EE5311 - Digital IC Design

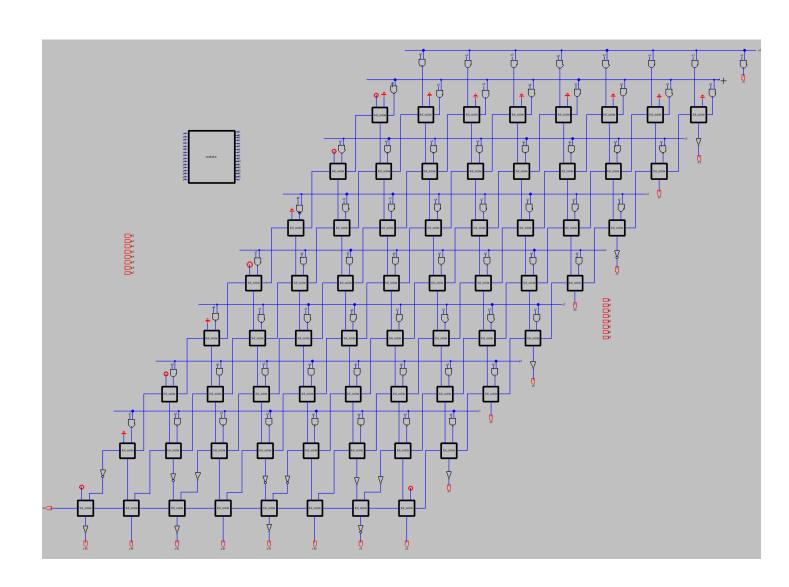
Assignment 4 - Schematic of a signed 8-bit Carry Save Multiplier

Member 1: Srivenkat A(EE18B038)

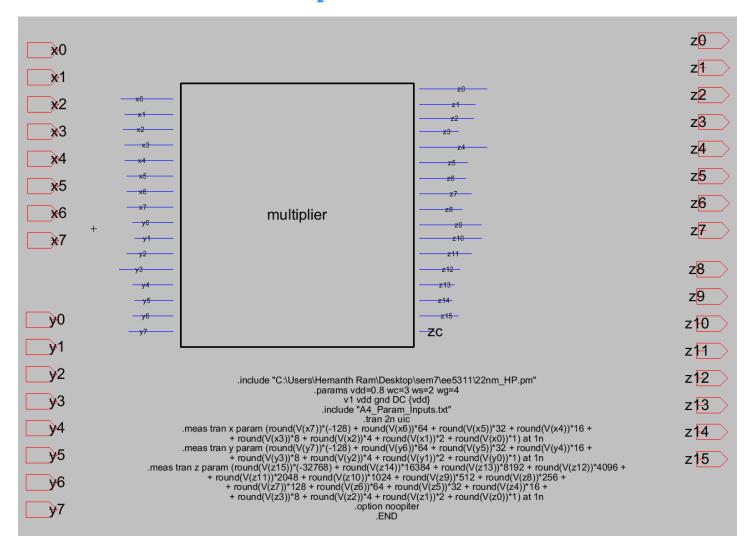
Member 2: Hemanth Ram G K (EE18B132)

Member 3: Sidesh S(EE18B032)

Schematic of CSM



Multiplier Testbench



Simulation output for 127 * -128



Interpreted voltage values for 127 * -128

x: (round(v(x7))*(-128) + round(v(x6))*64 + round(v(x5))*32 + round(v(x4))*16 + round(v(x3))*8 + round(v(x2))*4 + round(v(x1))*2 + round(v(x0))*1)=127y: (round(v(y7))*(-128) + round(v(y6))*64 + round(v(y5))*32 + round(v(y4))*16 + round(v(y3))*8 + round(v(y2))*4 + round(v(y1))*2 + round(v(y0))*1)=-128z: (round(v(z15))*(-32768) + round(v(z14))*16384 + round(v(z13))*8192 + round(v(z12))*4096 + round(v(z11))*2048 + round(v(z10))*1024 + round(v(z9))*512 + round(v(z8))*256 + round(v(z7))*128 + round(v(z6))*64 + round(v(z5))*32 + round(v(z4))*16 + round(v(z3))*8 + round(v(z2))*4 + round(v(z1))*2 + round(v(z0))*1)=-16256

Interpreted voltage values for -128 * 127

x: (round(v(x7))*(-128) + round(v(x6))*64 + round(v(x5))*32 + round(v(x4))*16 + round(v(x3))*8 + round(v(x2))*4 + round(v(x1))*2 + round(v(x0))*1)=-128y: (round(v(y7))*(-128) + round(v(y6))*64 + round(v(y5))*32 + round(v(y4))*16 + round(v(y3))*8 + round(v(y2))*4 + round(v(y1))*2 + round(v(y0))*1)=127z: (round(v(z15))*(-32768) + round(v(z14))*16384 + round(v(z13))*8192 + round(v(z12))*4096 + round(v(z11))*2048 + round(v(z10))*1024 + round(v(z9))*512 + round(v(z8))*256 + round(v(z7))*128 + round(v(z6))*64 + round(v(z5))*32 + round(v(z4))*16 + round(v(z3))*8 + round(v(z2))*4 + round(v(z1))*2 + round(v(z0))*1)=-16256

Interpreted voltage values for 0 * 127

x: (round(v(x7))*(-128) + round(v(x6))*64 + round(v(x5))*32 + round(v(x4))*16 + round(v(x3))*8 + round(v(x2))*4 + round(v(x1))*2 + round(v(x0))*1)=0y: (round(v(y7))*(-128) + round(v(y6))*64 + round(v(y5))*32 + round(v(y4))*16 + round(v(y3))*8 + round(v(y2))*4 + round(v(y1))*2 + round(v(y0))*1)=127z: (round(v(z15))*(-32768) + round(v(z14))*16384 + round(v(z13))*8192 + round(v(z12))*4096 + round(v(z11))*2048 + round(v(z10))*1024 + round(v(z9))*512 + round(v(z8))*256 + round(v(z7))*128 + round(v(z6))*64 + round(v(z5))*32 + round(v(z4))*16 + round(v(z3))*8 + round(v(z2))*4 + round(v(z1))*2 + round(v(z0))*1)=0

Interpreted voltage values for -128 * 0

x: (round(v(x7))*(-128) + round(v(x6))*64 + round(v(x5))*32 + round(v(x4))*16 + round(v(x3))*8 + round(v(x2))*4 + round(v(x1))*2 + round(v(x0))*1)=-128y: (round(v(y7))*(-128) + round(v(y6))*64 + round(v(y5))*32 + round(v(y4))*16 + round(v(y3))*8 + round(v(y2))*4 + round(v(y1))*2 + round(v(y0))*1)=0z: (round(v(z15))*(-32768) + round(v(z14))*16384 + round(v(z13))*8192 + round(v(z12))*4096 + round(v(z11))*2048 + round(v(z10))*1024 + round(v(z9))*512 + round(v(z8))*256 + round(v(z7))*128 + round(v(z6))*64 + round(v(z5))*32 + round(v(z4))*16 + round(v(z3))*8 + round(v(z2))*4 + round(v(z1))*2 + round(v(z0))*1)=0

Interpreted voltage values for -12 * 13

```
x: (\text{round}(v(x7))*(-128) + \text{round}(v(x6))*64 + \text{round}(v(x5))*32 + \text{round}(v(x4))*16 + \text{round}(v(x3))*8 + \text{round}(v(x2))*4 + \text{round}(v(x1))*2 + \text{round}(v(x0))*1)=-12}
y: (\text{round}(v(y7))*(-128) + \text{round}(v(y6))*64 + \text{round}(v(y5))*32 + \text{round}(v(y4))*16 + \text{round}(v(y3))*8 + \text{round}(v(y2))*4 + \text{round}(v(y1))*2 + \text{round}(v(y0))*1)=13}
z: (\text{round}(v(z15))*(-32768) + \text{round}(v(z14))*16384 + \text{round}(v(z13))*8192 + \text{round}(v(z12))*4096 + \text{round}(v(z11))*2048 + \text{round}(v(z10))*1024 + \text{round}(v(z9))*512 + \text{round}(v(z8))*256 + \text{round}(v(z7))*128 + \text{round}(v(z6))*64 + \text{round}(v(z5))*32 + \text{round}(v(z4))*16 + \text{round}(v(z3))*8 + \text{round}(v(z2))*4 + \text{round}(v(z1))*2 + \text{round}(v(z0))*1)=-156}
```

Interpreted voltage values for -1 * -1

```
x: (\text{round}(v(x7))*(-128) + \text{round}(v(x6))*64 + \text{round}(v(x5))*32 + \text{round}(v(x4))*16 + \text{round}(v(x3))*8 + \text{round}(v(x2))*4 + \text{round}(v(x1))*2 + \text{round}(v(x0))*1)=-1
y: (\text{round}(v(y7))*(-128) + \text{round}(v(y6))*64 + \text{round}(v(y5))*32 + \text{round}(v(y4))*16 + \text{round}(v(y3))*8 + \text{round}(v(y2))*4 + \text{round}(v(y1))*2 + \text{round}(v(y0))*1)=-1
z: (\text{round}(v(z15))*(-32768) + \text{round}(v(z14))*16384 + \text{round}(v(z13))*8192 + \text{round}(v(z12))*4096 + \text{round}(v(z11))*2048 + \text{round}(v(z10))*1024 + \text{round}(v(z9))*512 + \text{round}(v(z8))*256 + \text{round}(v(z7))*128 + \text{round}(v(z6))*64 + \text{round}(v(z5))*32 + \text{round}(v(z4))*16 + \text{round}(v(z3))*8 + \text{round}(v(z2))*4 + \text{round}(v(z1))*2 + \text{round}(v(z0))*1)=1
```

Interpreted voltage values for -128 * -128

```
x: (\text{round}(v(x7))^*(-128) + \text{round}(v(x6))^*64 + \text{round}(v(x5))^*32 + \text{round}(v(x4))^*16 + \text{round}(v(x3))^*8 + \text{round}(v(x2))^*4 + \text{round}(v(x1))^*2 + \text{round}(v(x0))^*1) = -128
y: (\text{round}(v(y7))^*(-128) + \text{round}(v(y6))^*64 + \text{round}(v(y5))^*32 + \text{round}(v(y4))^*16 + \text{round}(v(y3))^*8 + \text{round}(v(y2))^*4 + \text{round}(v(y1))^*2 + \text{round}(v(y0))^*1) = -128
z: (\text{round}(v(z15))^*(-32768) + \text{round}(v(z14))^*16384 + \text{round}(v(z13))^*8192 + \text{round}(v(z12))^*4096 + \text{round}(v(z11))^*2048 + \text{round}(v(z10))^*1024 + \text{round}(v(z9))^*512 + \text{round}(v(z8))^*256 + \text{round}(v(z7))^*128 + \text{round}(v(z6))^*64 + \text{round}(v(z5))^*32 + \text{round}(v(z4))^*16 + \text{round}(v(z3))^*8 + \text{round}(v(z2))^*4 + \text{round}(v(z1))^*2 + \text{round}(v(z0))^*1) = 16384
```

Interpreted voltage values for 103 * -57

```
x: (\text{round}(v(x7))^*(-128) + \text{round}(v(x6))^*64 + \text{round}(v(x5))^*32 + \text{round}(v(x4))^*16 + \text{round}(v(x3))^*8 + \text{round}(v(x2))^*4 + \text{round}(v(x1))^*2 + \text{round}(v(x0))^*1)=103
y: (\text{round}(v(y7))^*(-128) + \text{round}(v(y6))^*64 + \text{round}(v(y5))^*32 + \text{round}(v(y4))^*16 + \text{round}(v(y3))^*8 + \text{round}(v(y2))^*4 + \text{round}(v(y1))^*2 + \text{round}(v(y0))^*1)=-57
z: (\text{round}(v(z15))^*(-32768) + \text{round}(v(z14))^*16384 + \text{round}(v(z13))^*8192 + \text{round}(v(z12))^*4096 + \text{round}(v(z11))^*2048 + \text{round}(v(z10))^*1024 + \text{round}(v(z9))^*512 + \text{round}(v(z8))^*256 + \text{round}(v(z7))^*128 + \text{round}(v(z6))^*64 + \text{round}(v(z5))^*32 + \text{round}(v(z4))^*16 + \text{round}(v(z3))^*8 + \text{round}(v(z2))^*4 + \text{round}(v(z1))^*2 + \text{round}(v(z0))^*1)=-5871
```

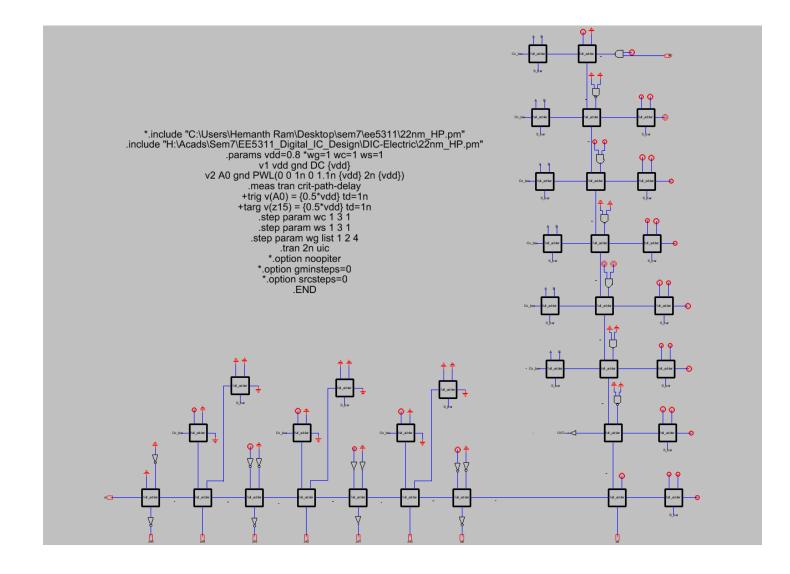
Interpreted voltage values for -50 * 50

```
x: (\text{round}(v(x7))*(-128) + \text{round}(v(x6))*64 + \text{round}(v(x5))*32 + \text{round}(v(x4))*16 + \text{round}(v(x3))*8 + \text{round}(v(x2))*4 + \text{round}(v(x1))*2 + \text{round}(v(x0))*1)=-50}
y: (\text{round}(v(y7))*(-128) + \text{round}(v(y6))*64 + \text{round}(v(y5))*32 + \text{round}(v(y4))*16 + \text{round}(v(y3))*8 + \text{round}(v(y2))*4 + \text{round}(v(y1))*2 + \text{round}(v(y0))*1)=50}
z: (\text{round}(v(z15))*(-32768) + \text{round}(v(z14))*16384 + \text{round}(v(z13))*8192 + \text{round}(v(z12))*4096 + \text{round}(v(z11))*2048 + \text{round}(v(z10))*1024 + \text{round}(v(z9))*512 + \text{round}(v(z8))*256 + \text{round}(v(z7))*128 + \text{round}(v(z6))*64 + \text{round}(v(z5))*32 + \text{round}(v(z4))*16 + \text{round}(v(z3))*8 + \text{round}(v(z2))*4 + \text{round}(v(z1))*2 + \text{round}(v(z0))*1)=-2500}
```

Interpreted voltage values for 79 * 81

```
x: (\text{round}(v(x7))*(-128) + \text{round}(v(x6))*64 + \text{round}(v(x5))*32 + \text{round}(v(x4))*16 + \text{round}(v(x3))*8 + \text{round}(v(x2))*4 + \text{round}(v(x1))*2 + \text{round}(v(x0))*1)=79
y: (\text{round}(v(y7))*(-128) + \text{round}(v(y6))*64 + \text{round}(v(y5))*32 + \text{round}(v(y4))*16 + \text{round}(v(y3))*8 + \text{round}(v(y2))*4 + \text{round}(v(y1))*2 + \text{round}(v(y0))*1)=81
z: (\text{round}(v(z15))*(-32768) + \text{round}(v(z14))*16384 + \text{round}(v(z13))*8192 + \text{round}(v(z12))*4096 + \text{round}(v(z11))*2048 + \text{round}(v(z10))*1024 + \text{round}(v(z9))*512 + \text{round}(v(z8))*256 + \text{round}(v(z7))*128 + \text{round}(v(z6))*64 + \text{round}(v(z5))*32 + \text{round}(v(z4))*16 + \text{round}(v(z3))*8 + \text{round}(v(z2))*4 + \text{round}(v(z1))*2 + \text{round}(v(z0))*1)=6399
```

Critical Path of CSM modelled separately



Inputs to Full Adders in Critical Path

- 1. Input A is closer than B to output and critical input is connected to A in every full adder.
- 2. For an edge in A, sum delay for different combinations of B, Ci in a Full Adder:

Inputs to (B, Cin) \ Edge Type	Rising	Falling	
00	48.9ps	75.7ps	
01	25.9ps	106ps	
10	133ps	129ps	
11	99.9ps	29.5ps	

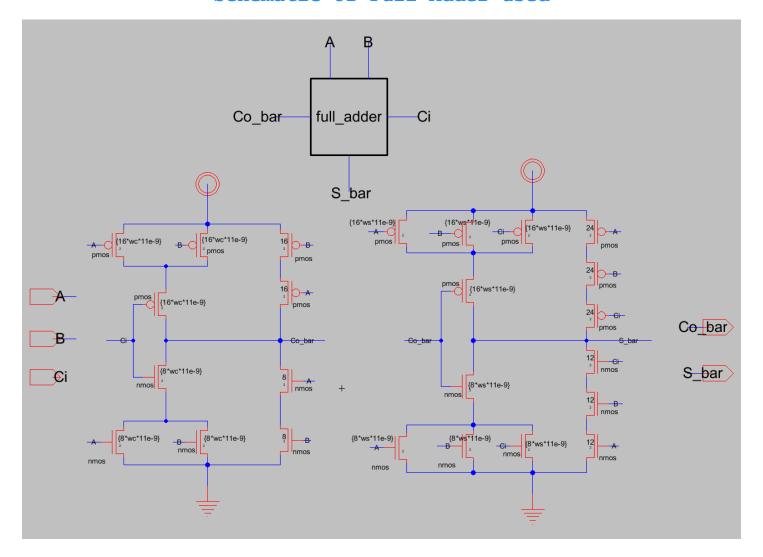
So, for both rising/falling edge in A, B=1, Cin=0 for max delay in sum propagation

3. For an edge in Carry in, Full Adder should be in propagation stage for max delay. Delays for different combinations of A/B in Full Adder:

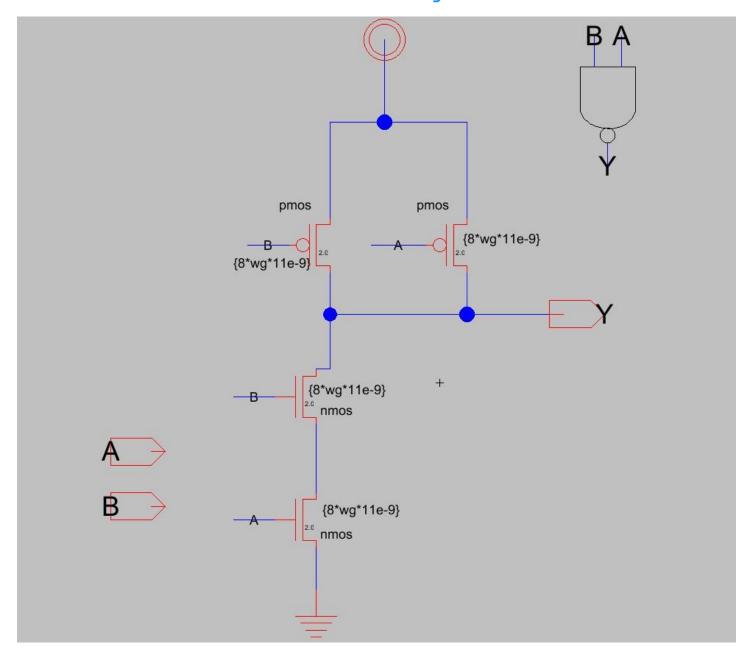
Inputs to (A, B) \ Edge Type	Rising	Falling	
01	29.9ps	10.6ps	
10	28.4ps	10.5ps	

So, for rising/falling edge in Cin, A=0, B=1 for max delay in carry propagation

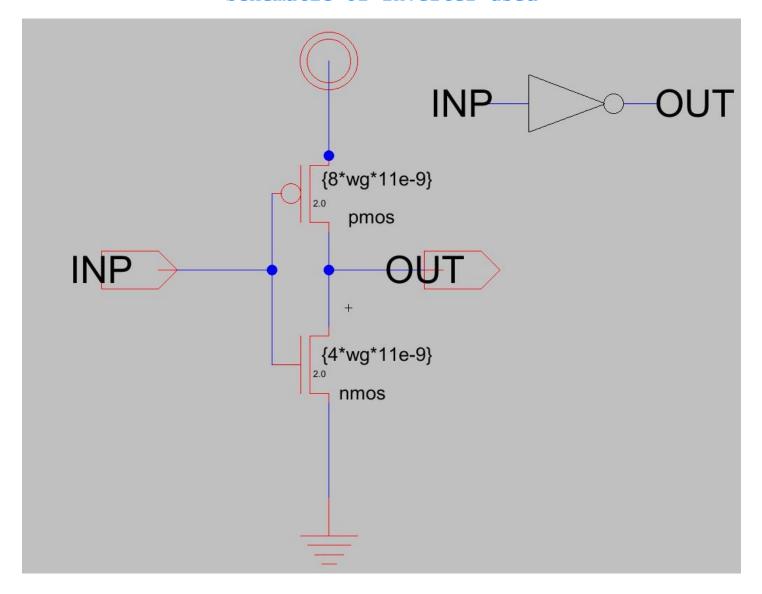
Schematic of Full Adder used



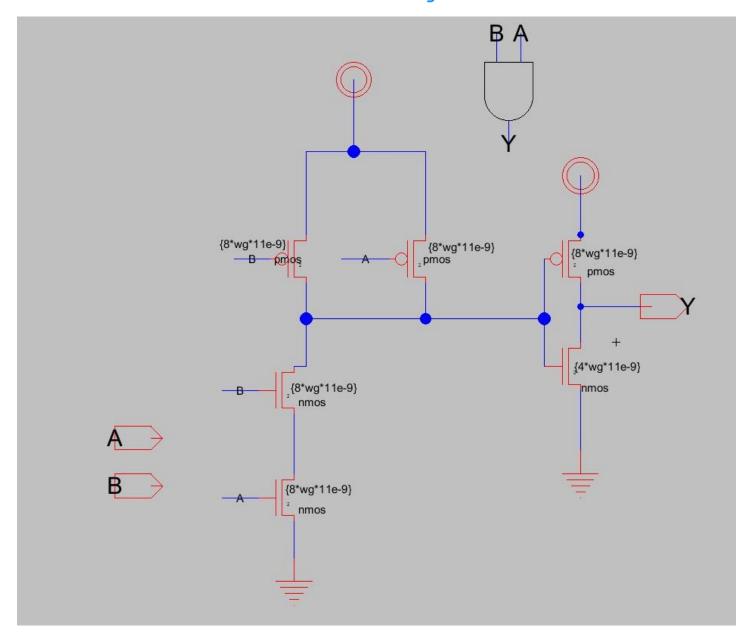
Schematic of NAND gate used



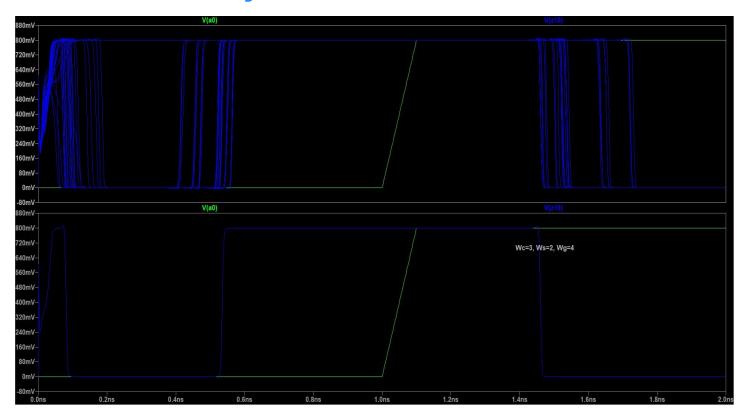
Schematic of Inverter used



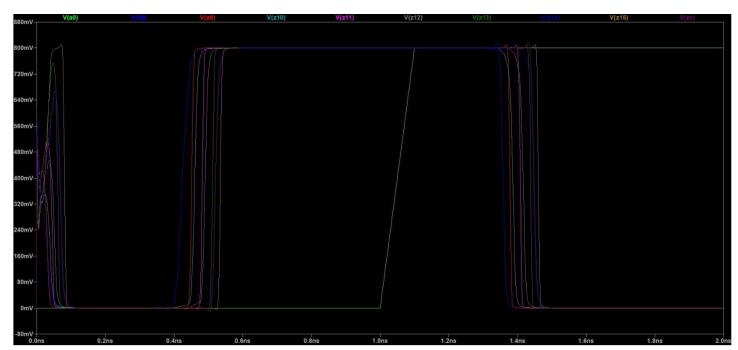
Schematic of AND gate used



Simulation of Critical Path Delay swept across possible gate size combinations



Simulation of Vector Merge outputs for critical input



Critical Path Delay tabulated across gate size combinations

step				crit-path-delay	FROM	то
1	wc=1	ws=1	wg=1	5.87E-10	1.05E-09	1.64E-09
2	wc=2	ws=1	wg=1	4.94E-10	1.05E-09	1.54E-09
3	wc=3	ws=1	wg=1	4.82E-10	1.05E-09	1.53E-09
4	wc=1	ws=2	wg=1	6.09E-10	1.05E-09	1.66E-09
5	wc=2	ws=2	wg=1	4.63E-10	1.05E-09	1.51E-09
6	wc=3	ws=2	wg=1	4.25E-10	1.05E-09	1.48E-09
7	wc=1	ws=3	wg=1	6.81E-10	1.05E-09	1.73E-09
8	wc=2	ws=3	wg=1	4.87E-10	1.05E-09	1.54E-09
9	wc=3	ws=3	wg=1	4.29E-10	1.05E-09	1.48E-09
10	wc=1	ws=1	wg=2	5.83E-10	1.05E-09	1.63E-09
11	wc=2	ws=1	wg=2	4.88E-10	1.05E-09	1.54E-09
12	wc=3	ws=1	wg=2	4.74E-10	1.05E-09	1.52E-09
13	wc=1	ws=2	wg=2	6.02E-10	1.05E-09	1.65E-09
14	wc=2	ws=2	wg=2	4.54E-10	1.05E-09	1.50E-09
15	wc=3	ws=2	wg=2	4.15E-10	1.05E-09	1.46E-09
16	wc=1	ws=3	wg=2	6.72E-10	1.05E-09	1.72E-09
17	wc=2	ws=3	wg=2	4.76E-10	1.05E-09	1.53E-09
18	wc=3	ws=3	wg=2	4.17E-10	1.05E-09	1.47E-09
19	wc=1	ws=1	wg=4	5.85E-10	1.05E-09	1.64E-09
20	wc=2	ws=1	wg=4	4.87E-10	1.05E-09	1.54E-09
21	wc=3	ws=1	wg=4	4.73E-10	1.05E-09	1.52E-09
22	wc=1	ws=2	wg=4	6.02E-10	1.05E-09	1.65E-09
23	wc=2	ws=2	wg=4	4.51E-10	1.05E-09	1.50E-09
24	wc=3	ws=2	wg=4	4.11E-10	1.05E-09	1.46E-09
25	wc=1	ws=3	wg=4	6.71E-10	1.05E-09	1.72E-09
26	wc=2	ws=3	wg=4	4.72E-10	1.05E-09	1.52E-09
27	wc=3	ws=3	wg=4	4.11E-10	1.05E-09	1.46E-09

Chosen Gate sizes

Full Adder:

Cout-bar: 3x

Sum-bar: 2x

Standard Cells:

NAND, AND, INV: 4x

