

# Goal\_programming

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This notebook contains Assignment- 5

## SUMMARY

The values 50 and 75 indicate that these are the LHS values for the respective constraints when the decision variables take their optimal values.

1. Producing 0 units of Product 1, 0 units of Product 2, and 15 units of Product 3 is the ideal production plan. Profit is maximized given the constraints.
- 2) The company employed 2,550 more people than it had planned. Even though exceeding the objective resulted in penalties, the expenses were mitigated by the production plan that maximized profits.
- 3) The optimization model solution indicates that the corporation can make up to \$225 million in profit. This is the maximum profit level that can be achieved within the given constraints and business environment.

```
library(lpSolveAPI)
```

## PROBLEM STATEMENT

The Research and Development Division of the Emax Corporation has developed three new products. A decision now needs to be made on which mix of these products should be produced. Management wants primary consideration given to three factors: total profit, stability in the workforce, and achieving an increase in the company's earnings next year from the \$75 million achieved this year. In particular, using the units given in the following table, they want to

Maximize  $Z = P - 6C - 3D$ ,

where

$P$  = total (discounted) profit over the life of the new products,

$C$  = change (in either direction) in the current level of employment,

$D$  = decrease (if any) in next year's earnings from the current year's level.

The amount of any increase in earnings does not enter into  $Z$ , because management is concerned primarily with just achieving some increase to keep the stockholders happy.

Questions:

1. Define  $y1+$  and  $y1-$ , respectively, as the amount over (if any) and the amount under (if any) the employment level goal. Define  $y2+$  and  $y2-$  in the same way for the goal regarding earnings next year. Define  $x1$ ,  $x2$ , and  $x3$  as the production rates of Products 1, 2, and 3, respectively. With these definitions, use the goal

programming technique to express  $y_1^+$ ,  $y_1^-$ ,  $y_2^+$  and  $y_2^-$  algebraically in terms of  $x_1$ ,  $x_2$ , and  $x_3$ . Also express  $P$  in terms of  $x_1$ ,  $x_2$  and  $x_3$ .

2. Express management's objective function in terms of  $x_1$ ,  $x_2$ ,  $x_3$ ,  $y_1^+$ ,  $y_1^-$ ,  $y_2^+$  and  $y_2^-$ .

3. Formulate and solve the linear programming model. What are your findings

### **SOLUTION**

The main objective of this problem is to maximize the profits made from previous years. So the considering the  $y^+$  and  $y^-$ , below is the objective.

$$\text{max: } 20x_1 + 15x_2 + 25x_3 - 6y_1^p - 6y_1^n - 3y_2^p - 3y_2^n$$

### **CONSTRAINTS**

$$6x_1 + 4x_2 + 5x_3 - y_1^p + y_1^n = 50;$$

$$8x_1 + 7x_2 + 5x_3 + y_2^n - y_2^p = 75; y_1^a \geq 0;$$

$$y_1^b \geq 0;$$

$$y_2^a \geq 0;$$

$$y_2^b \geq 0;$$

$$x_1 \geq 0;$$

$$x_2 \geq 0;$$

$$x_3 \geq 0;$$

where,

$x_1$  = Production rate of Product 1

$x_2$  = Production rate of Product 2

$x_3$  = Production rate of Product 3

$y_1^p$  = Variable representing the amount over the goal.(positive)

$y_1^n$  = Variable representing the amount under the goal.(negative)

$y_2^p$  = variable for the earnings representing amount over the goal.(positive)

$y_2^n$  = variable for the earnings representing amount over the goal.(negative)

Representing  $P$  in terms of  $x_1, x_2, x_3$

$$P = 20x_1 + 15x_2 + 25x_3$$

Now, solving the LP Model.

```
x <- read.lp("goal.lp") #Reading the LP file
x
```

```
## Model name:  
##   a linear program with 11 decision variables and 2 constraints
```

```
solve(x)
```

```
## [1] 0
```

#Solving the objective

```
get.objective(x) #get objective value
```

```
## [1] 225
```

```
get.variables(x)  # get values of decision variables
```

```
## [1] 0 0 15 25 0 0 0 0 0 0 0
```

```
get.constraints(x) #get constraint RHS values
```

```
## [1] 50 75
```