
EE5311 - Digital IC Design

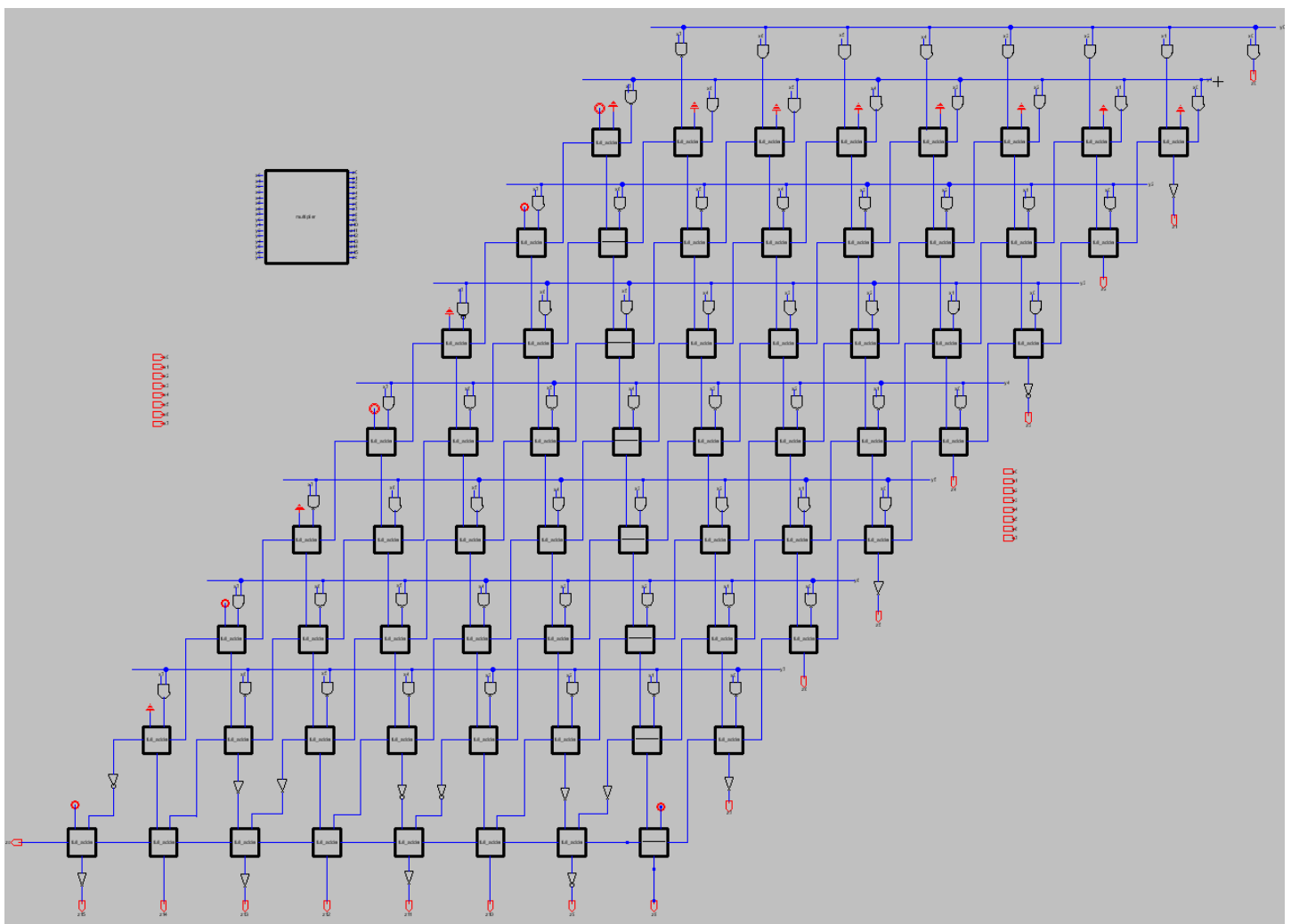
Assignment 4 - Schematic of a signed 8-bit Carry Save Multiplier

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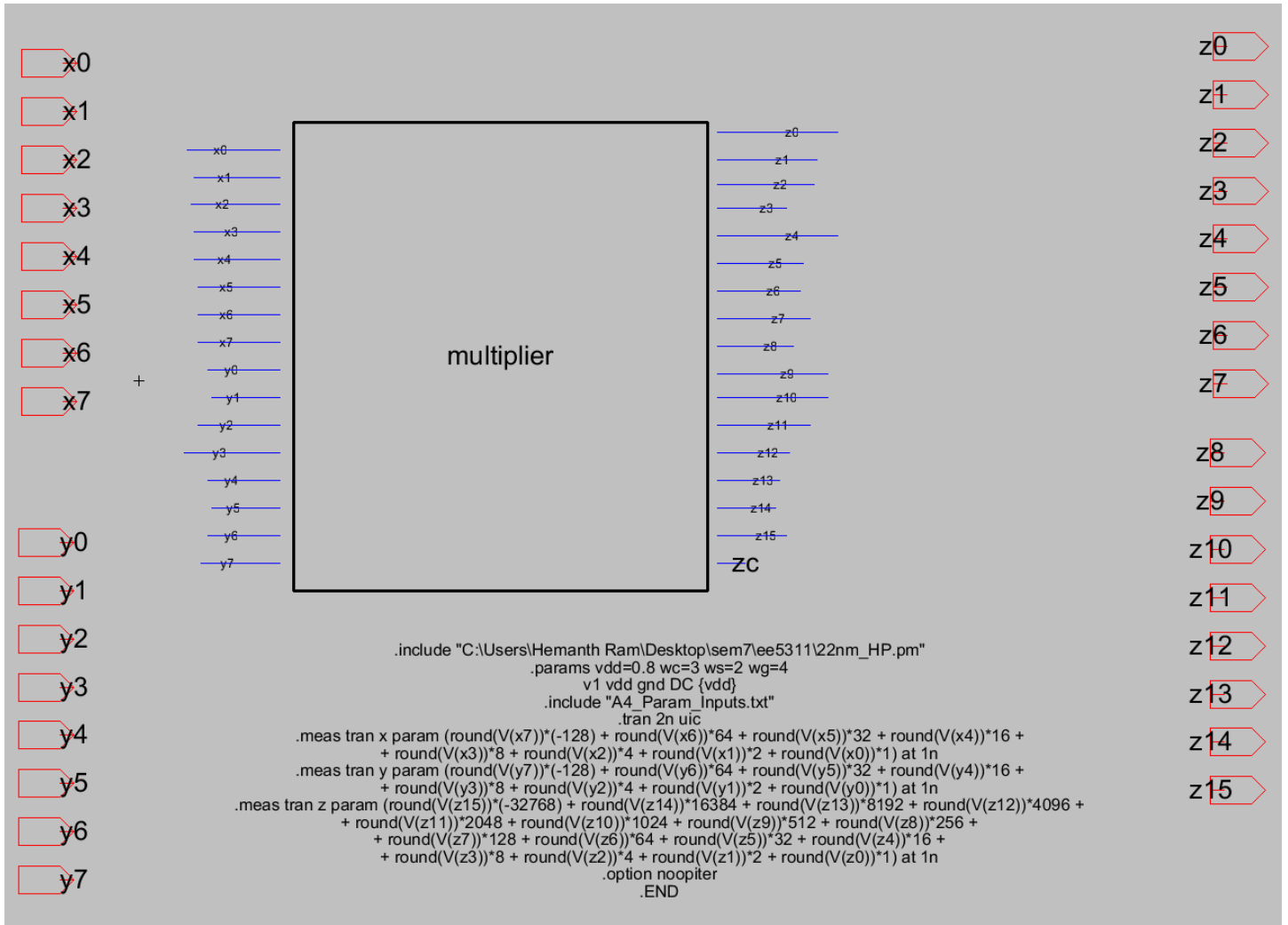
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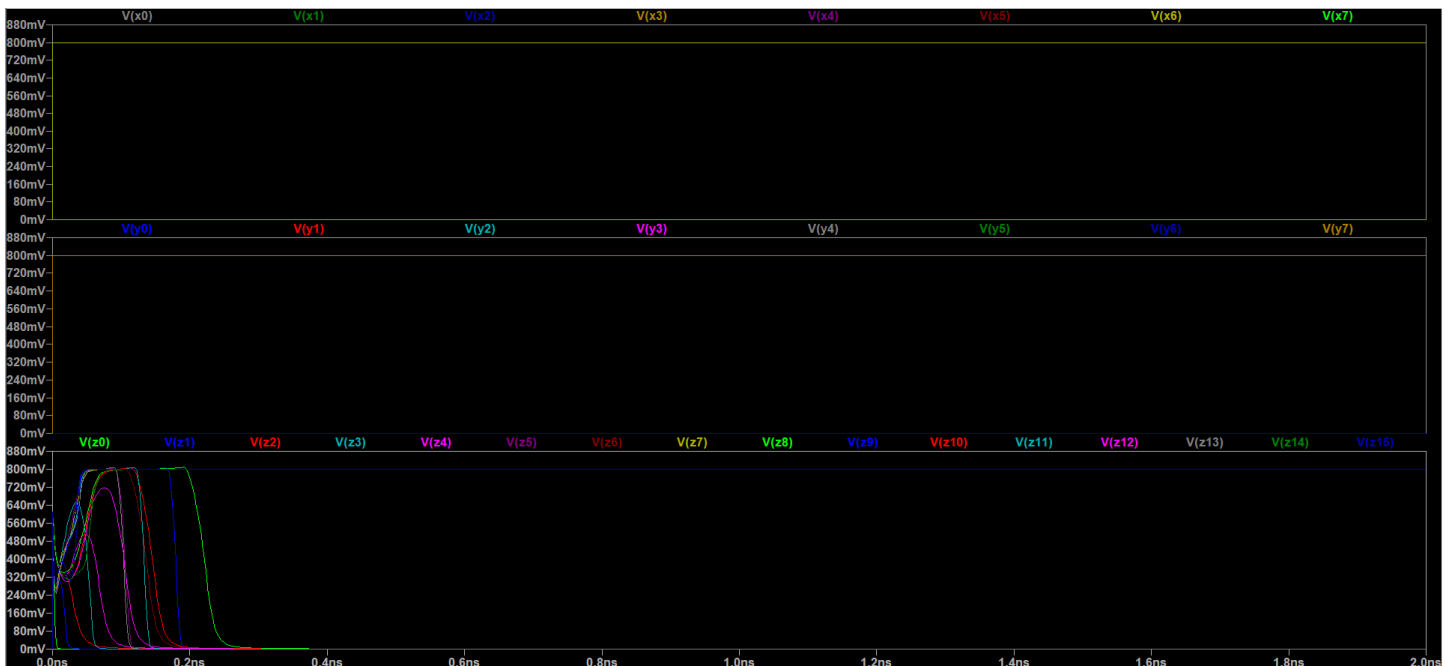
Schematic of CSM



Multiplier Testbench



Simulation output for $127 * -128$



Interpreted voltage values for 127 * -128

```
x: (round(v(x7))*(-128) + round(v(x6))*64 + round(v(x5))*32 + round(v(x4))*16 +
round(v(x3))*8 + round(v(x2))*4 + round(v(x1))*2 + round(v(x0))*1)=127
y: (round(v(y7))*(-128) + round(v(y6))*64 + round(v(y5))*32 + round(v(y4))*16 +
round(v(y3))*8 + round(v(y2))*4 + round(v(y1))*2 + round(v(y0))*1)=-128
z: (round(v(z15))*(-32768) + round(v(z14))*16384 + round(v(z13))*8192 +
round(v(z12))*4096 + round(v(z11))*2048 + round(v(z10))*1024 + round(v(z9))*512 +
round(v(z8))*256 + round(v(z7))*128 + round(v(z6))*64 + round(v(z5))*32 +
round(v(z4))*16 + round(v(z3))*8 + round(v(z2))*4 + round(v(z1))*2 + round(v(z0))*1)=-
16256
```

Interpreted voltage values for -128 * 127

```
x: (round(v(x7))*(-128) + round(v(x6))*64 + round(v(x5))*32 + round(v(x4))*16 +
round(v(x3))*8 + round(v(x2))*4 + round(v(x1))*2 + round(v(x0))*1)=-128
y: (round(v(y7))*(-128) + round(v(y6))*64 + round(v(y5))*32 + round(v(y4))*16 +
round(v(y3))*8 + round(v(y2))*4 + round(v(y1))*2 + round(v(y0))*1)=127
z: (round(v(z15))*(-32768) + round(v(z14))*16384 + round(v(z13))*8192 +
round(v(z12))*4096 + round(v(z11))*2048 + round(v(z10))*1024 + round(v(z9))*512 +
round(v(z8))*256 + round(v(z7))*128 + round(v(z6))*64 + round(v(z5))*32 +
round(v(z4))*16 + round(v(z3))*8 + round(v(z2))*4 + round(v(z1))*2 + round(v(z0))*1)=-
16256
```

Interpreted voltage values for 0 * 127

```
x: (round(v(x7))*(-128) + round(v(x6))*64 + round(v(x5))*32 + round(v(x4))*16 +
round(v(x3))*8 + round(v(x2))*4 + round(v(x1))*2 + round(v(x0))*1)=0
y: (round(v(y7))*(-128) + round(v(y6))*64 + round(v(y5))*32 + round(v(y4))*16 +
round(v(y3))*8 + round(v(y2))*4 + round(v(y1))*2 + round(v(y0))*1)=127
z: (round(v(z15))*(-32768) + round(v(z14))*16384 + round(v(z13))*8192 +
round(v(z12))*4096 + round(v(z11))*2048 + round(v(z10))*1024 + round(v(z9))*512 +
round(v(z8))*256 + round(v(z7))*128 + round(v(z6))*64 + round(v(z5))*32 +
round(v(z4))*16 + round(v(z3))*8 + round(v(z2))*4 + round(v(z1))*2 + round(v(z0))*1)=0
```

Interpreted voltage values for -128 * 0

```
x: (round(v(x7))*(-128) + round(v(x6))*64 + round(v(x5))*32 + round(v(x4))*16 +
round(v(x3))*8 + round(v(x2))*4 + round(v(x1))*2 + round(v(x0))*1)=-128
y: (round(v(y7))*(-128) + round(v(y6))*64 + round(v(y5))*32 + round(v(y4))*16 +
round(v(y3))*8 + round(v(y2))*4 + round(v(y1))*2 + round(v(y0))*1)=0
z: (round(v(z15))*(-32768) + round(v(z14))*16384 + round(v(z13))*8192 +
round(v(z12))*4096 + round(v(z11))*2048 + round(v(z10))*1024 + round(v(z9))*512 +
round(v(z8))*256 + round(v(z7))*128 + round(v(z6))*64 + round(v(z5))*32 +
round(v(z4))*16 + round(v(z3))*8 + round(v(z2))*4 + round(v(z1))*2 + round(v(z0))*1)=0
```

Interpreted voltage values for -12 * 13

```
x: (round(v(x7))*(-128) + round(v(x6))*64 + round(v(x5))*32 + round(v(x4))*16 +
round(v(x3))*8 + round(v(x2))*4 + round(v(x1))*2 + round(v(x0))*1)=-12
y: (round(v(y7))*(-128) + round(v(y6))*64 + round(v(y5))*32 + round(v(y4))*16 +
round(v(y3))*8 + round(v(y2))*4 + round(v(y1))*2 + round(v(y0))*1)=13
z: (round(v(z15))*(-32768) + round(v(z14))*16384 + round(v(z13))*8192 +
round(v(z12))*4096 + round(v(z11))*2048 + round(v(z10))*1024 + round(v(z9))*512 +
round(v(z8))*256 + round(v(z7))*128 + round(v(z6))*64 + round(v(z5))*32 +
round(v(z4))*16 + round(v(z3))*8 + round(v(z2))*4 + round(v(z1))*2 + round(v(z0))*1)=-
156
```

Interpreted voltage values for -1 * -1

```
x: (round(v(x7))*(-128) + round(v(x6))*64 + round(v(x5))*32 + round(v(x4))*16 +
round(v(x3))*8 + round(v(x2))*4 + round(v(x1))*2 + round(v(x0))*1)=-1
y: (round(v(y7))*(-128) + round(v(y6))*64 + round(v(y5))*32 + round(v(y4))*16 +
round(v(y3))*8 + round(v(y2))*4 + round(v(y1))*2 + round(v(y0))*1)=-1
z: (round(v(z15))*(-32768) + round(v(z14))*16384 + round(v(z13))*8192 +
round(v(z12))*4096 + round(v(z11))*2048 + round(v(z10))*1024 + round(v(z9))*512 +
round(v(z8))*256 + round(v(z7))*128 + round(v(z6))*64 + round(v(z5))*32 +
round(v(z4))*16 + round(v(z3))*8 + round(v(z2))*4 + round(v(z1))*2 + round(v(z0))*1)=1
```

Interpreted voltage values for -128 * -128

```
x: (round(v(x7))*(-128) + round(v(x6))*64 + round(v(x5))*32 + round(v(x4))*16 +
round(v(x3))*8 + round(v(x2))*4 + round(v(x1))*2 + round(v(x0))*1)=-128
y: (round(v(y7))*(-128) + round(v(y6))*64 + round(v(y5))*32 + round(v(y4))*16 +
round(v(y3))*8 + round(v(y2))*4 + round(v(y1))*2 + round(v(y0))*1)=-128
z: (round(v(z15))*(-32768) + round(v(z14))*16384 + round(v(z13))*8192 +
round(v(z12))*4096 + round(v(z11))*2048 + round(v(z10))*1024 + round(v(z9))*512 +
round(v(z8))*256 + round(v(z7))*128 + round(v(z6))*64 + round(v(z5))*32 +
round(v(z4))*16 + round(v(z3))*8 + round(v(z2))*4 + round(v(z1))*2 +
round(v(z0))*1)=16384
```

Interpreted voltage values for 103 * -57

```
x: (round(v(x7))*(-128) + round(v(x6))*64 + round(v(x5))*32 + round(v(x4))*16 +
round(v(x3))*8 + round(v(x2))*4 + round(v(x1))*2 + round(v(x0))*1)=103
y: (round(v(y7))*(-128) + round(v(y6))*64 + round(v(y5))*32 + round(v(y4))*16 +
round(v(y3))*8 + round(v(y2))*4 + round(v(y1))*2 + round(v(y0))*1)=-57
z: (round(v(z15))*(-32768) + round(v(z14))*16384 + round(v(z13))*8192 +
round(v(z12))*4096 + round(v(z11))*2048 + round(v(z10))*1024 + round(v(z9))*512 +
round(v(z8))*256 + round(v(z7))*128 + round(v(z6))*64 + round(v(z5))*32 +
round(v(z4))*16 + round(v(z3))*8 + round(v(z2))*4 + round(v(z1))*2 + round(v(z0))*1)=-
5871
```

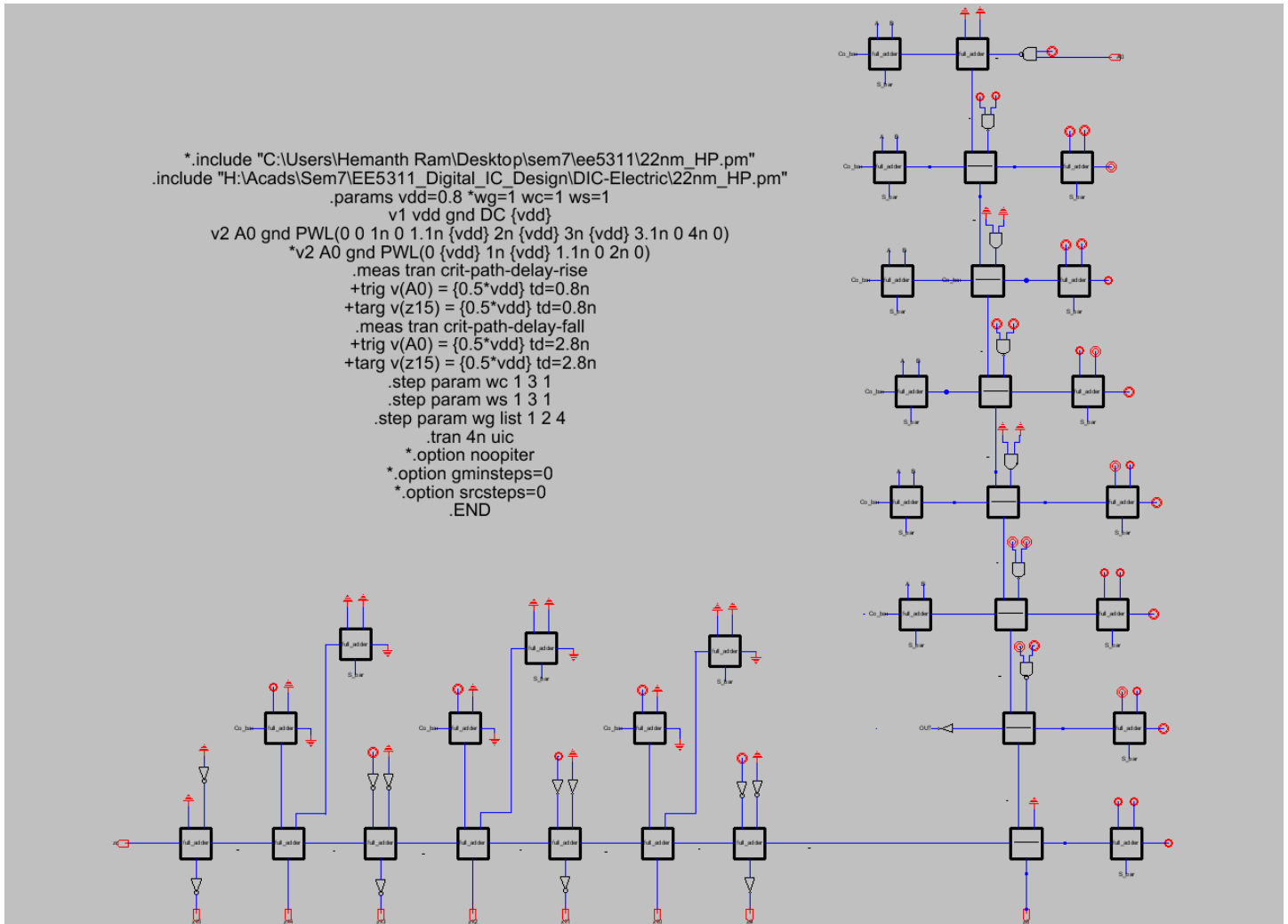
Interpreted voltage values for -50 * 50

```
x: (round(v(x7))*(-128) + round(v(x6))*64 + round(v(x5))*32 + round(v(x4))*16 +
round(v(x3))*8 + round(v(x2))*4 + round(v(x1))*2 + round(v(x0))*1)=-50
y: (round(v(y7))*(-128) + round(v(y6))*64 + round(v(y5))*32 + round(v(y4))*16 +
round(v(y3))*8 + round(v(y2))*4 + round(v(y1))*2 + round(v(y0))*1)=50
z: (round(v(z15))*(-32768) + round(v(z14))*16384 + round(v(z13))*8192 +
round(v(z12))*4096 + round(v(z11))*2048 + round(v(z10))*1024 + round(v(z9))*512 +
round(v(z8))*256 + round(v(z7))*128 + round(v(z6))*64 + round(v(z5))*32 +
round(v(z4))*16 + round(v(z3))*8 + round(v(z2))*4 + round(v(z1))*2 + round(v(z0))*1)=-
2500
```

Interpreted voltage values for 79 * 81

```
x: (round(v(x7))*(-128) + round(v(x6))*64 + round(v(x5))*32 + round(v(x4))*16 +
round(v(x3))*8 + round(v(x2))*4 + round(v(x1))*2 + round(v(x0))*1)=79
y: (round(v(y7))*(-128) + round(v(y6))*64 + round(v(y5))*32 + round(v(y4))*16 +
round(v(y3))*8 + round(v(y2))*4 + round(v(y1))*2 + round(v(y0))*1)=81
z: (round(v(z15))*(-32768) + round(v(z14))*16384 + round(v(z13))*8192 +
round(v(z12))*4096 + round(v(z11))*2048 + round(v(z10))*1024 + round(v(z9))*512 +
round(v(z8))*256 + round(v(z7))*128 + round(v(z6))*64 + round(v(z5))*32 +
round(v(z4))*16 + round(v(z3))*8 + round(v(z2))*4 + round(v(z1))*2 +
round(v(z0))*1)=6399
```

Critical Path of CSM modelled separately



Inputs to Full Adders in Critical Path

1. Input Cin is closer than A, B to output and critical input is connected to Cin in every full adder.
2. For an edge in Cin, sum delay for different combinations of A, B in a Full Adder:

Inputs to (A,B) \ Cin Edge Type	Rising	Falling
00	62.6ps	26.7ps
01	46.9ps	34.7ps
10	43.3ps	35.2ps
11	30.1ps	49.4ps

So, for max delay in sum propagation over both rising and falling edges, fix A=0, B=0.

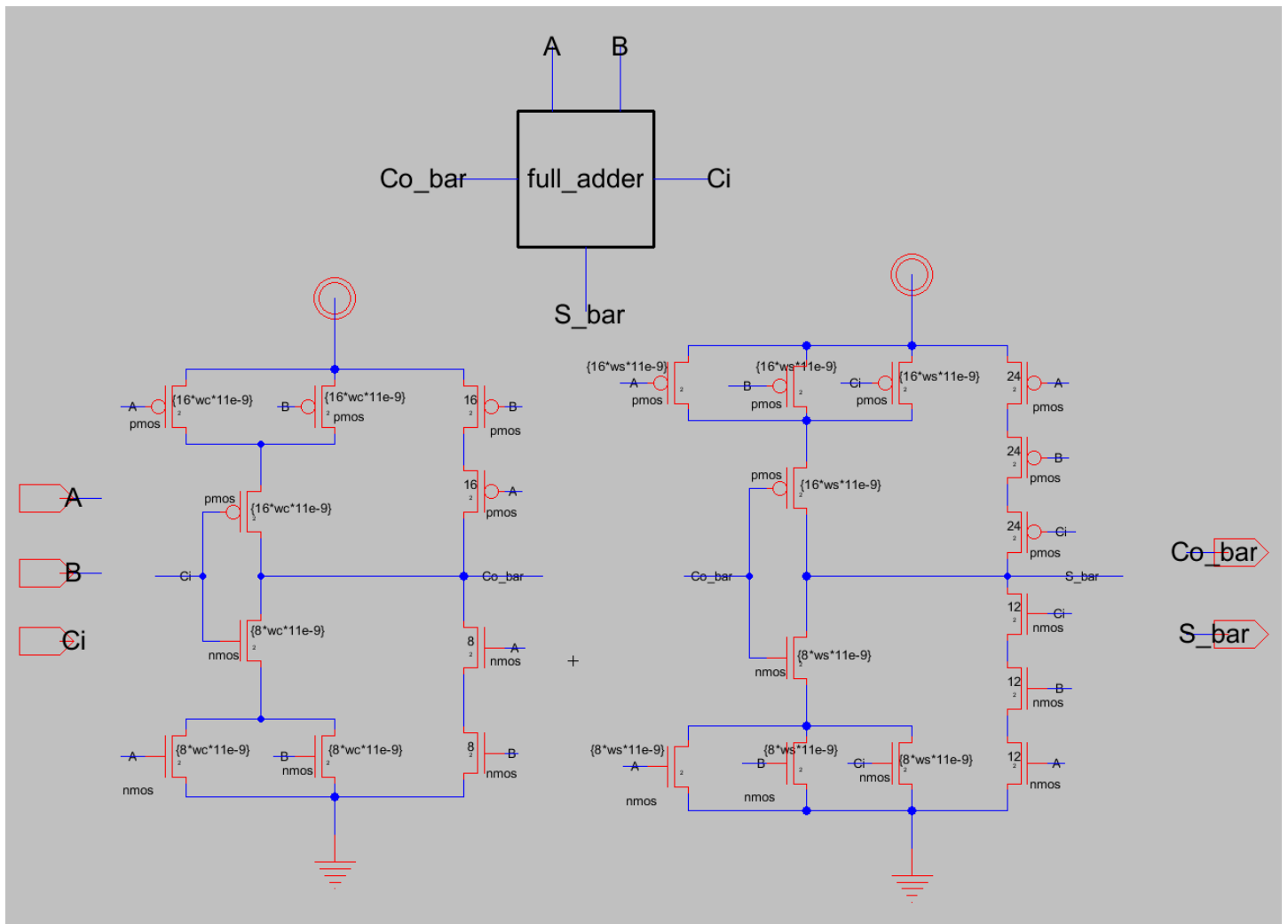
3. For an edge in Carry in, Full Adder should be in propagation stage for max delay. Delays for different combinations of A/B in Full Adder:

Inputs to (A, B) \ Cin Edge Type	Rising	Falling
01	30.2ps	9.37ps
10	27.7ps	9.27ps

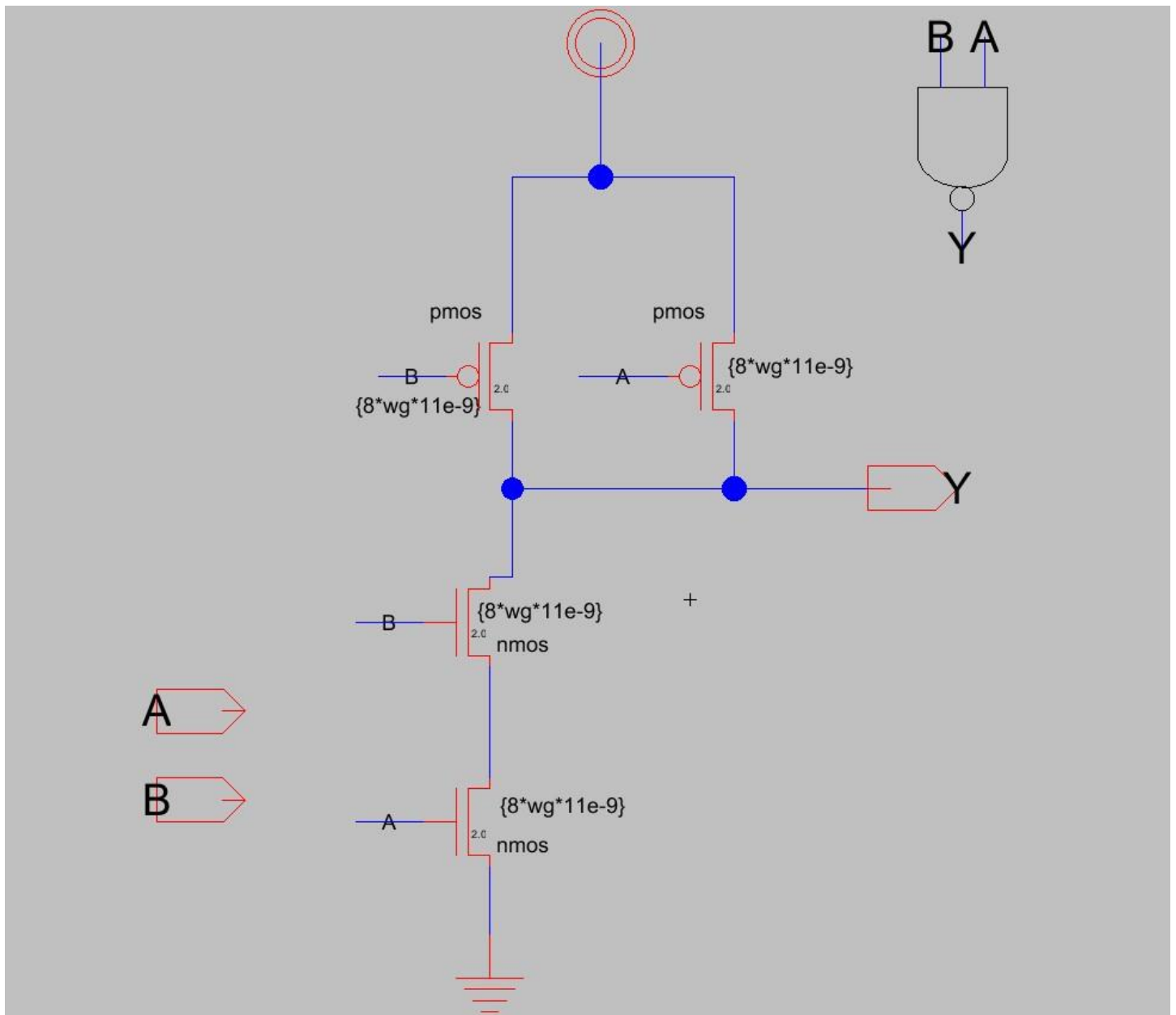
So, for rising/falling edge in Cin, A=0, B=1 for max delay in carry propagation

Sizes of FA, NAND, AND and INV gates used are parameterised

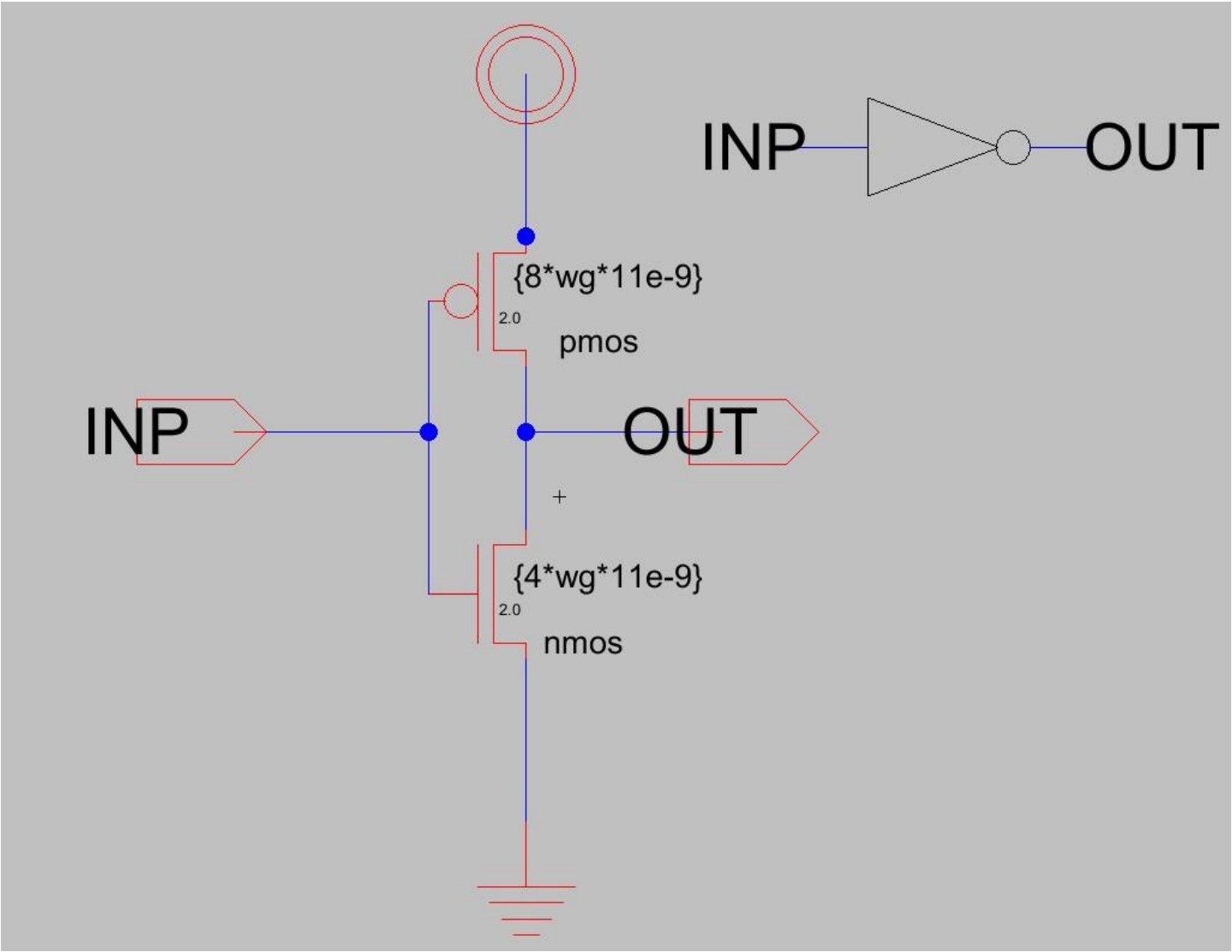
Schematic of Full Adder used



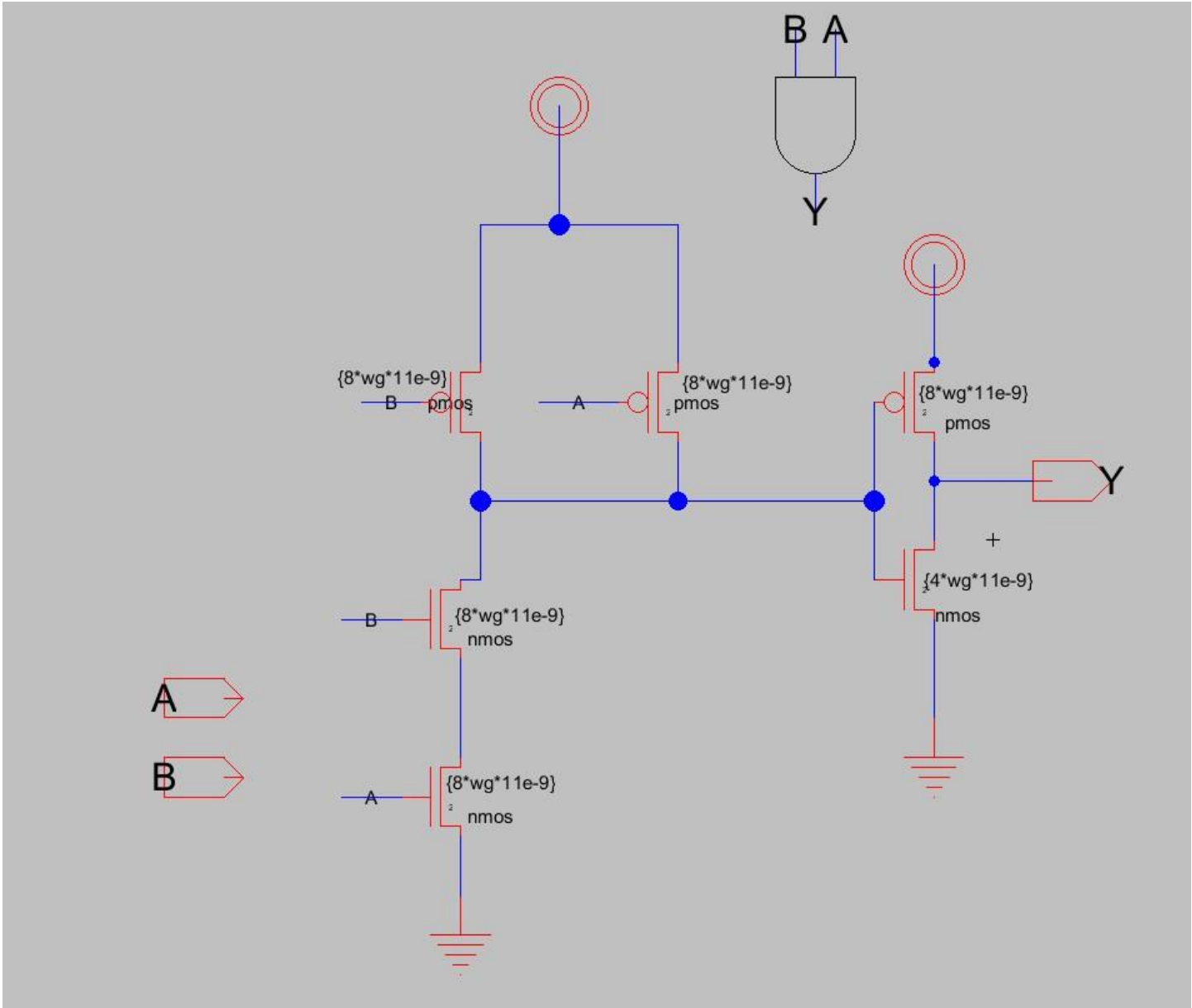
Schematic of NAND gate used



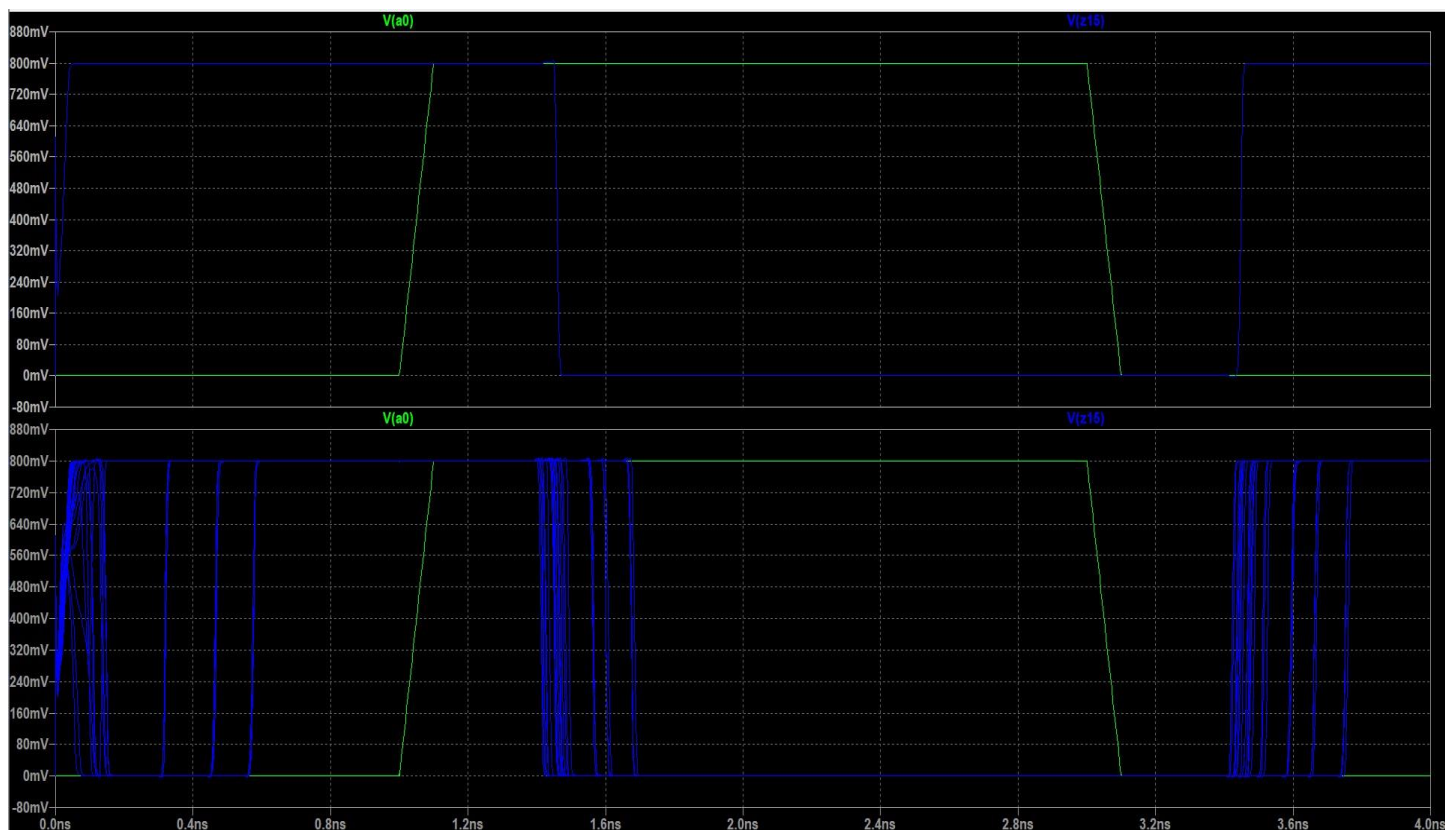
Schematic of Inverter used



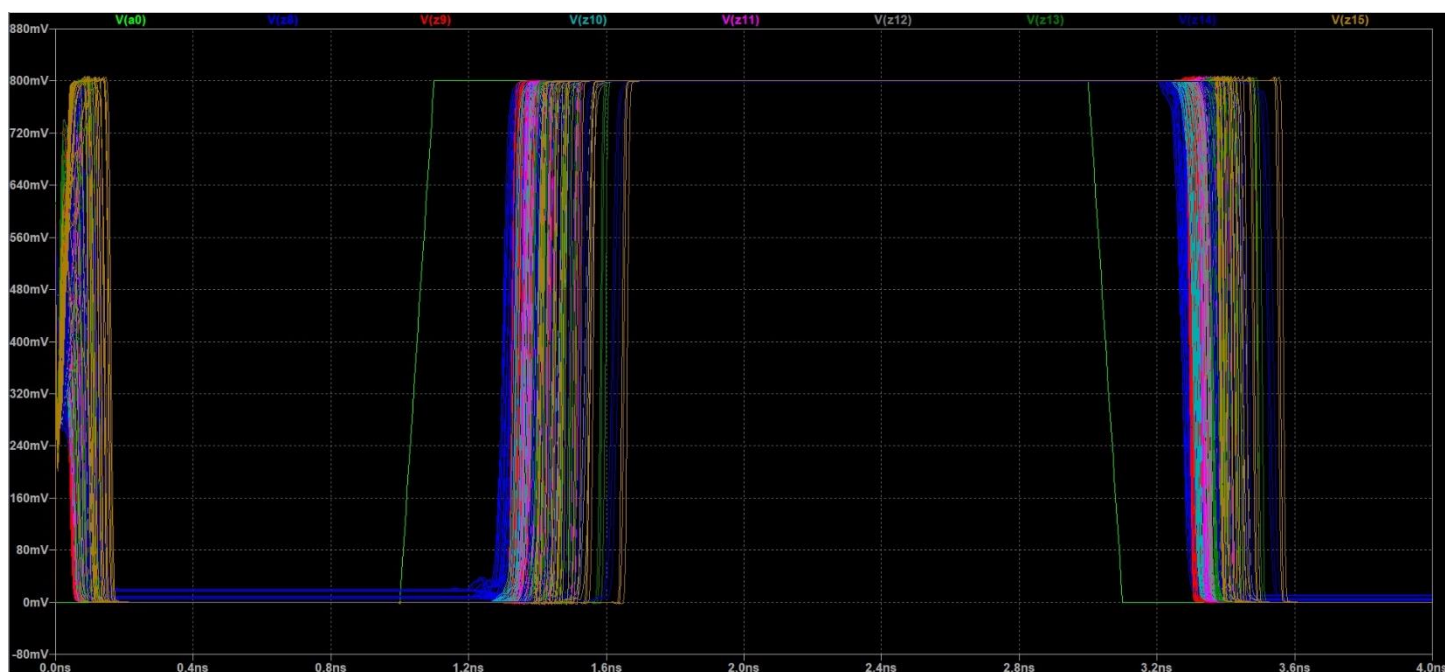
Schematic of AND gate used



Simulation of Critical Path Delay swept across possible gate size combinations



Simulation of Vector Merge outputs for critical input



Critical Path Delay tabulated across gate size combinations

step				Crit-Path-Rise	Crit-Path-Fall	Max t _{pd}	Area (unit_sq)
1	wc=1	ws=1	wg=1	5.15E-10	5.47E-10	5.47E-10	9049
2	wc=2	ws=1	wg=1	4.23E-10	4.22E-10	4.23E-10	9751
3	wc=3	ws=1	wg=1	4.10E-10	3.98E-10	4.10E-10	10679
4	wc=1	ws=2	wg=1	5.58E-10	6.19E-10	6.19E-10	11315
5	wc=2	ws=2	wg=1	4.14E-10	4.37E-10	4.37E-10	12017
6	wc=3	ws=2	wg=1	3.77E-10	3.86E-10	3.86E-10	12945
7	wc=1	ws=3	wg=1	6.34E-10	7.11E-10	7.11E-10	13899
8	wc=2	ws=3	wg=1	4.44E-10	4.76E-10	4.76E-10	14601
9	wc=3	ws=3	wg=1	3.87E-10	4.06E-10	4.06E-10	15529
10	wc=1	ws=1	wg=2	5.12E-10	5.44E-10	5.44E-10	9049
11	wc=2	ws=1	wg=2	4.16E-10	4.17E-10	4.17E-10	9751
12	wc=3	ws=1	wg=2	4.01E-10	3.91E-10	4.01E-10	10679
13	wc=1	ws=2	wg=2	5.51E-10	6.13E-10	6.13E-10	11315
14	wc=2	ws=2	wg=2	4.05E-10	4.29E-10	4.29E-10	12017
15	wc=3	ws=2	wg=2	3.66E-10	3.77E-10	3.77E-10	12945
16	wc=1	ws=3	wg=2	6.25E-10	7.03E-10	7.03E-10	13899
17	wc=2	ws=3	wg=2	4.33E-10	4.66E-10	4.66E-10	14601
18	wc=3	ws=3	wg=2	3.75E-10	3.95E-10	3.95E-10	15529
19	wc=1	ws=1	wg=4	5.15E-10	5.48E-10	5.48E-10	9049
20	wc=2	ws=1	wg=4	4.16E-10	4.17E-10	4.17E-10	9751
21	wc=3	ws=1	wg=4	4.00E-10	3.90E-10	4.00E-10	10679
22	wc=1	ws=2	wg=4	5.52E-10	6.13E-10	6.13E-10	11315
23	wc=2	ws=2	wg=4	4.03E-10	4.27E-10	4.27E-10	12017
24	wc=3	ws=2	wg=4	3.62E-10	3.73E-10	3.73E-10	12945
25	wc=1	ws=3	wg=4	6.24E-10	7.02E-10	7.02E-10	13899
26	wc=2	ws=3	wg=4	4.29E-10	4.63E-10	4.63E-10	14601
27	wc=3	ws=3	wg=4	3.69E-10	3.90E-10	3.90E-10	15529

For Cout=3x, Sum=2x, Nand=4x min delay is observed.

For Cout=3x, Sum=2x, Nand=1x, only a 3.5% delay improvement is observed but a much smaller nand gate is used.

But combination Cout=3x, Sum=1x, Nand=1x has only a 6% higher delay and 18% lesser area. So, chosen sizes are 3x for carry out block, 1x for sum block, 1x for the standard gates.

Chosen Gate sizes

Full Adder:

Cout-bar: 3x

Sum-bar: 1x

Standard Cells:

NAND, AND, INV: 1x

--End--

