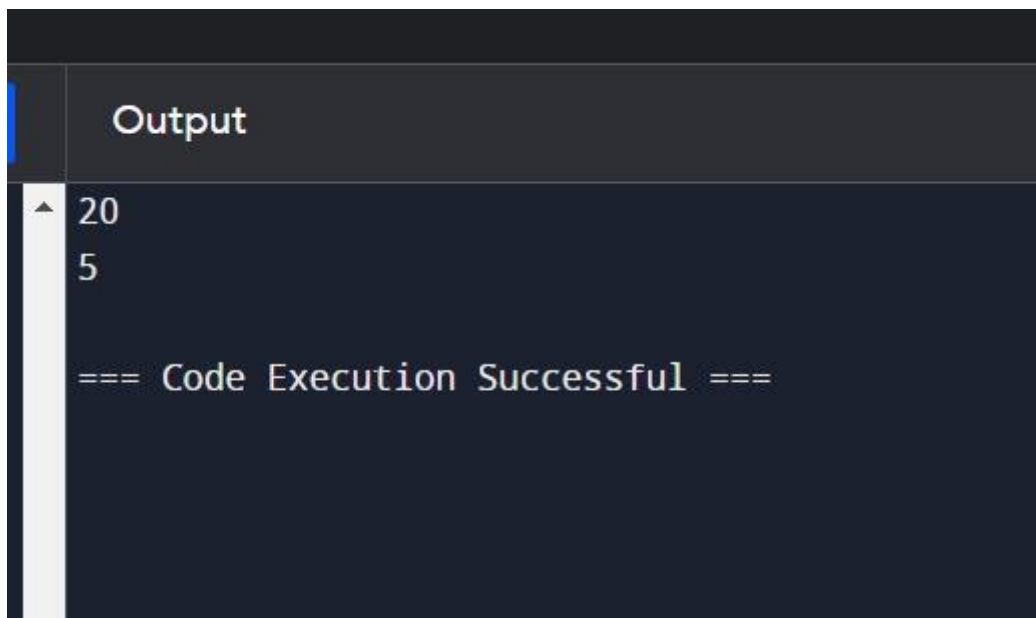
]

source2 = 0

print(dijkstra(graph2, source2))

```

Output:



```

Output
20
5

=== Code Execution Successful ===

```

Time complexity: $O(n^2)$