

8/9/25

# Apply A\* Algorithm

misplaced Tiles

Manhattan distance

Q.

2	8	3
1	6	4
7		5

Initial state

1	2	3
8		4
7	6	5

goal State

$$f(n) = g(n) + h(n)$$

2	8	3
1	6	4
7		5

$$g = 0$$

R

L

U

2	8	3
1	6	4
7	5	

$$H = 6 + 1 = 7$$

2	8	3
1	6	4
	7	5

$$H = 6 + 1 = 7$$

2	8	3
1		4
7	6	5

$$H = 3 + 1$$

R

L

U

D

2	8	3
1	4	
7	6	5

$$H = 5 + 2 = 7$$

2	8	3
	1	4
7	6	5

$$H = 4 + 2 = 6$$

2		3
1	8	4
7	6	5

$$H = 4 + 2 = 6$$

2	8	3
1	6	4
7		5

$$H = 5 + 2 = 7$$

R

D

U

R

L

D

2	8	3
1		4
7	6	5

$$H = 6$$

2	8	3
7	1	4
	6	5

$$H = 8$$

	8	3
2	1	4
7	6	5

$$H = 7$$

2	3	
1	8	4
7	6	5

$$H = 8$$

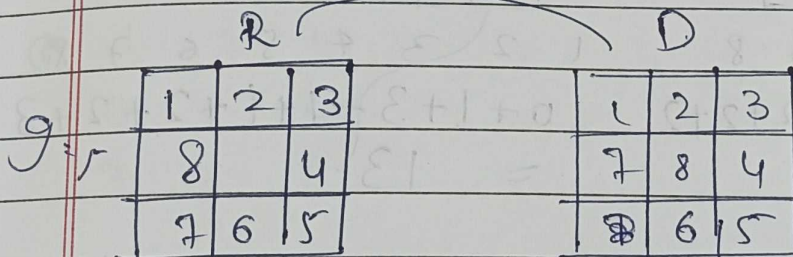
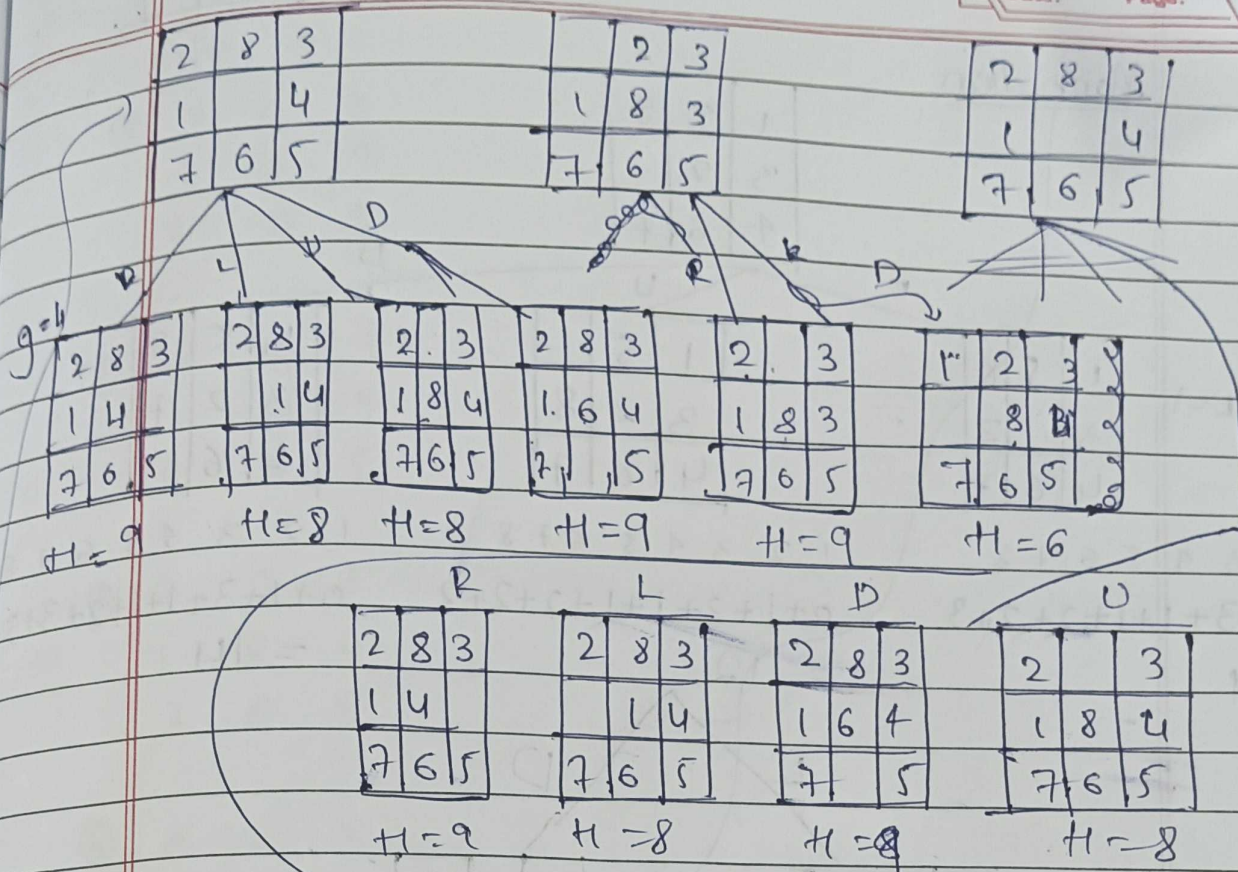
	2	3
1	8	4
7	6	5

$$H = 6$$

2	8	3
1		4
7	6	5

$$H = 6$$

g=3



Q. Manhattan

1	5	8
3	2	
4	6	7

initial state.

1	2	3
4	5	6
7	8	

goal state



goal:

1	2	3
4	5	6
7	8	

Manhattan

1	5	8
3	2	
4	6	7

L

U

D

Level-1

1	5	8
3		2
4	6	7

1	5	
3	2	8
4	6	7

1	5	8
3	2	7
4	6	

1 2 3 4 5 6 7 8

$$0+2+3+1+1+2+2+3 = 14$$

1 2 3 4 5 6 7 8

$$0+1+3+1+1+2+2+2 = 12$$

1 2 3 4 5 6 7 8

$$0+1+3+1+1+2+3+3 = 14$$

L

D

Level-2

1		5
3	2	8
4	6	7

1	5	8
3	2	
4	6	7

1 2 3 4 5 6 7 8

$$0+1+3+1+2+2+2+2 = 13$$

1 2 3 4 5 6 7 8

$$0+1+3+1+1+2+2+3 = 13$$

Algorithm (mis placed Tiles)

①. Start → put initial state in Open &

②. Pick state with smallest

③. If goal Stop

④. Expand neighbors

⑤. for each neighbor

$$g := \text{parent} \cdot g + 1$$

$$h = \text{misplaced tiles}$$

$$f = g + h$$

add/update in Open

6. Repeat until goal found @ open empty

0/p.

① 2 8 3  
 1 6 4  
 7 0 5

② 2 8 3  
 1 0 4  
 7 6 5

③ 2 0 3  
 1 8 4  
 7 6 5

④ 0 2 3  
 1 8 4  
 7 6 5

⑤ 1 2 3  
 0 8 4  
 7 6 5

⑥ 1 2 3  
 8 0 4  
 7 6 5

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goal:-

1	2	3
8		4
7	6	5

Mahalfan

2	8	3
1	6	4
7		5

R

L

D

2	8	3
1	6	4
	7	5

2	8	3
1	6	4
7	5	

2	8	3
1		4
7	6	5

1 2 3 4 5 6 7 8

1+1+0+0+0+1+1+2

6

1+1+0+0+1+1+0+2

6

1+1+0+0+0+0+0+0

= 4

L

R

D

D

2	8	3
	1	4
7	6	5

2	8	3
	1	4
7	6	5

2		3
1	8	4
7	6	5

2	8	3
1	6	4
7		5

2+1+0+0+0+0+0+2

5

1+1+0+1+0+

0+0+2=5

1+1+0+0+

0+0+0+1=3

1+1+0+0+0+

1+0+2=5

L

R

D

	2	3
1	8	4
7	6	5

2	3	
1	8	4
7	6	5

2	8	3
1		4
7	6	5

1+0+0+0+0+0+

0+1=2

1+1+1+0+0

0+0+1=4

1+1+0+0+0+0+

0+2=4

D

1	2	3
	8	4
7	6	5

R

→

1	2	3
8		4
7	6	5

0+0+0+0+0+

0+0+1=1

## Algorithm.

- ① Start with current puzzle state
- ② Create an empty list to keep track of file matches
- ③ For each file from 1 to 8:
  - if the file is in cur. pos, add 0 to the list
  - otherwise, add 1 to the list.
- ④ Check the list:
  - if the list contains all 0's the puzzle is solved = stop.
  - otherwise, make a move to get closer to the goal.
- ⑤ Repeat Steps 2 to 4 until, the puzzle is solved.

Output:

solution path:

2	8	3
1	6	4
7	0	5

⇓

2	8	3
1	0	4
7	6	5

⇓

2	0	3
1	8	4
7	6	5

0	2	3
1	8	4
7	6	5

⇓

1	2	3
0	8	4
7	6	5

⇓

1	2	3
8	0	4
7	6	5

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