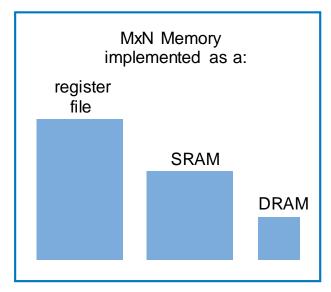
Systems

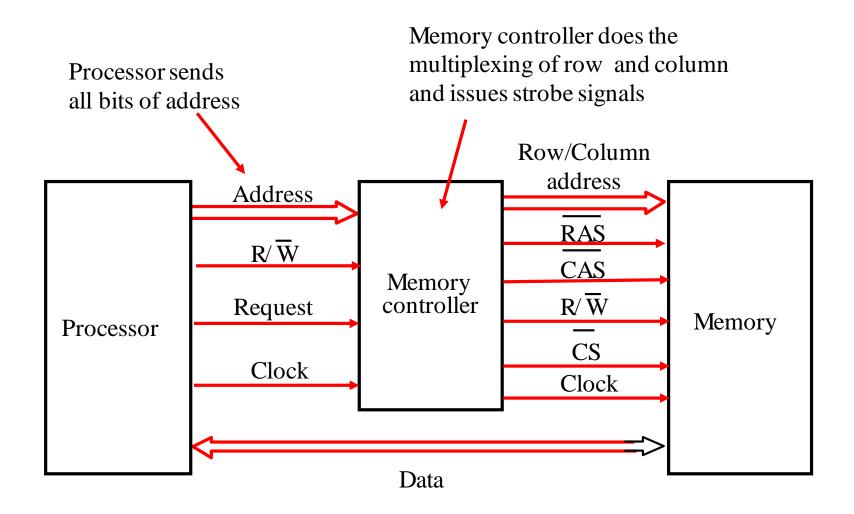


Comparing Memory

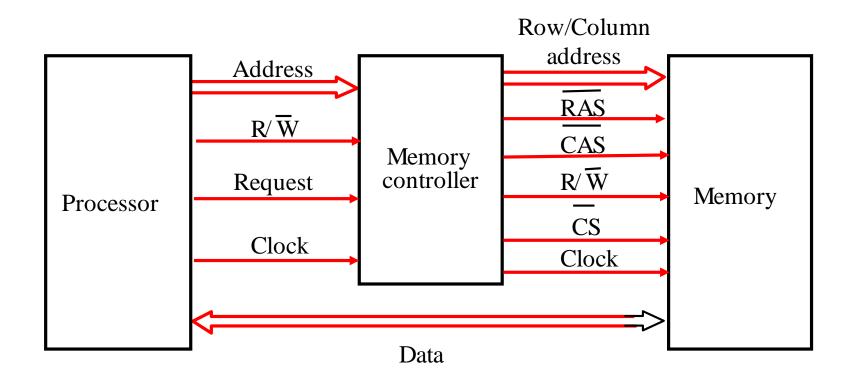
- Register file
 - Fastest
 - But biggest size
- SRAM
 - Fast
 - More compact than register file
- DRAM
 - Slowest (capacitor)
 - And refreshing takes time
 - But very compact (lower cost)
- Use register file for small items, SRAM for large items, and DRAM for huge items
 - Note: DRAM's big capacitor requires a special chip design process, so DRAM is often a separate chip



Size comparison for same number of bits (not to scale)



Use of a memory controller.



Memory controller provides the refresh control if not done on the chip

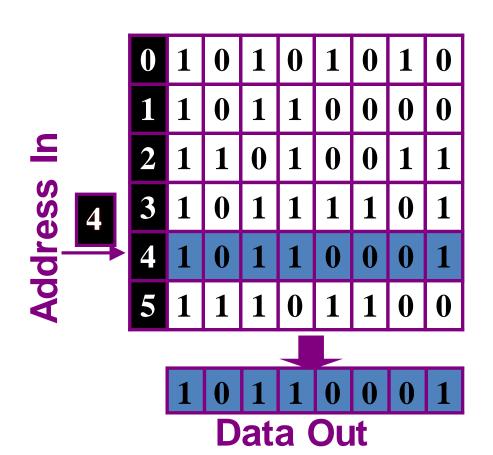
Refreshing typically once every 64 ms. At a cost of .2ms

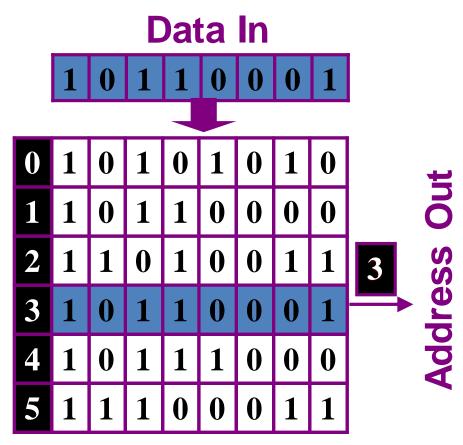
Less than .4% overhead

Use of a memory controller.

CAM

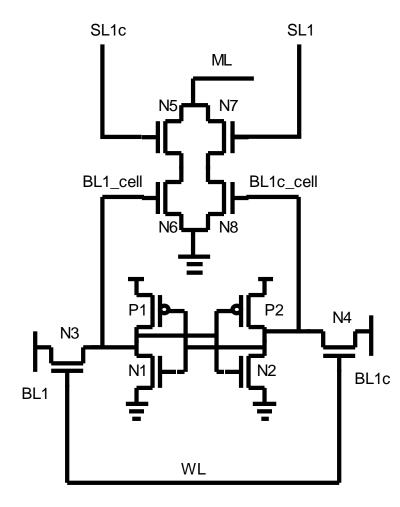
CAM vs. RAM





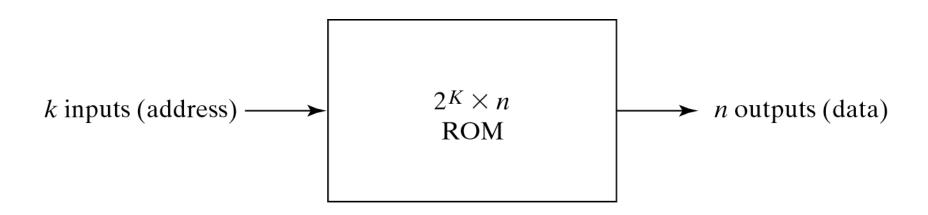
CAM

- Binary CAM Cell
 - ML pre-charged to V_{DD}
 - Match: ML remains at V_{DD}
 - Mismatch: ML discharges



Read-Only Memory

- A block diagram of a ROM is shown below. It consists of k address inputs and n data outputs.
- The number of words in a ROM is determined from the fact that k
 address input lines are needed to specify 2^k words.



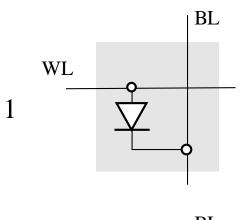
ROM Block diagram 2^k xn Module

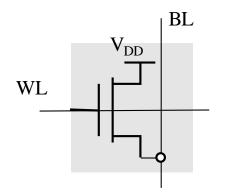
Read-Only Memory Cells

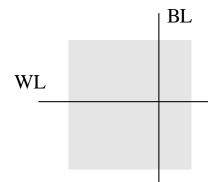
Bit line (BL) is resistively clamped to the ground, so its default value is 0

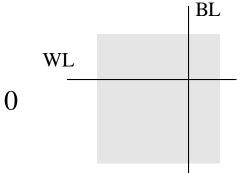
Diode disadvantage – no electrical isolation between bit and word lines

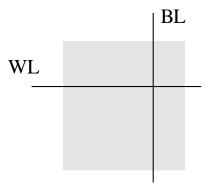
BL is resistively clamped to VDD, so its default value is 1

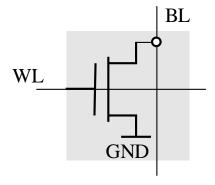












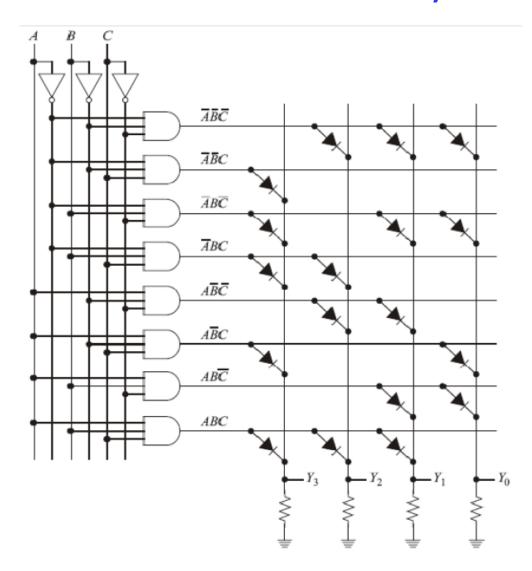
Diode ROM

MOS ROM 1

MOS ROM 2

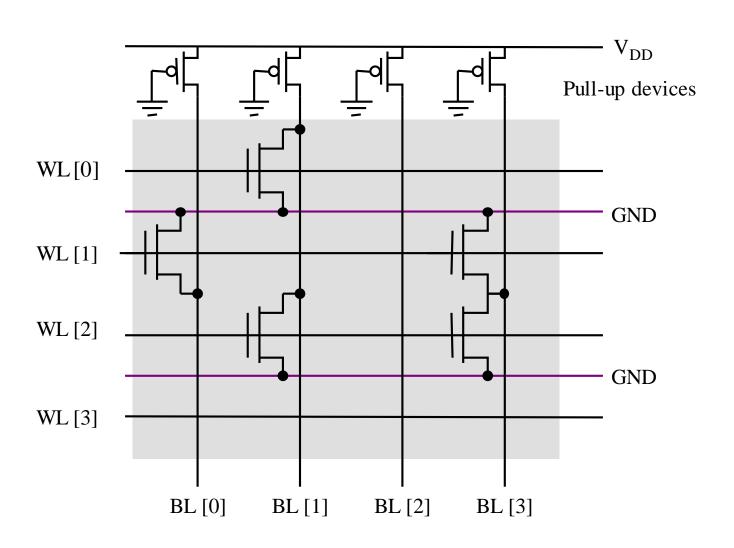
Nonvolatile Memory

ROM PROM EPROM

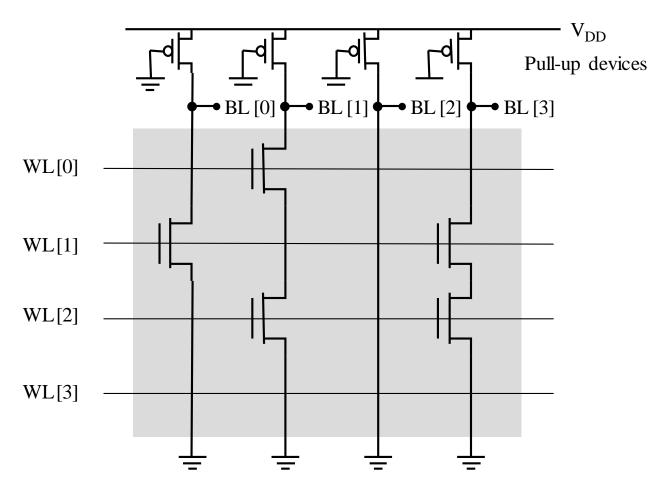


Read-only memory organization, with the fixed contents shown on the right.

MOS NOR ROM

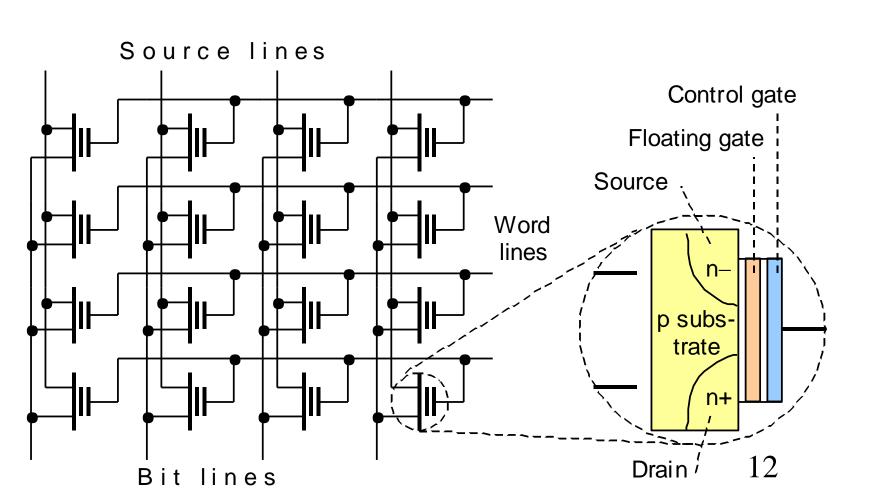


MOS NAND ROM



All word lines high by default with exception of selected row

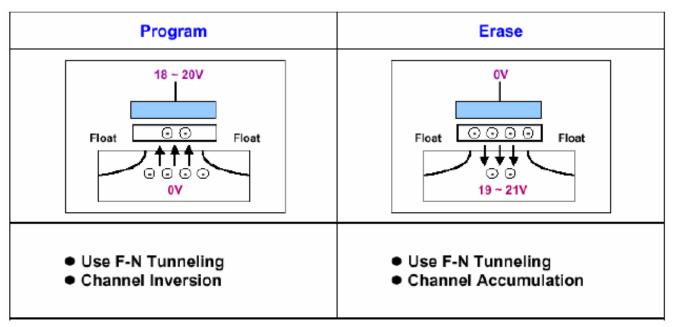
Flash Memory



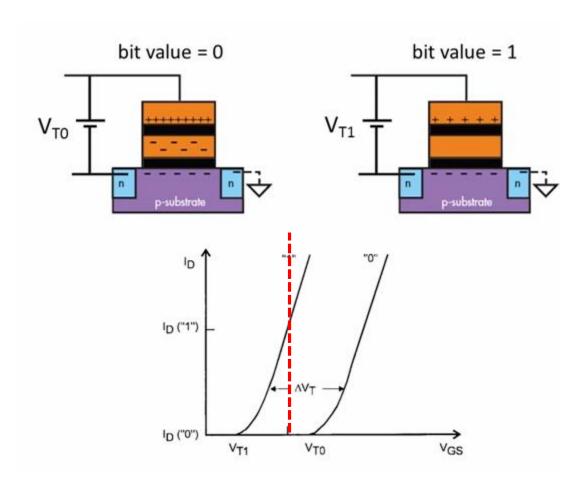
Flash memory

Flash memory

- Non volatile read only memory (ROM)
- Erase Electrically or UV (EPROM)
- Uses F-N tunneling for program & erase
- Reads like DRAM (~ns)
- Writes like DISK (~ms).

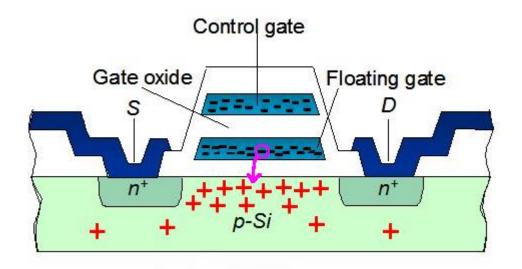


Reading Memory State



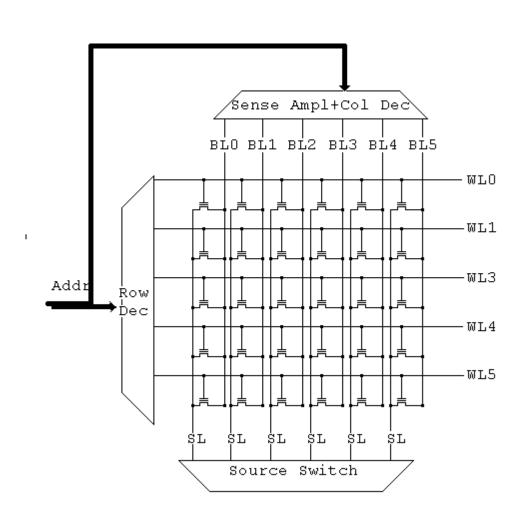
Change in Threshold Voltage due to **Screening Effect** of Floating Gate Read mode: Apply intermediate voltage, check whether current is flowing or not

Writing Memory State



Control gate voltage determines whether electrons are injected to, or push/pulled out of floating gate.

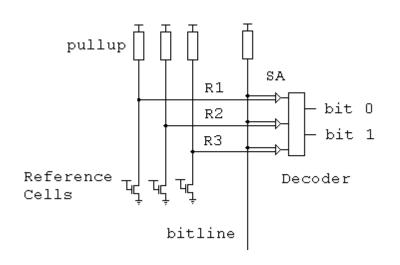
NOR Array



Reading:

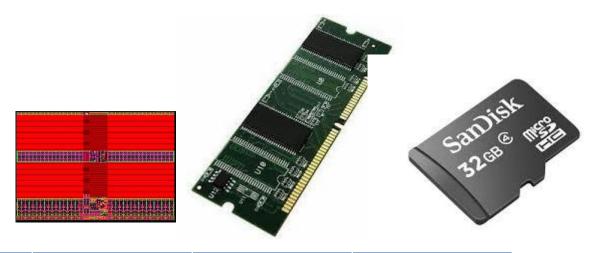
Assert a single word line.
The source lines are
asserted and the read of the
bitline gives the contents of
the cell.

Multi-Levels



 By using reference cells set at given levels and comparing them to the value from the bitline, we can determine the value stored.

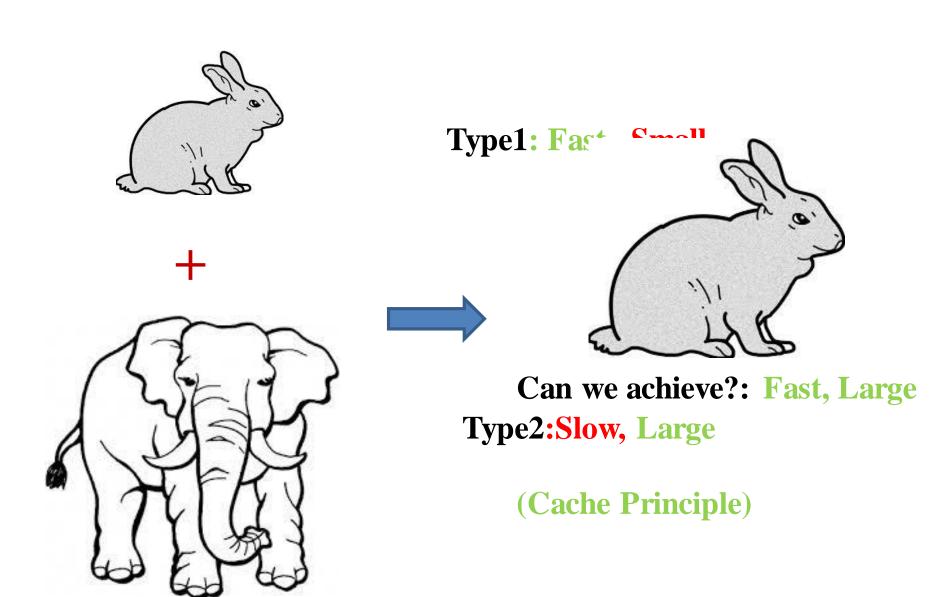
Review of memory technologies



Memory type	SRAM	DRAM	Flash
Speed	Very fast	Slow	Slow
Density	Low	High	Very high
Power	High	Low	Very low
Refresh	No	Yes	No
Mechanism	Bi-stable latch	Capacitor	FN tunneling

Memory Hierarchy

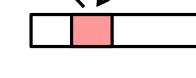
Actual Memory Systems



Locality

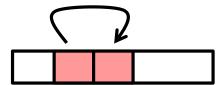
 Principle of Locality: Programs tend to use data and instructions with addresses near or equal to those they have used recently

Temporal locality:



 Recently referenced items are likely to be referenced again in the near future

Spatial locality:



Items with nearby addresses tend
 to be referenced close together in time

Locality Example

- Data references
 - Reference array elements in succession
 - Reference variable sum each iteration.
- Instruction references
 - Reference instructions in sequence.
 - Cycle through loop repeatedly.

```
sum = 0;
for (i = 0; i < n; i++)
    sum += a[i];
return sum;</pre>
```

Spatial locality

Temporal locality

Spatial locality

Temporal locality

Qualitative Estimates of Locality

- Claim: Being able to look at code and get a qualitative sense of its locality is a key skill for a professional programmer.
- Question: Does this function have good locality with respect to array a?

```
int sum_array_rows(int a[M][N])
{
   int i, j, sum = 0;

   for (i = 0; i < M; i++)
        for (j = 0; j < N; j++)
            sum += a[i][j];
   return sum;
}</pre>
```

Row-major order

$$\begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix}$$

Column-major order

```
\begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix}
```

1	2	3		row-major								
4	5	6	→	1	2	3	4	5	6	7	8	9
7	8	9		- Co					,		2	
1	2	3	column-major									
4	5	6	→	1	4	7	2	5	8	3	6	9

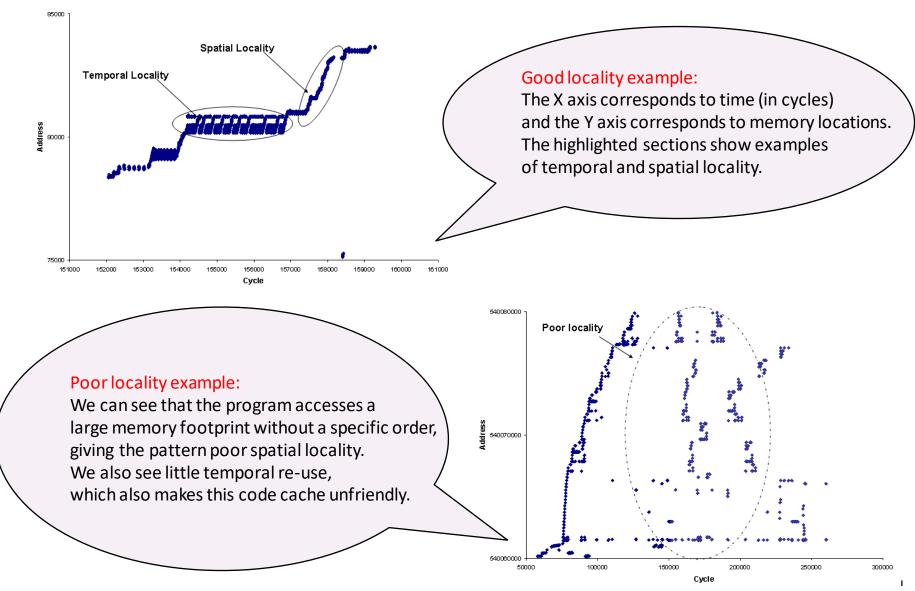
Locality Example

 Question: Does this function have good locality with respect to array a?

```
int sum_array_cols(int a[M][N])
{
   int i, j, sum = 0;

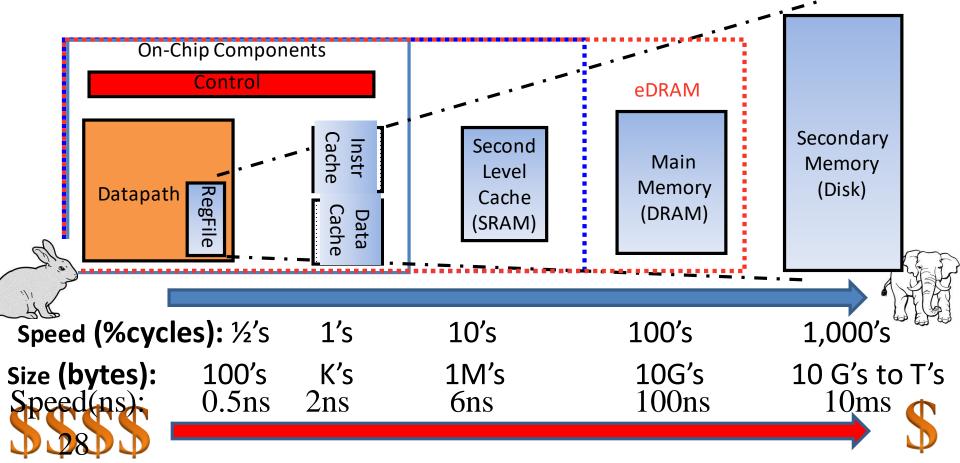
   for (j = 0; j < N; j++)
        for (i = 0; i < M; i++)
            sum += a[i][j];
   return sum;
}</pre>
```

Locality reference example



The Memory Hierarchy

- By taking advantage of the principle of locality
 - Can present the user with as much memory as is available in the cheapest technology
 - at the speed offered by the fastest technology

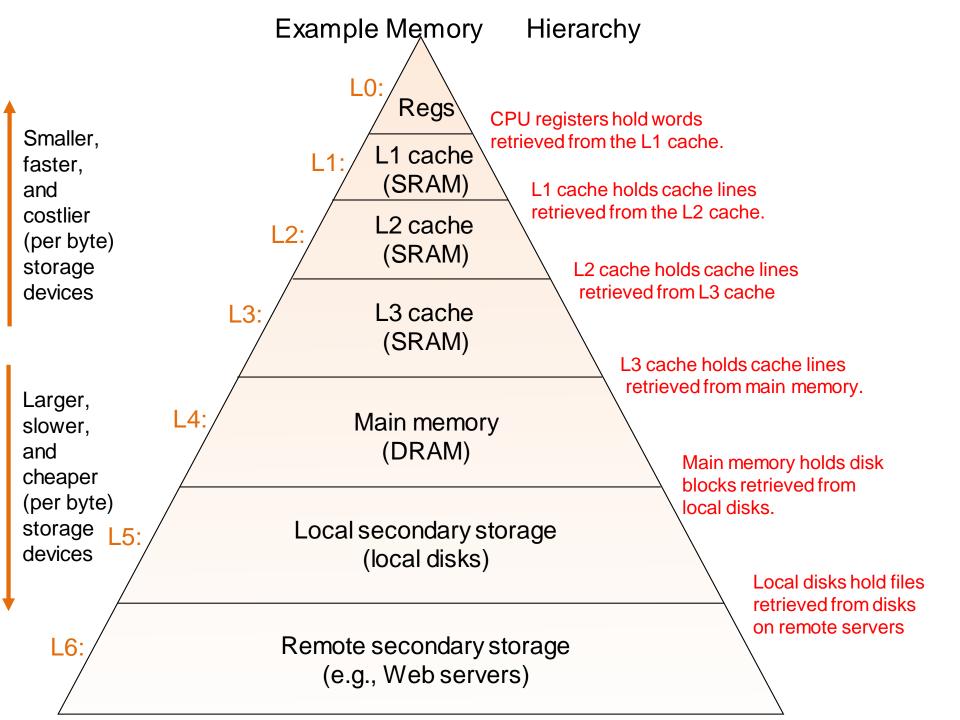


Cache Design

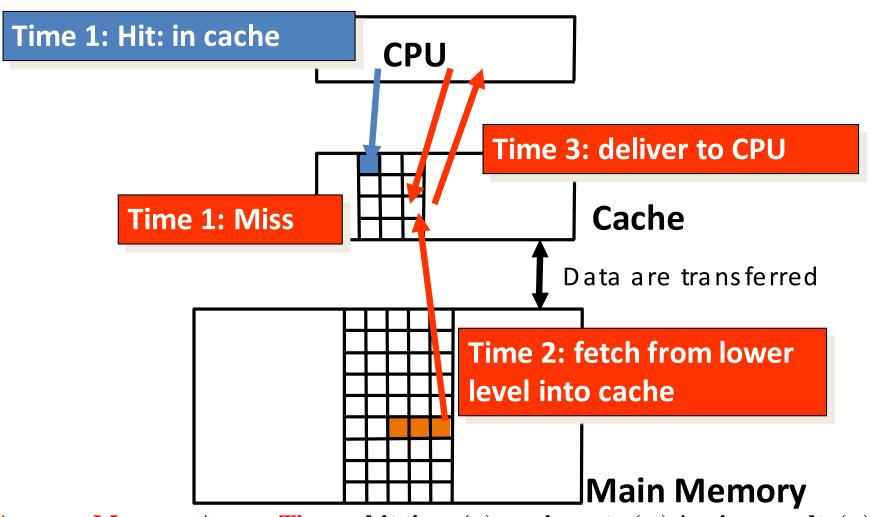
Maurice Wilkes, "Slave Memories and Dynamic Storage Allocation," IEEE Trans. On Electronic Computers, 1965

<u>Awards</u>: <u>Turing Award</u>, <u>IEEE John von Neumann</u> <u>Medal</u>, <u>Faraday Medal</u>, <u>Eckert–Mauchly Award</u>, Mountbatten Medal





Cache Example



Average Memory Access Time = hit time (t_c) + miss rate (m) * miss penalty (t_p) = t_c + m* t_p

31 **Hit time = Time 1 (tc)**

Miss penalty (tp)= Time 2 + Time 3

Example: Impact on Performance

- Suppose a processor executes at
 - Clock Rate = 1000 MHz (1 ns per cycle)
 - CPI = 1.1
 - 50% arith/logic, 30% ld/st, 20% control
- Suppose that 10% of memory operations get 50 cycle miss penalty
- 58 % of the time the processor is stalled waiting for memory!
- a 1% instruction miss rate would add an additional 0.5 cycles to the CPI!

32

Let's think about those numbers

- Huge difference between a hit and a miss
 - Could be 100x, if just L1 and main memory

- Would you believe 99% hits is twice as good as 97%?
 - Consider:
 cache hit time of 1 cycle
 miss penalty of 100 cycles
 - Average access time:

97% hits: 1 cycle + 0.03 * 100 cycles = 4 cycles 99% hits: 1 cycle + 0.01 * 100 cycles = 2 cycles

This is why "miss rate" is used instead of "hit rate"

Hierarchical Latency Analysis

- For a given memory hierarchy level i it has a technology-intrinsic access time of t_i , The perceived access time T_i is longer than t_i
- Except for the outer-most hierarchy, when looking for a given address there is
 - a chance (hit-rate h_i) you "hit" and access time is t_i
 - a chance (miss-rate m_i) you "miss" and access time $t_i + T_{i+1}$
 - $h_i + m_i = 1$
- Thus

$$T_i = h_i \cdot t_i + m_i \cdot (t_i + T_{i+1})$$
$$T_i = t_i + m_i \cdot T_{i+1}$$

keep in mind, h_i and m_i are defined to be the hit-rate and miss-rate of just the references that missed at L_{i-1}

Hierarchy Design Considerations

Recursive latency equation

$$T_i = t_i + m_i \cdot T_{i+1}$$

- The goal: achieve desired T₁ within allowed cost
- $T_i \approx t_i$ is desirable
- Keep m_i low
 - increasing capacity C_i lowers m_i, but beware of increasing t_i
 - lower m_i by smarter management
- Keep T_{i+1} low
 - faster lower hierarchies, but beware of increasing cost
 - introduce intermediate hierarchies as a compromise

Intel Pentium 4 Example

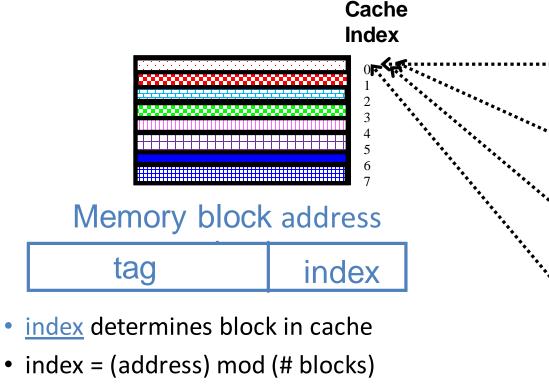
- 90nm P4, 3.6 GHz
- L1 D-cache

$$- C_1 = 16K$$

- $t_1 = 4$ cyc int / 9 cycle fp
- L2 D-cache
 - $C_2 = 1024 \text{ KB}$
 - $t_2 = 18$ cyc int / 18 cyc fp
- Main memory
 - $-t_3 = ~50$ ns or 180 cyc
- Notice
 - best case latency is not 1
 - worst case access latencies are into 500+ cycles

```
if m_1=0.1, m_2=0.1
         T_1=7.6, T_2=36
if m_1=0.01, m_2=0.01
         T_1=4.2, T_2=19.8
if m_1=0.05, m_2=0.01
         T_1=5.00, T_2=19.8
if m_1=0.01, m_2=0.50
         T_1=5.08, T_2=108
```

Simplest Cache: Direct Mapped



There is a Many-to-1 relationship between memory and cache

tags

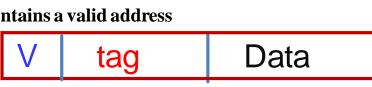
 contain the address information required to identify whether a word in the cache corresponds to the requested word.

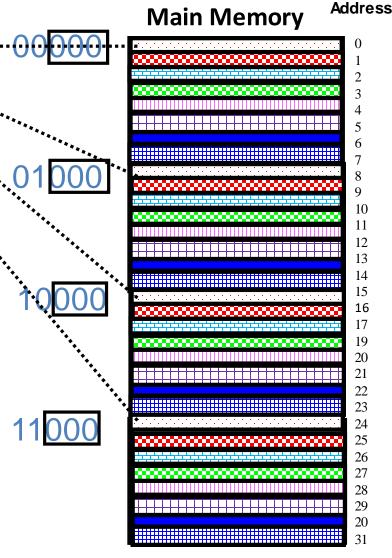
valid bit

• indicates whether an entry contains a valid address

Cache Table

Entry





Block

Direct Mapped Cache: Temporal Example



 Miss: valid
 lw
 \$1,22(\$0)

 Miss: valid
 lw
 \$2,26(\$0)

 Hit!
 lw
 \$3,22(\$0)

Index	Valid	Tag	Data
000	7		
001	7		
010	Υ	11	Memory[11010]
011	N		
100	N		
101	N		
110	Υ	10	Memory[10110]
111	N		

Direct Mapped Cache: Worst case, always miss!

-lw \$1,10 110 (\$0) -lw \$2,11 110 (\$0)

lw \$3,00 110 (\$0)

N

Miss: valid

Miss: tag

Miss: tag

lw \$1,22(\$0)

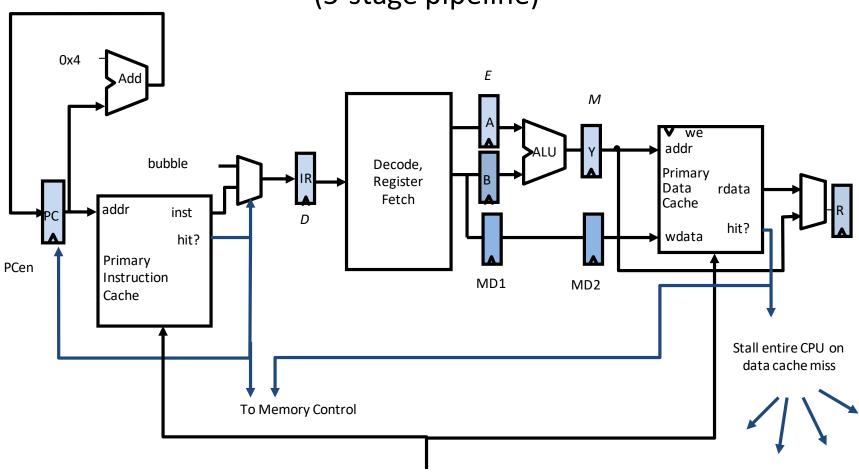
lw \$2,30(\$0)

lw \$3,6(\$0)

Index	Valid	Tag	Data
000	N		
001	N		
010	N		
011	N		
100	N		
101	N		
110	Υ	00	Memory[00110]

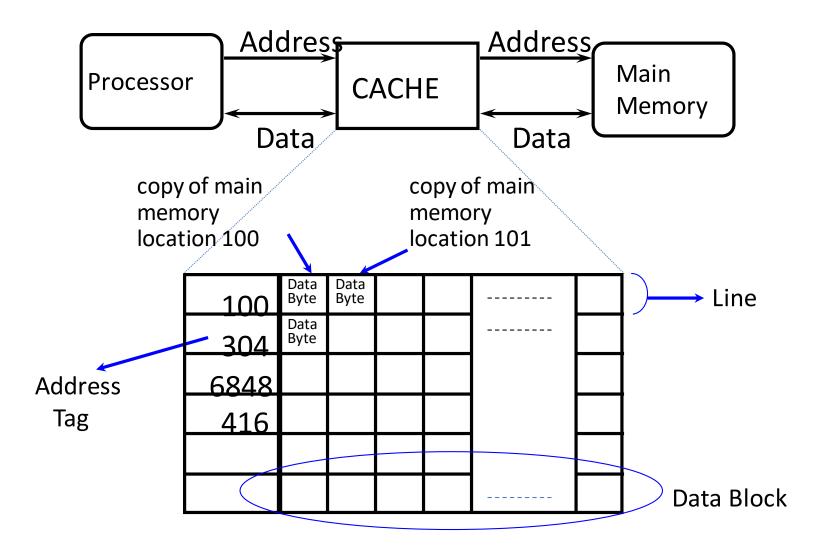
CPU-Cache Interaction

(5-stage pipeline)



Cache Refill Data from Lower Levels of Memory Hierarchy

Inside a Cache



Cache Algorithm (Read)

Look at Processor Address, search cache tags to find match. Then either

Found in cache a.k.a. HIT a.k.a. MISS

Return copy of data from cache

Read block of data from Main Memory

Wait ...

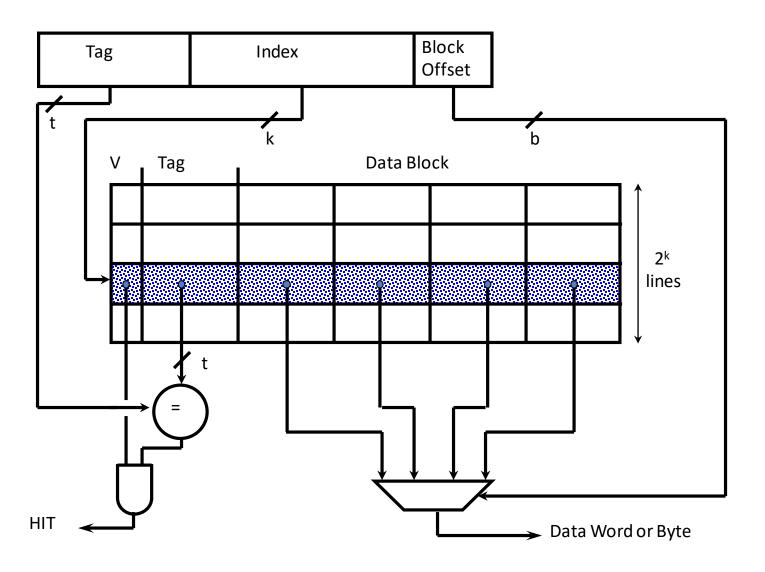
Return data to processor and update cache

Q: Which line do we replage?

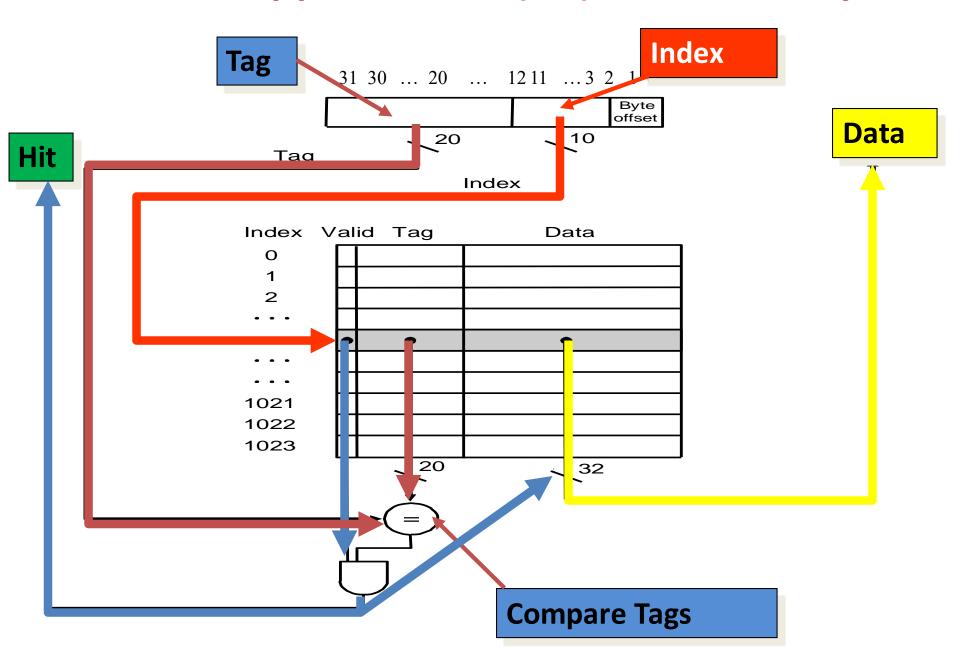
Caching Terminology

- block/line: the unit of information that can be exchanged between two adjacent levels in the memory hierarchy
- cache hit: when CPU finds a requested data item in the cache
- cache miss: when CPU does not find a requested data item in the cache
- miss rate (m): fraction of cache accesses that result in a miss
- hit rate (h): (1- miss rate)fraction of memory access found in the faster level (cache)
- hit time (t_c): time required to access the level 1 (cache)
- miss penalty (t_p): time required to replace a data unit in the faster level (cache) + time involved to deliver the requested data to the processor from the cache. (hit time << miss penalty)
- average memory access time (amat)= hit time (t_c) + miss rate (m) * miss penalty $(t_p) = t_c + (1-h)$ * t_p

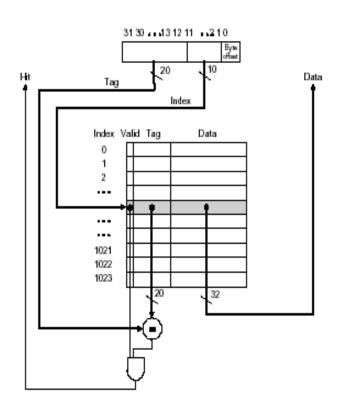
Direct-Mapped Cache



Direct Mapped Cache (4K): MIPS Example



Direct Mapped Cache [example]

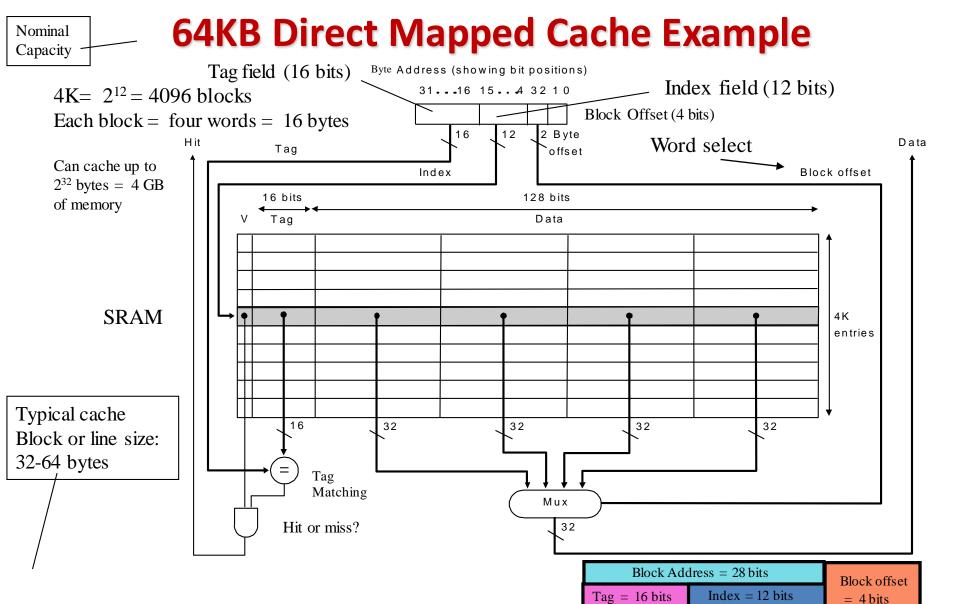


- What is the size of cache? 4K
- If I read 0000 0000 0000 0000 0000 1000 0001
- What is the index number checked?

• If the number was found, what are the inputs to comparator ?

Direct Mapped Cache [contd...]

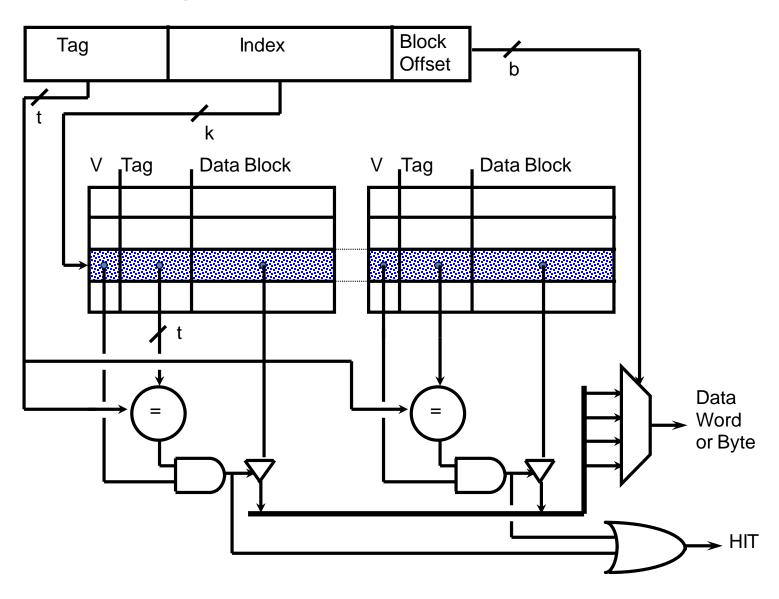
- Advantage
 - Simple
 - Fast
- Disadvantage
 - Mapping is fixed !!!



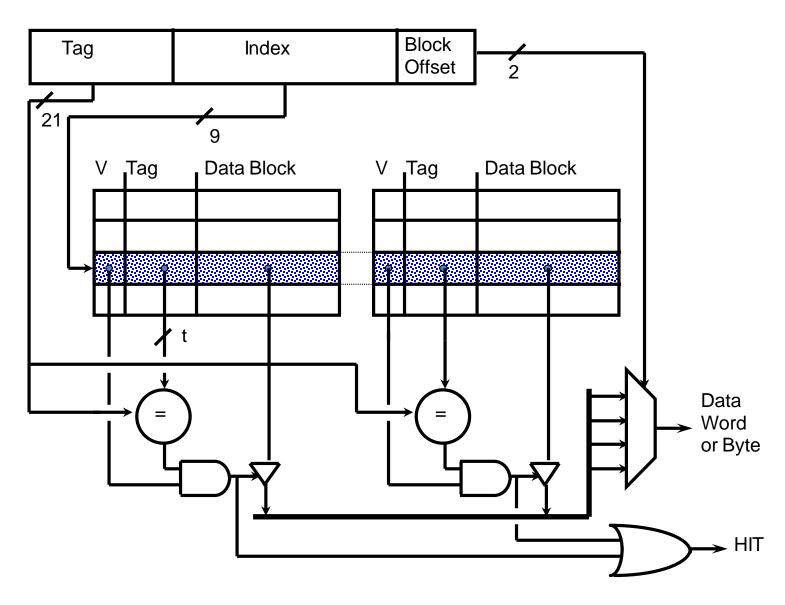
<u>Mapping Function:</u> Cache Block frame number = (Block address) MOD (4096) i.e. index field or 12 low bit of block address

Hit Access Time = SRAM Delay + Hit/Miss Logic Delay

2-Way Set-Associative Cache



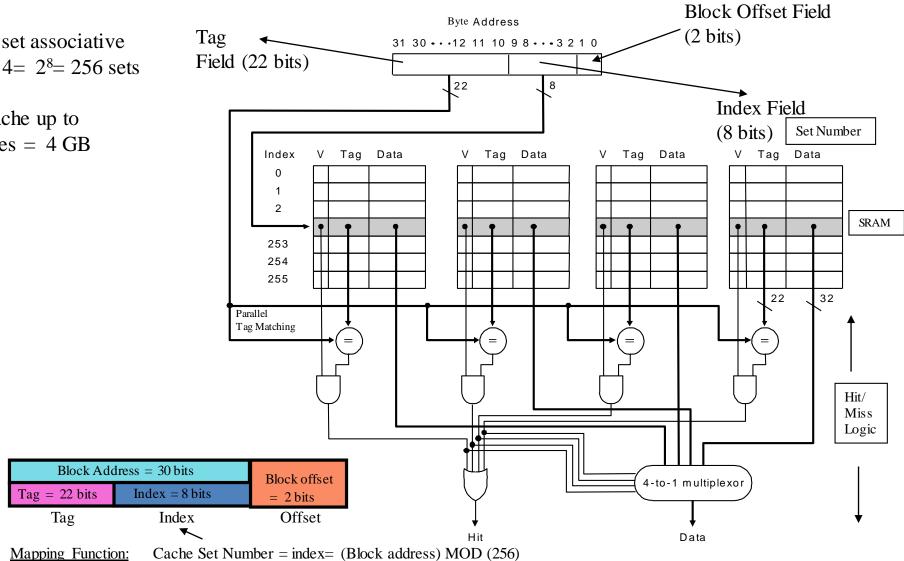
2-Way Set-Associative Cache(4K example)



4K Four-Way Set Associative Cache

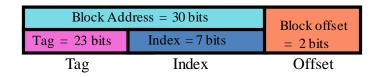
4-way set associative $1024 / 4 = 2^8 = 256 \text{ sets}$

Can cache up to 2^{32} bytes = 4 GB



4K (8, 16-Way ,.... Set Associative Cache

8 way=
$$4GB=32 \text{ bit} = 23(\text{tag})+7(\text{index})+2(\text{offset})$$



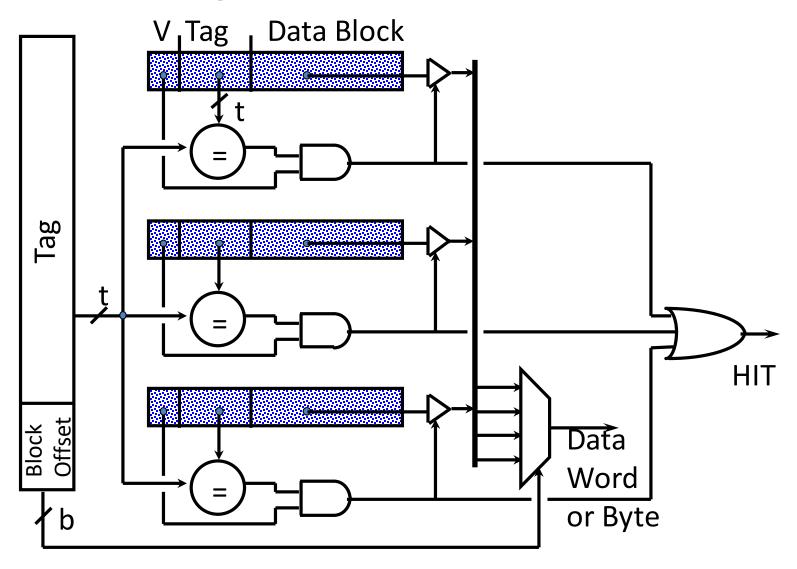
16 way = 24(tag) + 6(index) + 2(offset)



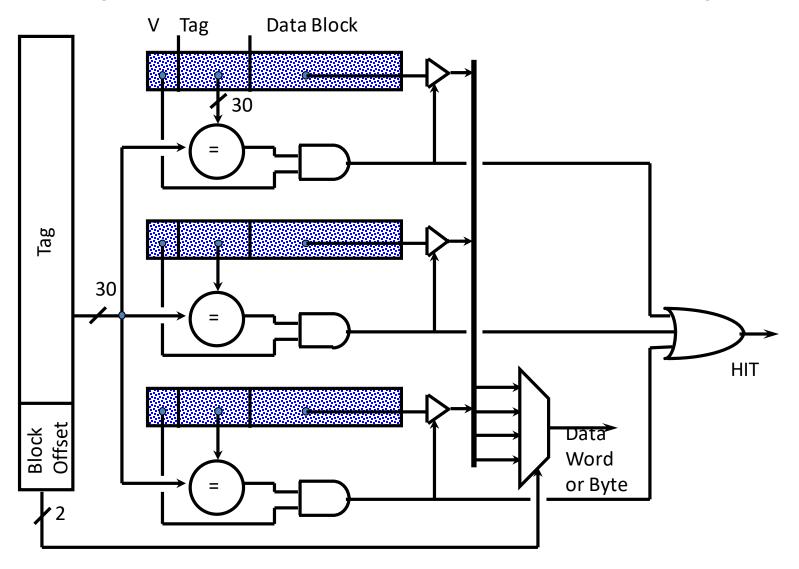
Fully Associative = 30(tag)+2(offset)



Fully Associative Cache

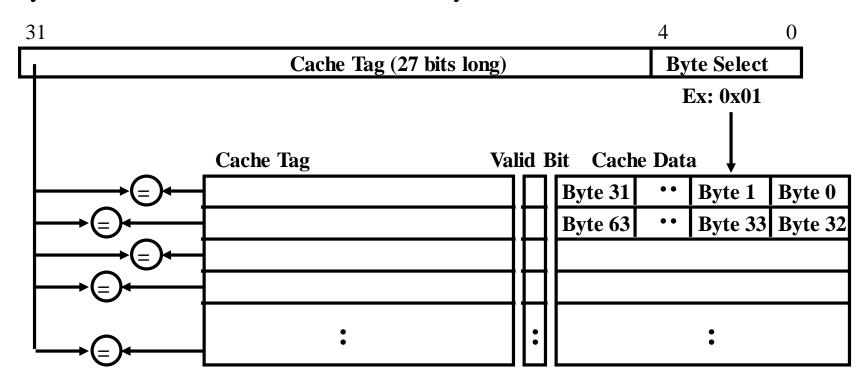


Fully Associative Cache(example)



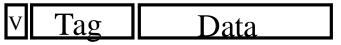
Fully Associative Cache

- Fully Associative Cache
 - Forget about the Cache Index
 - Compare the Cache Tags of all cache entries in parallel
 - Example: Block Size = 32 B blocks, we need N 27-bit comparators
- By definition: Conflict Miss = 0 for a fully associative cache



Calculating Number of Cache Bits Needed





Cache Block Frame (or just cache block)

Number of cache block frames

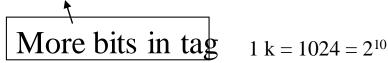
Address Fields

- How many total bits are needed for a direct- mapped cache with 64K Bytes of data and one word blocks, assuming a 32-bit address?
 - 64 Kbytes = 16 K words = 2^{14} words = 2^{14} blocks
 - Block size = 4 bytes => offset size = $log_2(4) = 2 bits$,
 - #sets = #blocks = 2^{14} => index size = 14 bits
 - Tag size = address size index size offset size = 32 14 2 = 16 bits
 - Bits/block = data bits + tag bits + valid bit = 32 + 16 + 1 = 49
 - Bits in cache = #blocks x bits/block = 2^{14} x 49 = 98 Kbytes

Actual number of bits in a cache block frame

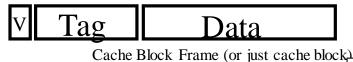
Capacity = 64 KB

- How many total bits would be needed for a 4-way set associative cache to store the same amount of data?
 - Block size and #blocks does not change.
 - #sets = #blocks/4 = $(2^{14})/4$ = 2^{12} => index size = 12 bits
 - Tag size = address size index size offset = 32 12 2 = 18 bits
 - Bits/block = data bits + tag bits + valid bit = 32 + 18 + 1 = 51
 - Bits in cache = $\#blocks \ x \ bits/block = 2^{14} \ x \ 51 = 102 \ Kbytes$
- Increase associativity => increase bits in cache



Calculating Cache Bits Needed





Address Fields

Nominal size

- How many total bits are needed for a direct-mapped cache with 64 KBytess of data and 8 word (32 byte) blocks, assuming a 32-bit address (it can cache 2³² bytes in memory)?
 - 64 Kbytes = 2^{14} words = $(2^{14})/8 = 2^{11}$ blocks

Number of cache block frames

- block size = 32 bytes
 - => offset size = block offset + byte offset = $log_2(32) = 5$ bits,
- #sets = #blocks = 2^{11} => index size = 11 bits
- tag size = address size index size offset size = 32 11 5 = 16 bits
- bits/block = data bits + tag bits + valid bit = $8 \times 32 + 16 + 1 = 273$ bits
- bits in cache = $\#blocks \times bits/block = 2^{11} \times 273 = 68.25 \text{ Kbytes}$
- Increase block size => decrease bits in cache.

Actual number of bits in a cache block frame

Fewer cache block frames thus fewer tags/valid bits

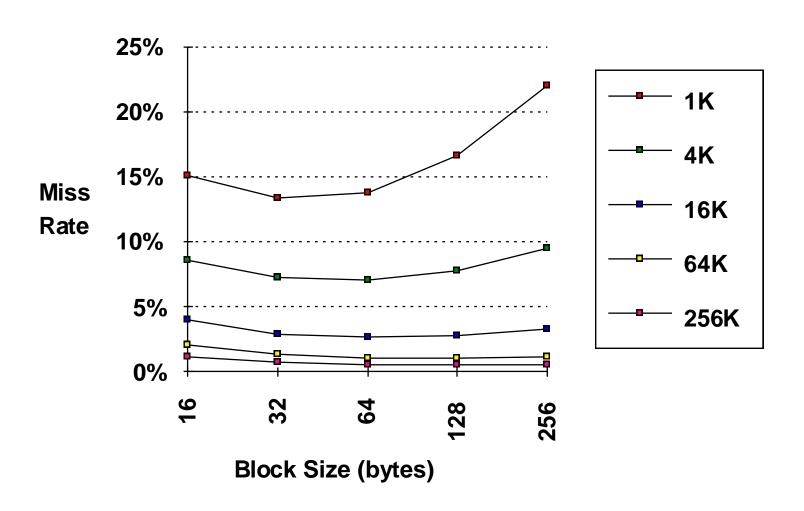
Word =
$$4 \text{ bytes}$$

$$1 \text{ k} = 1024 = 2^{10}$$

Cache Misses

- Compulsory (cold start or process migration, first reference): first access to a block
 - "Cold" fact of life: not a whole lot you can do about it
 - Note: If you are going to run "billions" of instruction,
 Compulsory Misses are insignificant
- Capacity:
 - Cache cannot contain all blocks access by the program
 - Solution: increase cache size
- Conflict (collision):
 - Multiple memory locations mapped to the same cache location
 - Solution 1: increase cache size
 - Solution 2: increase associativity
- Coherence (Invalidation): other process (e.g., I/O) updates memory

Reduce Misses via Larger Block Size



Problem 1

- (a) A 64KB, direct mapped cache has 16 byte blocks. If addresses are 32 bits, how many bits are used the tag, index, and offset in this cache?
- (b) How would the address be divided if the cache were 4-way set associative instead?

(c) How many bits is the index for a fully associative cache.

Problem 2

An ISA has 44 bit addresses with each addressable item being a byte. Design a four-way set associative cache with each of the four lines in a set containing 64 bytes. Assume that you have 256 sets in the cache.

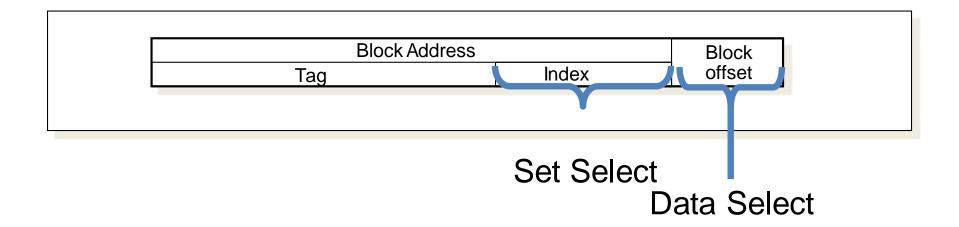
Design Options at Constant Cost

	Direct Mapped	N-way Set Associative	Fully Associative	
Cache Size	Big	Medium	Small	
Compulsory Miss	Same	Same	Same	
Conflict Miss	High	Medium	Zero	
Capacity Miss	Low	Medium **	High	
Coherence Miss	Same	Same	Same	

Four Questions for Cache Design

- Q1: Where can a block be placed in the upper level? (Block placement)
- Q2: How is a block found if it is in the upper level? (Block identification)
- Q3: Which block should be replaced on a miss? (*Block replacement*)
- Q4: What happens on a write? (Write strategy)

How is a block found if it is in the upper level?



- Direct indexing (using index and block offset), tag compares, or combination
- Increasing associativity shrinks index, expands tag

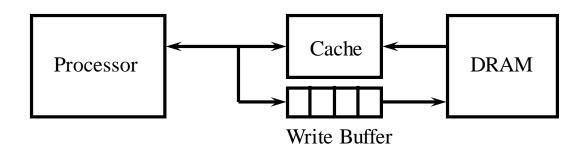
Which block should be replaced on a miss?

- Easy for Direct Mapped
- Set Associative or Fully Associative:
 - Random
 - LRU (Least Recently Used)

Associati	vity:	2-way		4-way		8-way
Size	LRU F	Random	LRU R	andom	LRU	Random
16 KB	5.2%	5.7%	4.7%	5.3%	4.4%	5.0%
64 KB	1.9%	2.0%	1.5%	1.7%	1.4%	1.5%
256 KB	1.15%	1.17%	1.13%	1.13%	1.12%	1.12%

What happens on a write?

- <u>Write through</u>—The information is written to both the block in the cache and to the block in the lower-level memory.
- Write back—The information is written only to the block in the cache. The modified cache block is written to main memory only when it is replaced.
 - is block clean or dirty?
- WT always combined with write buffers so that don't wait for lower level memory



Intel Cache Evolution ...

	Processor on which feature					
Problem	Solution	first appears				
External memory slower than the system bus.	Add external cache using faster memory technology.	386				
Increased processor speed results in external bus becoming a bottleneck for cache access.	Move external cache on-chip, operating at the same speed as the processor.	486				

Internal cache is rather small, due to limited space on chip Add external L2 cache using faster 486 technology than main memory Contention occurs when both the Instruction Prefetcher and Create separate data and instruction Pentium the Execution Unit simultaneously require access to the

caches. cache. In that case, the Prefetcher is stalled while the Execution Unit's data access takes place.

chip.

runs at higher speed than the main

dedicated to the L2 cache.

Add external L3 cache.

Move L3 cache on-chip.

(front-side) external bus. The BSB is

Move L2 cache on to the processor

Pentium II

Pentium III

Pentium 4

Pentium Pro Create separate back-side bus that

Increased processor speed results in external bus becoming a

Some applications deal with massive databases and must

have rapid access to large amounts of data. The on-chip

bottleneck for L2 cache access.

caches are too small.

Main memory Evolution

Year introduced	Chip size	\$ per MB	Total access time to a new row/column	Column access time to existing row
1980	64 Kbit	\$1500	250 ns	150 ns
1983	256 Kbit	\$500	185 ns	100 ns
1985	1 Mbit	\$200	135 ns	40 ns
1989	4 Mbit	\$50	110 ns	40 ns
1992	16 Mbit	\$15	90 ns	30 ns
1996	64 Mbit	\$10	60 ns	12 ns
1998	128 Mbit	\$4	60 ns	10 ns
2000	256 Mbit	\$1	55 ns	7 ns
2002	512 Mbit	\$0.25	50 ns	5 ns
2004	1024 Mbit	\$0.10	45 ns	3 ns

Comparison of Cache Sizes

Processor	Туре	Year of Introduction	L1 cachea	L2 cache	L3 cache
IBM 360/85	Mainframe	1968	16 to 32 KB	_	<u> </u>
PDP-11/70	Minicomputer	1975	1 KB	_	<u> </u>
VAX 11/780	Minicomputer	1978	16 KB	_	<u> </u>
IBM 3033	Mainframe	1978	64 KB	_	
IBM 3090	Mainframe	1985	128 to 256 KB		
Intel 80486	PC	1989	8 KB		<u> </u>
Pentium	PC	1993	8 KB/8 KB	256 to 512 KB	
PowerPC 601	PC	1993	32 KB	_	<u> </u>
PowerPC 620	PC	1996	32 KB/32 KB		444
PowerPC G4	PC/server	1999	32 KB/32 KB	256 KB to 1 MB	2 MB
IBM S/390 G4	Mainframe	1997	32 KB	256 KB	2 MB
IBM S/390 G6	Mainframe	1999	256 KB	8 MB	_
Pentium 4	PC/server	2000	8 KB/8 KB	256 KB	
IBM SP	High-end server/ supercomputer	2000	64 KB/32 KB	8 MB	
CRAY MTA _b	Supercomputer	2000	8 KB	2 MB	<u> </u>
<u> Itanium</u>	PC/server	2001	16 KB/16 KB	96 KB	4 MB
SGI Origin 2001	High-end server	2001	32 KB/32 KB	4 MB	<u> </u>
Itanium 2	PC/server	2002	32 KB	256 KB	6 MB
IBM POWER5	High-end server	2003	64 KB	1.9 MB	36 MB
CRAY XD-1	Supercomputer	2004	64 KB/64 KB	1MB	

Memory Hierarchy in Power 4/5

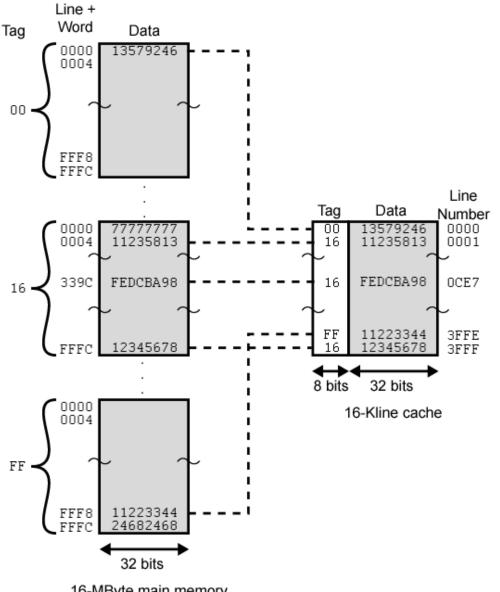
Cache	Capacity	Associativity	Lin e size	Write policy	Repl. alg	Comments
L1 I-cache	64 KB	Direct/2-way	128 B		LRU	Sector cache (4 sectors)
L1 D-cache	32 KB	2-way/4-way	128 B	Write- throug h	LRU	
L2 Unified	1.5 MB/2 MB	8-way/10- way	128 B	Write- back	Pseudo- LRU	
L3	32 MB/36MB	8-way/12- way	512 B	Write- back	?	Sector cache (4 sectors)

Latency	Latency P4 (1.7 GHz)	
L1 (I and D)	1	1
L2	12	13
L3	123	87
Main Memory	351	220

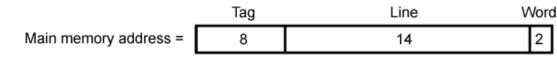
More examples: **Direct Mapping** Example (16M, 16K cache)

14(index) **8(tag)**





16-MByte main memory



Fully Associative Cache Organization

