

Bitwise Operators & Loops

→ Bitwise operators are used to perform bit-level operations.

operator	Description	operator	Description
&	Bitwise AND	<<	Bitwise left shift
	" OR	>>	" right "
^	" XOR	>>>	unsigned Right shift
~	" Complement		

1) Bitwise AND Operator

Return 1 if $\&$ only if both the operands are 1.

a	b	$a \& b$
0	0	0
0	1	0
1	0	0
1	1	1

Eg:- Bitwise AND of integer 2 & 3

$$2 = 00000010$$

$$3 = 00000011 \quad \&$$

$$\underline{00000010} \Rightarrow 2$$

$$\therefore 2 \& 3 = 2$$

2) Bitwise OR Operator

Return 1 if at least one of the operand is 1.

a	b	$a b$
0	0	0
0	1	1
1	0	1
1	1	1

Eg:- Bitwise OR of 7 | 4

$$7 = 00000111$$

$$4 = 00000100 \quad |$$

$$\underline{00000111} \Rightarrow 7$$

$$\therefore 7 | 4 = 7$$

3) Bitwise XOR Operator

Return 1 if $\&$ only if one of the operands is 1. However, if both the operands are 0 or 1 then the result is 0.

a	b	$a ^ b$
0	0	0
0	1	1
1	0	1
1	1	0

4) Bitwise NOT (\sim) operator

It changes binary digits 1 to 0 & 0 to 1

$$a \hookrightarrow a \quad \hookrightarrow = \text{Tilda}$$

0 1 0 = off (false)

1 0 1 = 0M (True)

Q Find unique element (use XOR operator)

→ Example of Bitwise AND, OR, NOT & XOR operator.

```

→ int main () {
    cout << (2 & 3);
    return 0;
}

```

2 = 0010
3 = 0011 \neq
0010 \Rightarrow 2

$$\text{Output} = 2 \quad \therefore 2 \neq 3 = 2$$

$\rightarrow \text{int main() } \{ \quad \longrightarrow \quad \delta = 0101$

`cout << (5 & 10);` $10 = \underline{1010} \neq$

return 0; 0 0 0 0 \Rightarrow 0

outPut = 0 ∵ 5 ≠ 10 = 0

\rightarrow int main() { \longrightarrow 5 = 0101 }

```
cout << (5 / 10);           10 = 10 10 OR(1)  
return 0;                  1111 => 15  
?
```

$$\text{output} = 15 \quad \therefore 51_{10} = 15$$

→ int main () { → 2 = 0 0 1 0

`cout << (213);` $3 = 0011 \text{ OR } (1)$

$$\overline{0011} \Rightarrow 3$$

→ int main() { → $i = 00000001$
 int num = 1; → $\sim i = 11111110$

$\text{cout} \ll \sim \text{num} \ll \text{endl};$ Here, the most left bit is
 $\text{cout} \ll (\sim \text{num}) \ll \text{endl};$ 1. That means it's a -ve number.
 $\text{cout} \ll \sim (\text{num}) \ll \text{endl};$ To access negative number, we've
 } to do 2's complement

Output = -2 I's complement = $0 + 1 + 1 \Rightarrow 0$
 -2 $11111110 = 00000001$
 -2 2's complement = Add 1 in I's complement

∴ That's why $\text{cout} \ll (\sim \text{num}),$ 00000001
 $\text{cout} \ll \sim \text{num} \neq$ + 1
 $\text{cout} \ll \sim (\text{num})$ $00000010 \Rightarrow 2$

Gives output as -2.

→ int main() { → $5 = 0101$
 $\text{cout} \ll (5^5);$ $5 = 0101$ XOR (^)
 return 0; $\underline{0000} \Rightarrow 0$

} ∴ $(5^5) = 0$

→ int main() { → $5 = 0101$
 $\text{cout} \ll (5^10);$ $10 = 1010$ XOR (^)
 return 0; $\underline{1111} \Rightarrow 15.$

} ∴ $(5^10) = 15$

→ int main() { → $4 = 0100$
 $\text{cout} \ll (4^7);$ $7 = 0111$ XOR (^)

} $\underline{0011} \Rightarrow 3$

```
+ int main() {
    cout << (5^ -5);
    return 0;
}
```

Output: -2

$$5 = 00000101$$

$$-5 = \cancel{1}111101 \text{ XOR } (^)$$

(1) 1111110

→ This MSB shows that XOR of
5^ -5 is a negative number

1's complement of $5^ -5$

$$5 = 00000101 = 00000001$$

$$1's = \cancel{1}1111010 \quad 2's \text{ complement of } (5^ -5) \quad 1's \text{ complement}$$

$$2's = \underline{11111011} + 1 = 00000001$$

$$\therefore 2's \text{ complement of } 5 \text{ is } -5 \quad \underline{00000010} + 1 \Rightarrow 2$$

That's why $(5^ -5)$ output is -2

→ Bitwise Left & Right Shift Operators.

1) Left Shift Operator:

The leftshift operator shift all bits towards the left by a certain no. of specified bits.

NOTE: Left shifting a number by certain positions is equivalent to multiplying the number by two raised to the power of the specified position. i.e.

leftshift x by n positions = $x \times 2^n$

Eg:- leftshift 3 by 2 positions ($3 \ll 2$) $\Rightarrow 3 \times 2^2 = 12$

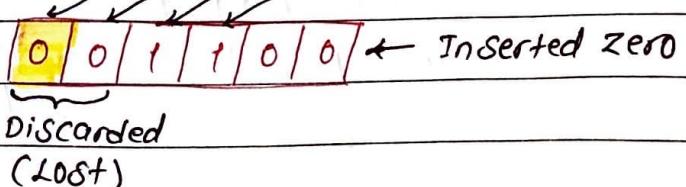
$$3 = 00000011$$



$$00001100 = 12$$

MSB LSB

$$\Rightarrow \boxed{0 \ 0 \ 1 \ 1} \Rightarrow 3$$



$$\therefore 3 \ll 2 = 12$$

→ int main () { → $a = 2 \Rightarrow 00000010$
 int a = 2;
 cout << (a << 1); $a << 1 = a$ is left shifted by 1 bit.
 return 0;
 }
 Output = 4
 $\therefore 2 << 1 = 4.$

$\Rightarrow 00000100 = 4.$

When shifting left, the most-significant (Left side) bit is lost & a '0' bit is inserted to the other end.

2) Right shift operator :

The right shift operator shifts all bits towards the right by a certain no. of specified bits.

NOTE: if when bits are shifted right then leading positions are filled with zeros.

∴ Right shifting a number by certain position is equivalent to dividing the number by two raised to the power of the specified position. i.e.

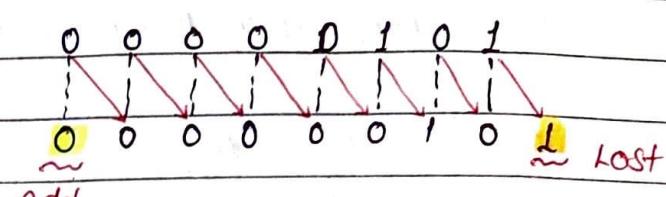
$$\text{Right shift } x \text{ by } n \text{ positions} = x/2^n$$

Eg:- Right shifting 14 by 1 position ($14 \gg 1$) $\Rightarrow 14/2^1 = 7$

$$14 = 00001110$$

\downarrow $\Rightarrow 000001110$
 00000111
 $\therefore 14 \gg 1 = 7$

→ int main() { → $n = 5 \Rightarrow 00000101$
 int n = 5; $n \gg 1 = n$ is rightshifted by 1 bit
 cout << (n >> 1);
 return 0;
 }
 output = 2

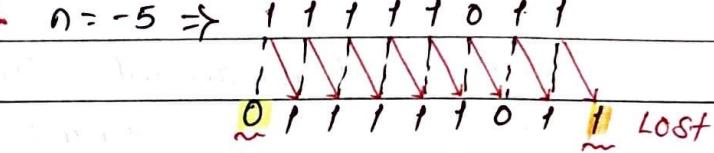


$\therefore 5 \gg 1 = 2 \Rightarrow 00000010 = 2$

When shifting right, the least-significant (Right-side) bit is lost
 & a '0' is inserted on other end.

→ Let see what happens when right shift a negative number.

int main() { → $n = -5 \Rightarrow 11111011$
 int n = -5;
 cout << (n >> 1);
 return 0;
 }



The msB shows that it is a positive number, but our output is a negative number.

→ In case of ^{lve} signed integer (hold +ve, -ve or 0) shifting a bit either left or right is handled by compiler.
 But, in case of ^{lve} unsigned integer (hold +ve, 0) shifting a bit right is not handled by compiler & it giving large number as output.

Eg:- int n = -100;
 cout << (n >> 1);
 output = -50
 (In case of signed integer)

unsigned int n = -100;
 cout << (n >> 1);
 output = 2147483598
 (Large number, in case of -ve Unsigned integer)

→ When we shift a number ~~is~~ either left or right by a negative number, then it throws warning & gives a garbage value.
Remember, it will not show error.

Eg:- `int a = 10;
cout << (a << -1);`

Output : 1846981242 (Garbage value)

→ Unary operators :

operator	operation	Equivalent To
<code>++ (increment)</code>	<code>num ++</code>	<code>num = num + 1</code>
<code>-- (decrement)</code>	<code>num --</code>	<code>num = num - 1</code>

→ Pre & Post Increment Operators.

Pre-Increment = `++a;`

↳ first value change & then value use.

Post-Increment = `a++;`

↳ first old value use & then value change.

→ Pre & Post Decrement Operators.

Pre-Decrement = `--a;`

↳ first value change & then new value use.

Post-Decrement = `a--;`

↳ first old value use & then value change.

Eg:- `int a = 10;` Output : 11, 11.

`int b = ++a;`

`cout << a;`

`cout << b;`

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```
int a = 10;  
int b = ++a; (a = a+1)  
b = a = a+1  
b = a = 10+1  
b = a = 11;
```

Here, we've Pre-Increment before the operand (i.e. $++a$). So the value of 'a' is first incremented from 10 to 11 & then assigned to b. Hence, b becomes 11.

Eg:- int a = 10;
int b = a++;
cout << a << endl;
cout << b << endl;
Output = 11
10

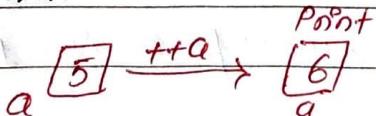
```
int a = 10;  
int b = a++ (a = a+1)  
b = a = a+1  
b = 10 = 10+1  
b = 10 & a = 10+1 = 11
```

Here, we've Post-Increment after the operand ($a++$). So the value of 'a' is first assigned to b. So b becomes 10 & 'a' is later incremented from 10 to 11.

Eg:- int main () {
int a = 5;
cout << (++a);
}

Output = 6

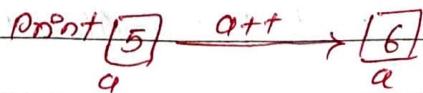
Here, in this type of case flow is most imp. Here, we're using Pre-Increment operator, so first value of 'a' is increased by 1 & then new value of 'a' is printed.



```
int main () {  
int a = 5;  
cout << (a++);  
}
```

Output = 5

Here, in this example, we are using Post-Increment operator. That means, first use the old value & then update the value. So first old value of 'a' is printed (i.e. 5) & then value of 'a' is updated to 6.



Eg:- int main () {

int a = 10;

cout << (--a)*10;

}

Output = 90

(--a) * 10;

first decrement the value
of a. & then multiply by
10 (i.e. 9 * 10 = 90)

int main () {

int a = 10;

cout << (a--) * 10;

}

Output = 100

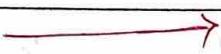
(a--) * 10;

first use the value of a &
multiplying by 10. Then decrement
the value of a. (i.e. 10 * 10 = 100)



int main () {

int a = 21;



a

21 22 23

cout << (++a); // 22

first increment, then use

cout << (a++); // 22

first use old value, then increment

cout << a; // 23

Just print the new value of a.

}



int main () {

int a = 10;

cout << (++a)*10; // 110

cout << (a++) * 10; // 110

cout << a; // 12

}

i) $(++a) * 10$; ⇒ first increment & then use. (i.e. $a = 11$)

$11 \times 10 = 110$; now value of a is 11

ii) $(a++) * 10$; ⇒ first use old value of a, then increment.

$11 \times 10 = 110$; now value of a is 12 (post-increment)

iii) $a = 12$; ⇒ At this time value of a is 12.

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```
int main () {  
    int a = 10;  
    cout << ((++a) * (a++));  
}  
  
Output = 121
```

$$\begin{aligned} ++a &= 11 \text{ (First increment)} \\ a++ &= 10 \text{ (First use old value)} \\ (++) &\neq (a++) \\ &= 11 * 11 \\ &= 121. \end{aligned}$$

```
int main () {  
    int a = 10;  
    cout << ((a++) * (++a));  
}  
  
Output = 120
```

$$\begin{aligned} a++ &= 10 \text{ (First use old value)} \\ &\text{increment the value of } a \\ &\text{by 1.) i.e. } a = \textcircled{11} \\ ++a &= \underline{11+1} = 12 \text{ (First increment then use the value)} \\ \therefore (a++) &= 10 \neq (++a) = 12. \\ (a++) * (++a) &= 120. \end{aligned}$$

```
int main () {  
    int a = 10;  
    int b = --a;  
    cout << a; // 9  
    cout << b; // 9  
}
```

$$\begin{aligned} a &= 10; \\ b &= --a; \text{ first decrement \& then use the value} \\ b &= a-1 = 10-1 = 9. \\ \therefore a &= 9 \neq b = 9 \end{aligned}$$

```
int main () {  
    int a = 10;  
    int b = a--;  
    cout << a; // 9  
    cout << b; // 10  
}
```

$$\begin{aligned} a &= 10; \\ b &= a--; \text{ first use then change} \\ \therefore b & \text{use the old value of } a. \\ b &= 10. \text{ After this process } a \\ &\text{is decrement by 2.} \\ \therefore a &= a-1 \Rightarrow 10-1 = 9. \\ a &= 9 \neq b = 10. \end{aligned}$$