

2P1

High Performance Computing

Assignment 3

Date of completion: - 4.9.2020

Title :- Parallel Sorting Algorithms

Problem Statement :- For Bubble sort and Merge sort, based on existing sequential algorithms, design & implement parallel algorithm utilizing all resources available.

Objectives :- Study parallel execution of sorting algorithm
Study open MP for parallel computing.

Outcomes :- students will be able to
- Implement sorting algorithms in open MP.

Software / Hardware Requirement :- Ubuntu OS, open MP, API, editor.

Theory

Parallel Sorting :-

a) Parallel Bubble Sort

i) Implement as a pipeline

ii) Let local size = n/m of processors

iii) We divide the array into blocks and each process

executes the bubble sort on the part including comparing the last.

element with the first one belonging to the next thread

- iv) Implement with loop for $j=0$ to $n-1$.
- v) For each iteration of j , each thread needs to wait until previous thread has finished that iterations
- vi) Synchronization mode to be used is 'barrier'.

b) Parallel Merge Sort.

- i) These steps are performed
 - 1) Divide
 - 2) Conquer
 - 3) Combine
- ii) Collect sort list onto one processor
- iii) Merge implements as they come together
- iv) Simple tree structure is obtained.

Algorithm

Bubble Sort

```
for  $k=0$  to  $n-2$ 
  if  $k$  is even then
    for  $i=0$  to  $n/2-1$  do in parallel
      if  $A[2i] > A[2i+1]$  then
        swap  $A[2i]$  &  $A[2i+1]$ 
    end for
  else for  $i=0$  to  $n/2-2$  do in parallel
    if  $A[2i+1] > A[2i+2]$  then
      swap  $A[2i+1]$  &  $A[2i+2]$ 
    end for
  end if
end for
```


Parallel Merge Sort

1. $mid > size/2$

if both children present in tree then

send mid, firstchild

send size-mid, secondchild

send list, mid, firstchild

send list from mid, size-mid, secondchild

call merge (list, 0, mid, list, mid+1, size, temp, 0, size)

Store temp in another array list

else

call parallelMergeSort (list, 0, size)

if $i \geq 0$ then

send list, size, parent

Analysis

	Time Complexity	Bubble Sort.	Merge Sort
Sequential	Best	$O(n)$	$O(n \log n)$
	Average	$O(n^2)$	$O(n \log n)$
Parallel	Best	$O(n)$	$O(n)$
	Average	$O(n \log n)$	$O(n \log n)$

Test Case:-

for $n = 1000$

Time for parallel execution:- 0.0039 ms

Time for serial execution:- 0.0021 s

Bubble Sort

Merge Sort

0.00017

1.8

for $n = 100$

parallel execution time:- 0.00093

0.00018

serial execution time:- 0.00003

1.6

Conclusion:- Thus I completed the sorting algorithms using parallel reduction and understood the algorithms.

Assignment 3

1) Merge Sort

CODE:

```
code = ""
#include<iostream>
#include<omp.h>

using namespace std;

void printArray(int *arr, int size) {
    for(int i=0; i<size; i++) {
        cout<<arr[i]<<" ";
    }
    cout<<endl;
}

void merge(int* arr, int start, int mid, int end) {
    int len = (end - start) + 1;
    int temp[len];
    int cur = 0;
    int i = start;
    int j = mid + 1;
    while(i <= mid && j <= end){
        if(arr[i] < arr[j]) {
            temp[cur] = arr[i];
            cur++;
            i++;
        }
        else {
            temp[cur] = arr[j];
            cur++;
            j++;
        }
    }
    if(i <= mid) {
        while(i <= mid) {
            temp[cur] = arr[i];
            i++;
            cur++;
        }
    }
    else if(j <= end) {
        while(j <= end) {
            temp[cur] = arr[j];
            j++;
            cur++;
        }
    }
    cur = 0;
    for(i=start; i<=end; i++) {
        arr[i] = temp[cur];
        cur++;
    }
}

void mergeSort(int *arr, int start, int end) {
    if(start < end) {
        int mid = (start+end) / 2;
```

```

#pragma omp parallel sections
{
#pragma omp section
mergeSort(arr, start, mid);
#pragma omp section
mergeSort(arr, mid+1, end);
}
merge(arr, start, mid, end);
}
}

int main(int argc, char *argv[]) {
int size = 100;
int a[size];
double start, end;
omp_set_num_threads(2);
for(int i=0; i<size; i++) {
a[i] = rand()% 100;
}
//int a[] = {7,33,5,5,23,111,75,34,77,121,120};
for(int i=0; i<size; i++)
cout<<" "<<a[i];
cout<<endl;
start = omp_get_wtime();
mergeSort(a, 0, size-1);
printArray(a, size);
end = omp_get_wtime();
cout<<"Time parallel = "<<(end-start)<<endl;
return 0;
}

```

""""

```

text_file = open("code.cpp", "w")
text_file.write(code)
text_file.close()
!g++ -fopenmp code.cpp
!./a.out

```

OUTPUT:

colab.research.google.com/drive/17B6wt5_w7xAEYI93KV2rlgOBlhVm_LD#scrollTo=gCIRneySzDLV

Colaboratory

CommentShareSettings

RAMDiskEditing

Untitled8.ipynb

FileEditViewInsertRuntimeToolsHelp

+ Code+ Text

```
mergeSort(a, 0, size-1);

printArray(a, size);

end = omp_get_wtime();

cout<<"Time parallel = "<<(end-start)<<endl;

return 0;

}

'''

text_file = open("merge.cpp", "w")
text_file.write(code)
text_file.close()
!g++ -fopenmp code.cpp
!./a.out
```

89383 30886 92777 36915 47793 38335 85386 60492 16649 41421 2362 90027 68690 20059 97763 13926 80540 83426 89172 55736 5211 95368 2567 56429 65782 21530 22862 6

0 1 2 3 3 3 4 4 8 8 9 10 11 12 13 13 13 14 14 17 17 19 20 20 23 24 25 25 26 29 29 30 30 31 31 33 33 34 35 36 36 37 39 40 41 42 42 43 44 44 48 48 49 50 50

.....

Time Serial= 33.779499

.....

Time Parallel= 44.832556

2) Bubble sort

CODE:

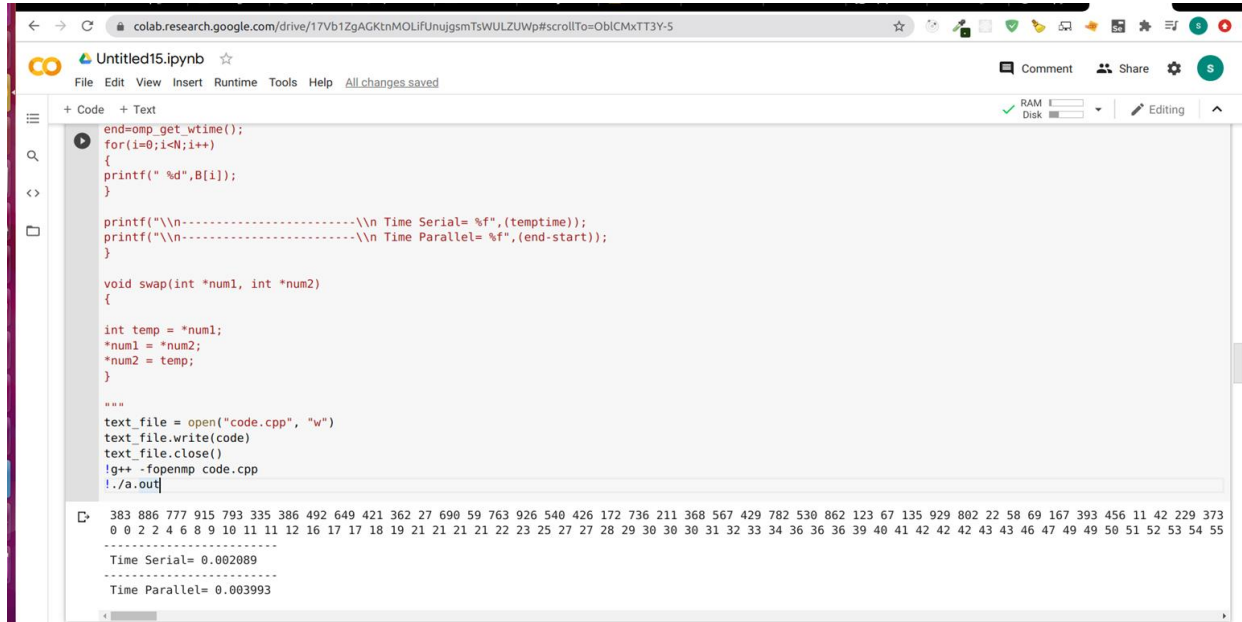
```
code = """"#include <omp.h>
#include <stdio.h>
#include <stdlib.h>
void swap(int *,int *);
int main (int argc, char *argv[]) {
int SIZE =1000;
int A[SIZE],B[SIZE];
for(int i=0;i<SIZE;i++)
{
A[i]=rand()%SIZE;
B[i]=A[i];
printf(" %d",A[i]);
}
printf("\n\n");
//int A[5] = {6,9,1,3,7};
int N = SIZE;
int i=0, j=0;
int first;
double start,end;
start = omp_get_wtime();
for (int i = 0; i < N-1; i++) {
for (int j = 0; j < N-i-1; j++) {
if (B[j] > B[j+1])
{
// swap arr[j+1] and arr[i]
int temp = B[j];
B[j] = B[j+1];
B[j+1] = temp;
}
}
}
end = omp_get_wtime();
double temptime = end -start;
start=omp_get_wtime();
for( i = 0; i < N-1; i++ )
{
first = i % 2;
#pragma omp parallel for default(none),shared(A,first,N)
for( j = first; j < N-1; j += 1 )
{
if( A[ j ] > A[ j+1 ] )
{
swap( &A[ j ], &A[ j+1 ] );
}
}
}
end=omp_get_wtime();
for(i=0;i<N;i++)
{
printf(" %d",B[i]);
}
printf("\n\n-----\n Time Serial= %f",(temptime));
printf("\n\n-----\n Time Parallel= %f",(end-start));
}

void swap(int *num1, int *num2)
{
int temp = *num1;
*num1 = *num2;
*num2 = temp;}"""""
```



```
text_file = open("code.cpp", "w")
text_file.write(code)
text_file.close()
!g++ -fopenmp code.cpp
!./a.out
```

OUTPUT:



The screenshot shows a Google Colab notebook titled "Untitled15.ipynb". The code cell contains the following C++ code:

```
end=omp_get_wtime();
for(i=0;i<N;i++)
{
    printf(" %d",B[i]);
}

printf("\n-----\n Time Serial= %f", (temptime));
printf("\n-----\n Time Parallel= %f", (end-start));
}

void swap(int *num1, int *num2)
{
    int temp = *num1;
    *num1 = *num2;
    *num2 = temp;
}

// ...

text_file = open("code.cpp", "w")
text_file.write(code)
text_file.close()
!g++ -fopenmp code.cpp
!./a.out
```

The output of the code is displayed below the code cell:

```
383 886 777 915 793 335 386 492 649 421 362 27 690 59 763 926 540 426 172 736 211 368 567 429 782 530 862 123 67 135 929 802 22 58 69 167 393 456 11 42 229 373
0 0 2 2 4 6 8 9 10 11 11 12 16 17 17 18 19 21 21 21 22 23 25 27 27 28 29 30 30 31 32 33 34 36 36 36 39 40 41 42 42 42 43 43 46 47 49 49 50 51 52 53 54 55
-----
Time Serial= 0.002089
-----
Time Parallel= 0.003993
```