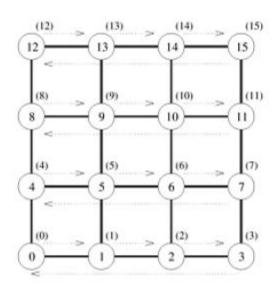
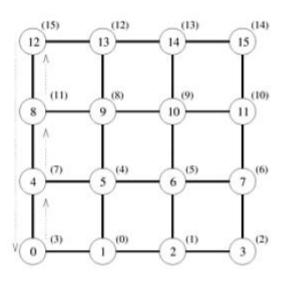
Circular Shift

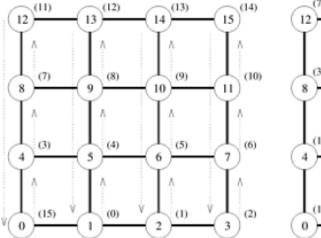
$M_{0,p-1}$	$M_{1,p-1}$	$M_{p-1, p-1}$		$M_{p-1,0}$	$M_{p-1,1}$	$M_{p-1, p-1}$
:	:	:		:	:	:
M _{0,1}	M 1,1	$M_{p-1,1}$		M _{1.0}	M 1.1	M 1,p-1
$M_{0,0}$	M _{1,0}	$M_{p-1,0}$	All-to-all personalized	$M_{0,0}$	$M_{0,1}$	$M_{0,p-1}$
0	1	• (p-1)	communication	0	1	. (p-1)

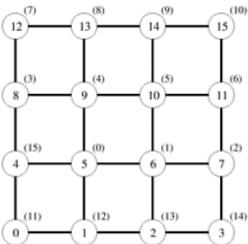
The communication steps in a circular 5-shift on a 4 x 4 Mesh





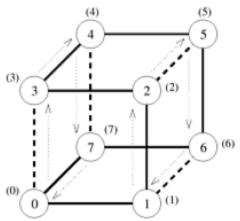
- (a) Initial data distribution and the first communication step
- (b) Step to compensate for backward row shifts



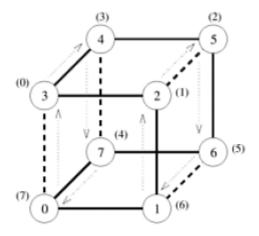


- (c) Column shifts in the third communication step
- (d) Final distribution of the data

The mapping of an eight-node linear array onto a three dimensional hypercube to perform a circular 5-shift as a combination of a 4-shift and a 1-shift

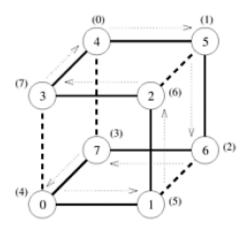




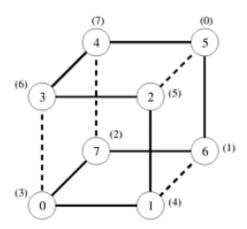


Second communication step of the 4-shift

(a) The first phase (a 4-shift)



(b) The second phase (a 1-shift)



(c) Final data distribution after the 5-shift

Circular *q*-shifts on an 8-node hypercube for

1 <= q < 8

