# Daltech, Dalhousie University Department of Electrical and Computer Engineering

## ECED 4502 - Digital Signal Processing

Lab 2 – Spectrum Aliasing and Foldback using GNURadio

## **Objectives**

The objective of this lab is to become familiar with the use of GNURadio and to observe the effects of sampling the signal below the Nyquist sampling rate which is twice the maximum frequency in the spectrum of the original analog signal. In this lab we demonstrate this effect for sinusoidal and square wave signals. The background material for this lab is provided at the end of this lab write-up.

#### **Procedure**

- I. Use the previously posted instruction on Brightspace to install GNURadio. Once Installation is finished. Open "GNURadio Companion". It will open an initial screen of GNURadio as illustrated in Fig. 1.
- II. When the initial splash screen appears, choose "File→Open". Navigate to the downloaded file directory and choose "Exercise\_Sampling\_and\_Aliasing.grc", it should bring the screen shown in the Fig. 2 and run the program by going into "Run→Execute" or press F6. The screen showed in Fig.4 should appear with the default configuration.
- III. Refer Fig. 3 which illustrate the different blocks of the Flow Chart. For first part of the lab (refer Fig.4 (a)), double click on the signal source block and make sure your amplitude is 1 and offset value is 0. so the DC offset is eliminated. Perform the experiment and answer questions 1 through 5.
- IV. For the second part (refer Fig.4 (b)), double click on the signal source block and make sure your amplitude is 1 and offset value is -0.5. And select the Square wave when the Output GUI (Fig. 5) popped on the screen. For the triangular wave, keep the amplitude and offset value as it is and when Output GUI (Fig. 5) popped on the screen, select triangle.

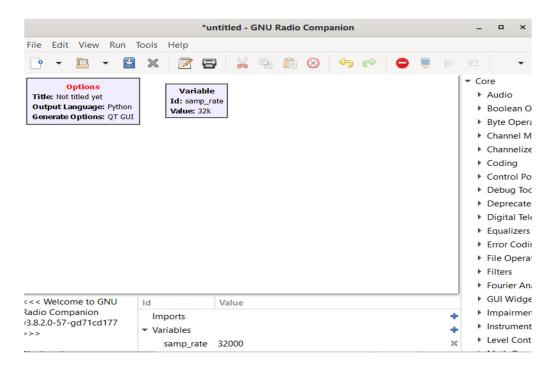


Fig.1. Initial GNURadio welcome screen

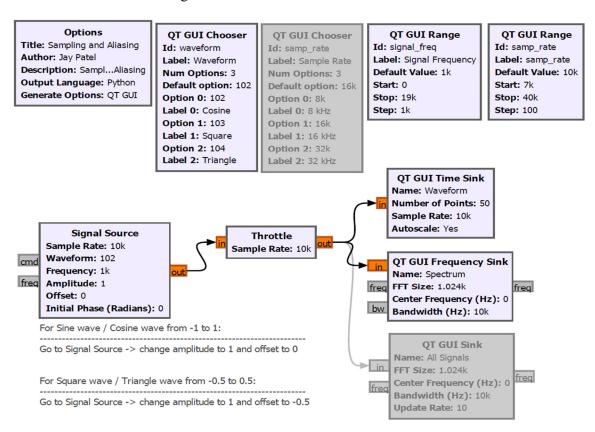


Fig. 2 Sampling and Aliasing GNURadio Experiment Setup

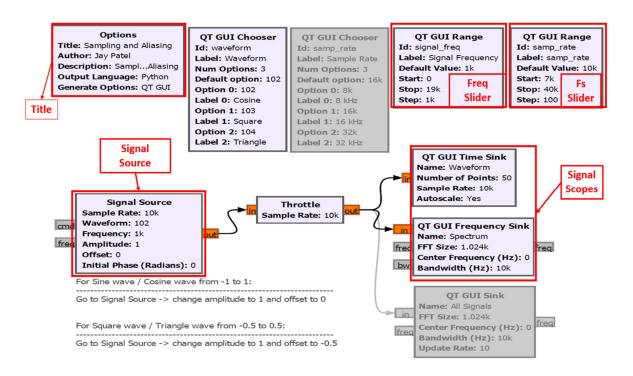
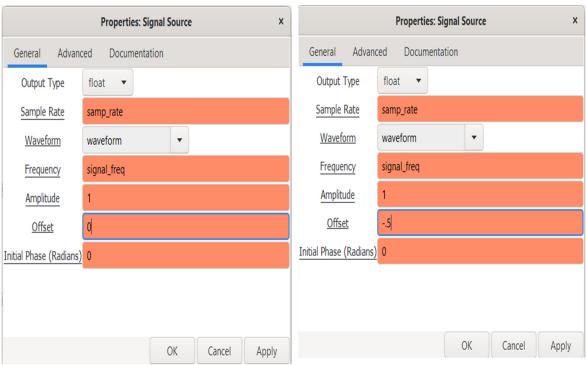


Fig. 3 Introduction to Flow Graph



(a) For cosine wave, Signal Source Block configuration

(b) For Square & Triangle wave, Signal Source Block configuration

Fig. 4 Signal Source Block configuration

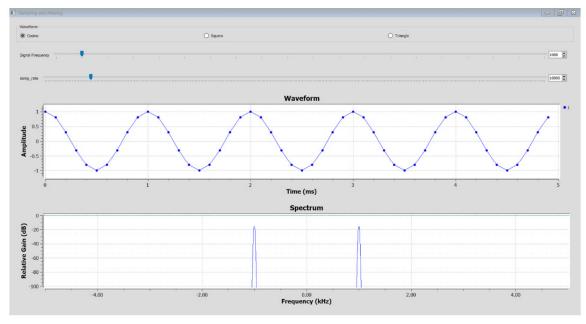


Fig. 5 Output GUI

There are two graphs located on the screen. The top graph is the sampled signal in time domain as seen by the computer. The bottom graph is the same signal in the frequency domain, its Fourier transform.

# Questions

- 1. The initial set-up for the sampling frequency Fs is 10 KHz. The input signal to be sampled is a **sinusoidal waveform**. Please observe the sampled signal at the output of the GUI, its waveform in the time domain and its frequency spectrum with log-scale (dB). Is this signal the same as the original input signal? Explain.
- 2. Keep the sampling frequency on 10KHz. Increase the input frequency from 10 KHz to 20 KHz and describe changes you see in the time domain sampled signal.
- 3. Varying the frequency of the sinusoidal signal from 1 to 20 KHz, please observe the spectrum of the sampled signal on screen, and record frequencies of these signals and enter them in the table as follows:

$f_{in}(kHz)$	1	3	5	7	9	11	13	15	17	19
f <sub>out</sub> (kHz)										

From the observation above, you will observe the foldback effect of the sampled signal. Can you find the frequency of input signal when the foldback effect occurred? How does the foldback effect happen?

4. Change the sampling frequency to 40 KHz, and repeat the procedure of step3 then enter your results in the table as follows:

$f_{in}(kHz)$	1	3	5	7	9	11	13	15	17	19
$f_{out}(\mathrm{kHz})$										

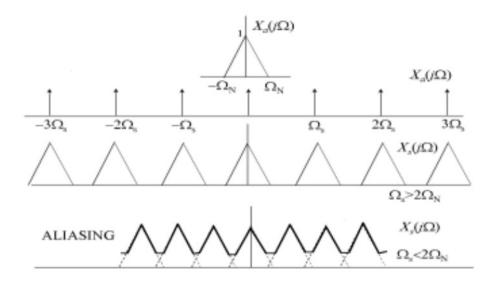
Similarly, from the table above, can you find the foldback effect? Explain.

- 5. Comparing step3 with step4, what can you conclude? When and why does the foldback effect happen?
- 6. In this part you will observe the aliasing effect introduced in the sampling of another periodic signal. Change the input signal from the sine wave to a 50% **square wave** with 1 Vp-p, 1 kHz, and set the sampling frequency to 20 KHz. Observe the harmonics characteristics of the output signal on your screen and sketch your results. Explain each frequency of the spikes your observed.
- 7. Keeping the sampling frequency at 20 KHz, use 2 KHz first & 3 KHz next as the frequency of the input signal. Can you find any aliasing effect on the spectrum of the output signal? If your answer is "Yes", please explain how the spectrum aliasing happen for each input signal, 2 KHz and 3 KHz. If your answer is "No", please give a reason and comment on your observations.
- 8. Change the sampling frequency to 10 KHz, repeat step6 with the same 1 KHz, 50% square wave, pay attention to the behavior of the spikes and their frequencies in the spectrum of the sampled signal.
- 9. Keeping the sampling frequency at 10 KHz, use 2 KHz first & 3 KHz next as the frequency of the signal. Can you find any aliasing effect on the spectrum of the sampled signal? If your answer is "Yes", please explain how the spectrum

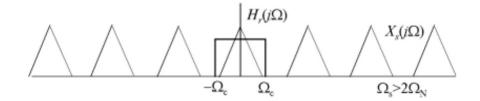
- aliasing happen for each input signal, 2 KHz and 3 KHz. If your answer is "No", please give a reason and comment on your observations.
- 10. Keeping the sampling frequency at 10 KHz, use now a **triangular waveform** with 2 KHz first & 3 KHz next as its frequency. Can you find any aliasing effect on the spectrum of the sampled signal? If your answer is "Yes", please explain how the spectrum aliasing happen for each input signal, 2 KHz and 3 KHz. If your answer is "No", please give a reason and comment on your observations. Also, acknowledge any difference in the amplitude spectrum of the sampled signal with respect to that of the corresponding square wave.

## **Theoretical Background**

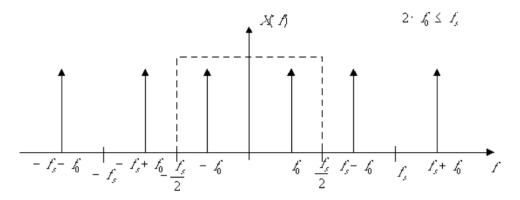
When a signal is sampled, it is multiplied in the time domain by another signal called a pulse train. A pulse train is just a repeating pulse at constant time intervals the sampling period. The Fourier transform of the pulse train is again a pulse train with deltas separated in the frequency domain by the sampling frequencies  $f_s$ . In the frequency domain, the sampling procedure produces the same result as convolving the spectrum of the original signal with the pulse train. This procedure creates an exact duplicate of the Fourier transform of the input signal (analog prototype) centered at different multiples of the sampling frequency (the frequency of the pulses in the pulse train), as shown in figure below.



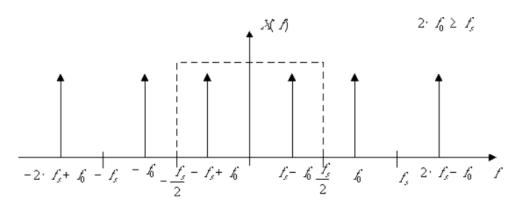
Ideally, the original signal can be filtered out from the sampled signal with the aid of low-pass reconstruction filters. These filters will attenuate or "cut-off" any duplication of the spectrum of the analog prototype signals occurring at higher frequencies. However, this can only happen if the sampling rate is large enough to prevent the replicated signals from interfering with one another. For example, if the signal is sampled at too low of a rate, then the neighboring duplicate signals will start to overlap. This overlapping of signals prevents us from filtering out the original. This distortion is referred to as aliasing. To avoid aliasing, the sampling frequency must be higher than two times the maximum frequency of the original signal. At exactly two times the original signals frequency, the spectrum of the sampled signal is composed of segments of the original that just barely touches one another. This frequency is known as the Nyquist rate.



Assume we are sampling a sine wave of frequency  $f_0$  at the rate  $f_s$  higher than the Nyquist rate  $(f_s/2)$ . After filtering out the duplicate images of spectrum, we get the following signal at the output in the frequency domain, which is the same as the spectrum of the original sinusoidal waveform.



However, if we increase the frequency of the original signal, the sidebands move further apart, until they surpass the limits of the filter. However, the sidebands of the adjacent duplicates also spread apart, causing them to enter the range of the low-pass reconstruction filter as shown below:



So rather than observing at the output of the reconstruction filter the sinusoidal signal with frequency  $f_0$ , we observe the sinusoid with frequency  $f_s$  -  $f_0$ . This effect is known as foldback. Foldback is an effect of filtering out the higher frequencies. In general case, we can have a foldback from higher segment so the relation for the output signal frequency is  $kf_s$  -  $f_0$  (where k is the integer –the segment number from which we are getting the foldback).