

## **Tutorial -6 (13/10/2020)**

1. Build a PDA for language  $L = \{wcw' \mid w=\{0, 1\}^*\}$  where  $w'$  is the reverse of  $w$ .
2. Build a PDA for language  $L = \{0^n 1^m 2^m 3^n \mid n \geq 1, m \geq 1\}$
3. Given Grammar G1:  
     $S \rightarrow aSb$   
     $S \rightarrow e$   
Grammar G2:  
     $R \rightarrow cRd$   
     $R \rightarrow e$   
If  $L(G) = L(G1) \cup L(G2)$ , the number of productions the new starting variable would have:  
    a) 2  
    b) 3  
    c) 4  
    d) 1
4. Let  $G = (\{S, C\}, \{a, b\}, P, S)$  where  $P$  consists of  $S \rightarrow aCa$ ,  $C \rightarrow aCa \mid b$ . Find  $L(G)$ .
5. Find  $L(G)$  where  $G = (\{S\}, \{0, 1\}, \{S \rightarrow 0S1, S \rightarrow \epsilon\}, S)$
6. Construct CFG without  $\epsilon$  production from :  
     $S \rightarrow a \mid Ab \mid aBa$   
     $A \rightarrow b \mid \epsilon$   
     $B \rightarrow b \mid A$
7. Consider the grammar  $P = \{S \rightarrow aS \mid aSbS \mid \epsilon\}$  is ambiguous by constructing:  
    (a) two parse trees  
    (b) two leftmost derivation  
    (c) rightmost derivation
8. Find the grammar for the language  $L = \{a^{2n}bc, \text{ where } n \geq 1\}$
9. What are the applications of Context free languages?
10.  $L$  exactly consists of all strings  $w \in \Sigma^*$  such that  $w = \text{reverse}(w)$  and the length of  $w$  is divisible by 4 (i.e.,  $w$  has length  $4n$  for some  $n = 0, 1, 2, 3, \dots$ ).

L defined over  $\Sigma$  falls into which one of the following categories:

- (i) L is a regular language.
- (ii) L is a context-free language, but not a regular language.
- (iii) L is recursively enumerable, but not a context-free language.

**Questions to be solved latest by Saturday (17/10/2020)**

1. Construct a PDA for language  $L = \{0^n 1^m \mid n \geq 1, m \geq 1, m > n+2\}$
2. Let  $L = \{a^{3n} b^{2n} : n = 0, 1, 2, \dots\}$   
Give a pushdown automaton that accepts L.
3. Let  $L = \{a^{2n} : n \geq 0\}$   
L defined over  $\Sigma$  falls into which one of the following categories. Give a proper justification of your answer.
  - (i) L is a regular language.
  - (ii) L is a context-free language, but not a regular language.
  - (iii) L is recursively enumerable, but not a context-free language.

**NOTE:** Upload your solutions only through the given link. Name your pdf file with the format **<rollno\_name\_tutorialno>**. Do not mail your solutions elsewhere.

Link to upload the solutions:

[https://docs.google.com/forms/d/e/1FAIpQLSdpnjMVnxzEUPuHsvplhykgwleCC5MgEYKXrKauEH8TF7Dkig/viewform?usp=sf\\_link](https://docs.google.com/forms/d/e/1FAIpQLSdpnjMVnxzEUPuHsvplhykgwleCC5MgEYKXrKauEH8TF7Dkig/viewform?usp=sf_link)